

# Mantle geodynamics

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*with materials from lectures by Stéphane Labrosse, Maëlis Arnould,  
Yanick Ricard, Maylis Landeau, Catherine Thoraval*

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ÉCOLE DE  
**PHYSIQUE DES HOCHES**



# Mantle geodynamics

- 1. Evidence for surface (plate) and deep (mantle) motions**  
*+ orders of magnitude*
- 2. Dynamic models to understand the mantle** (past & present)
- 3. Mantle and plate dynamics : modelling diversity and recipes**
- 4. Progress and perspectives**

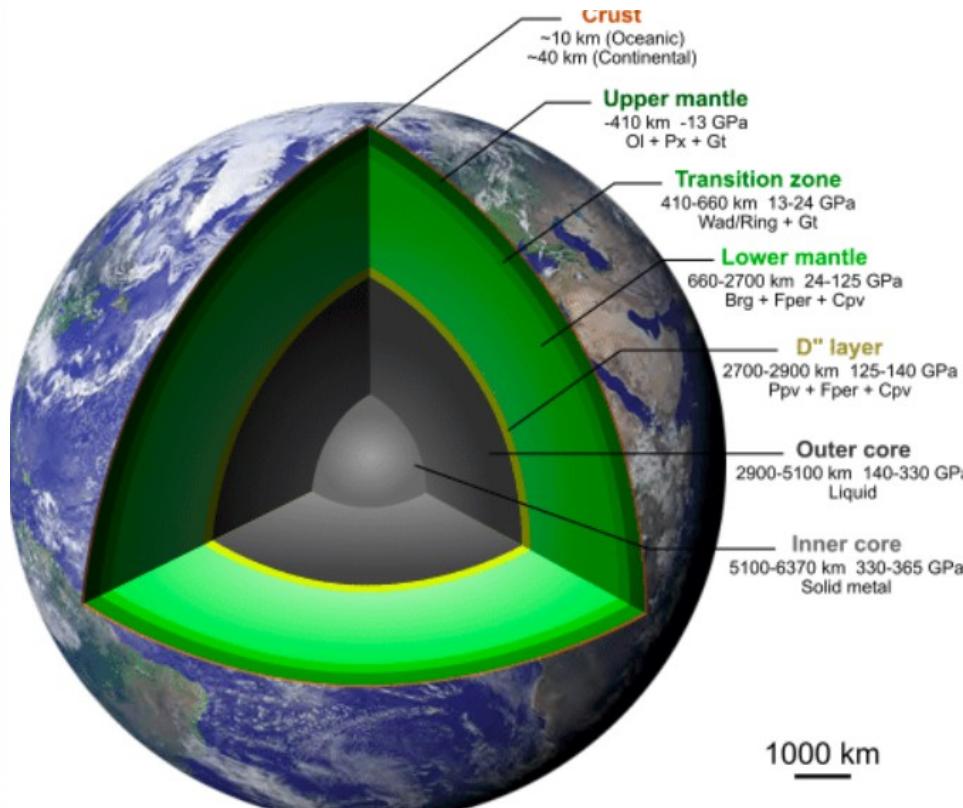
# Mantle geodynamics

- 1. Evidence for surface (plate) and deep (mantle) motions  
+ *orders of magnitude***
- 2. Dynamic models to understand the mantle (past & present)**
- 3. Mantle and plate dynamics : modelling diversity and recipes**
- 4. Progress and perspectives**

# Although we cannot feel or see it... solid Earth moves...!?

Mantle from 10 to 2900 km

- deepest borehole on Earth = ???

