### CSCI446/946 Big Data Analytics

Week 3 Data Analytic Methods Using R

School of Computing and Information Technology
University of Wollongong Australia

### Data Analytic Methods Using R

- Introduction to R
  - R, RStudio, Data I/O, Attribute and Data Types
  - Descriptive statistics
- Exploratory Data Analysis
  - Visualization before analysis
  - Visualizing single or multiple variables
- Statistical Methods for Evaluation
  - Hypothesis Testing, ANOVA

All the figures, tables and codes are from the book "<u>Data Science and Big Data Analytics:</u> <u>Discovering, Analyzing, Visualizing and Presenting Data</u>" unless indicated otherwise.

### Data Analytic Methods Using R

- The success of a data analysis project requires a deep understanding of the data
- It requires a toolbox for mining and presenting the data
  - Basic statistical measures
  - Creation of graphs and plots
  - Identify relationships and patterns
- R: popularity and versatility

- A programming language and software framework for statistical analysis and graphics
- Comprehensive R Archive Network
- An overview the basic functionality of R
- We begin with understanding the flow of a basic R script to address an analytic problem
  - Command-line interface (CLI)
  - Graphical user interface (GUI)

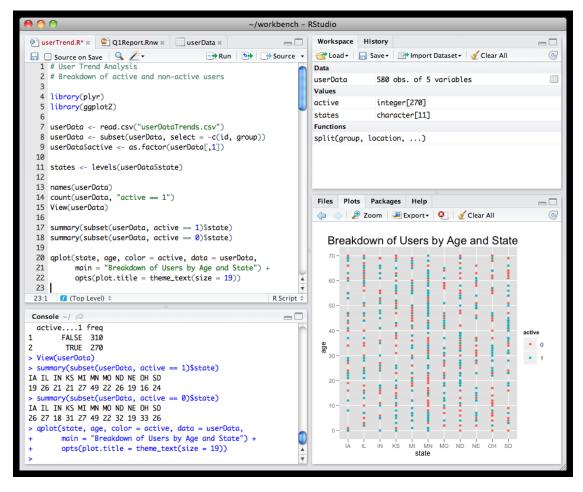
#### The first example

The first example

```
# perform a statistical analysis (fit a linear
regression model)
results <- lm(sales$sales_total ~ sales$num_of_orders)
results
summary(results)

# perform some diagnostics on the fitted model
# plot histogram of the residuals
hist(results$residuals, breaks = 800)</pre>
```

R Graphical User Interface (RStudio)



- Scripts
- Workspace
- Plots
- Console

- Help functionality
  - Help(lm) or ?lm
- Edit() and fix()
  - Allow to update the contents of an R variable
- Save.image() function to create .Rdata file
- Load.image() function to load .Rdata file
- Please install R and RStudio to try out the R examples

Data Import and Export

```
sales <- read.csv("c:/data/yearly_sales.csv")

setwd("c:/data/")
sales <- read.csv("yearly_sales.csv")

# add a column for the average sales per order
sales$per_order <- sales$sales_total/sales$num_of_orders

# export data as tab delimited without the row names
write.table(sales, "sales_modified.txt", sep="\t",
row.names=FALSE)</pre>
```

Automatically save plots

```
# export a histogram to a jpeg
jpeg(file="c:/data/sales_hist.jpeg") # create a new jpeg
file
hist(sales$num_of_orders) # export histogram to jpeg
dev.off() # shut off the graphic device
```

- More information
  - https://cran.r-project.org/doc/manuals/rrelease/R-data.html

Attribute and Data Types

 Attributes: Nominal, Ordinal, Interval, and Ratio (NOIR)

	Categorical (Qualitative)		Numeric (Quantitative)		
	Nominal	Ordinal	Interval	Ratio	
Definition	The values represent labels that distinguish one from another.	Attributes imply a sequence.	The difference between two values is meaningful.	Both the difference and the ratio of two values are meaningful.	
Examples	ZIP codes, nationality, street names, gender, employee ID numbers, TRUE or FALSE	Quality of diamonds, academic grades, magnitude of earthquakes	Temperature in Celsius or Fahrenheit, cal- endar dates, latitudes	Age, temperature in Kelvin, counts, length, weight	
Operations	=, ≠	=, ≠,	=, ≠,	=,≠,	
		<, ≤, >, ≥	<, ≤, >, ≥,	<, ≤, >, ≥,	
			+, -	+, -,	
				x.÷	

- Data Types
  - Numeric, character, logical (and list)

```
i <- 1
                             # create a numeric variable
sport <- "football"</pre>
                             # create a character variable
flag <- TRUE
                             # create a logical variable
                             # returns "numeric"
class(i)
typeof(i)
                             # returns "double"
class(sport)
                             # returns "character"
typeof(sport)
                             # returns "character"
class(flag)
                             # returns "logical"
typeof(flag)
                             # returns "logical"
```

- Vectors
  - A basic building block for data in R
  - Simple R variables are actually vectors
  - Can only consist of values in the same class

```
# Vectors
is.vector(i)  # returns TRUE
is.vector(flag)  # returns TRUE
is.vector(sport)  # returns TRUE
```

