



**DO NOT SHARE  
SLIDES AND CLASS MATERIALS  
ON ONLINE SITES**

Course Home

# Advanced Logic Design

## Microprogrammed Control

Mingoo Seok  
Columbia University

# Example: GCD Processor

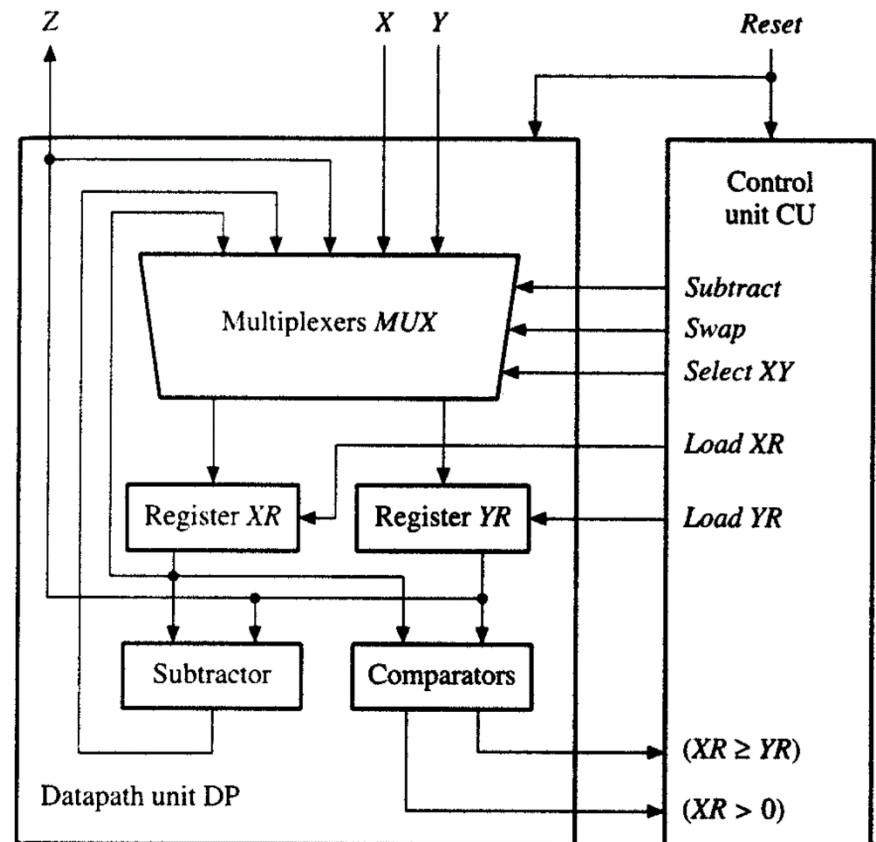
$$\text{gcd}(a,a) = a$$

$$\text{gcd}(a,b) = \text{gcd}(a-b, b) \quad \text{if } a > b,$$

$$\text{gcd}(a,b) = \text{gcd}(a, b-a) \quad \text{otherwise.}$$

# Hardware for the GCD Processor

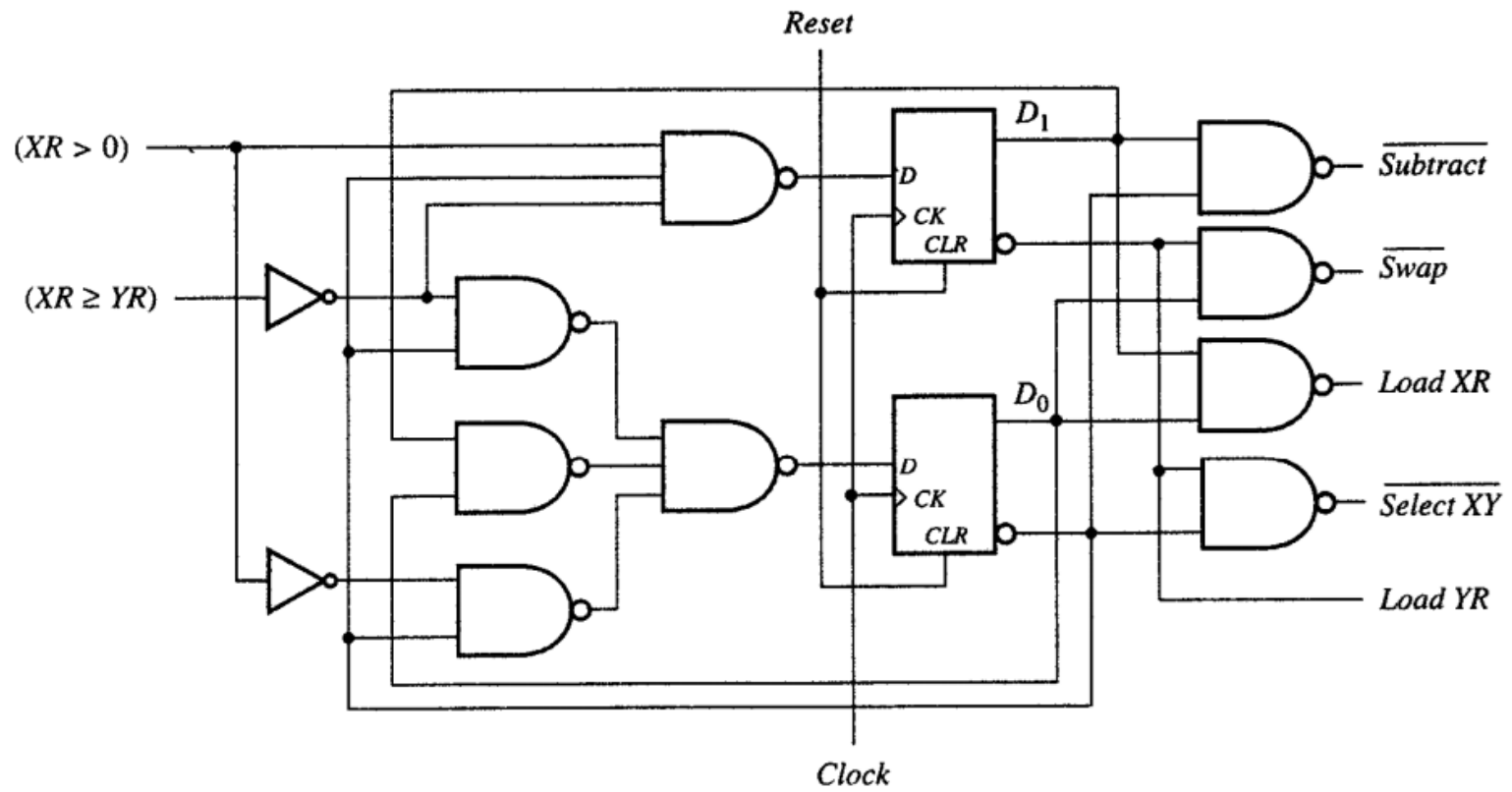
$\text{gcd}(a,a) = a$   
 $\text{gcd}(a,b) = \text{gcd}(a-b, b)$  if  $a > b$ ,  
 $\text{gcd}(a,b) = \text{gcd}(a, b-a)$  otherwise.