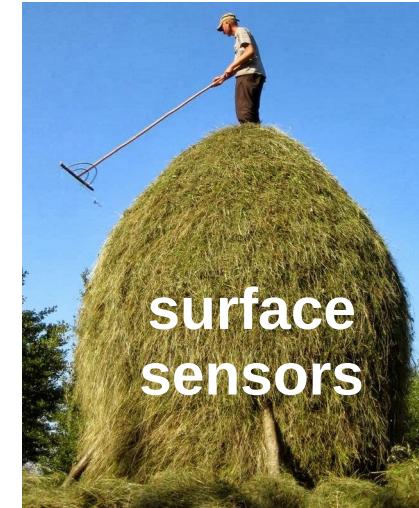
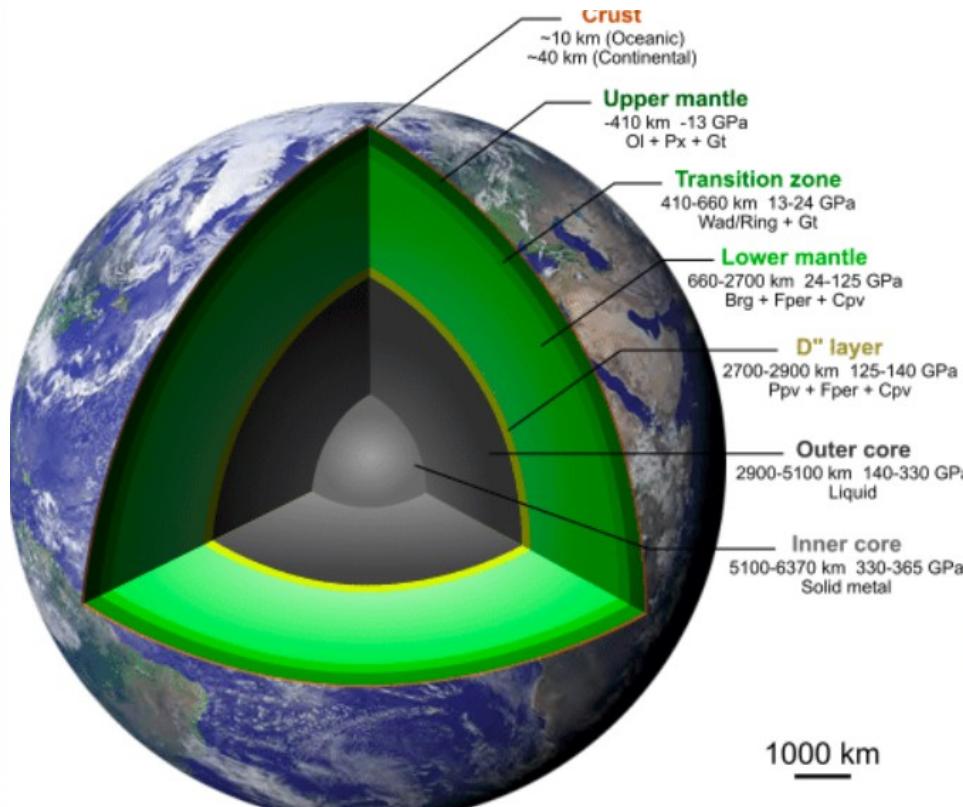


