# **Mini-Project 2**

# 1. Color Image Demosaicing

## Implementation of DemosaicImage.m

#### 1. Nearest Neighbors

For nearest neighbor interpolation, the value of the nearest neighbor the value of the nearest neighbor is copied to interpolate the value of the pixel.

The code snippet shown below creates masks for the Bayer pattern for the red, green and blue pattern.

It ensures that the additional pixels at the edges of the Bayer pattern, are truncated, to match the size of the image.

```
+29 p2_latex.tar.gz × demosaicImage.m × evalDemosaicing.m × runDemosaicing.m × mosaicImage.m × evalDemosaicing.m
                                                                                                           +
118
                                    Nearest neighbour algorithm
119
120
     function mosim = demosaicNN(im)
121
        %mosim = demosaicBaseline(im);
122
123 -
        [imageWidth,imageHeight]=size(im);
124
125
        %creating masks for the bayer pattern
126 -
        bayer_red = repmat([1 0; 0 0], ceil(imageWidth/2),ceil(imageHeight/2));
127 -
        bayer_blue = repmat([0 0; 0 1], ceil(imageWidth/2),ceil(imageHeight/2));
128 -
        bayer_green = repmat([0 1; 1 0], ceil(imageWidth/2),ceil(imageHeight/2));
129
130
        %truncating the extra pixels at the edges
131 -
        if (mod(imageWidth,2))==1
132 -
          bayer red(size(bayer red,1),:)=[];
133 -
           bayer blue(size(bayer blue,1),:)=[];
134 -
          bayer green(size(bayer green,1),:)=[];
135 -
        end
136 -
        if (mod(imageHeight, 2) == 1)
137 -
          bayer red(:,size(bayer red,2))=[];
138 -
           bayer blue(:,size(bayer blue,2))=[];
139 -
           bayer_green(:,size(bayer_green,2))=[];
140 -
```

The code snippet first extracts the red, green and blue components of the image using the mask of the Bayer filter.

It then deduces the green pixels at the missing points (at the location of the red and blue pixels) using the appropriate filter and is added to the green component of the image. After this, the red pixels are interpolated at green and blue pixel locations and similarly the blue pixels are interpolated at the blue and green pixel locations, using appropriate filters and added to the respective red and blue components of the image. The filter values are obtained using the nearest neighbors of the pixels, such that the nearest neighbor is copied to interpolate the value of the respective pixels.

The three layers are combined to form the image.

```
demosaicImage.m × evalDemosaicing.m × runDemosaicing.m × mosaicImage.m × evalDemosaicing.m
                                                                                                           +
142
         extracting the red, green and blue components of the image using the mask
143
144 -
         red image = im.*bayer red;
145 -
         blue_image = im.*bayer_blue;
146 -
         green_image = im.*bayer_green;
147
148
         %deducing the green pixels at missing points
149 -
         green = green image+imfilter(green image,[0 1]);
150
151
         %deducing the red pixels at missing points
         redValue=im(1:2:imageWidth,1:2:imageHeight);
152 -
153 -
         meanRed = mean(mean(redValue));
154
         %red@blue
155 -
         red_1 = imfilter(red_image, [0 0;0 1], meanRed);
156
         %red@green
157 -
         red 2 = imfilter(red image, [0 1;1 0], meanRed);
158
         %combine
159 -
         red = red image + red 1 +red 2;
160
161
         %deducing the blue pixels at missing points
162 -
         blueValue=im(1:2:imageWidth,1:2:imageHeight);
163 -
         meanBlue = mean(mean(blueValue));
164
         %blue@red
165 -
         blue_1 = imfilter(blue_image, [0 0;0 1], meanBlue);
166
         %blue@green
167 -
        blue 2 = imfilter(blue image, [0 1:1 0], meanBlue);
168
         %combine
169 -
        blue = blue_image + blue_1 +blue_2;
170
171 -
        mosim(:,:,1) = red;
172 -
        mosim(:,:,2) = green;
173 -
        mosim(:,:,3) = blue;
```

#### 2. Linear Interpolation

For linear interpolation, the value of the nearest neighbor the average values of the neighbors is taken to interpolate the value of the pixel.

The code snippet shown below creates masks for the Bayer pattern for the red, green and blue pattern.

It ensures that the additional pixels at the edges of the Bayer pattern, are truncated, to match the size of the image.

```
p2_latex.tar.gz × demosaicImage.m × evalDemosaicing.m × runDemosaicing.m × mosaicImage.m × evalDemosaicing.m
175
176
177
       function mosim = demosaicLinear(im)
178
       179
        % mosim = repmat(im, [1 1 3]);
180
181 -
        [imageWidth,imageHeight]=size(im);
182
183
        %creating masks for the bayer pattern
184 -
        bayer_red = repmat([1 0; 0 0], ceil(imageWidth/2),ceil(imageHeight/2));
185 -
        bayer_blue = repmat([0 0; 0 1], ceil(imageWidth/2),ceil(imageHeight/2));
186 -
        bayer_green = repmat([0 1; 1 0], ceil(imageWidth/2),ceil(imageHeight/2));
187
188
        %truncating the extra pixels at the edges
189 -
        if (mod(imageWidth,2))==1
190 -
           bayer red(size(bayer red,1),:)=[];
191 -
           bayer blue(size(bayer blue,1),:)=[];
192 -
           bayer green(size(bayer green,1),:)=[];
193 -
194 -
        if (mod(imageHeight, 2) == 1)
195 -
           bayer_red(:,size(bayer_red,2))=[];
196 -
           bayer_blue(:,size(bayer_blue,2))=[];
197 -
           bayer_green(:,size(bayer_green,2))=[];
198 -
```

The code snippet first extracts the red, green and blue components of the image using the mask of the Bayer filter.

It then deduces the green pixels at the missing points (at the location of the red and blue pixels) using the appropriate filter and is added to the green component of the image. After this, the red pixels are interpolated at green and blue pixel locations and similarly the blue pixels are interpolated at the blue and green pixel locations, using appropriate filters and added to the respective red and blue components of the image. The filter values are obtained by taking the average of the pixels of the neighborhood of the corresponding layers, such that the average of the pixel values is used to interpolate the value of the respective pixels.

The three layers are combined to form the image.

```
200
         %extracting the red, green and blue components of the image using the mask
201 -
        red image = im.*bayer red;
202 -
        blue_image = im.*bayer_blue;
203 -
        green_image = im.*bayer_green;
204
205
        %deducing the green pixels at missing points
206 -
        green = green image + imfilter(green image, [0 1 0;1 0 1; 0 1 0]/4);
207
208
        %deducing the red pixels at missing points
209 -
        red_1 = imfilter(red_image, [1 0 1;0 0 0;1 0 1]/4);
210 -
        red 2 = imfilter(red image, [0 1 0;1 0 1;0 1 0]/2);
        red = red image+red 1+red 2;
211 -
212
        %deducing the blue pixels at missing points
213
        blue_1 = imfilter(blue_image, [1 0 1;0 0 0;1 0 1]/4);
214 -
215 -
        blue_2 = imfilter(blue_image, [0 1 0;1 0 1;0 1 0]/2);
        blue = blue_image+blue_1+blue_2;
216 -
217
218 -
        mosim(:,:,1) = red;
219 -
        mosim(:,:,2) = green;
220 -
        mosim(:,:,3) = blue;
```

## 3. Adaptive Gradient Interpolation

For adaptive gradient interpolation, the difference of the values of the top and bottom pixels (vertical gradient) is compared to the difference of the values of the values of the left and right pixels (horizontal gradient). If the vertical gradient is greater than the horizontal gradient, then the vertical gradient, then the average of the left and right pixels is assigned to the center pixel. If the horizontal gradient is greater than the vertical gradient, then the average of the top and bottom pixels is assigned to the center pixel.