# State Table of the Control Unit

State	Inputs ( $XR > 0$ ) ( $XR \geq YR$ )			Outputs				
	0—	10	11	<i>Subtract</i>	<i>Swap</i>	<i>Select XY</i>	<i>Load XR</i>	<i>Load YR</i>
$S_0$ (Begin)	$S_3$	$S_1$	$S_2$	0	0	1	1	1
$S_1$ (Swap)	$S_2$	$S_2$	$S_2$	0	1	0	1	1
$S_2$ (Subtract)	$S_3$	$S_1$	$S_2$	1	0	0	1	0
$S_3$ (End)	$S_3$	$S_3$	$S_3$	0	0	0	0	0

# Hardwired Control



# Microprogram: Concept

- High level description of a double precision ADD:
  - ADD AL, BL
  - ADDC AH, BH
- Low level description: microprogram

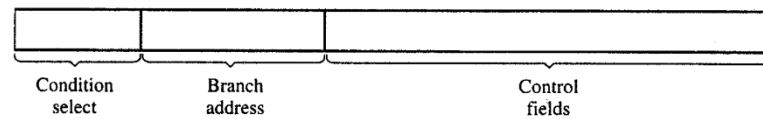
Cycle	Function Select	Storage Control	Data Routing
1	Add	Read AL, Read BL, Write AL	...
2	Add with carry	ReadAH, Read BH, Write AH	...