#### Vectors

```
u <- c("red", "yellow", "blue") # create a vector "red" "yellow" "blue"</pre>
                                 # returns "red" "yellow" "blue"
u
u[1]
                                 # returns "red" (1st element in u)
                                 # create a vector 1 2 3 4 5
v <- 1:5
                                 # returns 1 2 3 4 5
V
sum(v)
                                 # returns 15
W < - V * 2
                                 # create a vector 2 4 6 8 10
                                 # returns 2 4 6 8 10
W
                                 # returns 6 (the 3rd element of w)
w[3]
                                 # sums two vectors element by element
Z \leftarrow V + W
                                 # returns 3 6 9 12 15
Z
                                 # returns FALSE FALSE TRUE TRUE TRUE
z > 8
z[z > 8]
                                 # returns 9 12 15
z[z > 8 | z < 5]
                                 # returns 3 9 12 15 ("|" denotes "or")
```

 vector() function, by default, create a logical vector

```
a <- vector(length=3)</pre>
                                 # create a logical vector of length 3
                                 # returns FALSE FALSE FALSE
a
b <- vector(mode="numeric", 3) # create a numeric vector of length 3
                                 # returns "double"
typeof(b)
                                 # assign 3.1 to the 2nd element
b[2] < 3.1
                                 # returns 0.0 3.1 0.0
h
c <- vector(mode="integer", 0) # create an integer vector of length 0</pre>
                                 # returns integer(0)
C
length(c)
                                 # returns 0
```

#### Arrays and Matrices

```
# the dimensions are 3 regions, 4 quarters, and 2 years
quarterly_sales <- array(0, dim=c(3,4,2))
quarterly sales[2,1,1] <- 158000
quarterly sales
sales matrix <- matrix(0, nrow = 3, ncol = 4)</pre>
sales matrix
install.packages("matrixcalc") # install, if necessary
library(matrixcalc)
# build a 3x3 matrix
M \leftarrow matrix(c(1,3,3,5,0,4,3,3,3),nrow = 3,ncol = 3)
M %*% matrix.inverse(M) # multiply M by inverse(M)
```

- Data Frames
  - A structure for storing and accessing several variables of possibly different data types
  - Preferred input format for many R functions

 List: a collection of objects that can be of various types, including other lists

```
sales <- read.csv("c:/data/yearly_sales.csv")
class(sales)
typeof(sales)

# build an assorted list of a string, a numeric,
# a list, a vector, and a matrix
housing <- list("own", "rent")
assortment <- list("football", 7.5, housing, v, M)
assortment</pre>
```

- Factors: a categorical variable, typically with a few finite levels such as "F" and "M"
- Factors can be ordered or not ordered

```
# Factors

class(sales$gender)  # returns "factor"
is.ordered(sales$gender)  # returns FALSE
```

Use of factors is important in R statistical modelling functions

- Contingency Tables
  - A class of objects used to store the observed counts across the factors for a given dataset
  - The basis for performing a statistical test on the independence of the factors

```
# build a contingency table based on the gender and
spender factors
sales_table <- table(sales$gender,sales$spender)
sales table
```

- Contingency Tables
  - A class of objects used to store the observed counts across the factors for a given dataset
  - The basis for performing a statistical test on the independence of the factors

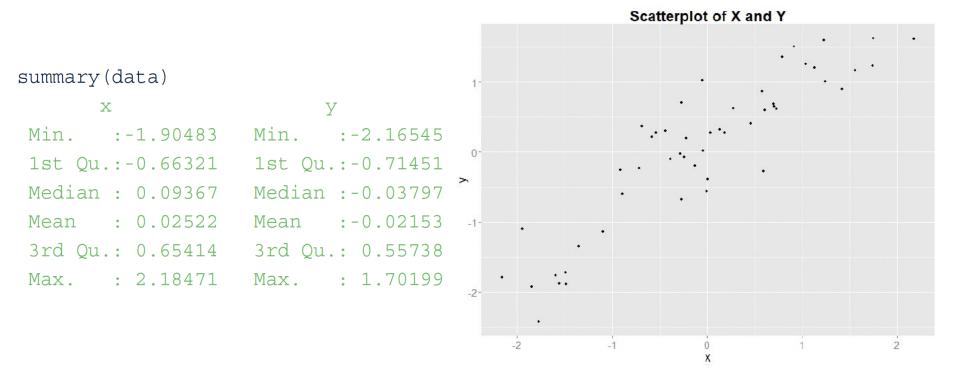
```
class(sales_table) # returns "table"
typeof(sales_table) # returns "integer"
dim(sales_table) # returns 2 3

# performs a chi-squared test
summary(sales_table)
```

- Descriptive Statistics
  - Summary() function: mean, median, min, max
  - R functions include descriptive statistics

```
# to simplify the function calls, assign
x <- sales$sales_total</pre>
y <- sales$num of orders
cor(x,y)
                 # returns 0.7508015 (correlation)
cov(x,y)
                 # returns 345.2111 (covariance)
IQR(x)
                 # returns 215.21 (interquartile range)
mean(x)
                 # returns 249.4557 (mean)
median(x)
                 # returns 151.65 (median)
range(x)
                 # returns 30.02 7606.09 (min max)
sd(x)
                 # returns 319.0508 (std. dev.)
var(x)
                 # returns 101793.4 (variance)
```