The code snippet shown below creates masks for the Bayer pattern for the red, green and blue pattern.

It ensures that the additional pixels at the edges of the Bayer pattern, are truncated, to match the size of the image.

```
× mosaicImage.m
+29 p2_latex.tar.gz × demosaicImage.m × evalDemosaicing.m
                                                                                       × evalDemosaicing.m
221
222
223
                                      Adaptive gradient
224
225
       function mosim = demosaicAdagrad(im)
         mosim = demosaicBaseline(im);
226 -
227
228 -
         [imageWidth,imageHeight]=size(im);
229
230
         %creating masks for the bayer pattern
231 -
        bayer red = repmat([1 0; 0 0], ceil(imageWidth/2),ceil(imageHeight/2));
232 -
        bayer blue = repmat([0 0; 0 1], ceil(imageWidth/2),ceil(imageHeight/2));
233 -
        bayer_green = repmat([0 1; 1 0], ceil(imageWidth/2),ceil(imageHeight/2));
234
235
         %truncating the extra pixels at the edges
236 -
        if (mod (imageWidth, 2)) ==1
237 -
            bayer_red(size(bayer_red,1),:)=[];
238 -
           baver blue(size(baver blue,1),:)=[];
239 -
           bayer green(size(bayer green,1),:)=[];
240 -
241 -
        if (mod (imageHeight, 2) == 1)
242 -
           bayer_red(:,size(bayer_red,2))=[];
           bayer_blue(:,size(bayer_blue,2))=[];
243 -
244 -
           bayer_green(:,size(bayer_green,2))=[];
245 -
```

The code snippet first extracts the red, green and blue components of the image using the mask of the Bayer filter.

The green pixels at the position of the red and blue pixels are interpolated by comparing the horizontal gradient and the vertical gradient of the red and blue pixel layers, and replacing the green pixels with the appropriate averages.

After this, the red pixels are interpolated at green and blue pixel locations and similarly the blue pixels are interpolated at the blue and green pixel locations, using appropriate filters and added to the respective red and blue components of the image. The filter values are obtained by taking the average of the pixels of the neighborhood of the corresponding layers, such that the average of the pixel values is used to interpolate the value of the respective pixels.

The three layers are combined to form the image.

```
247
         %extracting the red, green and blue components of the image using the mask
248 -
         red_image = im.*bayer_red;
249 -
         blue image = im.*bayer blue;
250 -
         green_image = im.*bayer_green;
251
252
         %deducing the green pixels at the missing points
253 -
         green = green_image + imfilter(green_image, [0 1 0; 1 0 1; 0 1 0]);
254 -
       for x = 3:2: (imageWidth-2)
255 -
            for y = 3:2:(imageHeight-2)
256 -
                 horizontal gradient = abs((red image(x,y-2)+red image(x,y+2))/2 - red image(x,y));
257 -
                 vertical gradient = abs((red image(x-2,y)+red image(x+2,y))/2 - red image(x,y));
258 -
                 if(horizontal gradient<vertical gradient)</pre>
259 -
                     mosim(x,y,2) = (green(x,y-1)+green(x,y+1))/2;
260 -
                 elseif (horizontal_gradient>vertical_gradient)
261 -
                      mosim(x,y,2) = (green(x-1,y)+green(x+1,y))/2;
262 -
263 -
                     mosim(x,y,2) = (green(x-1,y) + green(x+1,y) + green(x,y-1) + green(x,y+1))/4;
264 -
                 end
265 -
             end
266 -
       - end
```

```
267 - for x = 4:2: (imageWidth-2)
268 - for y = 4:2: (imageHeight-2)
                horizontal gradient = abs((blue image(x,y-2)+blue image(x,y+2))/2 - blue image(x,y));
269 -
270 -
                vertical gradient = abs((blue image(x-2,y)+blue image(x+2,y))/2 - blue image(x,y));
271 -
                if (horizontal_gradient<vertical_gradient)
272 -
                   mosim(x,y,2) = (green(x,y-1)+green(x,y+1))/2;
273 -
                elseif (horizontal_gradient>vertical_gradient)
274 -
                    mosim(x, y, 2) = (green(x-1, y) + green(x+1, y))/2;
275 -
276 -
                    mosim(x,y,2) = (green(x-1,y) + green(x+1,y) + green(x,y-1) + green(x,y+1))/4;
277 -
278 -
            end
279 -
280
281
        %deducing the blue pixels at missing points
282 -
        blue_1 = imfilter(blue_image, [1 0 1;0 0 0;1 0 1]/4);
283 -
        blue_2 = imfilter(blue_image, [0 1 0;1 0 1;0 1 0]/2);
284 -
        blue = blue_image+blue_1+blue_2;
285
286
        %deducing the red pixels at missing points
287 -
        red_1 = imfilter(red_image, [1 0 1;0 0 0;1 0 1]/4);
288 -
        red 2 = imfilter(red image, [0 1 0;1 0 1;0 1 0]/2);
289 -
        red = red_image+red_1+red_2;
290
291 -
        mosim(:,:,1) = red;
292 -
       mosim(:,:,3) = blue;
```

## **Results**

The figure shows the errors for the three different methods implemented, for the 10 given images. It is seen that these methods produce significantly better results the baseline model of demosaicing.

```
Command Window
  >> evalDemosaicing
      image baseline nn linear adagrad
  #
  1
      balloon.jpeg 0.179239 0.026872 0.016389 0.016101
      cat.jpg 0.099966 0.027676 0.014445 0.014887
ip.jpg 0.231587 0.029006 0.018174 0.024435
puppy.jpg 0.094093 0.020216 0.008351 0.008254
  2
  3
  4
      squirrel.jpg 0.121964 0.042743 0.024781
  5
                     0.181449 0.030610 0.017935
  6
                                                       0.018425
      pencils.jpg
  7
      house.png 0.117667 0.034542 0.018978 0.018178
      light.png 0.097868 0.032120 0.018538
                                                  0.018115
  8
      sails.png 0.074946 0.027171 0.015554
  9
                                                   0.014718
  10 tree.jpeg 0.167812 0.032858 0.018794 0.018224
      average 0.136659 0.030381 0.017194 0.017610
f_{x} >>
```

# 2. Image Denoising

# a) Gaussian Filtering

A Gaussian filter with a size of 3x3 was used to filter the image. The error was calculated over a range of sigmas in the range 0.1 to 2 with a step size of 0.1.

```
23
       %% Denoising algorithm (Gaussian filtering)
24 - for sigma = 0.1:0.1:2
25 -
          gaussian_filter=fspecial('gaussian',[3 3],sigma);
26 -
         filtered image1=imfilter(noise1, gaussian filter);
27 -
         filtered image2=imfilter(noise2,gaussian filter);
         error_1=sum(sum((im - filtered_image1).^2));
28 -
         error_2=sum(sum((im - filtered_image2).^2));
29 -
30 -
          fprintf('Sigma, Error 1, Error 2: %.2f %.2f% .2f\n', sigma, error 1, error 2);
31 -
          figure;
32 -
         imshow(filtered_image1);
33 -
         figure;
34 -
          imshow(filtered image2);
35 - end
```