# Microprogram: Definition

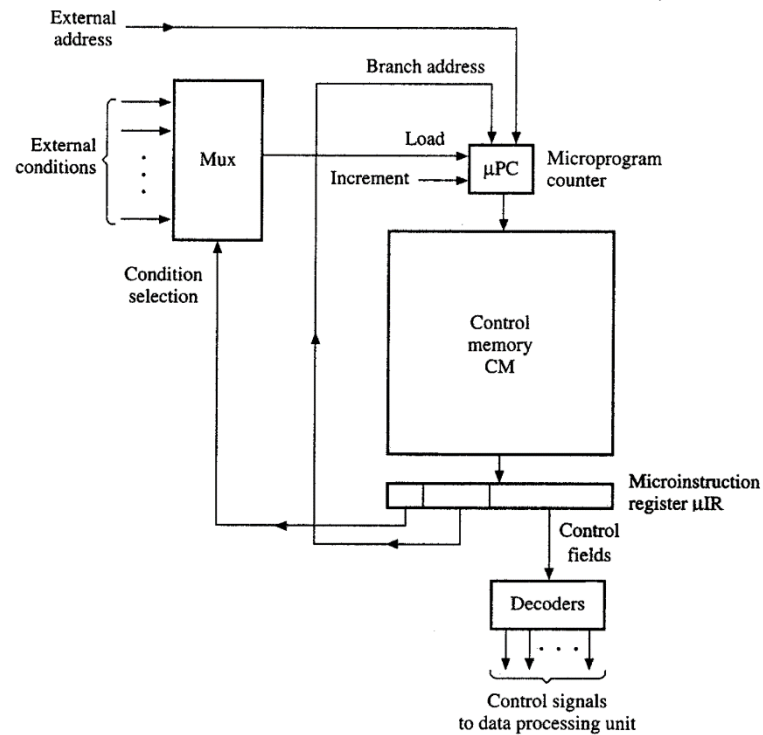
- Microprogram
  - Program stored in memory that generates all the control signals required to execute the instruction set correctly
  - Consists of microinstructions
- Microinstruction
  - Contains a control word and a sequencing word
  - **Control word**: all the control information required for one clock cycle
  - **Sequencing word**: information needed to decide the *next* microinstruction address
- Control memory (control storage)
  - Storage in the microprogrammed control unit to store the microprogram



# Microprogramed Control



(a)