> we *barely* measure  
the surface (**slow**) motions

# Although we cannot feel or see it... solid Earth moves...!?

Mantle from 10 to 2900 km

- deepest borehole on Earth = 12 km

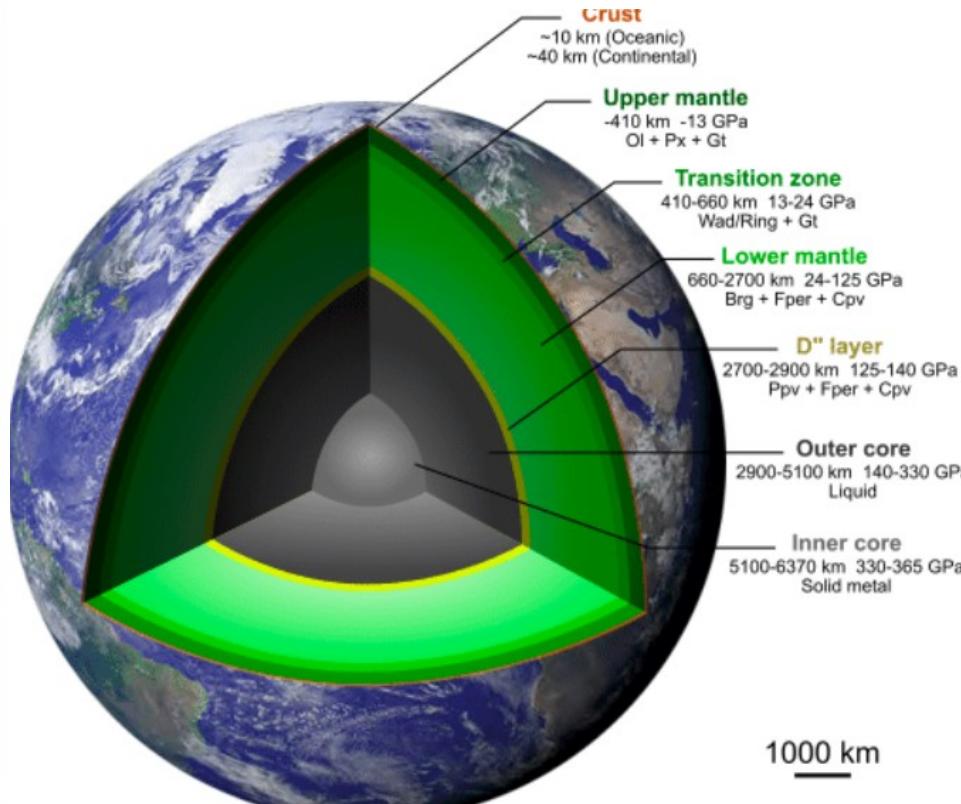


> we *barely* measure  
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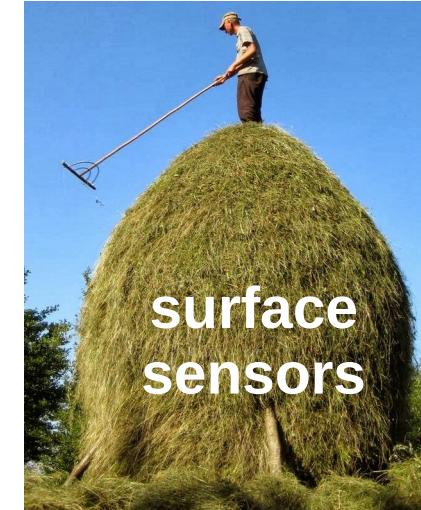
# Although we cannot feel or see it... solid Earth moves...!?

Mantle from 10 to 2900 km

- deepest borehole on Earth = 12 km



Yoshizaki & McDonough 2021

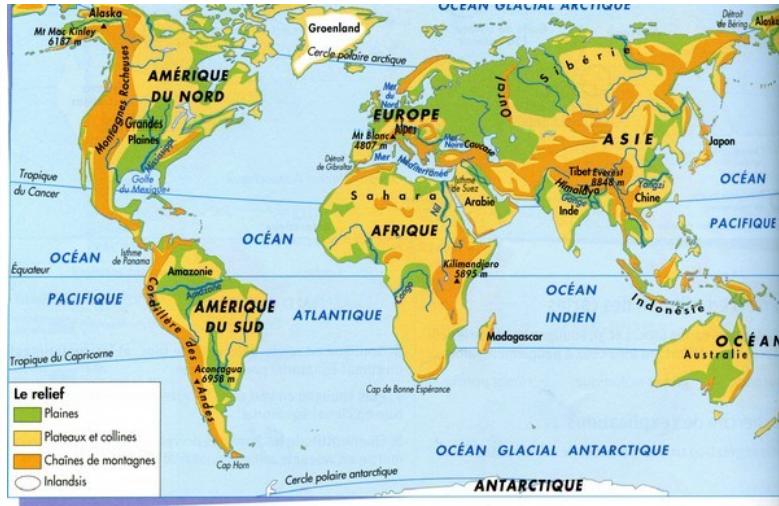


- > we *barely* measure the **surface (slow) motions**
- > inaccessible deep Earth : argument for deep dynamics is necessarily **indirect**