The result for saturn1g and saturn1sp is shown below, where it is seen that sigma = 1.5 gives the minimum error for image 1 while sigma = 2 gives the minimum error for image 2.

```
Command Window
  Input, Errors: 692.66 1982.10
  Sigma, Error 1, Error 2: 0.10 692.66 1982.10
  Sigma, Error 1, Error 2: 0.20 692.64 1982.04
  Sigma, Error 1, Error 2: 0.30 673.67 1923.49
  Sigma, Error 1, Error 2: 0.40 517.21 1439.69
  Sigma, Error 1, Error 2: 0.50 327.15 847.74
  Sigma, Error 1, Error 2: 0.60 230.03 539.03
  Sigma, Error 1, Error 2: 0.70 190.39 407.91
  Sigma, Error 1, Error 2: 0.80 173.84 349.80
  Sigma, Error 1, Error 2: 0.90 166.45 321.63
  Sigma, Error 1, Error 2: 1.00 162.95 306.81
  Sigma, Error 1, Error 2: 1.10 161.25 298.47
  Sigma, Error 1, Error 2: 1.20 160.41 293.53
  Sigma, Error 1, Error 2: 1.30 160.02 290.47
  Sigma, Error 1, Error 2: 1.40 159.87 288.52
  Sigma, Error 1, Error 2: 1.50 159.84 287.23
  Sigma, Error 1, Error 2: 1.60 159.88 286.37
  Sigma, Error 1, Error 2: 1.70 159.95 285.78
  Sigma, Error 1, Error 2: 1.80 160.04 285.37
  Sigma, Error 1, Error 2: 1.90 160.13 285.09
  Sigma, Error 1, Error 2: 2.00 160.22 284.89
```

The result for saturn2g and saturn2sp is shown below, where it is seen that sigma=2 gives the minimum error for both images.

```
Command Window
  >> evalDenoising
  Input, Errors: 3118.10 3829.28
  Sigma, Error 1, Error 2: 0.10 3118.10 3829.28
  Sigma, Error 1, Error 2: 0.20 3118.02 3829.17
  Sigma, Error 1, Error 2: 0.30 3035.40 3718.08
  Sigma, Error 1, Error 2: 0.40 2352.06 2799.31
  Sigma, Error 1, Error 2: 0.50 1513.72 1671.84
  Sigma, Error 1, Error 2: 0.60 1074.49 1080.74
  Sigma, Error 1, Error 2: 0.70 886.96 828.04
  Sigma, Error 1, Error 2: 0.80 803.42 715.24
  Sigma, Error 1, Error 2: 0.90 762.72 660.13
  Sigma, Error 1, Error 2: 1.00 741.19 630.87
  Sigma, Error 1, Error 2: 1.10 729.01 614.25
  Sigma, Error 1, Error 2: 1.20 721.74 604.29
  Sigma, Error 1, Error 2: 1.30 717.22 598.05
  Sigma, Error 1, Error 2: 1.40 714.30 594.00
  Sigma, Error 1, Error 2: 1.50 712.36 591.29
  Sigma, Error 1, Error 2: 1.60 711.04 589.44
  Sigma, Error 1, Error 2: 1.70 710.13 588.15
  Sigma, Error 1, Error 2: 1.80 709.49 587.22
  Sigma, Error 1, Error 2: 1.90 709.04 586.56
  Sigma, Error 1, Error 2: 2.00 708.71 586.07
```

# b) Median Filtering

A median filter of various sizes in the range 1x1 to 5x5 was applied to the image, and the error for every size was calculated.

```
%% Denoising algorithm (Median filtering)
37 - ☐ for m=1:5
38 - for n=1:5
39 -
               filtered image3=medfilt2(noise1,[m n]);
40 -
               filtered image4=medfilt2(noise2,[m n]);
41 -
              error_3=sum(sum((im - filtered_image3).^2));
42 -
               error_4=sum(sum((im - filtered_image4).^2));
43 -
               fprintf('Neighborhood Length, Neighborhood Width, Error 1, Error2: %.2f %.2f %.2f %.2f %.2f %.
44 -
               figure;
45 -
               imshow(filtered_image3);
46 -
              figure;
               imshow(filtered_image4);
47 -
48 -
           end
49 -
       end
```

It is seen from the output of saturn1g and saturn1sp shown below that, for a window size of 5\*5, the error for the first image is minimum and for a patch size of 3\*3, the error for the second image is minimum.

```
Command Window
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 1.00 692.66 1982.10
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 2.00 401.15 1036.15
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 3.00 330.38 171.06
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 4.00 249.92 113.77
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 5.00 228.91 25.80
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 1.00 409.90 1038.08
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 2.00 268.62 138.94
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 3.00 194.99 46.37
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 4.00 177.92 56.58
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 5.00 149.45 42.12
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 1.00 337.92 170.53
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 2.00 191.61 42.02
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 3.00 140.10 8.78
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 4.00 124.81 33.72
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 5.00 103.21 13.04
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 1.00 265.82 123.78
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 2.00 184.58 59.10
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 3.00 135.24 40.28
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 4.00 131.03 58.64
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 5.00 110.24 42.44
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 1.00 248.94 37.60
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 2.00 156.55 42.64
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 3.00 114.65 16.93
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 4.00 111.39 41.20
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 5.00 91.99 19.14
```

It is seen from the output of saturn2g and saturn2sp shown below that, for a window size of 5\*5, the error for the first image is minimum and for a patch size of 3\*3, the error for the second image is minimum.

```
Command Window
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 1.00 3118.10 3829.28
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 2.00 1774.52 2006.83
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 3.00 1501.92 588.17
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 4.00 1067.96 349.06
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 1.00 5.00 1009.07 114.94
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 1.00 1771.96 2022.16
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 2.00 1081.48 358.80
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 3.00 787.15 97.89
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 4.00 649.61 70.63
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 2.00 5.00 544.01 53.63
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 1.00 1508.59 575.92
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 2.00 786.14 86.84
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 3.00 607.87 18.57
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 4.00 465.09 40.96
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 3.00 5.00 407.90 20.69
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 1.00 1078.95 345.44
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 2.00 653.38 73.16
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 3.00 472.08 47.65
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 4.00 397.44 67.55
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 4.00 5.00 336.20 50.32
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 1.00 1022.67 130.62
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 2.00 554.46 51.39
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 3.00 418.22 24.63
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 4.00 338.60 48.78
  Neighborhood Length, Neighborhood Width, Error 1, Error2: 5.00 5.00 292.39 25.26
```

## c) Non-local Means Filtering

The non-local means filter takes the mean of all the neighboring pixels of an image in a window, weighted by how similar the pixels are to the target pixel.

The function shown below, implements a non-linear filter kernel, where the weight of the pixel in a patch reduces by a factor of (2\*distance+1)<sup>2</sup>. Therefore, the center pixel is weighed the highest, and as we move away from the center, the pixel weights are reduced by this factor.

```
_evalDenoising.m × evalDenoising.m × evalDenoising.m ×
                                                                                                        nl means.m ×
                              × gaussian.m × med.m ×
     function [means_kernel] = nl_means(patch_size)
       means_kernel = zeros(2*patch_size+1, 2*patch_size+1);
     for distance = 1:patch size
3 -
          weight = (1/(2*distance+1))^2;
5 -
           for x=-distance:distance
              for y=-distance:distance
7 -
                  means kernel(patch size+1-x,patch size+1-y)=means kernel(patch size+1-x,patch size+1-y)+weight;
8 -
9 -
          end
10 -
      end
       means_kernel = means_kernel./patch_size;
```

The function implemented below, denoises the image using the non-local means algorithm described in the work of Buades. et al [1]. In this, first, a non-linear kernel of a size equal to the patch size is created. Then two patches around the two target pixels are created in a window, taking appropriate limits for the boundaries of the window.