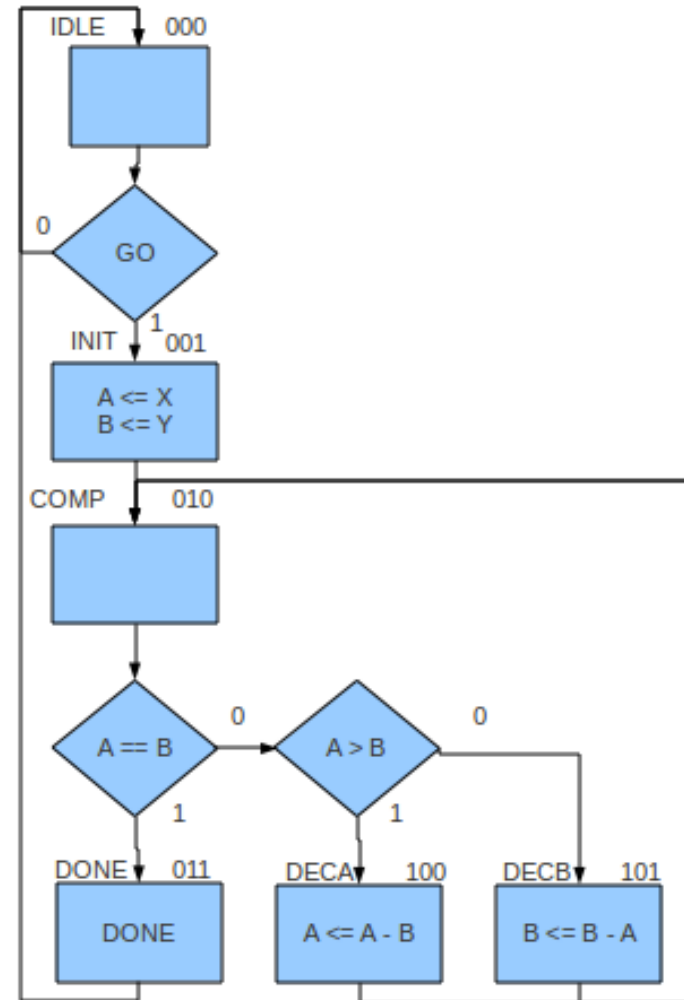
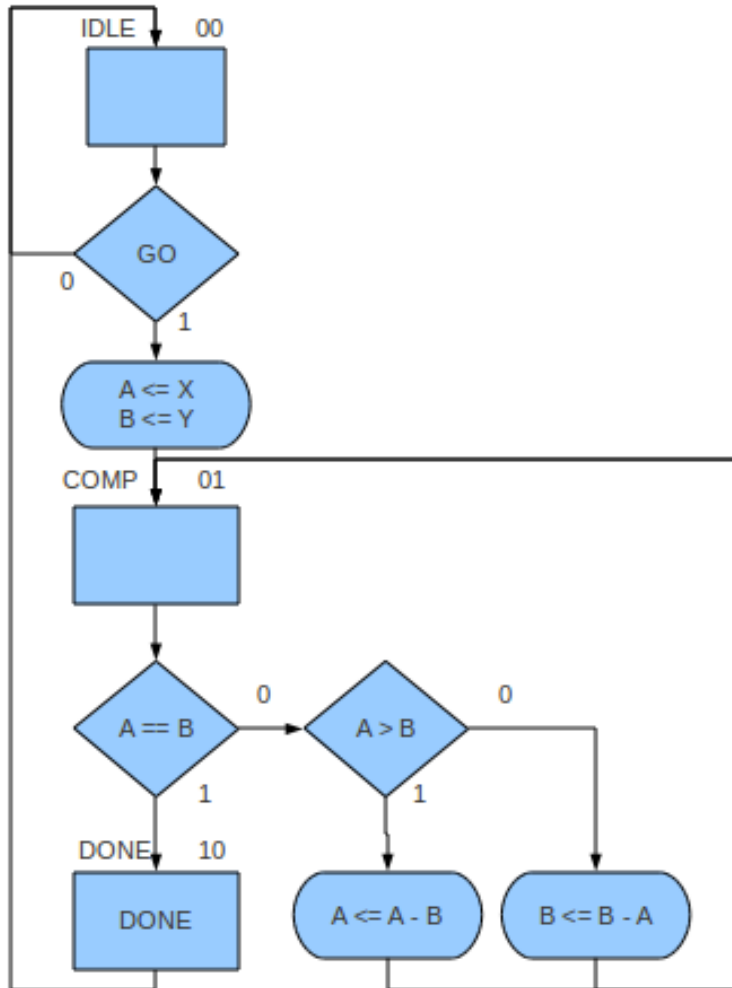
# Example: GCD Processor