# Argument for surface motions : ocean topography

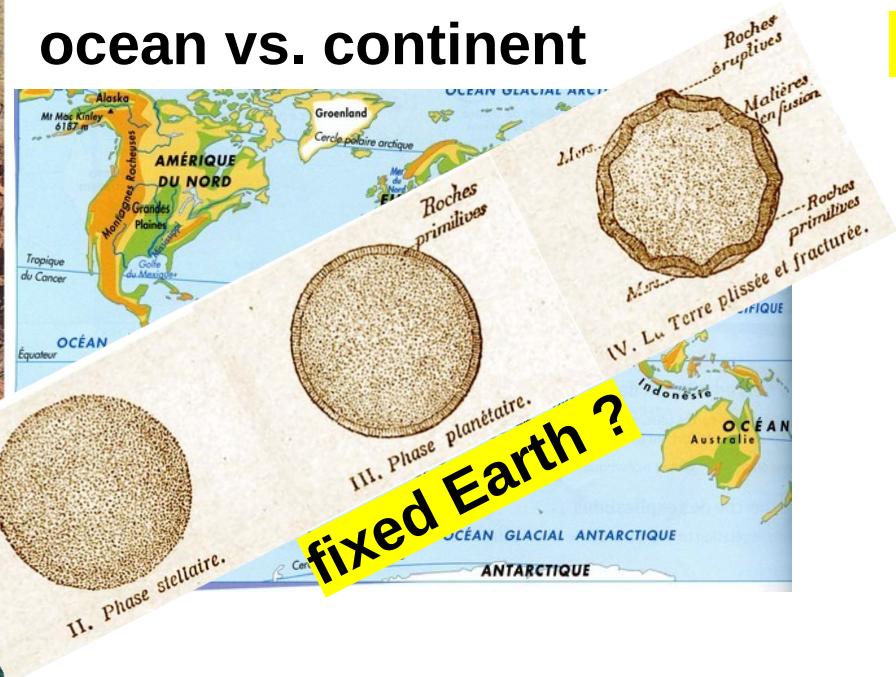
## ocean vs. continent



# Argument for surface motions : ocean topography

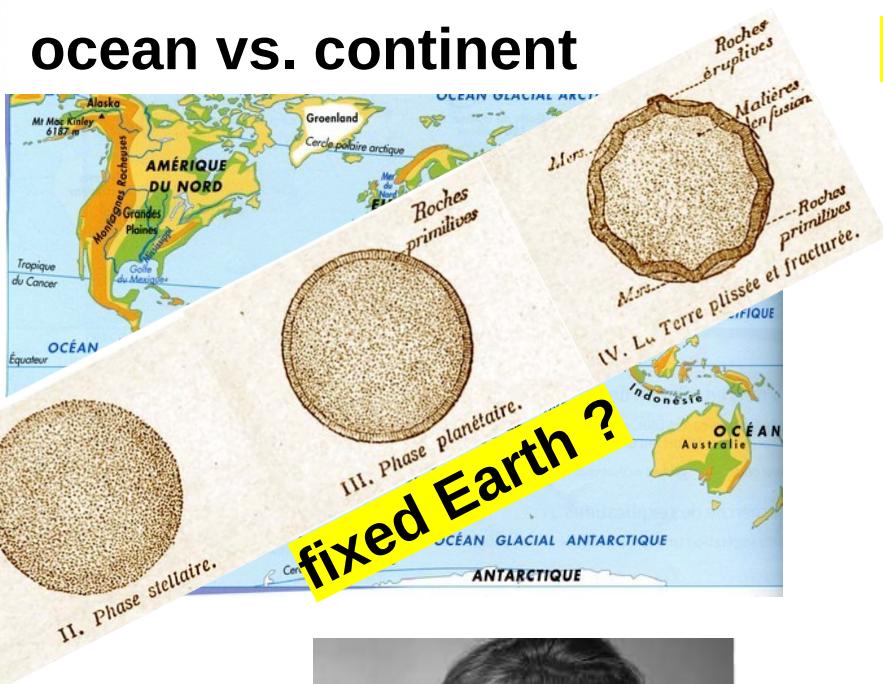
**ocean vs. continent**

... but is the sea floor uniform ?