After that, the sum of squared differences between the two patches is calculated, weighted by the non-linear kernel.

A Gaussian weighing function [2], defined by

$$weight = e^{\frac{-|P(x)-P(y)|^2}{\gamma^2}}$$

was calculated, and was multiplied to the image pixel at each point in the patch and was stored as an cumulative sum. The denoised image was this cumulative sum divided by the cumulative sum of the weighing factors.

```
🕤 🗙 🌠 Variables - filtered_image2
 +27 NLmeansfilter.m × gaussian.m × med.m × __evalDenoising.m × evalDenoising.m × evalDenoising.m × evalDenoising.m × | nl_mean_out.m × +
      function [denoised image] = nl mean out(image in, window size, patch size, gamma)
3 -
       [imageWidth, imageHeight]=size(image in);
 4 -
       denoised_image = zeros(imageWidth,imageHeight);
 5 -
       image_in = padarray(image_in,[patch_size,patch_size],'circular');
       nl_kernel = nl_means(patch_size);
 8 -
       nl_kernel = nl_kernel/sum(sum(nl_kernel));
 9
10 -
       squared_gamma = gamma*gamma;
11
12 -  for x = 1:imageWidth
13 -
          for y = 1:imageHeight
14
15 -
               x_new = x+patch_size;
               y_new = y+patch_size;
16 -
17
18 -
               wind_1 = image_in(x_new-patch_size:x_new+patch_size,y_new-patch_size:y_new+patch_size);
19
20 -
               wind max = 0;
21 -
               ave = 0;
22 -
               s_cum = 0;
23
24 -
               min_r = max(x_new-window_size,patch_size+1);
25 -
               max_r = min(x_new+window_size, imageWidth+patch_size);
26 -
               min_s = max(y_new-window_size, patch_size+1);
27 -
               max_s = min(y_new+window_size, imageHeight+patch_size);
28
28
29 -
               for i = min_r:max_r
30 -
                   for j = min_s:max_s
31
32 -
                        if(i==x_new && j==y_new)
33 -
                           continue;
34 -
36 -
                        wind 2 = image in(i-patch size:i+patch size, j-patch size);
37
                       diff = sum(sum(nl_kernel.*(wind_1-wind_2).*(wind_1-wind_2)));
38 -
39
40 -
                        weigh_param = exp(-diff/squared_gamma);
41
42 -
                        if weigh param > wind max
43 -
                           wind max = weigh param;
44 -
45
46 -
                        s_cum = s_cum+weigh_param;
47 -
                        ave = ave +weigh_param*image_in(i,j);
48 -
                   end
49 -
               end
50
               ave = ave + wind_max*image_in(x_new,y_new);
51 -
52 -
               s_cum = s_cum + wind max;
53
54 -
               if s cum > 0
55 -
                    denoised_image(x,y) =ave/s_cum;
56 -
57 -
                   denoised_image(x,y) = image_in(x,y);
58 -
               end
59 -
           end
60 -
      end
61 -
       figure;
62 -
       imshow(denoised_image);
63 -
```

In the main function, the function which performs non-local means, defined above is called, with different values of window size, patch size and gamma. It is seen that the following values of window, size, patch size and gamma produce the least error for the two noisy images.

```
%% Denoising alogirthm (Non-local means)
51
52 - filtered_image5 = nl_mean_out(noise1, 8, 2, 0.1);
53 - filtered_image6 = nl_mean_out(noise2, 4, 2, 0.25);
54 - error_5=sum(sum((im - filtered_image5).^2));
55 - error_6=sum(sum((im - filtered_image6).^2));
56 - fprintf('Error 1, Error2: %.2f %.2f\n', error_5,error_6);
57
```

#### Error for saturn1g and saturn1sp

```
Command Window

>> evalDenoising
Input, Errors: 692.66 1982.10
Error 1, Error2: 97.17 123.96

Error for saturn2g and saturn2sp

Command Window
Error 1, Error2: 946.26 262.98
>>
```

# **Qualitative Comparison of the Denoising Algorithm**

The table shown below compares the minimum noises obtained by the various algorithms for the given images.

Algorithm and Parameters	Error for Saturn1g		Error for Saturn1sp	
Gaussian filter	Sigma	Error	Sigma	Error
	1.5	159.84	2	284.89
Median filter	Window Size	Error	Window Size	Error
	5*5	8.78	3*3	91.19
Non local means filter	Window Size Patch Size Gamma	Error	Widow Size Patch Size Gamma	Error
	8 2 0.1	97.17	4 2 0.25	123.96

Algorithm and Parameters	Error for Saturn2g		Error for Saturn2sp	
Gaussian filter	Sigma	Error	Sigma	Error
	2	708.71	2	586.07
Median filter	Window Size	Error	Window Size	Error
	5*5	292.39	3*3	18.57
Non local means filter	Window Size	Error	Widow Size	Error
	Patch Size		Patch Size	
	Gamma		Gamma	
	8	514.91	4	262.98
	2		2	
	0.25		0.25	

It is seen that, median filtering produces the best results for all the images, because, median filtering handles the outliers in a more efficient way.

# 3. Extension 1

# a) Linear Transformation of Color Spaces

The implementation of this is similar to the one done in Color Demosaicing (Question 1) apart from the transformation of color spaces.

```
📝 Editor - C:\Users\User\Documents\UMass Amherst\Semester 1\COMPSCI 670 - Computer Vision\Mini Projects\2\p2_code\code\demosaicImage.m
294
295
                                  Transformed Color Spaces - Linear
296
     ☐ function mosim = demosaicTransformation(im)
298
        [imageWidth,imageHeight]=size(im);
300 -
301
        %creating masks for the bayer pattern
302
303 -
       bayer_red = repmat([1 0; 0 0], ceil(imageWidth/2),ceil(imageHeight/2));
304 -
       {\tt bayer\_blue = repmat([0\ 0;\ 0\ 1],\ ceil(imageWidth/2),ceil(imageHeight/2));}
305 -
       bayer_green = repmat([0 1; 1 0], ceil(imageWidth/2),ceil(imageHeight/2));
306
307
        %truncating the extra pixels at the edges
308 -
       if(mod(imageWidth,2))==1
309 -
          bayer_red(size(bayer_red,1),:)=[];
310 -
          bayer_blue(size(bayer_blue,1),:)=[];
311 -
          bayer_green(size(bayer_green,1),:)=[];
312 -
313 -
       if (mod(imageHeight,2)==1)
314 -
         bayer red(:,size(bayer red,2))=[];
315 -
          bayer blue(:,size(bayer blue,2))=[];
316 -
          bayer green(:,size(bayer green,2))=[];
317 -
```

