Deep Learning

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Contents

We	ebsite			vii
Ac	knowle	dgments	V	iii
No	tation			хi
1	Introd 1.1 1.2	uction Who Should Read This Book?		1
I	Applied	d Math and Machine Learning Basics	29	
2	2.1 2.2 2.3 2.4 2.5 2.6 2.7 2.8 2.9 2.10 2.11 2.12	Eigendecomposition42Singular Value Decomposition44The Moore-Penrose PseudoinverseThe Trace Operator46The Determinant47Example: Principal Components Analysis	31 7 40	31
		i		
СО	NTENTS	3		
	3.2 3.3 3.4 3.5 3.6 3.7 3.8 3.9	Random Variables 56 Probability Distributions 56 Marginal Probability 58 Conditional Probability 59 The Chain Rule of Conditional Probabilities 59 Independence and Conditional Independence Expectation, Variance and Covariance 62 Common Probability Distributions 62	60	0

	3.10	Oseiui Fioperiles di Common Functions	
	3.11	Bayes' Rule 70	
	3.12	Technical Details of Continuous Variables	
	3.13	Information Theory	
	3.14	Structured Probabilistic Models	. 75
4	Nume	erical Computation	80
	4.1	Overflow and Underflow	80
	4.2	Poor Conditioning 8	32
	4.3	Gradient-Based Optimization	. 82
	4.4	Constrained Optimization	93
	4.5	Example: Linear Least Squares	96
5	Mach	ine Learning Basics	98
	5.1	Learning Algorithms	99
	5.2	Capacity, Overfitting and Underfitting	
	5.3	Hyperparameters and Validation Sets	
	5.4	Estimators, Bias and Variance	
	5.5	Maximum Likelihood Estimation	
	5.6	Bayesian Statistics	
	5.7	Supervised Learning Algorithms	
	5.8	Unsupervised Learning Algorithms	
	5.9	Stochastic Gradient Descent	
	5.10	Building a Machine Learning Algorithm	
	5.11	Challenges Motivating Deep Learning	
	0.11	Chairing S Wolfvaling Deep Learning	100
П	Deep	Networks: Modern Practices	166
6	Deep	Feedforward Networks	168
6	Deep 6.1	Feedforward Networks Example: Learning XOR	168 171
6		Feedforward Networks Example: Learning XOR	171
6	6.1	Example: Learning XOR	171
6	6.1	Example: Learning XOR	171
6	6.1	Example: Learning XOR	171
6	6.1	Example: Learning XOR	171
	6.1	Example: Learning XOR	171
	6.1 6.2 NTENTS	Example: Learning XOR	171
	6.1 6.2	Example: Learning XOR	171
	6.1 6.2 NTENTS	Example: Learning XOR	171 177 1
	6.1 6.2 NTENTS	Example: Learning XOR	171 177 1 97
	6.1 6.2 NTENTS	Example: Learning XOR	171 177 1 97 204
	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6	Example: Learning XOR	171 177 1 97 204
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22	171 177 1 97 204 24 228
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul	Example: Learning XOR Gradient-Based Learning ii Hidden Units	171 177 1 97 204 24 228 230
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization	171 177 197 204 24 228 230 237
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2	Example: Learning XOR Gradient-Based Learning ii Hidden Units Architecture Design Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems	171 177 197 204 24 228 230 237 239
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2 7.3	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems Dataset Augmentation 2	171 177 197 204 24 228 230 237 239
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2 7.3 7.4	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems Dataset Augmentation 2 Noise Robustness	171 177 197 204 24 228 230 237 239 240 242
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2 7.3 7.4 7.5	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems Dataset Augmentation 2 Noise Robustness 5 Semi-Supervised Learning	171 177 197 204 24 228 230 237 239 240 242 243
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2 7.3 7.4 7.5 7.6	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems Dataset Augmentation 2 Noise Robustness Semi-Supervised Learning Multi-Task Learning 2	171 177 177 1 97 204 24 230 237 239 240 242 243 44
CON	6.1 6.2 NTENTS 6.3 6.4 6.5 6.6 Regul 7.1 7.2 7.3 7.4 7.5 7.6 7.7	Example: Learning XOR Gradient-Based Learning ii Hidden Units 19 Architecture Design 1 Back-Propagation and Other Differentiation Algorithms Historical Notes 22 arization for Deep Learning Parameter Norm Penalties Norm Penalties as Constrained Optimization Regularization and Under-Constrained Problems Dataset Augmentation 2 Noise Robustness 5 Semi-Supervised Learning	171 177 197 204 24 228 230 237 239 240 242 243 44