# Argument for surface motions : ocean topography

ocean vs. continent



Mary Tharp, Bruce Heezen - 1957

... but is the sea floor uniform ?

NO !!!

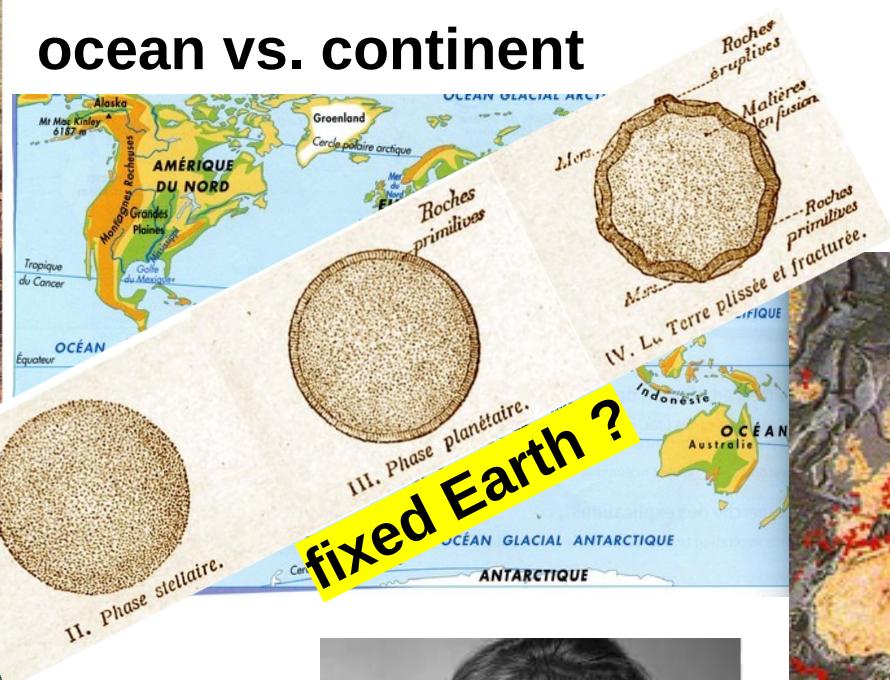


# Argument for surface motions : ocean topography

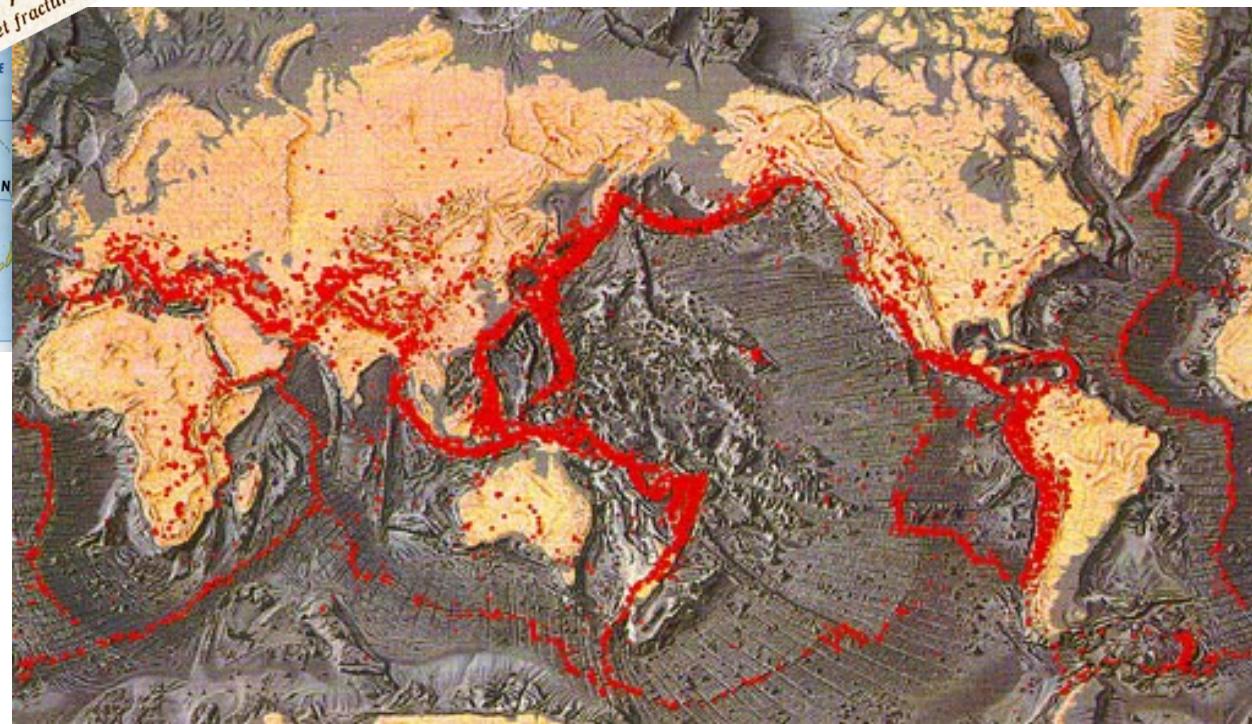
ocean vs. continent