The red and blue channels are divided by the green channels, after replacing the green pixels with value zero with the next minimum value in the green matrix.

```
📝 Editor - C:\Users\User\Documents\UMass Amherst\Semester 1\COMPSCI 670 - Computer Vision\Mini Projects\2\p2_code\code\demosaicImage.m
 +26 prepareData.m × alignChannels.m × HW3.m × convolution.m × run.m × first.m × p2_latex.tar.gz × demosaicImage.m ×
         %extracting the red, green and blue components of the image using the mask
319
320
321 -
         red image = im.*bayer red;
322 -
         blue image = im.*bayer blue;
323 -
         green_image = im.*bayer_green;
324
325
         %deducing the green pixels at missing points
326 -
         green = green_image + imfilter(green_image, [0 1 0;1 0 1; 0 1 0]/4);
327
328
         %checking for pixel values to be zero and correcting it
329 -
         min_green = min(min(green(green~=0)));
330 -
         green(green==0) = min_green;
331
332
         %transforming the images
333 -
         red image = red image./green;
334 -
         red image = red image.*bayer red;
335
336 -
         blue_image = blue_image./green;
337 -
         blue_image = blue_image.*bayer_blue;
```

After demosaicing, the color spaces are transformed back to the original color space by applying the inverse transformation.

```
📝 Editor - C.\Users\User\Documents\UMass Amherst\Semester 1\COMPSCI 670 - Computer Vision\Mini Projects\2\p2_code\code\demosaicImage.n
+26 prepareData.m × alignChannels.m × HW3.m × convolution.m × run.m × first.m × p2_latex.tar.gz × demosaicImage.m × +
339
         %deducing the red pixels at missing points
340 -
        red_1 = imfilter(red_image, [1 0 1; 0 0 0; 1 0 1]/4);
341 -
        red_2 = imfilter(red_image, [0 1 0;1 0 1;0 1 0]/2);
342 -
        red = red_image+red_1+red_2;
343
344
         %deducing the blue pixels at missing points
345 -
        blue_1 = imfilter(blue_image, [1 0 1;0 0 0;1 0 1]/4);
346 -
        blue 2 = imfilter(blue image, [0 1 0;1 0 1;0 1 0]/2);
347 -
        blue = blue_image+blue_1+blue_2;
348
349
        %applying inverse transformation
350 -
        mosim(:,:,1) = red.*green;
351 -
        mosim(:,:,2) = green;
       mosim(:,:,3) = blue.*green;
352 -
```

# b) Logarithmic Transformation of Color Spaces

The implementation of this is similar to the one done in Color Demosaicing (Question 1) apart from the transformation of color spaces.

```
🗾 Editor - C:\Users\User\Documents\UMass Amherst\Semester 1\COMPSCI 670 - Computer Vision\Mini Projects\2\p2_code\code\demosaicImage.m
 +26 prepareData.m × alignChannels.m × HW3.m × convolution.m × run.m × first.m × p2_latex.tar.gz × demosaicImage.m × +
354
355
                                      Transformed Color Spaces - Logarithmic
356
      Function mosim = demosaicLogTransformation(im)
357
358
         %mosim = demosaicBaseline(im);
359
360 -
         [imageWidth,imageHeight]=size(im);
361
         %creating masks for the bayer pattern
362
363 -
        bayer_red = repmat([1 0; 0 0], ceil(imageWidth/2),ceil(imageHeight/2));
364 -
        bayer_blue = repmat([0 0; 0 1], ceil(imageWidth/2),ceil(imageHeight/2));
365 -
        bayer_green = repmat([0 1; 1 0], ceil(imageWidth/2),ceil(imageHeight/2));
366
367
         %truncating the extra pixels at the edges
368 -
        if (mod(imageWidth,2)) ==1
369 -
           bayer_red(size(bayer_red,1),:)=[];
370 -
           bayer blue(size(bayer blue,1),:)=[];
371 -
           bayer green(size(bayer green,1),:)=[];
372 -
373 -
        if (mod (imageHeight, 2) == 1)
374 -
           bayer_red(:,size(bayer red,2))=[];
375 -
           bayer blue(:,size(bayer blue,2))=[];
376 -
           bayer_green(:,size(bayer_green,2))=[];
377 -
378
```

The red and blue channels are divided by the green channels and the logarithm of the ratio is taken. In this case, none of the channel values can be zero, so the pixels with a value of zero are replaced with the next minimum value.

After demosaicing, the color spaces are transformed back to the original color space by applying the inverse transformation.

```
💋 Editor - C:\Users\User\Documents\UMass Amherst\Semester 1\COMPSCI 670 - Computer Vision\Mini Projects\2\p2_code\code\demosaicImage.m
 +26 prepareData.m × alignChannels.m × HW3.m × convolution.m × run.m × first.m × p2_latex.tar.gz × demosaicImage.m × +
         %extracting the red, green and blue components of the image using the mask
379
380
381 -
         green_image = im.*bayer_green;
382 -
        blue_image = im.*bayer_blue;
383 -
         red_image = im.*bayer_red;
384
385
         %deducing the green pixels at missing points
386 -
         green = green_image + imfilter(green_image, [0 1 0;1 0 1; 0 1 0]/4);
387
388
         %checking for pixel values to be zero and correcting it
389 -
        min green = min(min(green(green~=0)));
        green(green==0) = min_green;
390 -
391
392 -
        min_blue = min(min(blue_image(blue_image~=0)));
393 -
        blue_image(blue_image==0) = min_blue;
394
395 -
        min_red = min(min(red_image(red_image~=0)));
396 -
         red_image(red_image==0) = min_red;
397
398
         %transforming the images
399 -
         red image = log(red image./green);
         red_image = red_image.*bayer_red;
400 -
401
402 -
        blue image = log(blue image./green);
403 -
        blue_image = blue_image.*bayer_blue;
404
         %deducing the red pixels at missing points
405
        red_1 = imfilter(red_image, [1 0 1;0 0 0;1 0 1]/4);
406 -
407 -
        red 2 = imfilter(red_image, [0 1 0;1 0 1;0 1 0]/2);
408 -
        red = red_image+red_1+red_2;
409
410
        deducing the blue pixels at missing points
411 -
        blue_1 = imfilter(blue_image, [1 0 1;0 0 0;1 0 1]/4);
412 -
        blue_2 = imfilter(blue_image, [0 1 0;1 0 1;0 1 0]/2);
413 -
        blue = blue_image+blue_1+blue_2;
414
415
        %applying the inverse transformation
416 -
        mosim(:,:,1) = exp(red).*green;
417 -
        mosim(:,:,2) = green;
        mosim(:,:,3) = exp(blue).*green;
418 -
```

#### **Results**

	=				adagrad	_	s log_trans
							0.021362
	cat.jpg	0.099966	0.027676	0.014445	0.014887	0.012443	0.011917
	ip.jpg	0.231587	0.029006	0.018174	0.024435	0.018852	0.018668
	puppy.jpg	0.094093	0.020216	0.008351	0.008254	0.008699	0.007259
	squirrel.jp	g 0.12196	0.0427	43 0.0247	81 0.0247	56 0.01998	0.019200
	pencils.jpg	0.18144	9 0.0306	10 0.0179	35 0.0184	25 0.01910	0.019217
	house.png	0.117667	0.034542	0.018978	0.018178	0.016336	0.015066
	light.png	0.097868	0.032120	0.018538	0.018115	0.016069	0.015438
	sails.png	0.074946	0.027171	0.015554	0.014718	0.014198	0.012822
0	tree.jpeg	0.167812	0.032858	0.018794	0.018224	0.018014	0.016034

From the results shown in the figure above, we see that linear and logarithmic transformation of color spaces do produce significantly better results than other methods. So, it can be a

good idea to implement color space transformation to images, if the computational complexity of computing the transformation (dividing and taking logarithms and their inverses) is not of a major concern to the system it is being developed for.

