

ITI1100A

Group Discussion 3

UNIVERSITY OF OTTAWA

Discussion Objective

Some practice problems on Gate Level Minimization
of Boolean Expression

Basic K-Map Representation

Two Variable K-Map

m_0	m_1
m_2	m_3

(a)

y	0	1
x	m_0 $x'y'$	m_1 $x'y$
1	m_2 xy'	m_3 xy

(b)

Three Variable K Map

m_0	m_1	m_3	m_2
m_4	m_5	m_7	m_6

(a)

yz	00	01	11	10
x	m_0 $x'y'z'$	m_1 $x'y'z$	m_3 $x'yz$	m_2 $x'yz'$
1	m_4 $xy'z'$	m_5 $xy'z$	m_7 xyz	m_6 xyz'

(b)

Question 3.1

Simplify the following Boolean functions, using three-variable maps:

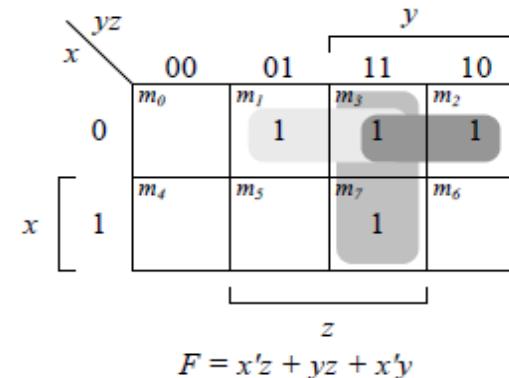
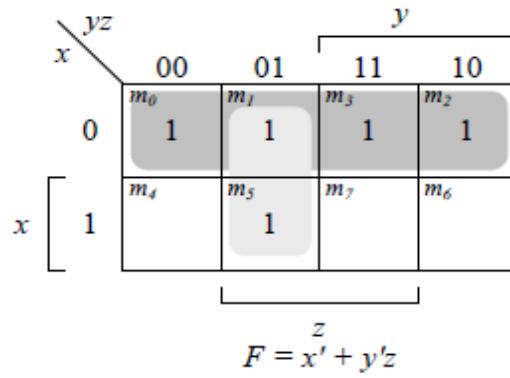
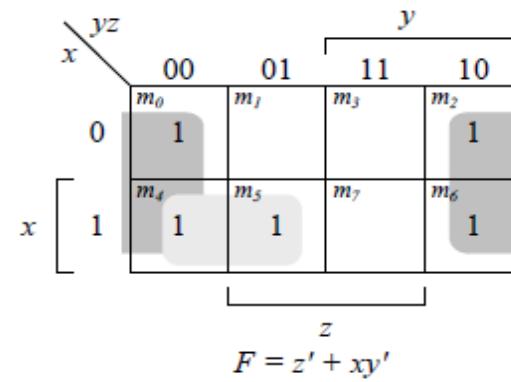
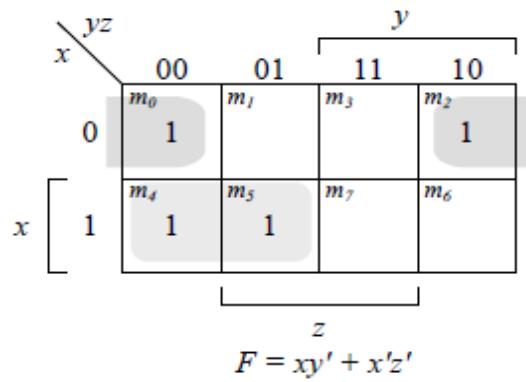
(a) $F(x, y, z) = (0, 2, 4, 5)$

(b) $F(x, y, z) = (0, 2, 4, 5, 6)$

(c) $F(x, y, z) = (0, 1, 2, 3, 5)$

(d) $F(x, y, z) = (1, 2, 3, 7)$

Solution 3.1



Question 3.3

Simplify the following Boolean expressions, using three-variable maps:

