

## Linear Programming Problem Procedure

**Step 1:** Formulate the LP Problem.

**Step 2:** Introduce Slack / auxiliary variables.

- If constraint type is  $\leq$  Introduce  $+S$
- If constraint type is  $\geq$  Introduce  $-S + A$
- If constraint type is  $=$  introduce  $A$

**Step 3:** Find the initial basic solution.

**Step 4:** Establish a simplex table and enter all variable coefficients. If the objective function is maximization, enter the opposite sign co-efficient and if minimization, enter without changing the sign.

**Step 5:** Take the most negative coefficient in the objective function,  $Z_j$  to identify the key column (the corresponding variable is the entering variable of the next iteration table).

**Step 6:** Find the ratio between the solution value and the coefficient of the key key column. Enter the values in the minimum ratio column.

**Step 7:** Take the minimum positive value available in the minimum ratio column to identify the key row. (The corresponding variable is the leaving variable of the table).

**Step 8:** The intersection element of the key column and key row is the pivotal element.

**Step 9:** Construct the next iteration table by eliminating the leaving variable and introducing the entering variable.

**Step 10:** Convert the pivotal element as 1 in the next iteration table and compute the other elements in that row accordingly. This is the pivotal equation row (not key row).

**Step 11:** Other elements in the key column must be made zero. For simplicity, form the equations as follows: Change the sign of the key column element, multiply with pivotal equation element and add the corresponding variable.

**Step 12:** Check the values of objective function. If there are negative values, the solution is not an optimal one; go to step 5. Else, if all the values are positive, optimality is reached. Non-negativity for objective function value is not considered. Write down the values of  $x_1, x_2, \dots, x_n$  and calculate the objective function for maximization or minimization.