### References

[1]. Buades, Antoni (20–25 June 2005). "A non-local algorithm for image denoising". *Computer Vision and Pattern Recognition*, 2005. **2**: 60–65. <u>doi:10.1109/CVPR.2005.38</u>

[2] https://en.wikipedia.org/wiki/Non-local\_means

# Appendix 1: Code for Color Image Demosaicing with Extension 1

```
function output = demosaicImage(im, method)
% DEMOSAICIMAGE computes the color image from mosaiced
input
% OUTPUT = DEMOSAICIMAGE(IM, METHOD) computes a
demosaiced OUTPUT from
% the input IM. The choice of the interpolation METHOD
can be
   'baseline', 'nn', 'linear', 'adagrad'.
% This code is part of:
% CMPSCI 670: Computer Vision
  University of Massachusetts, Amherst
   Instructor: Subhransu Maji
응
000
switch lower(method)
   case 'baseline'
       output = demosaicBaseline(im);
   case 'nn'
       output = demosaicNN(im); % Implement this
   case 'linear'
       output = demosaicLinear(im); % Implement this
   case 'adagrad'
       output = demosaicAdagrad(im); % Implement this
   case 'transformation'
       output = demosaicTransformation(im); % Extra
Implementation
   case 'log transformation'
       output = demosaicLogTransformation(im); % Extra
Implementation
end
                         Baseline demosacing algorithm.
                         The algorithm replaces missing
values with the
                        mean of each color channel.
%_____
function mosim = demosaicBaseline(im)
```

```
mosim = repmat(im, [1 1 3]); % Create an image by
stacking the input
[imageHeight, imageWidth] = size(im);
% Red channel (odd rows and columns);
redValues = im(1:2:imageHeight, 1:2:imageWidth);
meanValue = mean(mean(redValues));
mosim(:,:,1) = meanValue;
mosim(1:2:imageHeight, 1:2:imageWidth,1) =
im(1:2:imageHeight, 1:2:imageWidth);
% Blue channel (even rows and colums);
blueValues = im(2:2:imageHeight, 2:2:imageWidth);
meanValue = mean(mean(blueValues));
mosim(:,:,3) = meanValue;
mosim(2:2:imageHeight, 2:2:imageWidth,3) =
im(2:2:imageHeight, 2:2:imageWidth);
% Green channel (remaining places)
% We will first create a mask for the green pixels (+1
green, -1 not green)
mask = ones(imageHeight, imageWidth);
mask(1:2:imageHeight, 1:2:imageWidth) = -1;
mask(2:2:imageHeight, 2:2:imageWidth) = -1;
greenValues = mosim(mask > 0);
meanValue = mean(greenValues);
% For the green pixels we copy the value
greenChannel = im;
greenChannel(mask < 0) = meanValue;</pre>
mosim(:,:,2) = greenChannel;
                          Nearest neighbour algorithm
%_____
function mosim = demosaicNN(im)
%mosim = demosaicBaseline(im);
[imageWidth, imageHeight] = size(im);
%creating masks for the bayer pattern
bayer red = repmat([1 0; 0 0],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer blue = repmat([0\ 0;\ 0\ 1],
ceil(imageWidth/2), ceil(imageHeight/2));
```

```
bayer green = repmat([0 1; 1 0],
ceil(imageWidth/2),ceil(imageHeight/2));
%truncating the extra pixels at the edges
if (mod(imageWidth, 2)) ==1
   bayer red(size(bayer red,1),:)=[];
   bayer blue(size(bayer blue,1),:)=[];
   bayer green(size(bayer green,1),:)=[];
if (mod (imageHeight, 2) ==1)
   bayer red(:,size(bayer red,2))=[];
   bayer blue(:, size(bayer blue, 2)) = [];
   bayer green(:,size(bayer green,2))=[];
end
%extracting the red, green and blue components of the
image using the mask
red image = im.*bayer red;
blue image = im.*bayer blue;
green image = im.*bayer green;
%deducing the green pixels at missing points
green = green image+imfilter(green image,[0 1]);
%deducing the red pixels at missing points
redValue=im(1:2:imageWidth,1:2:imageHeight);
meanRed = mean(mean(redValue));
%red@blue
red 1 = imfilter(red image, [0 0;0 1], meanRed);
%red@green
red 2 = imfilter(red image, [0 1;1 0], meanRed);
%combine
red = red image + red 1 +red 2;
%deducing the blue pixels at missing points
blueValue=im(1:2:imageWidth,1:2:imageHeight);
meanBlue = mean(mean(blueValue));
%blue@red
blue 1 = imfilter(blue image, [0 0;0 1], meanBlue);
%blue@green
blue 2 = imfilter(blue image, [0 1;1 0], meanBlue);
%combine
blue = blue image + blue 1 +blue 2;
mosim(:,:,1) = red;
mosim(:,:,2) = green;
```

```
mosim(:,:,3) = blue;
   -----
                            Linear interpolation
function mosim = demosaicLinear(im)
% mosim = demosaicBaseline(im);
% mosim = repmat(im, [1 1 3]);
[imageWidth, imageHeight] = size(im);
%creating masks for the bayer pattern
bayer red = repmat([1 0; 0 0],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer blue = repmat([0\ 0;\ 0\ 1],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer green = repmat([0 1; 1 0],
ceil(imageWidth/2),ceil(imageHeight/2));
%truncating the extra pixels at the edges
if (mod (imageWidth, 2)) ==1
   bayer red(size(bayer red, 1),:)=[];
   bayer blue(size(bayer blue,1),:)=[];
   bayer green(size(bayer green,1),:)=[];
end
if (mod (imageHeight, 2) ==1)
   bayer red(:,size(bayer red,2))=[];
   bayer blue(:, size(bayer blue, 2)) = [];
   bayer green(:,size(bayer green,2))=[];
end
%extracting the red, green and blue components of the
image using the mask
red image = im.*bayer red;
blue image = im.*bayer blue;
green image = im.*bayer green;
%deducing the green pixels at missing points
green = green image + imfilter(green image, [0 1 0;1 0 1;
0 \ 1 \ 01/4);
%deducing the red pixels at missing points
red 1 = imfilter(red image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
red 2 = imfilter(red image, [0\ 1\ 0; 1\ 0\ 1; 0\ 1\ 0]/2);
red = red image+red 1+red 2;
```

```
%deducing the blue pixels at missing points
blue 1 = imfilter(blue image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
blue 2 = imfilter(blue image, [0\ 1\ 0; 1\ 0\ 1; 0\ 1\ 0]/2);
blue = blue image+blue 1+blue 2;
mosim(:,:,1) = red;
mosim(:,:,2) = green;
mosim(:,:,3) = blue;
%______
                      Adaptive gradient
function mosim = demosaicAdagrad(im)
mosim = demosaicBaseline(im);
[imageWidth, imageHeight] = size(im);
%creating masks for the bayer pattern
bayer red = repmat([1 0; 0 0],
ceil(imageWidth/2), ceil(imageHeight/2));
bayer blue = repmat([0\ 0;\ 0\ 1],
ceil(imageWidth/2), ceil(imageHeight/2));
bayer green = repmat([0 1; 1 0],
ceil(imageWidth/2),ceil(imageHeight/2));
%truncating the extra pixels at the edges
if (mod(imageWidth, 2)) == 1
   bayer red(size(bayer red, 1),:)=[];
   bayer blue(size(bayer blue,1),:)=[];
   bayer green(size(bayer green,1),:)=[];
end
if (mod (imageHeight, 2) ==1)
   bayer red(:, size(bayer red, 2)) = [];
   bayer blue(:, size(bayer blue, 2)) = [];
   bayer green(:,size(bayer green,2))=[];
end
%extracting the red, green and blue components of the
image using the mask
red image = im.*bayer red;
blue image = im.*bayer blue;
green image = im.*bayer green;
%deducing the green pixels at the missing points
```

```
green = green image + imfilter(green image, [0 1 0; 1 0
1; 0 1 01);
for x = 3:2: (imageWidth-2)
    for y = 3:2:(imageHeight-2)
         horizontal gradient = abs((red image(x,y-
2) + red image (x, y+2) / 2 - red image (x, y);
         vertical gradient = abs((red image(x-
(x,y) + red image(x+2,y))/2 - red image(x,y);
         if (horizontal gradient<vertical gradient)</pre>
             mosim(x, y, 2) = (green(x, y-1) + green(x, y+1))/2;
         elseif (horizontal gradient>vertical gradient)
              mosim(x,y,2) = (green(x-1,y) + green(x+1,y))/2;
         else
             mosim(x, y, 2) = (qreen(x-
1, y) +green (x+1, y) +green (x, y-1) +green (x, y+1)) /4;
    end
end
for x = 4:2: (imageWidth-2)
    for y = 4:2:(imageHeight-2)
         horizontal gradient = abs((blue image(x,y-
2) +blue image((x, y+2))/2 - blue image((x, y));
         vertical gradient = abs((blue image(x-
(x,y) + blue image(x+2,y))/2 - blue_image(x,y));
         if (horizontal gradient<vertical gradient)</pre>
             mosim(x, y, 2) = (green(x, y-1) + green(x, y+1))/2;
         elseif (horizontal gradient>vertical gradient)
              mosim(x,y,2) = (green(x-1,y) + green(x+1,y))/2;
         else
             mosim(x, y, 2) = (green(x-
(x, y) + green(x+1, y) + green(x, y-1) + green(x, y+1)) / 4;
         end
    end
end
%deducing the blue pixels at missing points
blue 1 = imfilter(blue image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
blue 2 = imfilter(blue image, [0 \ 1 \ 0; 1 \ 0 \ 1; 0 \ 1 \ 0]/2);
blue = blue image+blue 1+blue 2;
%deducing the red pixels at missing points
red 1 = imfilter(red image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
red 2 = imfilter(red image, [0\ 1\ 0; 1\ 0\ 1; 0\ 1\ 0]/2);
red = red image+red 1+red 2;
mosim(:,:,1) = red;
mosim(:,:,3) = blue;
```

```
Transformed Color Spaces - Linear
%-----
function mosim = demosaicTransformation(im)
 %mosim = demosaicBaseline(im);
[imageWidth, imageHeight] = size(im);
%creating masks for the bayer pattern
bayer red = repmat([1 0; 0 0],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer blue = repmat([0\ 0;\ 0\ 1],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer green = repmat([0 1; 1 0],
ceil(imageWidth/2),ceil(imageHeight/2));
%truncating the extra pixels at the edges
if (mod (imageWidth, 2)) ==1
  bayer red(size(bayer red, 1),:)=[];
  bayer blue(size(bayer blue,1),:)=[];
  bayer green(size(bayer green,1),:)=[];
end
if (mod (imageHeight, 2) == 1)
  bayer red(:, size(bayer red, 2)) = [];
  bayer blue(:, size(bayer blue, 2)) = [];
  bayer green(:,size(bayer green,2))=[];
end
%extracting the red, green and blue components of the
image using the mask
red image = im.*bayer red;
blue image = im.*bayer blue;
green image = im.*bayer green;
%deducing the green pixels at missing points
green = green image + imfilter(green image, [0 1 0;1 0 1;
0 \ 1 \ 0]/4);
%checking for pixel values to be zero and correcting it
min green = min(min(green(green~=0)));
green(green==0) = min green;
%transforming the images
red image = red image./green;
```

```
red image = red image.*bayer red;
blue image = blue image./green;
blue image = blue image.*bayer blue;
%deducing the red pixels at missing points
red 1 = imfilter(red image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
red 2 = imfilter(red image, [0\ 1\ 0; 1\ 0\ 1; 0\ 1\ 0]/2);
red = red image+red 1+red 2;
%deducing the blue pixels at missing points
blue 1 = imfilter(blue image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
blue 2 = imfilter(blue image, [0 \ 1 \ 0; 1 \ 0 \ 1; 0 \ 1 \ 0]/2);
blue = blue image+blue 1+blue 2;
%applying inverse transformation
mosim(:,:,1) = red.*green;
mosim(:,:,2) = green;
mosim(:,:,3) = blue.*green;
%______
            Transformed Color Spaces - Logarithmic
function mosim = demosaicLogTransformation(im)
 %mosim = demosaicBaseline(im);
[imageWidth, imageHeight] = size(im);
%creating masks for the bayer pattern
bayer red = repmat([1 0; 0 0],
ceil(imageWidth/2), ceil(imageHeight/2));
bayer blue = repmat([0\ 0;\ 0\ 1],
ceil(imageWidth/2),ceil(imageHeight/2));
bayer green = repmat([0 1; 1 0],
ceil(imageWidth/2),ceil(imageHeight/2));
%truncating the extra pixels at the edges
if (mod (imageWidth, 2)) ==1
   bayer red(size(bayer red, 1),:)=[];
   bayer blue(size(bayer blue,1),:)=[];
   bayer green(size(bayer green,1),:)=[];
end
if (mod (imageHeight, 2) == 1)
   bayer red(:, size(bayer red, 2)) = [];
   bayer blue(:, size(bayer blue, 2)) = [];
   bayer green(:,size(bayer green,2))=[];
```