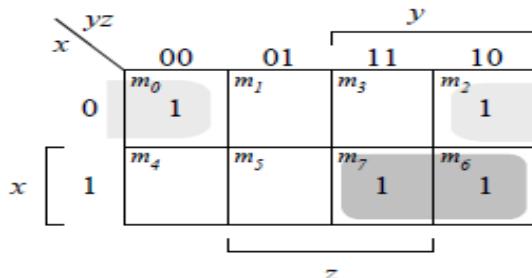
(a) $F(x, y, z) = xy + x' y' z' + x' yz'$

(b) $F(x, y, z) = x' y' + yz + x'yz'$

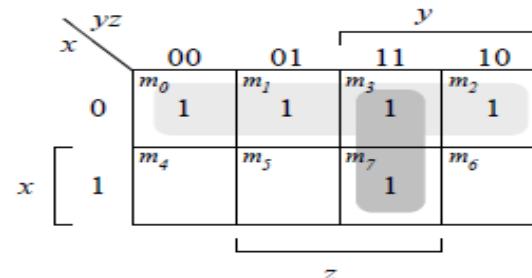
(c) $F(x, y, z) = x'y + yz' + y'z'$

(d) $F(x, y, z) = x'yz + xy'z' + xy'z$

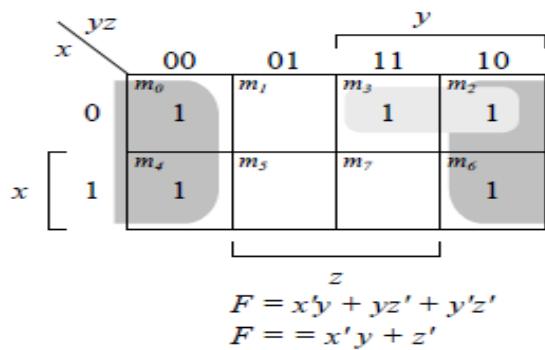
Solution 3.3



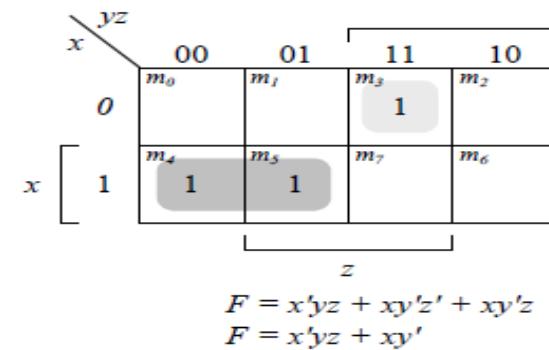
(a) $F = xy + x'y'z' + x'yz'$
 $F = xy + x'z'$



(b) $F = x'y' + yz + x'yz'$
 $F = x' + yz$



$F = x'y + yz' + y'z'$
 $F = x'y + z'$



$F = x'yz + xy'z' + xy'z$
 $F = x'yz + xy'$

(c)

(d)

Question 3.6

Simplify the following Boolean expressions, using four-variable maps:

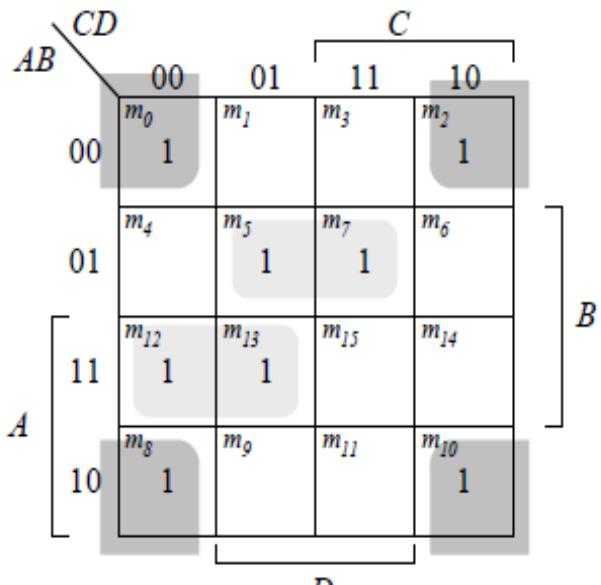
(a) $A'B'C'D' + AC'D' + B'CD' + A'BCD + BC'D$

