

## **STATISTICS ASSIGNMENT- 4**

1. The central limit theorem states that if you have a population with mean  $\mu$  and standard deviation  $\sigma$  and take sufficiently large random samples from the population with replacement, then the distribution of the sample means will be approximately normally distributed. Sufficiently large samples are term as sample set over 30 samples. Therefore, as a sample size increases, the sample mean and standard deviation will be closer in value to the population mean  $\mu$  and standard deviation  $\sigma$ . Central limit theorem is important as in the real world and practical datasets, the samples size is sufficiently larger, thus we can infer the distribution of the sample set will be a Gaussian/normal distribution. In a standard normal distribution 68% of the data lies under  $-1$  to  $+1$  standard deviation, 95% data lies under  $-2$  to  $+2$  std and 99.7% data lies in  $-3$  to  $+3$  std. And the remaining 0.3% data consists of outliers.

2. Sampling is a process of selecting, manipulate and analyze a subset of the entire population. The samples are selected such that they represent the population. As a data scientist we analyze and find patterns data on the representative sample subset and validate those finding on the entire population using hypothesis testing. Sampling allows the data scientist to work on a smaller data set representing the entire population. Sampling methods can be classified into 2 types, probabilistic sampling methods and non-probabilistic types. Some of the sampling techniques I know are from probability sampling are simple random sampling, systematic, stratified and cluster sampling. From non-probabilistic sampling method, Convenience and Judgmental are known to me.

3. Type 1 error, is the error caused by rejecting a null hypothesis when it is true. Type II error is the error that occurs when the null hypothesis is accepted when it is not true. Type 1 error is the conclusion for false positives while type 2 error concludes false negative. Type 1 error is also called as the significance of the test. Type 2 error is also called as the beta error. As a result of type 1 error, then we might end up believing that the hypothesis works even when it doesn't. Whereas, as result of type 2 error, we might end up believing that the hypothesis works even when it doesn't.

4. Normal distribution is a type of probability density function in a shape of a bell curve. It is also known as a Gaussian distribution curve. For an ideal normally distributed data mean, median and the mode all lie on the same point, that is the peak of the bell curve. For a normally distributed feature 68.26% of the data lies in the 1st standard deviation, 95.44% of the data lies in the 2nd standard deviation area and 99.73% of data lies within 3 standard deviations of the feature.

5. Covariance is a measure of the joint variability of two random variables. Correlation it is obtained by dividing the covariance of the two variables by the product of their standard deviations. The covariance values of the variable can lie anywhere between  $-\infty$  to  $+\infty$  whereas the values of correlation are between -1 to +1. Also, correlation is a unit-free measure whereas covariance is not a unit-free measure.

6. Univariate analysis is done using a single feature from the dataset, bivariate analysis is performed using 2 features whereas multi-feature analysis is performed using more than 2 variables. Plots used for visualizing univariate analysis are count plots, histograms, density curves, distribution plots etc. Plots used for visualizing bivariate analysis are bar plots, scatter plots, joint plots, strip plots etc. Multivariate analysis plots are made by adding hue data as an indication to the bivariate plots.

7. Sensitivity informs us about the proportion of actual positive cases that have been predicted as positive by our model. It is also known as the true positive rate. It is also known as recall.

8. Hypothesis testing is the process used to evaluate the strength of evidence from the sample and provides a framework for making determinations related to the population. This sample is selected using one of the various sampling methods, probabilistic or non-probabilistic.  $H_0$  is the notation for null hypothesis whereas  $H_1$  is the notation for alternate hypothesis. For a two-tailed test, the null hypothesis ( $H_0$ ) should be rejected when the test value is in either of two critical regions on either side of the distribution of the test value and vice versa for alternate hypothesis.

9. Quantitative data can be counted, measured, and expressed using numbers. Qualitative data is descriptive and conceptual. Qualitative data can be categorized based on traits and characteristics. Simply, we can say that the data which can be measured and represented by numbers is called quantitative data.

There are two types of quantitative data: -

**Discrete data:** - Data which can be represented by integers or which doesn't contain any continuous values is known to be discrete data.

Ex: - number of tickets sold in a day, Age etc

**Continuous data**: - Data which is represented in the form of decimals or continuous values is called continuous data.

Ex: - Temperature, height etc.

10. Range is calculated by: highest value – lowest value IQR is calculated by: upper quartile (Q3) – lower quartile (Q1). This one of the method helpful in detecting outliers in the data.

11. A bell curve distribution represents the normal/ Gaussian distribution. In a bellcurve distribution the mean will be zero and the standard deviation is + or - 1

12. Two of the many methods to find outliers are Z-score and IQR .

In Z-score method, Outliers are those whose zscore values are  $> +3$  or  $< -3$ .

In IQR method we will subtract the 25<sup>th</sup> percentile from 75<sup>th</sup> percentile as outliers.

Ideally Zscore is considered the best method for treating the outliers.

13. The P value or calculated probability is the estimated probability of rejecting the null hypothesis ( $H_0$ ) of a study question when that hypothesis is true. A smaller p-value means that there is stronger evidence in favor of the alternative hypothesis. If the probability or p-value is less than 0.05 or doesn't come under 95% confidence level, then we reject null hypothesis. Similarly, if the p-value is not less than the significance level pr confidence level then we fail to reject the null hypothesis.

14. Binomial Probability formula:  $P(X) = \frac{n!}{(n-X)! X!} * (p)^X * (q)^{n-X}$  Where X is the total number of successes. p is the probability caused by success of an individual trail q is the probability caused by failure of an individual train ( $q = 1-p$ ) n Is the number of trials.