 Linear relationship and distributions are more difficult to see from descriptive statistics



- Detect patterns and anomalies in the data
  - Through exploratory data analysis by visualization
  - Visualization gives a succinct, holistic view
  - Visualization is an important facet at the initial data exploration

```
Scatterplot of X and Y
# Figure 3-5
x \leftarrow rnorm(50)
y < -x + rnorm(50, mean=0, sd=0.5)
data <- as.data.frame(cbind(x, y))</pre>
summary(data)
library(ggplot2)
ggplot(data, aes(x=x, y=y)) +
  geom_point(size=2) +
  ggtitle("Scatterplot of X and Y") +
  theme(axis.text=element_text(size=12),
         axis.title = element_text(size=14),
         plot.title = element_text(size=20, face="bold"))
```

Visualization Before Analysis

#	1	#	2	#	3	#	4
х	у	х	у	х	у	х	у
4	4.26	4	3.10	4	5.39	8	5.25
5	5.68	5	4.74	5	5.73	8	5.56
6	7.24	6	6.13	6	6.08	8	5.76
7	4.82	7	7.26	7	6.42	8	6.58
8	6.95	8	8.14	8	6.77	8	6.89
9	8.81	9	8.77	9	7.11	8	7.04
10	8.04	10	9.14	10	7.46	8	7.71
11	8.33	11	9.26	11	7.81	8	7.91
12	10.84	12	9.13	12	8.15	8	8.47
13	7.58	13	8.74	13	12.74	8	8.84
14	9.96	14	8.10	14	8.84	19	12.50

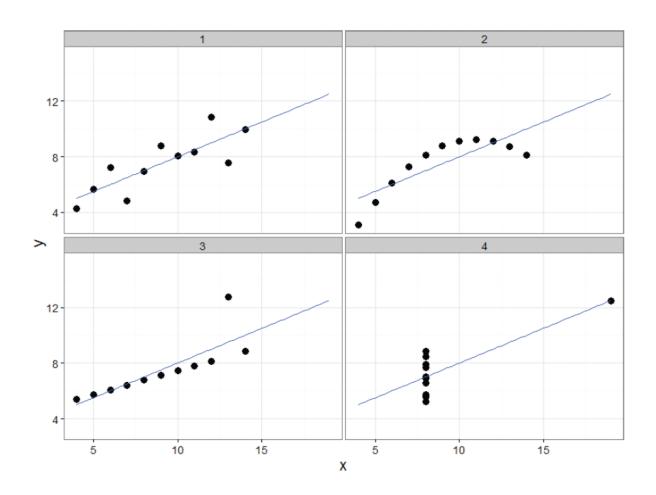
Figure 3-6 Anscombe's quartet

 The four data sets have nearly identical statistical properties

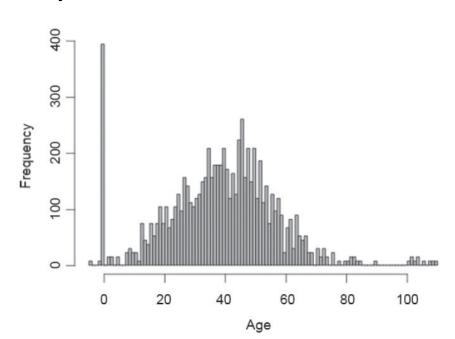
**TABLE 3-3** Statistical Properties of Anscombe's Quartet

Statistical Property	Value		
Mean of X	9		
Variance of <i>y</i>	11		
Mean of <i>y</i>	7.50 (to 2 decimal points)		
Variance of <i>y</i>	4.12 or 4.13 (to 2 decimal points)		
Correlations between <i>x</i> and <i>y</i>	0.816		
Linear regression line	y = 3.00 + 0.50x (to 2 decimal points)		

However, the reality is a different story...

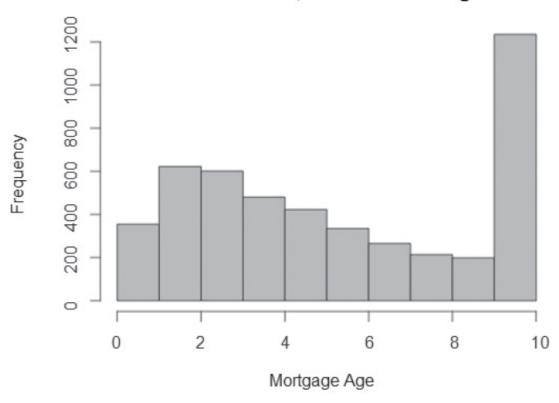


- Dirty Data
  - Detect dirty data with visualization
  - Look for anomalies, verify with domain knowledge
  - Clean the data appropriately



Any dirty data?