(b) $x'z + w'xy' + w(x'y + xy')$

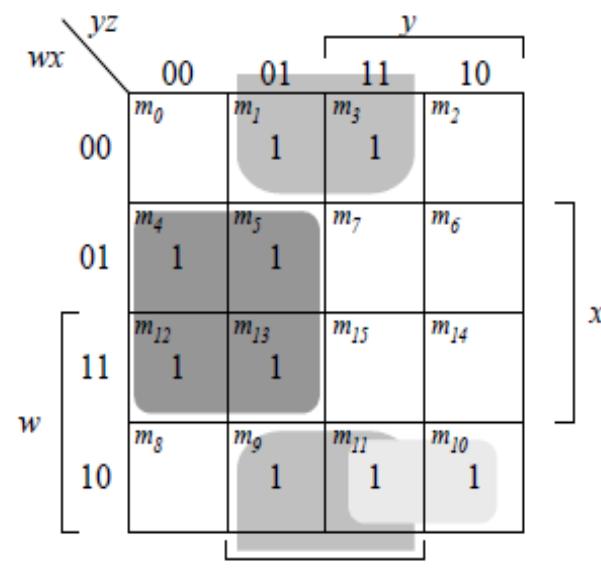
(c) $A'B'C'D + AB'D + A'BC' + ABCD + AB'C$

(d) $A'B'C'D' + BC'D + A'C'D + A'BCD + ACD'$

Solution 3.6

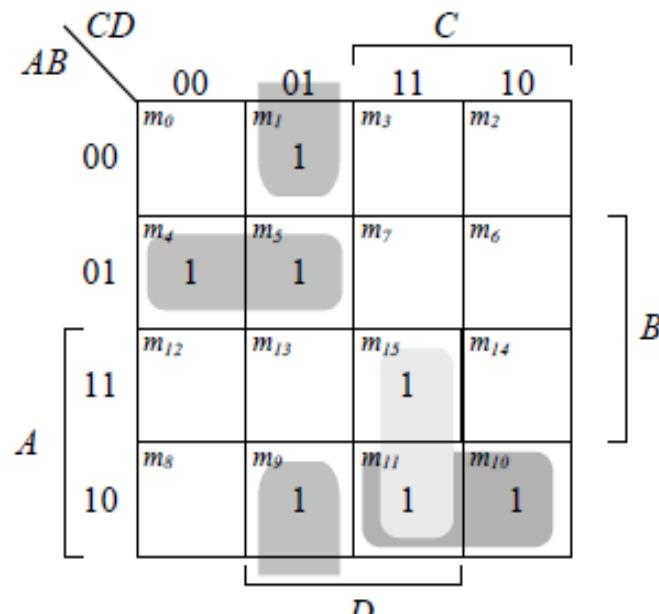


(a) $F = B'D' + A'BD + ABC'$

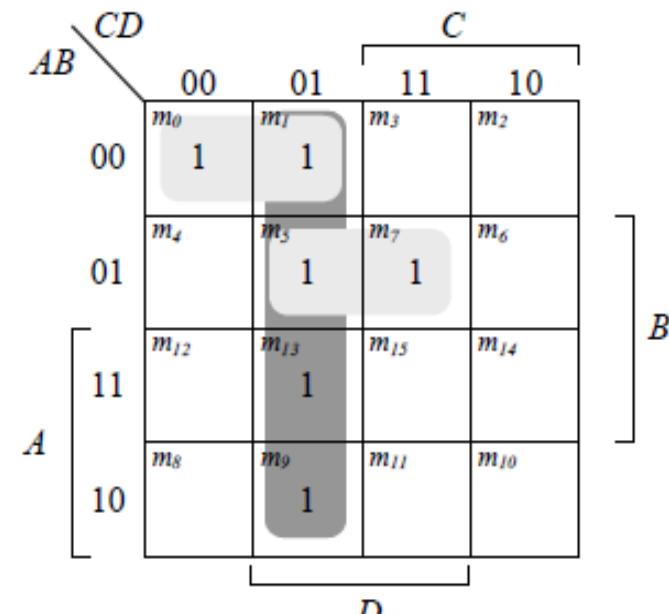


(b) $F = xy' + x'z + wx'y$

Solution 3.6 (Continuation)