#### end

```
%extracting the red, green and blue components of the
image using the mask
green image = im.*bayer green;
blue image = im.*bayer blue;
red image = im.*bayer red;
%deducing the green pixels at missing points
green = green image + imfilter(green image, [0 1 0;1 0 1;
0 \ 1 \ 01/4);
%checking for pixel values to be zero and correcting it
min green = min(min(green(green~=0)));
green(green==0) = min green;
min blue = min(min(blue image(blue image\sim=0));
blue image(blue image==0) = min blue;
min red = min(min(red image(red image~=0)));
red image(red image==0) = min red;
%transforming the images
red image = log(red image./green);
red image = red image.*bayer red;
blue image = log(blue image./green);
blue image = blue image.*bayer blue;
%deducing the red pixels at missing points
red 1 = imfilter(red image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
red 2 = imfilter(red image, [0\ 1\ 0; 1\ 0\ 1; 0\ 1\ 0]/2);
red = red image+red 1+red 2;
%deducing the blue pixels at missing points
blue 1 = imfilter(blue image, [1 \ 0 \ 1; 0 \ 0 \ 0; 1 \ 0 \ 1]/4);
blue 2 = imfilter(blue image, [0 \ 1 \ 0; 1 \ 0 \ 1; 0 \ 1 \ 0]/2);
blue = blue image+blue 1+blue 2;
%applying the inverse transformation
mosim(:,:,1) = exp(red).*green;
mosim(:,:,2) = green;
mosim(:,:,3) = exp(blue).*green;
```

```
% Entry code for evaluating demosaicing algorithms
% The code loops over all images and methods, computes
the error and
% displays them in a table.
% This code is part of:
9
   CMPSCI 670: Computer Vision
응
   University of Massachusetts, Amherst
90
    Instructor: Subhransu Maji
% Path to your data directory
dataDir = fullfile('C:','Users','User','Documents','Umass
Amherst', 'Semester 1', 'COMPSCI 670 - Computer
Vision','Mini Projects','2','p2 data','data','demosaic');
% Path to your output directory
outDir = fullfile('C:','Users','User','Documents','Umass
Amherst', 'Semester 1', 'COMPSCI 670 - Computer
Vision', 'Mini
Projects','2','p2 code','output','demosaic');
if ~exist(outDir, 'file')
    mkdir(outDir);
end
% List of images
imageNames = {'balloon.jpeg', 'cat.jpg',
'ip.jpg', 'puppy.jpg', 'squirrel.jpg', ...
              'pencils.jpg',
                             'house.png', 'light.png',
'sails.png', 'tree.jpeg'};
numImages = length(imageNames);
% List of methods you have to implement
methods = {'baseline', 'nn', 'linear', 'adagrad',
'transformation','log transformation'};
numMethods = length(methods);
% Global variables
display = false;
error = zeros(numImages, numMethods);
% Loop over methods and print results
fprintf([repmat('-',[1 100]),'\n']);
fprintf('# \t image \t\t baseline \t nn \t\t linear \t
adagrad \t linear trans \t log trans \n');
fprintf([repmat('-',[1 100]),'\n']);
```

```
for i = 1:numImages,
    fprintf('%i \t %s ', i, imageNames{i});
    for j = 1:numMethods,
        thisImage = fullfile(dataDir, imageNames{i});
        thisMethod = methods{j};
        [error(i,j), colorIm] = runDemosaicing(thisImage,
thisMethod, display);
        fprintf('\t %f ', error(i,j));
        % Write the output
        outfileName = fullfile(outDir,
[imageNames{i}(1:end-5) '-' thisMethod '-dmsc.jpg']);
        imwrite(colorIm, outfileName);
    end
    fprintf('\n');
end
% Compute average errors
fprintf([repmat('-',[1 100]),'\n']);
fprintf(' \t %s ', 'average');
for j = 1:numMethods,
        fprintf('\t %f ', mean(error(:,j)));
end
fprintf('\n');
fprintf([repmat('-',[1 100]),'\n']);
```