$$\text{gcd}(a,a) = a$$

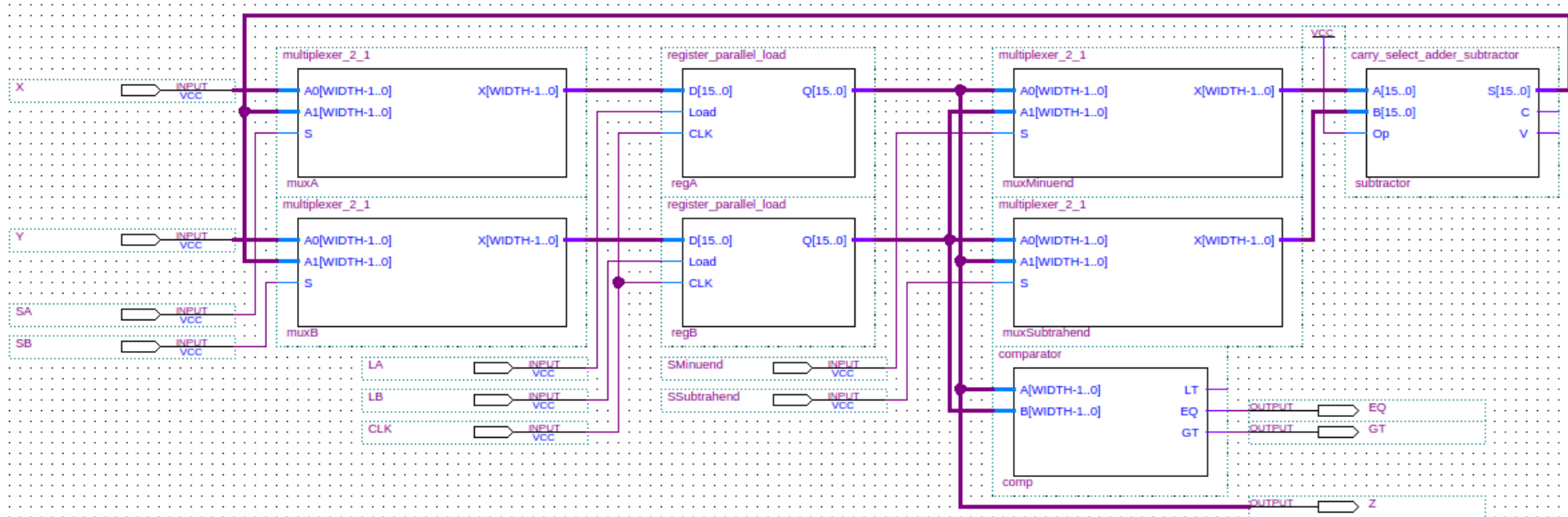
$$\text{gcd}(a,b) = \text{gcd}(a-b, b) \quad \text{if } a > b,$$

$$\text{gcd}(a,b) = \text{gcd}(a, b-a) \quad \text{otherwise.}$$

# ASM: Mealy vs Moore



# Datapath



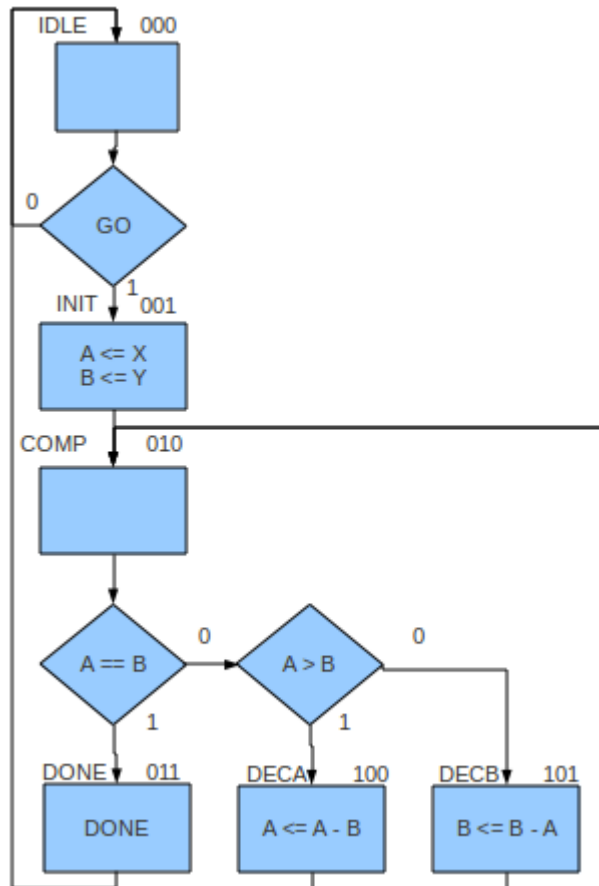
# Microprogram

- The ASM now comprises six states (IDLE, INIT, COMP, DECA, DECB, and DONE). This increase in the number of states will impact computation time as each state transition takes a clock period.
- We have six states so we will need six addresses, therefore a ROM address will comprise three bits ( $2^2=4 < 6 < 2^3=8$ )

