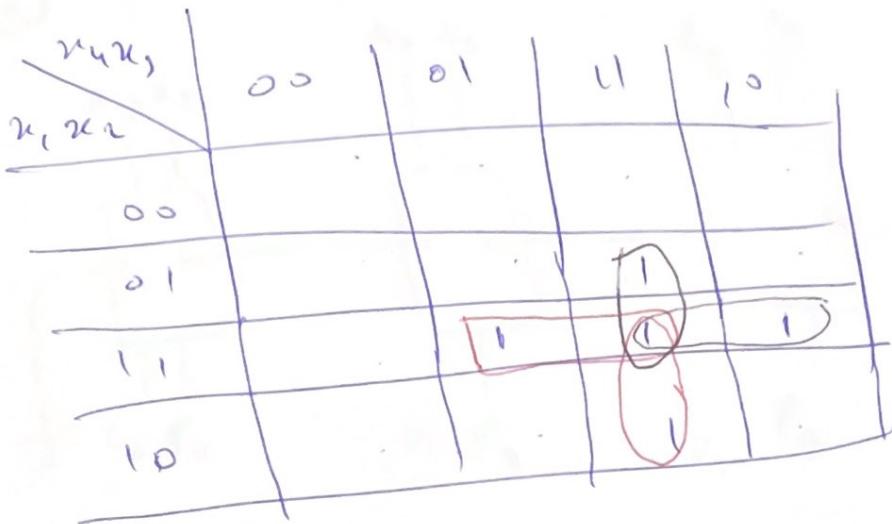


(1)

## Question 1

	$x_4$	$x_3$	$x_2$	$x_1$	$f$
0	0	0	6	0	0
1	0	6	0	1	0
2	0	0	1	0	0
3	0	0	1	1	6
4	0	1	0	6	0
5	0	1	0	1	0
6	0	1	1	0	0
7	0	1	1	1	1
8	1	0	0	0	0
9	1	0	0	1	0
10	1	0	1	0	0
11	1	0	1	1	1
12	1	1	0	0	0
13	1	1	0	1	1
14	1	1	1	0	1
15	1	1	1	1	1

(2)

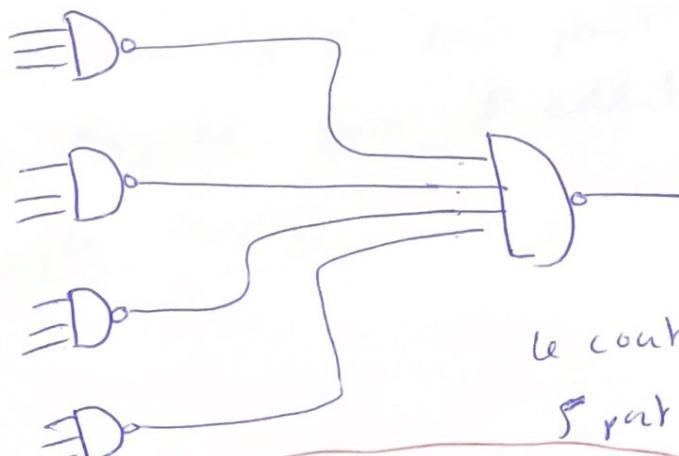


$$f = u_1 u_2 u_3 + u_2 u_3 u_4 + u_1 u_3 u_4 + u_1 u_2 u_4$$

~~$$f = u_1 u_2 (u_3 + u_4) + u_2 u_4 (u_1 + u_3)$$~~

$$f = \overline{f} = \overline{u_1 u_2 u_3} + \overline{u_2 u_3 u_4} + \overline{u_1 u_3 u_4} + \overline{u_1 u_2 u_4}$$

$$f = \overline{u_1 u_2 u_3} \cdot \overline{u_2 u_3 u_4} \cdot \overline{u_1 u_3 u_4} \cdot \overline{u_1 u_2 u_4}$$



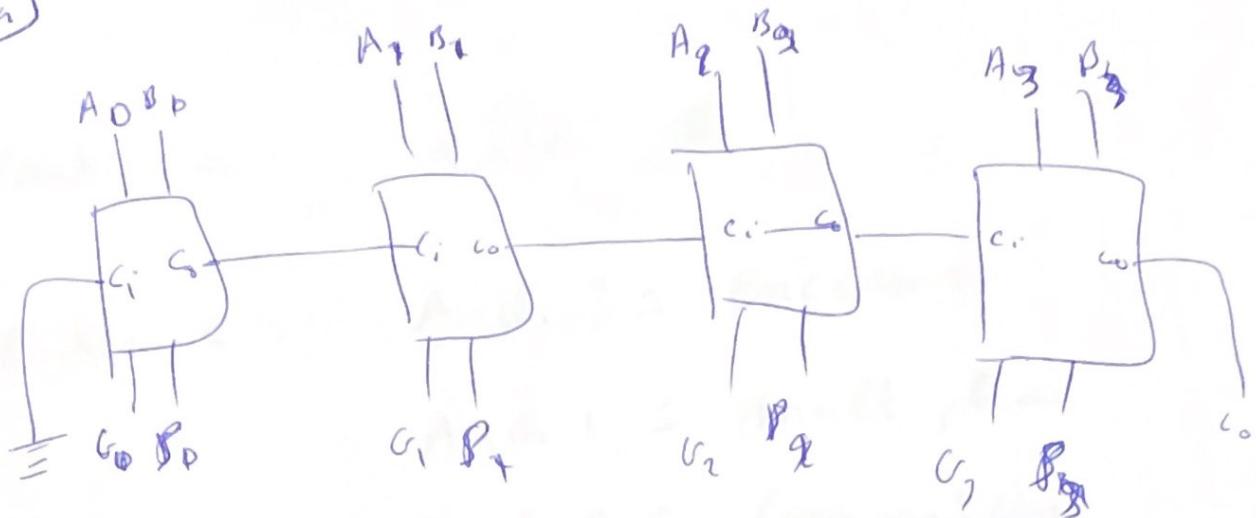
le cout est:

5 port NAND + 16

le cout total = 21

## Question 2

Part a)



$$C_i = C_{in}$$

$$C_o = C_{out}$$

Part b)

La somme plus rapide que l'additionneur précédent

L'addition en part a est plus rapide que l'additionneur précédent car il n'a pas de nipple carry.

### Question III

Partie a: alter # 1

Partie c: And 3 = Encoder

And 1 = multiplexer

And 2 = Computer.

for  
every example is

int (a,b,c : In STD-logic;  
q\_n : out · STD-logic);

and example.

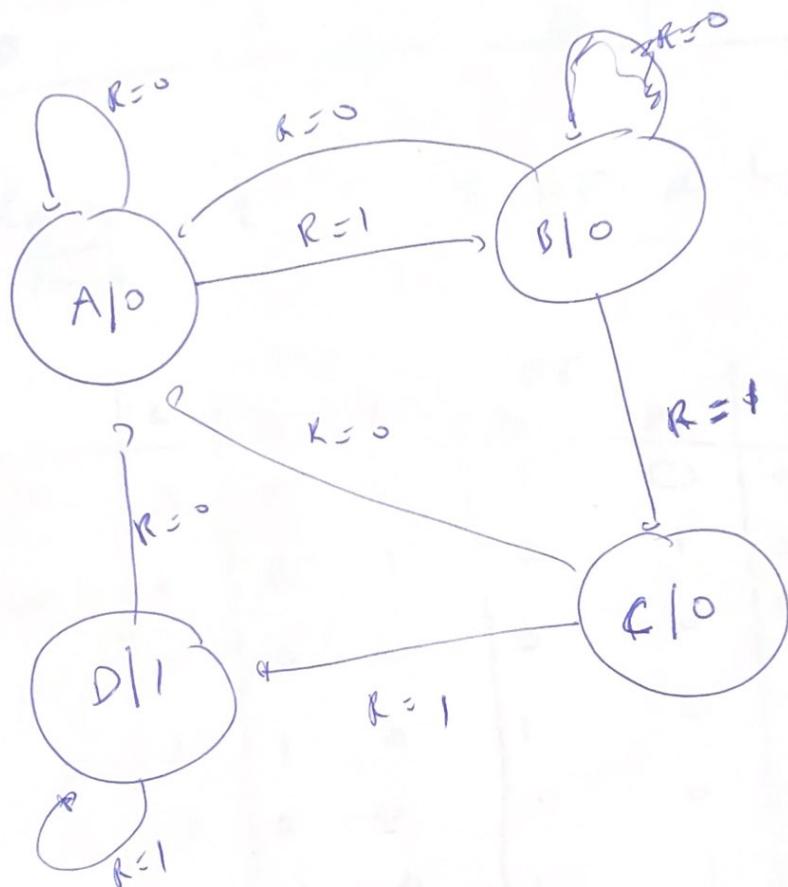
Question 4

A =

B =

C =

D =



P.S

P.S

Output

	$R=0$	$R=1$	$Q$
A	A	B	0
B	A	C	0
C	A	D	0
D	A	D	1

$$n = \frac{\log 4}{\log 2} = 2$$

2 F.F.  $\rightarrow$  1 Lyrre D

P.S	$x$	$y_2$	$y_1$	FF	$P.Q$	$Q$
00	0	0	0	0	0	0
00	1	0	1	0	1	0
00	0	0	0	0	0	0
01	0	0	0	1	0	0
01	1	1	0	0	0	0
01	0	0	0	0	0	0
10	0	1	1	1	1	0
10	1	0	0	0	0	0
11	0	1	1	1	1	1
11	1	0	0	0	0	0

$P_2$

$\bar{y}_1 y_1$	00	01	11	10
$R$	0	0	0	0
0	0	0	0	0
1	0	0	0	0

~~$D_2$~~

$$D_2 = y_2 \bar{y}_1 R + R(\bar{y}_2 y_1 + y_2 \bar{y}_1)$$

$$D_2 = y_2 \bar{y}_1 R + (y_2 \oplus y_1) R.$$

$P_1$

$\bar{y}_1 y_1$	00	01	11	10
$R$	0	0	0	0
0	0	0	0	0
1	0	0	0	0

$$\begin{aligned} D_1 &= \bar{R} (\bar{y}_2 \bar{y}_1) + R (\bar{y}_2 \bar{y}_1 + y_2 y_1) \\ &= \bar{R} y_2 \bar{y}_1 + R (y_2 \oplus y_1) \end{aligned}$$

$Z$

$\bar{y}_1 y_1$	00	01	11	10
$R$	0	0	0	0
0	0	0	0	0
1	0	0	0	0

$$Z = y_2 y_1$$