(c) $F = A'BC' + B'C'D + ACD + AB'C'$



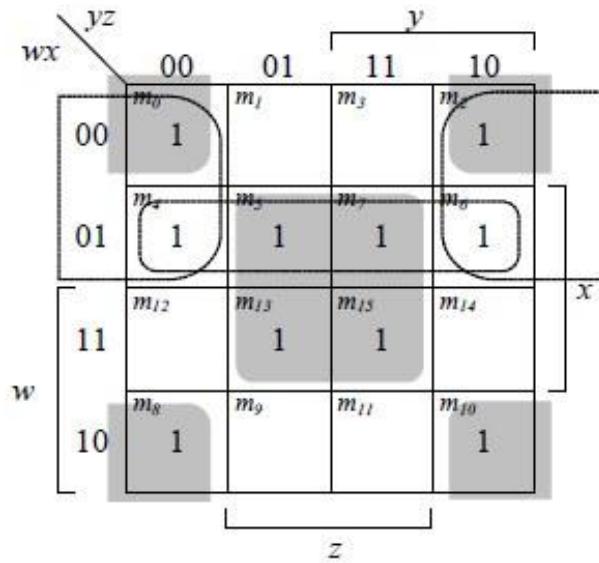
(d) $F = C'D + A'BD + A'B'C'$

Question 3.9

Find all the prime implicants for the following Boolean functions, and determine which are essential:

- (a) $F(w, x, y, z) = \Sigma(0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$
- (b) $F(A, B, C, D) = \Sigma(0, 2, 3, 5, 7, 8, 10, 11, 14, 15)$

Solution 3.9

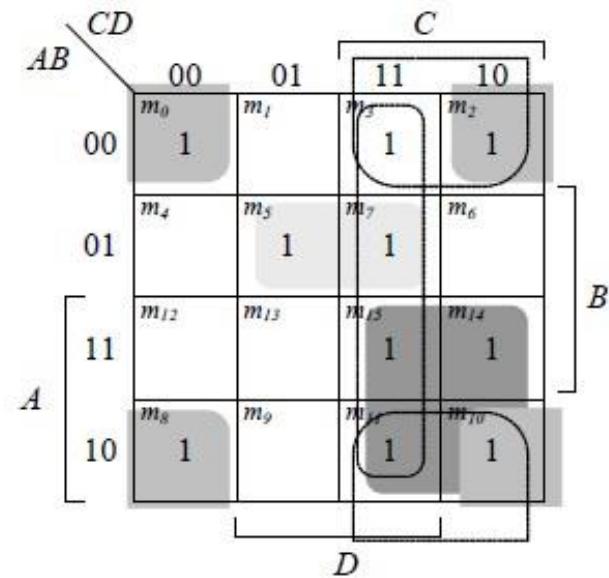


(a)

Essential: $xz, x'z'$

Non-essential: $w'x, w'z'$

$$F = xz + x'z' + (w'x \text{ or } w'z')$$



(b)

Essential: $B'D', AC, A'BD$

Non-essential: $CD, B'C$

$$F = B'D' + AC + A'BD + (CD \text{ OR } B'C)$$

Question 3.13

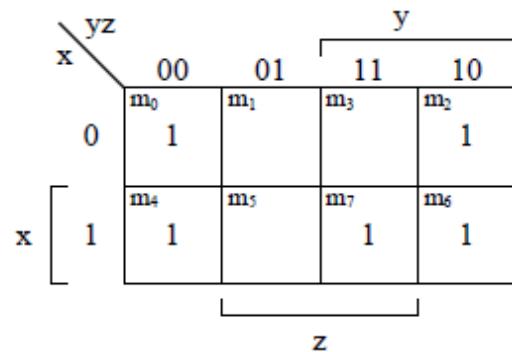
Simplify the following expressions to (1) sum-of-products and (2) products-of-sums:

(a) $x' z' + y' z' + yz' + xy$

(b) $ACD' + C'D + AB' + ABCD$

Solution 3.13

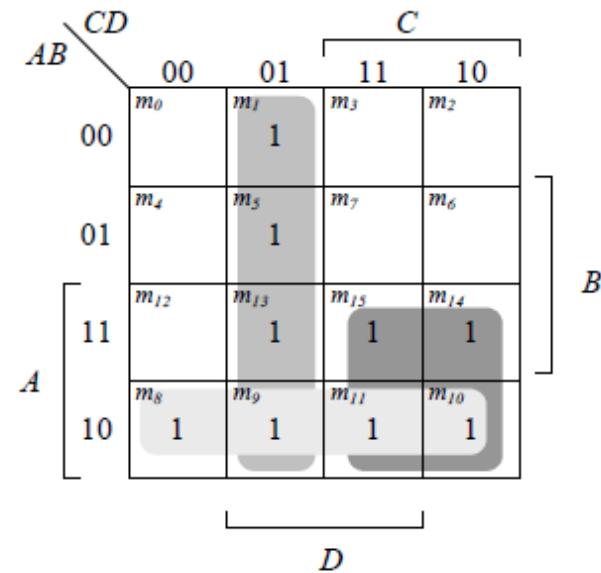
(a) $F = x'z' + y'z' + yz' + xy = x'z' + z' + xy = z' + xy$



$$F' = x'z + y'z$$

$$F = (x + z')(y + z')$$

(b) $F = ACD' + C'D + AB' + ABCD$



$$F = AC + AB' + C'D$$

$$F' = A'C + A'D' + BC'D'$$

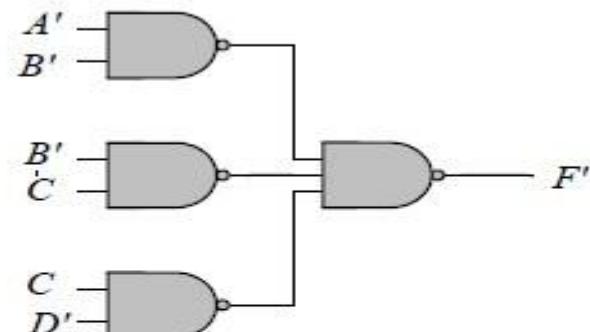
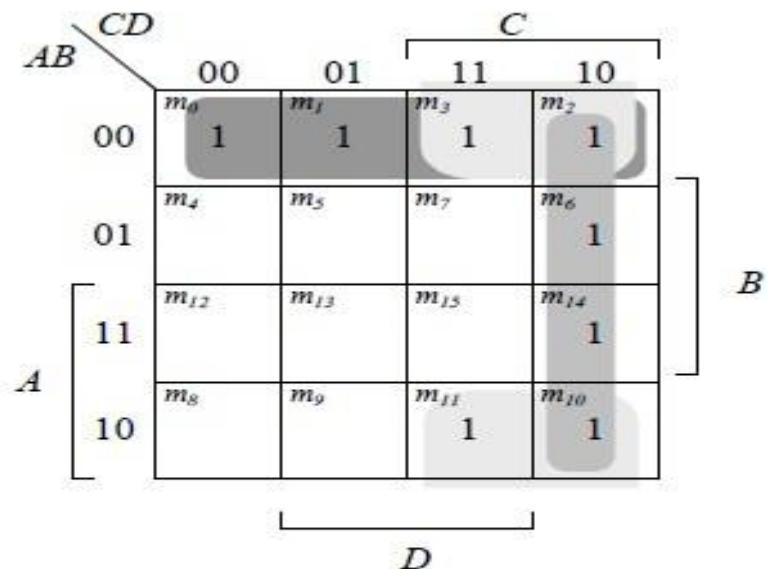
$$F = (A + C')(A + D)(B' + C + D)$$

Question 3.17

Draw a NAND logic diagram that implements the complement of the following function:

$$F(A, B, C, D) = \Sigma(0, 1, 2, 3, 6, 10, 11, 14)$$

Solution 3.17



$$F = A'B' + B'C + CD'$$

$$F = ((A + B)(B + C')(C' + D))'$$

$$F = ((A'B')'(B'C)'(CD'))'$$

$$F' = (A'B')'(B'C)'(CD')'$$

THANK YOU