# Branch

- We'll also encode the next microinstruction address in the current microinstruction being executed. This means that the instruction will need an address to jump to for each possible combination of the three condition inputs (GO, EQ and GT).
- In the worst case, each instruction can be followed by one of the eight instructions. This requires each instruction needs to contain 8 ( $2^3$ ) addresses. Since each address is three bits, we may need 24 bits just for addresses. Too much!
- Looking at the ASM we see that we can get away with less than half of that. In the instruction that checks GO we only need *two* addresses: the address to jump to on  $GO == 0$  and the address to jump to on  $GO == 1$ . In the instruction that will compare A and B we only need *three* addresses:  $EQ == 0 \ \& \ GT == 0$ ,  $EQ == 0 \ \& \ GT == 1$ , and  $EQ == 1 \ \& \ GT == 0$ .
- Since we can't execute these two instructions at the same time we can get away with the worst case which is three target addresses, so we need only *3 addresses (9 bits)*.
- We'll call these three target addresses Next00, Next01, and Next10. We'll also use a signal SEL to tell us how to interpret these three addresses.

# Branch



SEL	Next00	Next01	Next10
0	GO == 0	GO == 1	Unused
1	EQ == 0 & GT == 0	EQ == 0 & GT == 1	EQ == 1 & GT == 0

# Datapath Control Signal & Control Unit Output

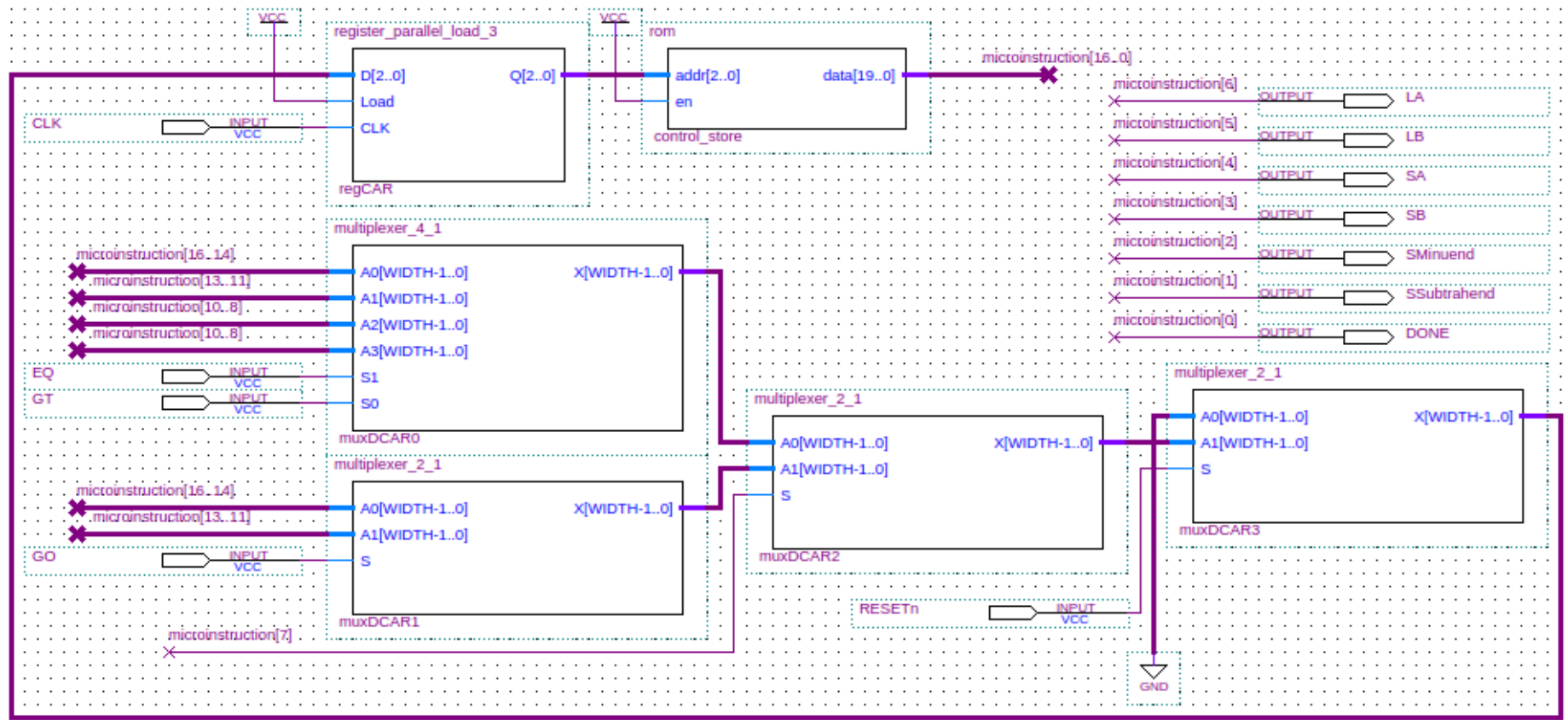
- For the datapath control signalling we need six bits: LA, LB, SA, SB, SMinuend, and SSubtrahend. These control signals are Moore outputs so they depend only upon control unit state (or current control store address).
- For the control unit output we need only one bit: DONE. Again, this is a Moore output that only depends upon control unit state (or current control store address).