Portfolio Distribution, Years Since Origination

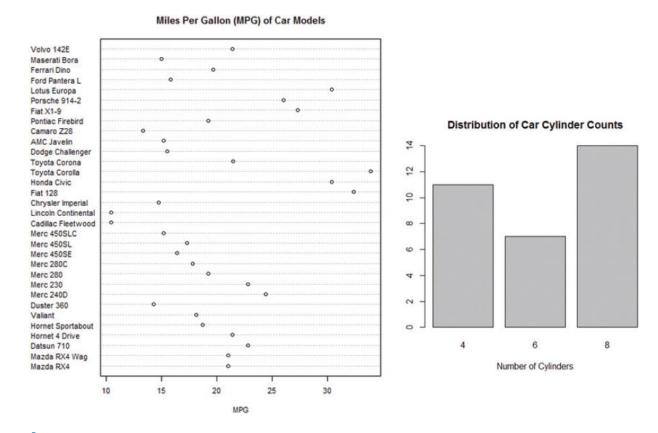


#### Visualizing a Single Variable

**TABLE 3-4** Example Functions for Visualizing a Single Variable

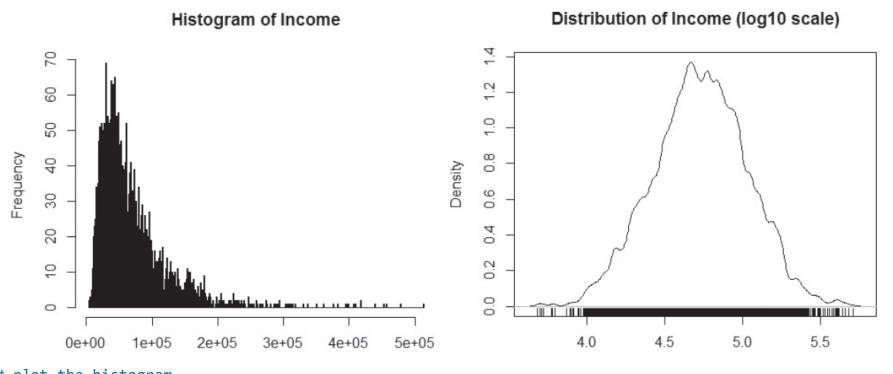
Function	Purpose
plot(data)	Scatterplot where x is the index and y is the value; suitable for low-volume data
barplot(data)	Barplot with vertical or horizontal bars
dotchart(data)	Cleveland dot plot [12]
hist(data)	Histogram
plot(density(data))	Density plot (a continuous histogram)
stem(data)	Stem-and-leaf plot
rug( <b>data</b> )	Add a rug representation (1-d plot) of the data to an existing plot

Visualizing a Single Variable



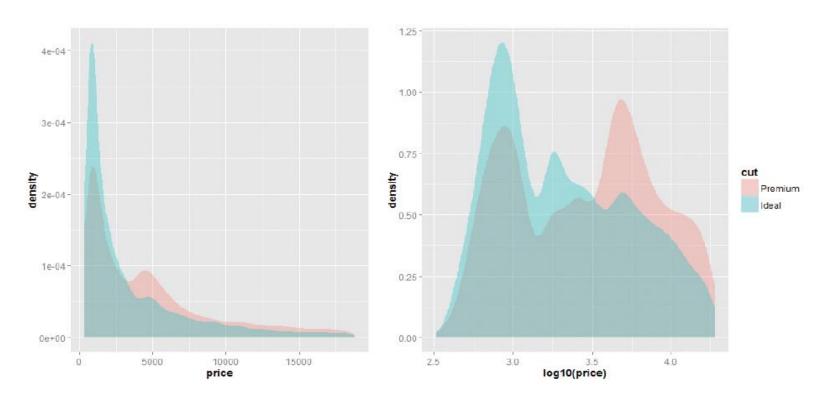
## Dotchart and Barplot ##
dotchart(mtcars\$mpg,labels=row.names(mtcars),cex=.7, main="Miles Per Gallon (MPG) of Car Models", xlab="MPG")
barplot(table(mtcars\$cyl), main="Distribution of Car Cylinder Counts", xlab="Number of Cylinders")

Visualizing a Single Variable (log transformation)



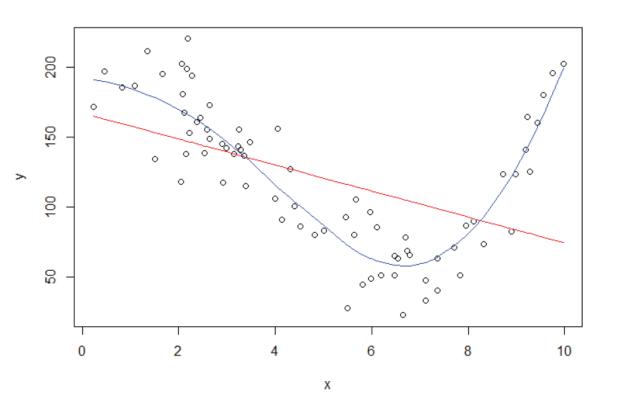
```
# plot the histogram
hist(income, breaks=500, xlab="Income", main="Histogram of Income")
# density plot
plot(density(log10(income), adjust=0.5), main="Distribution of Income (log10 scale)")
# add rug to the density plot
rug(log10(income))
```

Visualizing a Single Variable (unimodal or multimodal?)