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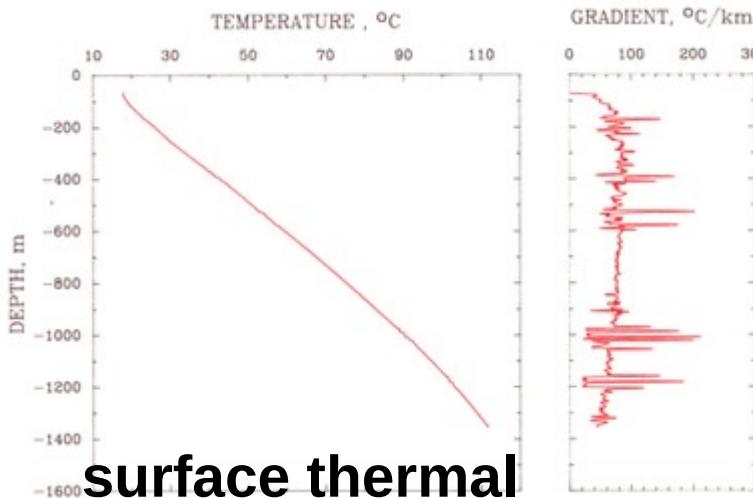
**NO > plate boundaries vs. plates !**



Mary Tharp, Bruce Heezen - 1957



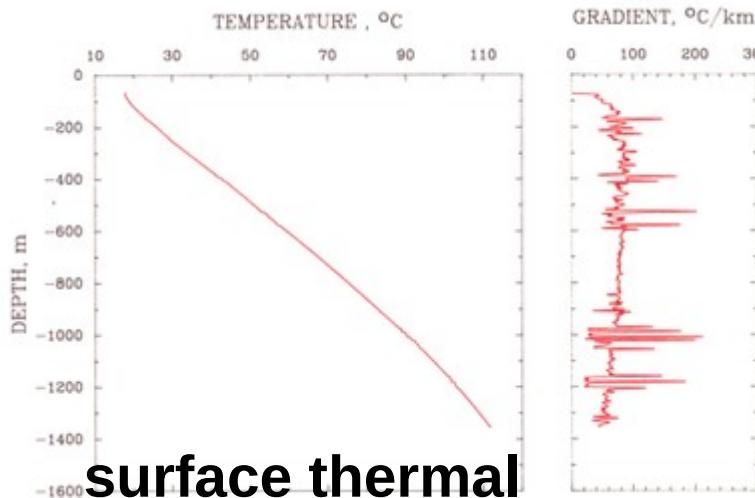
# Argument for solid Earth motions : Earth's internal temperature & surface heat flow



**surface thermal  
gradient ~ 30°C/km**

extrapolation to 6400 km depth  
= 200 000°C ??? gas ?!