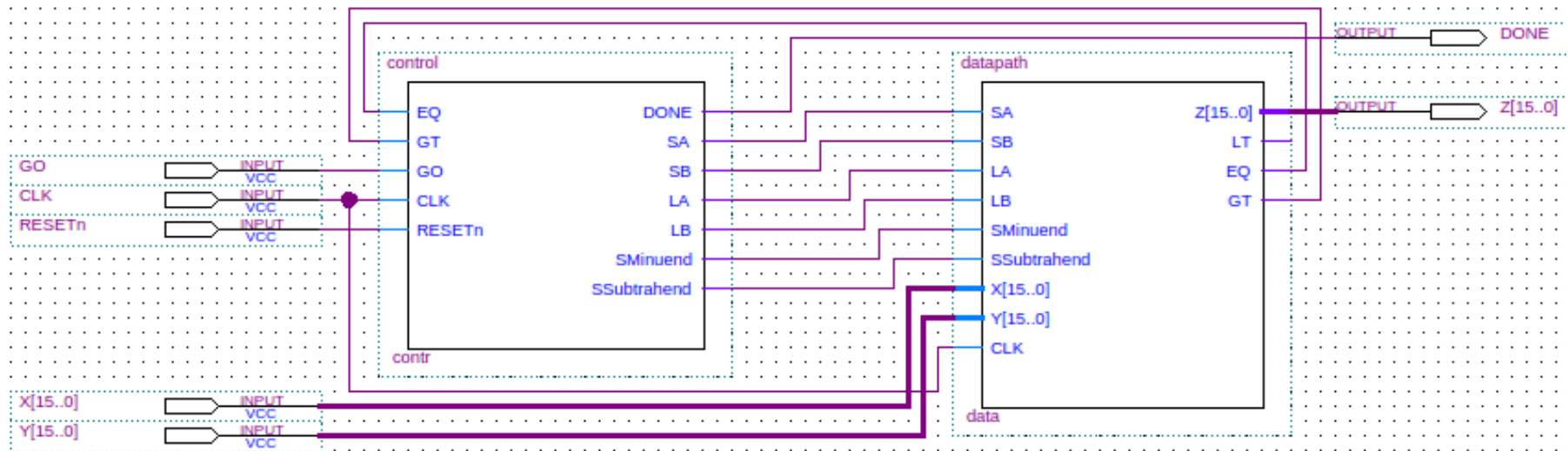
# Control Storage

	Control Word										
	Target Addresses				Datapath Control						Control Unit Output
Address	Next 00	Next 01	Next 10	SEL	LA	LB	SA	SB	SMin uend	SSubt rahend	DONE
000	000	001	000	1	0	0	0	0	0	0	0
001	010	010	010	1	1	1	0	0	0	0	0
010	101	100	011	0	0	0	0	0	0	0	0
011	000	000	000	0	0	0	0	0	0	0	1
100	010	010	010	0	1	0	1	0	0	0	0
101	010	010	010	0	0	1	0	1	1	1	0

# Microprogrammed Control



# Datapath + MP-ed Control



Full Verilog code:

[http://barrywatson.se/dd/dd\\_microprogrammed\\_nonprogrammable\\_control\\_unit\\_gcd.html](http://barrywatson.se/dd/dd_microprogrammed_nonprogrammable_control_unit_gcd.html)

# Comments

- Microprogramming helps in making a control unit which may be changed by changing the content of the memory
- As compared to a hard-wired control unit, it is slow due to the fetch timing of the instruction from the memory