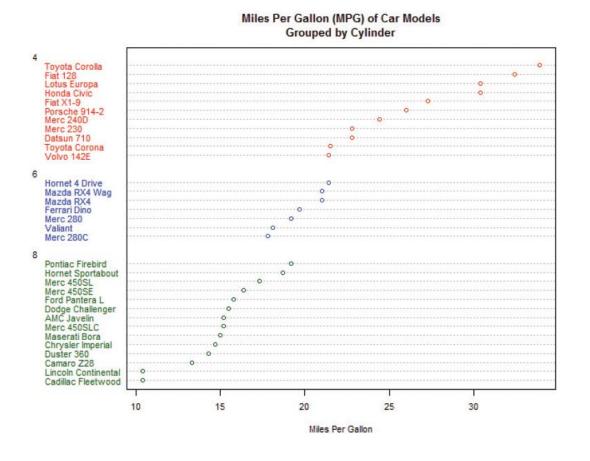
```
# plot density plot of diamond prices
ggplot(niceDiamonds, aes(x=price, fill=cut)) + geom_density(alpha = .3, color=NA)
# plot density plot of the log10 of diamond prices
ggplot(niceDiamonds, aes(x=log10(price), fill=cut)) + geom_density(alpha = .3, color=NA)
```

Examining Multiple Variable



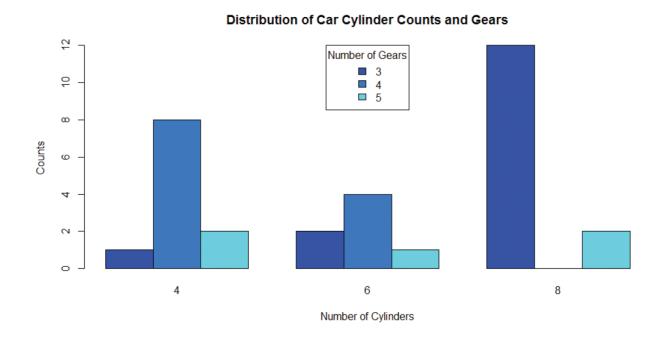
```
# 75 numbers between 0 and 10 of
uniform distribution
x \leftarrow runif(75, 0, 10)
x \leftarrow sort(x)
y \leftarrow 200 + x^3 - 10 * x^2 + x +
rnorm(75, 0, 20)
lr < -lm(y \sim x) # linear
regression
poly <- loess(y \sim x) # LOESS
fit <- predict(poly) # fit a</pre>
nonlinear line
plot(x,y)
# draw the fitted line for the
linear regression
points(x, lr$coefficients[1] +
lr$coefficients[2] * x,
       type = "1", col = 2)
# draw the fitted line with LOESS
points(x, fit, type = "l", col =
4)
```

#### Examining Multiple Variable

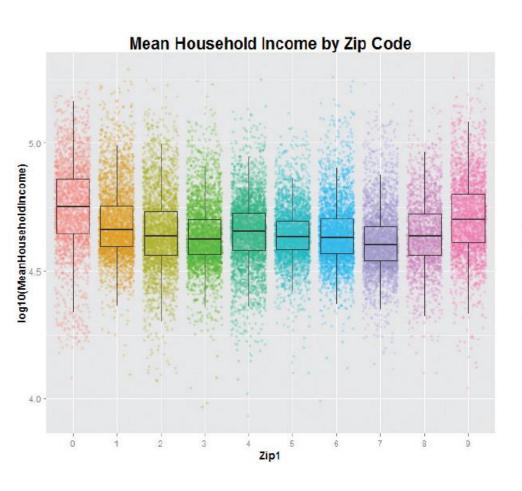


```
# sort by mpg
cars <-
mtcars[order(mtcars$mpg),]
# grouping variable must be a
factor
cars$cyl <- factor(cars$cyl)</pre>
cars$color[cars$cyl==4] <-</pre>
"red"
cars$color[cars$cvl==6] <-</pre>
"blue"
cars$color[cars$cyl==8] <-</pre>
"darkgreen"
dotchart(cars$mpg,
labels=row.names(cars),
cex=.7, groups= cars$cv1,
          main="Miles Per
Gallon (MPG) of Car
Models\nGrouped by Cylinder",
          xlab="Miles Per
Gallon", color=cars$color,
gcolor="black")
```