	7.10	Sparse Representations
	7.11	Bagging and Other Ensemble Methods
	7.12	Dropout
	7.12	Adversarial Training
	7.14	Tangent Distance, Tangent Prop, and Manifold Tangent Classifier 270
8	Optim	nization for Training Deep Models 274
	8.1	How Learning Differs from Pure Optimization 275
	8.2	Challenges in Neural Network Optimization 282
	8.3	Basic Algorithms
	8.4	Parameter Initialization Strategies
	8.5	Algorithms with Adaptive Learning Rates 306
	8.6	Approximate Second-Order Methods 310
	8.7	Optimization Strategies and Meta-Algorithms 317
9	Conv	olutional Networks 330
Ŭ	9.1	The Convolution Operation
	9.2	·
		Motivation
	9.3	Pooling
	9.4	Convolution and Pooling as an Infinitely Strong Prior 345
	9.5	Variants of the Basic Convolution Function 347
	9.6	Structured Outputs
	9.7	Data Types 360
	9.8	Efficient Convolution Algorithms
	9.9	Random or Unsupervised Features
		iii
СО	NTENTS	6
	0.40	The Newson's office Paris for Consolutional Naturals
	9.10	
	9.11	Convolutional Networks and the History of Deep Learning 371
10	Seque	ence Modeling: Recurrent and Recursive Nets 373
	10.1	Unfolding Computational Graphs
	10.2	Recurrent Neural Networks
	10.3	Bidirectional RNNs
	10.4	Encoder-Decoder Sequence-to-Sequence Architectures 396
	10.5	Deep Recurrent Networks
	10.6	Recursive Neural Networks 400
	10.7	The Challenge of Long-Term Dependencies 401
	10.8	Echo State Networks
	10.9	Leaky Units and Other Strategies for Multiple Time Scales 406
		The Long Short-Term Memory and Other Gated RNNs 408
		·
		Optimization for Long-Term Dependencies
	10.12	Explicit Memory
11	Praction	cal Methodology 421
	11.1	Performance Metrics
	11.2	Default Baseline Models
	11.3	
	11.4	•

11. 11.	1 1 99 9 1 1 1 1 1 1	
12 App	plications 443	3
	.1 Large-Scale Deep Learning	
12	.2 Computer Vision	
	.3 Speech Recognition	
	.4 Natural Language Processing	
12	.5 Other Applications 478	
III De	eep Learning Research 486	;
13 Line	ear Factor Models 489	
13	.1 Probabilistic PCA and Factor Analysis	
13	.2 Independent Component Analysis (ICA)	
	.3 Slow Feature Analysis 493	
13	.4 Sparse Coding	
	iv	
CONTE	NTS	
13	.5 Manifold Interpretation of PCA	
14 Aut	pencoders 50	2
14	.1 Undercomplete Autoencoders 503	
14	- ····g	
14		3
14.		
14	5	
14. 14.	5	
14		
14		
15 Rer	presentation Learning 526	
15	· · · · · · · · · · · · · · · · · · ·	3
15	.2 Transfer Learning and Domain Adaptation 536	
15	.3 Semi-Supervised Disentangling of Causal Factors 5	41
15	· · · · · · · · · · · · · · · · · · ·	
15	·	
15	.6 Providing Clues to Discover Underlying Causes 55	4
16 Stri	uctured Probabilistic Models for Deep Learning 558	
16	· · · · · · · · · · · · · · · · · · ·	
16		
16		
16		
16		
16	·	
16	7 The Deen Learning Approach to Structured Probabilistic Models	585

U.,	THE BOOK	Loairing	, ippi odoi	i to otraotaroa	i iobabiliotio modolo	~

17 Monte	e Carlo Methods	590
17.1	Sampling and Monte Carlo Methods	590
17.2	1 3	
17.3	Markov Chain Monte Carlo Methods	595
17.4		
17.5	The Challenge of Mixing between Separated Modes	599
18 Confr	onting the Partition Function	605
18.1	The Log-Likelihood Gradient 6	06
18.2	Stochastic Maximum Likelihood and Contrastive Divergence	ce 607
	V	
CONTENT	re	
CONTENT	S	
18.3	Pseudolikelihood	
18.4		617
18.5		
18.6	Noise-Contrastive Estimation 6	20
18.7	Estimating the Partition Function 62	23
19 Appro	oximate Inference	631
19.1		
19.2	•	
19.3		
19.4	5	
19.5	Learned Approximate Inference	651
	Generative Models	654
20.1	Boltzmann Machines	
20.2		
20.3	Deep Belief Networks	
20.4 20.5	Deep Boltzmann Machines	
20.5		
20.0		
20.7	Boltzmann Machines for Structured or Sequential Outputs Other Boltzmann Machines	
20.9	Back-Propagation through Random Operations	
	Directed Generative Nets	
	Drawing Samples from Autoencoders	
	2 Generative Stochastic Networks	
	3 Other Generation Schemes	
	4 Evaluating Generative Models	
	5 Conclusion	
Bibliogra	phy	721

Index 777

Website

www.deeplearningbook.org

This book is accompanied by the above website. The website provides a variety of supplementary material, including exercises, lecture slides, corrections of mistakes, and other resources that should be useful to both readers and instructors.