# **Appendix 2: Code for Image Denoising**

```
% This code is part of:
9
    CMPSCI 670: Computer Vision
9
    University of Massachusetts, Amherst
9
9
    Instructor: Subhransu Maji
% Load images
im = im2double(imread('C:/Users/User/Documents/UMass
Amherst/Semester 1/COMPSCI 670 - Computer Vision/Mini
Projects/2/p2 data/data/denoising/saturn.png'));
noise1 = im2double(imread('C:/Users/User/Documents/UMass
Amherst/Semester 1/COMPSCI 670 - Computer Vision/Mini
Projects/2/p2 data/data/denoising/saturn-noise2g.png'));
noise2 = im2double(imread('C:/Users/User/Documents/UMass
Amherst/Semester 1/COMPSCI 670 - Computer Vision/Mini
Projects/2/p2 data/data/denoising/saturn-noise2sp.png'));
% Compute errors
error1 = sum(sum((im - noise1).^2));
error2 = sum(sum((im - noise2).^2));
fprintf('Input, Errors: %.2f %.2f\n', error1, error2)
% Display the images
figure(1);
subplot(1,3,1); imshow(im); title('Input');
subplot(1,3,2); imshow(noise1); title(sprintf('SE %.2f',
error1));
subplot(1,3,3); imshow(noise2); title(sprintf('SE %.2f',
error2));
%% Denoising algorithm (Gaussian filtering)
for sigma = 0.1:0.1:2
    gaussian filter=fspecial('gaussian',[3 3],sigma);
    filtered image1=imfilter(noise1,gaussian filter);
    filtered image2=imfilter(noise2, gaussian filter);
    error 1=sum(sum((im - filtered image1).^2));
    error 2=sum(sum((im - filtered image2).^2));
    fprintf('Sigma, Error 1, Error 2: %.2f %.2f% .2f\n',
sigma, error 1, error 2);
     figure;
9
      imshow(filtered image1);
     figure;
      imshow(filtered image2);
end
%% Denoising algorithm (Median filtering)
```

```
for m=1:5
    for n=1:5
        filtered image3=medfilt2(noise1,[m n]);
        filtered image4=medfilt2(noise2,[m n]);
        error 3=sum(sum((im - filtered image3).^2));
        error 4=sum(sum((im - filtered image4).^2));
        fprintf('Neighborhood Length, Neighborhood Width,
Error 1, Error2: %.2f %.2f %.2f% .2f\n', m, n,
error 3, error 4);
          figure;
          imshow(filtered image3);
          figure;
          imshow(filtered image4);
    end
end
%% Denoising alogirthm (Non-local means)
filtered image5 = nl mean out(noise1, 10, 2, 0.5);
filtered image6 = nl mean out(noise2, 4, 2, 0.25);
error 5=sum(sum((im - filtered image5).^2));
error 6=sum(sum((im - filtered image6).^2));
fprintf('Error 1, Error2: %.2f %.2f\n', error 5,error 6);
%% Function to build the non-linear kernel
function [means kernel] = nl means(patch size)
means kernel = zeros(2*patch size+1, 2*patch size+1);
for distance = 1:patch size
    weight = (1/(2*distance+1))^2;
    for x=-distance:distance
        for y=-distance:distance
            means kernel(patch size+1-x,patch size+1-
y) = means kernel(patch size+1-x, patch size+1-y) + weight;
        end
    end
means kernel = means kernel./patch size;
end
%% Function to perform non local means denoising
function [denoised image] = nl mean out(image in,
window size, patch size, gamma)
[imageWidth, imageHeight] = size(image in);
denoised image = zeros(imageWidth,imageHeight);
```

```
image in =
padarray(image in,[patch size,patch size],'circular');
nl kernel = nl means(patch size);
nl kernel = nl kernel/sum(sum(nl kernel));
squared gamma = gamma*gamma;
for x = 1:imageWidth
    for y = 1:imageHeight
        x new = x+patch size;
        y new = y+patch size;
        wind 1 = image in(x new-
patch size:x new+patch size,y new-
patch size:y new+patch size);
        wind max = 0;
        ave = 0;
        s cum = 0;
        min r = max(x new-window size,patch_size+1);
        \max r = \min(x \text{ new+window size,})
imageWidth+patch size);
        min s = max(y new-window size, patch size+1);
        \max s = \min(y \text{ new+window size,})
imageHeight+patch size);
        for i = min r:max r
            for j = min s:max s
                 if (i==x new && j==y new)
                     continue;
                 end
                wind 2 = image in(i-
patch size:i+patch size, j-patch size:j+patch size);
                diff = sum(sum(nl kernel.*(wind 1-
wind_2).*(wind 1-wind 2)));
                weigh param = exp(-diff/squared gamma);
                 if weigh param > wind max
                     wind max = weigh param;
                 end
```

```
s_cum = s_cum+weigh_param;
    ave = ave +weigh_param*image_in(i,j);
    end
end

ave = ave + wind_max*image_in(x_new,y_new);
    s_cum = s_cum + wind_max;

if s_cum > 0
        denoised_image(x,y) = ave/s_cum;
else
        denoised_image(x,y) = image_in(x,y);
    end
end
figure;
imshow(denoised_image);
end
```