Examining Multiple Variable

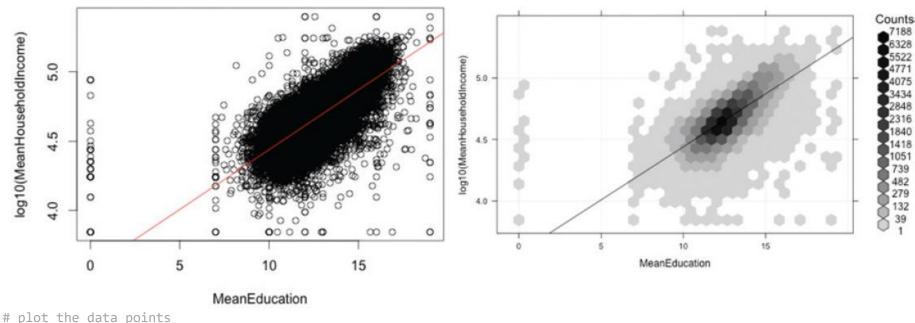


Examining Multiple Variable (box-and-whisker plot)



```
## Box-and-Whisker Plot ##
DF <- read.csv("c:/data/zipIncome.csv", header=TRUE,</pre>
sep=",")
# Remove outliers
DF <- subset(DF, DF$MeanHouseholdIncome > 7000 &
DF$MeanHouseholdIncome < 200000)</pre>
summary(DF)
library(ggplot2)
# plot the jittered scatterplot w/ boxplot
# color-code points with zip codes
# the outlier.size=0 prevents the boxplot from
plotting the outlier
ggplot(data=DF, aes(x=as.factor(Zip1),
y=log10(MeanHouseholdIncome))) +
  geom point(aes(color=factor(Zip1)), alpha=0.2,
position="jitter") +
  geom boxplot(outlier.size=0, alpha=0.1) +
  guides(colour=FALSE) +
  ggtitle ("Mean Household Income by Zip Code")
# simple boxplot
boxplot(log10(MeanHouseholdIncome) ~ Zip1, data=DF)
title ("Mean Household Income by Zip Code")
```

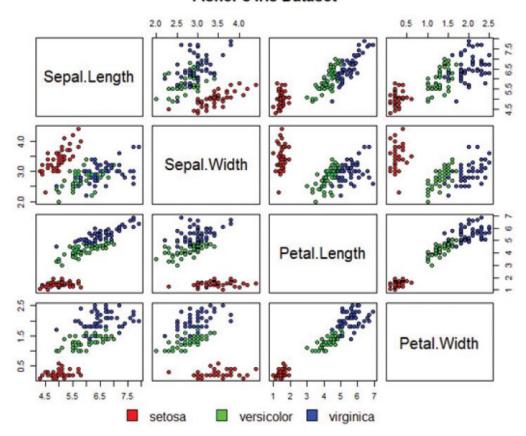
Examining Multiple Variable (hexbinplot for large data)



```
plot(log10(MeanHouseholdIncome) ~ MeanEducation, data=DF)
# add a straight fitted line of the linear regression
abline(lm(log10(MeanHouseholdIncome) ~ MeanEducation, data=DF), col='red')
install.packages("hexbin")
library(hexbin)
# "g" adds the grid, "r" adds the regression line; sqrt transform on the count gives more dynamic range to the shading;
# inv provides the inverse transformation function of trans
hexbinplot(log10(MeanHouseholdIncome) ~ MeanEducation, data=DF, trans = sqrt, inv = function(x) x^2, type=c("g", "r"))
```

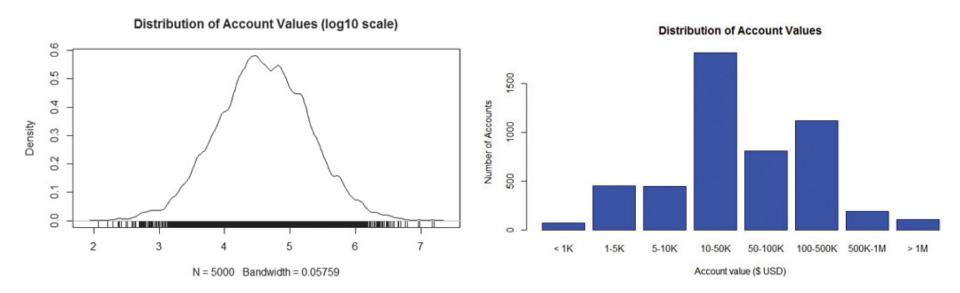
Examining Multiple Variable (scatterplot matrix)

#### Fisher's Iris Dataset



```
# define the colors
colors <- c("red", "green",</pre>
"blue")
# draw the plot matrix
pairs(iris[1:4], main = "Fisher's
Iris Dataset",
      pch = 21, bg =
colors[unclass(iris$Species)] )
# set graphical parameter to clip
plotting to the figure region
par(xpd = TRUE)
# add legend
legend(0.2, 0.02, horiz = TRUE,
as.vector(unique(iris$Species)),
       fill = colors, bty = "n")
```

Data Exploration Versus Presentation



Presenting the same data to different audience

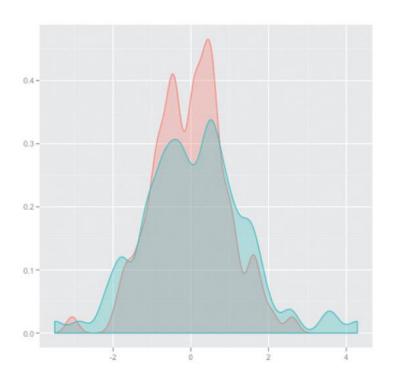
- Statistics is crucial because it may exist throughout the entire Data Analytics Lifecycle
  - Initial data exploration and data preparation
  - Model building and planning
    - Best input variables, predictability
  - Evaluation of the final models
    - Accuracy, better than guess or another one?
  - Assessment of the new models when deployed
    - Sound prediction? Have desired effect?

- Hypothesis Testing
  - Form an assertion and test it with data
  - Common assumption (there is no difference)
  - Null hypothesis (*H<sub>0</sub>*)
  - Alternative hypothesis (H<sub>A</sub>)
- Example: identify the effect of drug A compared to drug B on patients
  - What are the  $H_0$  and  $H_A$ ?

