

Objective:

to generate data of degree 3 polynomial and fit models of degree 1, degree 3 and degree 13 polynomial and compare their performances.

Tasks:

Task 1: Data generation

- generate 500 samples of the target variable y using the equation , $y=0.5x^3-x^2+2$ and add noise
- Visualize the generated data points

Task 2: Polynomial regression (500 samples)

Fit polynomial regression models of the following degree to the generated data:(use polynomial features library from Scikit-learn)

- Linear Regression model(Degree - 1)
- Polynomial Regression model (Degree - 3)
- Polynomial Regression model (Degree - 13)
- Compare the estimated model co-efficients to the actual ground truth equations
- Evaluate the model performance using metrics: MSE , MAE, R²

Task 1 Code:

```
In [3]: import numpy as np
import matplotlib.pyplot as plt

# Set random seed for reproducibility
np.random.seed(42)

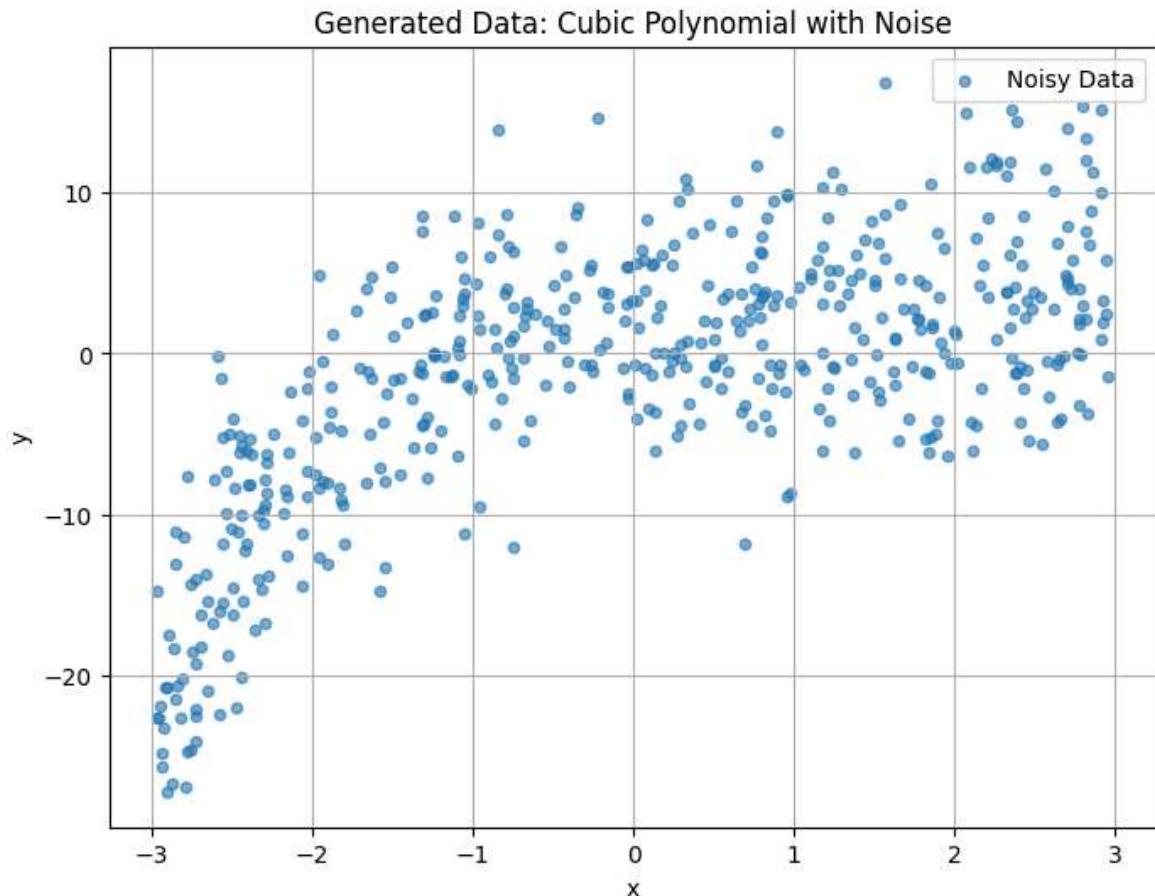
# Number of samples
n_samples = 500

# Generate input data
x = np.random.uniform(-3, 3, n_samples)

# True underlying function
y_true = 0.5 * x**3 - x**2 + 2

# Add Gaussian noise
noise = np.random.normal(0, 5, n_samples)
y = y_true + noise
```

```
# Visualize the generated data
plt.figure(figsize=(8, 6))
plt.scatter(x, y, s=20, alpha=0.6, label="Noisy Data")
plt.xlabel("x")
plt.ylabel("y")
plt.title("Generated Data: Cubic Polynomial with Noise")
plt.legend()
plt.grid(True)
plt.show()
```



Task 2 Code:

In [4]:

```
import numpy as np
import pandas as pd
from sklearn.preprocessing import PolynomialFeatures
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score

# Reshape X for sklearn
X = x.reshape(-1, 1)
y_target = y

# Degrees to test
degrees = [1, 3, 13]

results = []

for degree in degrees:
    # Polynomial feature transformation
    poly = PolynomialFeatures(degree=degree, include_bias=True)
```

```
X_poly = poly.fit_transform(X)

# Linear regression on transformed features
model = LinearRegression()
model.fit(X_poly, y_target)

# Predictions
y_pred = model.predict(X_poly)

# Evaluation metrics
mse = mean_squared_error(y_target, y_pred)
mae = mean_absolute_error(y_target, y_pred)
r2 = r2_score(y_target, y_pred)

results.append({
    "Degree": degree,
    "MSE": mse,
    "MAE": mae,
    "R2": r2,
    "Coefficients": model.coef_,
    "Intercept": model.intercept_
})

# Display coefficients
print(f"\nPolynomial Degree {degree}")
print("Intercept:", model.intercept_)
for i, coef in enumerate(model.coef_):
    print(f"x^{i}: {coef:.4f}")

# Convert results to dataframe
results_df = pd.DataFrame(results)
print("\nModel Performance Summary")
print(results_df[["Degree", "MSE", "MAE", "R2"]])
```

Polynomial Degree 1
Intercept: -1.2555889536901006
 x^0 : 0.0000
 x^1 : 3.0521

Polynomial Degree 3
Intercept: 2.5318007492252086
 x^0 : 0.0000
 x^1 : 0.1944
 x^2 : -1.1537
 x^3 : 0.4978

Polynomial Degree 13
Intercept: 2.034565317696061
 x^0 : 0.0000
 x^1 : -3.5659
 x^2 : 0.8056
 x^3 : 11.4449
 x^4 : -1.5138
 x^5 : -9.8695
 x^6 : 0.3932
 x^7 : 3.9528
 x^8 : -0.0272
 x^9 : -0.7787
 x^{10} : -0.0021
 x^{11} : 0.0738
 x^{12} : 0.0002
 x^{13} : -0.0027

Model Performance Summary

	Degree	MSE	MAE	R2
0	1	39.476836	5.097990	0.430638
1	3	25.005302	3.992331	0.639356
2	13	24.379374	3.912345	0.648384