

COMS3008A: Parallel Computing

Exercises 9

2021-10-21

1 Objectives

- Apply MPI point-to-point and collective communication functions to write MPI programs.
- Apply MPI derived datatypes in MPI programs.

2 Problems

For the solutions of the following problems, you are expected to use MPI derived datatypes wherever possible.

1. Write an MPI program that sends the upper triangular portion of a square matrix stored on process 0 to process 1.
2. Write a dense matrix transpose function: Suppose a dense $n \times n$ matrix \mathbf{A} is stored on process 0. Create a derived datatype representing a single column of \mathbf{A} . Send each column of \mathbf{A} to process 1, but have process 1 receive each column into a row. When the function returns, \mathbf{A} should be stored on process 0 and \mathbf{A}^T on process 1.
3. Suppose we have p number of MPI processes, each holds a $k \times n$ matrix \mathbf{A}_{sub} , and a vector \mathbf{x}_{sub} of k dimensions (or components), where $kp = n$. If we put together all \mathbf{A}_{sub} matrices from each process in the order of process ranks, we can obtain the full matrix \mathbf{A} . Similarly, if we put together all \mathbf{x}_{sub} vectors together, we can obtain the full vector \mathbf{x} . Using such a distributed setting of a matrix and a vector among processes, write an MPI program that computes $\mathbf{B} = \mathbf{A}\mathbf{x}$, where each process holds only k rows of \mathbf{B} that corresponds to the k rows of \mathbf{A} .
4. Continued from problem 3, given the same distributed setting of \mathbf{A} and \mathbf{x} among the p processes, how would you compute $\mathbf{B} = \mathbf{A}^T\mathbf{x}$ in a communication efficient manner? Implement your method.

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5. Write an MPI program that completes Example 6 in Lec9 slides, where each process sends a particle to all the other processes using the derived datatype given in this example.