- Hypothesis Testing
  - Clearly state Null and Alternative hypotheses
  - Either reject the null hypothesis in favour of the alternative or not reject the null hypothesis

Application	Null Hypothesis	Alternative Hypothesis
Accuracy Forecast	Model X <i>does not predict</i> better than the existing model.	Model X <i>predicts</i> better than the existing model.
Recommendation Engine	Algorithm Y <i>does not produce</i> better recommendations than the current algorithm being used.	Algorithm Y <i>produces</i> better recommendations than the current algorithm being used.
Regression Modeling	This variable <i>does not affect</i> the outcome because its coefficient is <i>zero</i> .	This variable <i>affects</i> outcome because its coefficient is not <i>zero</i> .

- Difference of Means (A common hypothesis test)
  - Whether two populations are different?
  - Compare their means based on sampled data



- What are  $H_0$  and  $H_A$ ?

- Student's t-test
  - Assume that distributions of the two populations have equal but unknown variance
  - If each population is normally distributed with the same mean and with the same variance, then

$$T = \frac{\overline{X}_{1} - \overline{X}_{2}}{S_{p} \sqrt{\frac{1}{n_{1}} + \frac{1}{n_{2}}}}$$

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

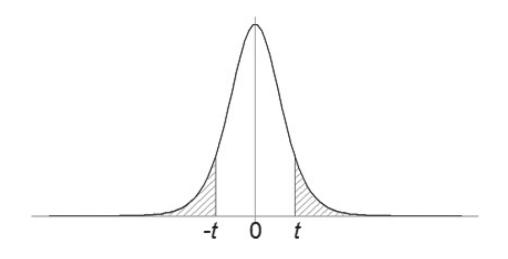
T (the *t-statistic*) follows a <u>t-distribution</u> with (n<sub>1</sub>+n<sub>2</sub>-2) degree of freedom

#### • Student's t-test

 If the observed T is far from zero such that the probability of observing such a value of T is unlikely, one would reject the null hypothesis

$$T = \frac{X_1 - X_2}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$

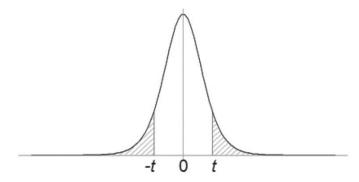


#### • Student's t-test

- Significance level of the test (α): the probability of rejecting the null hypothesis, when the null hypothesis is actually TRUE
- So, what does it mean by setting  $\alpha = 0.05$ ?
- Find T\* such that  $P(|T| ≥ T^*) = α$
- Reject  $H_0$  if  $|T| \ge T^*$

$$T = \frac{\overline{X}_1 - \overline{X}_2}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

$$S_p^2 = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2}$$



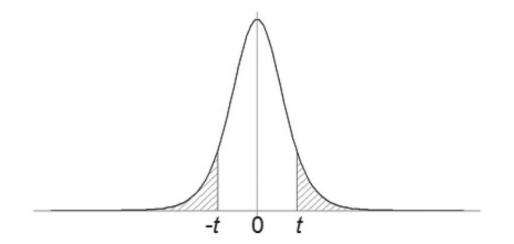
• Student's *t*-test (an example)

```
# generate random observations from the two populations
x <- rnorm(10, mean=100, sd=5) # normal distribution centered at 100
y <- rnorm(20, mean=105, sd=5) # normal distribution centered at 105
t.test(x, y, var.equal=TRUE) # run the Student's t-test
Two Sample t-test
data: x and y
t = -1.7828, df = 28, p-value = 0.08547
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
  -6.1611557 0.4271893
sample estimates:
 mean of x mean of y
102.2136 105.0806
```

• Student's *t*-test (an example)

```
# obtain t value for a two-sided test at a 0.05 significance level
qt(p=0.05/2, df=28, lower.tail= FALSE)
2.048407
```

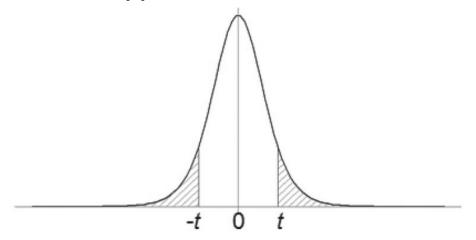
- Shall we reject or accept the null hypothesis?
- What does the "two-sided test" mean?



