

Solve the linear programming using the simplex method:

- i. Maximize  $Z = 10x_1 + 6x_2$   
subject to,  
 $6x_1 + 4x_2 \leq 80$   
 $4x_1 + 6x_2 \leq 100$   
where  $x_1, x_2 \geq 0$
- ii. Maximize  $Z = 4x_1 + 8x_2$   
subject to,  
 $x_1 + 2x_2 \leq 5$   
 $x_1 + x_2 \leq 4$   
where  $x_1, x_2 \geq 0$
- iii. Maximize  $Z = 6x_1 + 7x_2$   
subject to,  
 $x_1 - x_2 \leq 12$   
 $x_1 + 3x_2 \leq 18$   
where  $x_1, x_2 \geq 0$
- iv. Minimize  $Z = 6x + 8y$   
With subject to constraints,  
 $4x + 3y \geq 120$   
 $3x + 6y \geq 120$   
Where  $x, y \geq 0$
- v. Minimize  $Z = 60x_1 + 80x_2$   
With subject to constraint,  
 $x_1 \leq 400$   
 $x_2 \geq 200$   
 $x_1 + x_2 = 500$   
where  $x_1, x_2 \geq 0$
- vi. Minimize  $Z = 3x + 2y$   
with subject to constraint,  
 $2x + 4y \geq 10$   
 $4x + 2y \geq 10$   
 $y \geq 4$   
where  $x, y \geq 0$

## Answers

- i.  $x_1 = 13.33, x_2 = 0, \text{Max}(Z) = 133.33$
- ii.  $x_1 = 0, x_2 = 5/2, \text{Max}(Z) = 20$
- iii.  $x_1 = 13.5, x_2 = 1.5, \text{Max}(Z) = 91.5$
- iv.  $x = 24, y = 8, \text{Min}(Z) = 208$
- v.  $x_1 = 300, x_2 = 200, \text{Min}(Z) = 34,000$
- vi.  $x = 4, y = 1/2, \text{Max}(Z) = 13$