Spray

First, we build the graph where the nodes represent the locations in the cube, and edges a path between them. (with some hashing method)

Because of the invariance in parity, the graph is bipartite.

The problem asks for a minimum vertex cover now, which can be computed using the maximal coupling algorithm