- Student's *t*-test (an example)
  - What does the "p-value" mean?

```
t = -1.7828, df = 28, p-value = 0.08547
```

- The sum of  $P(T \le -t)$  and  $P(T \ge t)$
- p-value offers the probability of observing |T| ≥ t
   given the null hypothesis is TRUE



- Student's *t*-test (an example)
  - What is the "95 percent confidence interval"?

```
95 percent confidence interval:
-6.1611557 0.4271893
```

- A confidence level is an interval estimate of a population parameter based on sample data
- The above "95 percent confidence interval" straddles the TRUE value of the difference of the population means 95% of the time

#### • Welch's t-test

- Shall be used when the equal population variance assumption is NOT justified
- It uses the sample variance for each population instead of the pooled sample variance
- Still assume two populations are normal with the same mean

$$T_{welch} = \frac{\overline{X}_1 - \overline{X}_2}{\sqrt{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}}$$

• Welch's t-test

```
t.test(x, y, var.equal=FALSE) # run the Welch's t-test
Welch Two Sample t-test
data: x and y
t = -1.6596, df = 15.118, p-value = 0.1176
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
  -6.546629 0.812663
sample estimates:
 mean of x mean of y
102.2136 105.0806
```

- Wilcoxon Rank-Sum Test
  - What if the two populations are not normal?
- Parametric test
  - Makes assumptions about the population distributions from which the samples are drawn
- Nonparametric test
  - Shall be used if the populations cannot be assumed (or transformed) to be normal

- Wilcoxon Rank-Sum Test
  - A nonparametric test to check whether two populations are identically distributed
  - It uses "ranks" instead of numerical outcomes to avoid specific assumption about the distribution
- How to conduct the test
  - Rank two samples as if they are from one group
  - Sum assigned ranks for one population's sample
  - Determine the significance of the rank-sums

Wilcoxon Rank-Sum Test

```
wilcox.test(x, y, conf.int = TRUE)
Wilcoxon rank sum test
data: x and y
W = 55, p-value = 0.04903
alternative hypothesis: true location shift is not equal to 0
95 percent confidence interval:
  -6.2596774 -0.1240618
sample estimates:
  difference in location
-3.417658
```

p-value: the probability of the rank-sums of this magnitude being observed assuming that the population distributions are identical

- Type I and Type II Errors
  - Type I error: the rejection of the null hypothesis when the null hypothesis is TRUE
  - The probability of type I error is denoted by  $\alpha$
  - Type II error: the acceptance of the null hypothesis when the null hypothesis is FALSE
  - The probability of type II error is denoted by  $\beta$
- Power (statistical power)
  - The probability of correcting rejecting the null hypothesis  $(1-\beta)$

- ANOVA (Analysis of Variance)
  - What if there are more than two populations?
  - Multiple t-test may not perform well now
- A generalization of the hypothesis testing
  - ANOVA tests if any of the population means differ from the other population means
  - Each population is assumed to be normal and have the same variance

ANOVA (Analysis of Variance)

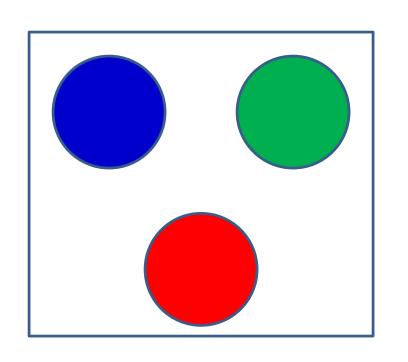
$$H_0: \mu_1 = \mu_2 = \ldots = \mu_n$$

 $\mathbf{H}_{\mathbf{A}}: \mu_i \neq \mu_j$  for at least one pair of i, j

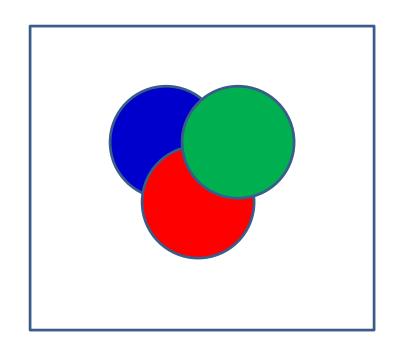
- Compute F-test statistic
  - Between-groups mean sum of squares
  - Within-groups mean sum of squares

$$S_B^2 = \frac{1}{k-1} \sum_{i=1}^k n_i \cdot (\overline{x}_i - \overline{x}_0)^2 \qquad S_W^2 = \frac{1}{n-k} \sum_{i=1}^k \sum_{j=1}^{n_i} (x_{ij} - \overline{x}_i)^2$$

ANOVA (Analysis of Variance)



$$F = \frac{S_B^2}{S_W^2}$$



$$S_B^2 = \frac{1}{k-1} \sum_{i=1}^k n_i \cdot (\overline{x}_i - \overline{x}_0)^2 \qquad S_W^2 = \frac{1}{n-k} \sum_{i=1}^k \sum_{j=1}^{n_i} (x_{ij} - \overline{x}_i)^2$$

- ANOVA (Analysis of Variance)
  - Measures how different the means are relative to the variability within each group
  - The larger the F-test statistic, the greater the likelihood that the difference of means are due to something other than chance alone
  - The F-test statistic follows an F-distribution

$$F = \frac{S_B^2}{S_W^2}$$

ANOVA (Analysis of Variance)

Shall we accept or reject the null hypothesis?

- ANOVA (Analysis of Variance)
  - Additional tests for each pair of groups
  - Tukey's Honest Significant Difference (HSD)

## Recap: Data Analytic Methods Using R

- Introduction to R
  - R, RStudio, Data I/O, Attribute and Data Types
  - Descriptive statistics
- Exploratory Data Analysis
  - Visualization before analysis
  - Visualizing single or multiple variables
- Statistical Methods for Evaluation
  - Hypothesis Testing, ANOVA