# Argument for solid Earth motions : Earth's internal temperature & surface heat flow



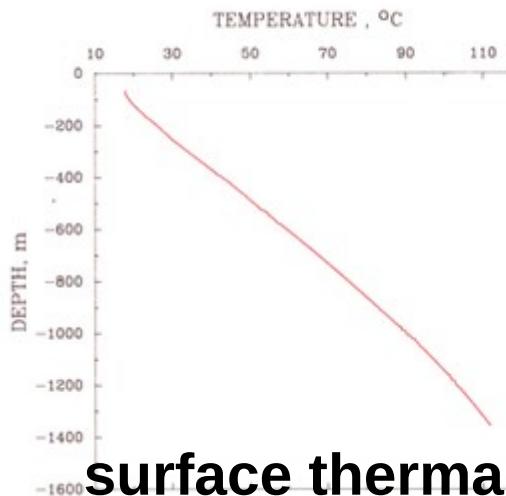
**surface thermal  
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- need a reduced thermal gradient
  - > **convective heat transport**
  - and **motion** of Earth's interior ?

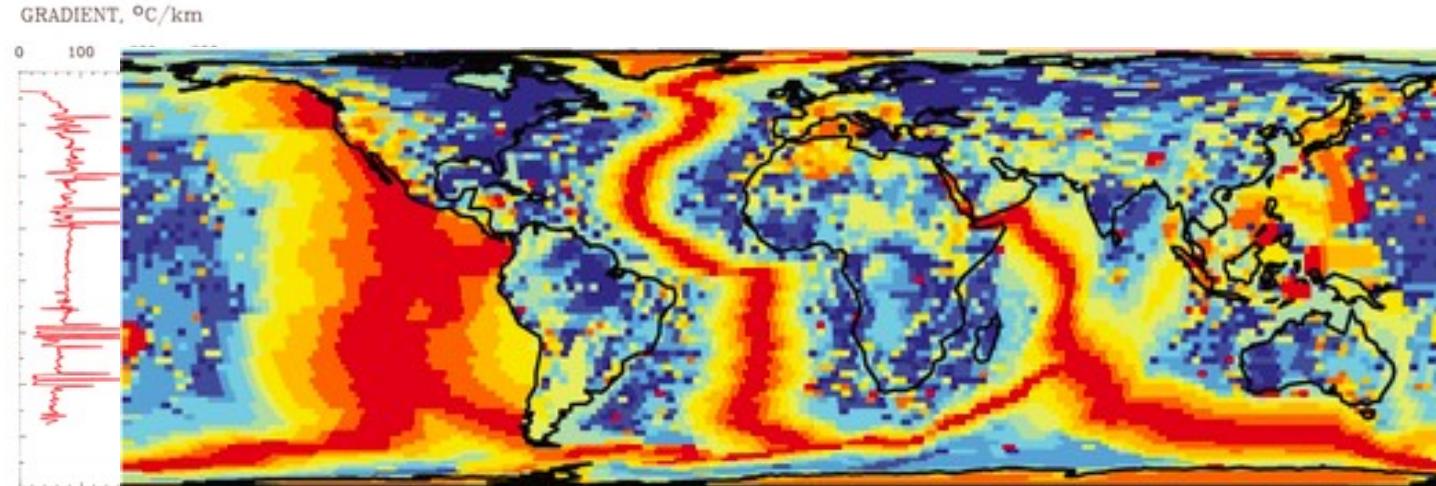


# Argument for solid Earth motions : Earth's internal temperature & surface heat flow

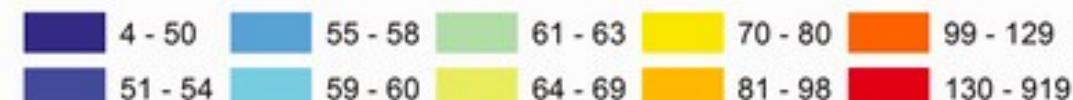


surface thermal  
gradient ~ **30°C/km**

extrapolation to 6400 km depth  
= 200 000°C ??? gas ?!



Final Estimate of Heat Flow (mW m<sup>-2</sup>) (Area-weighted Median)

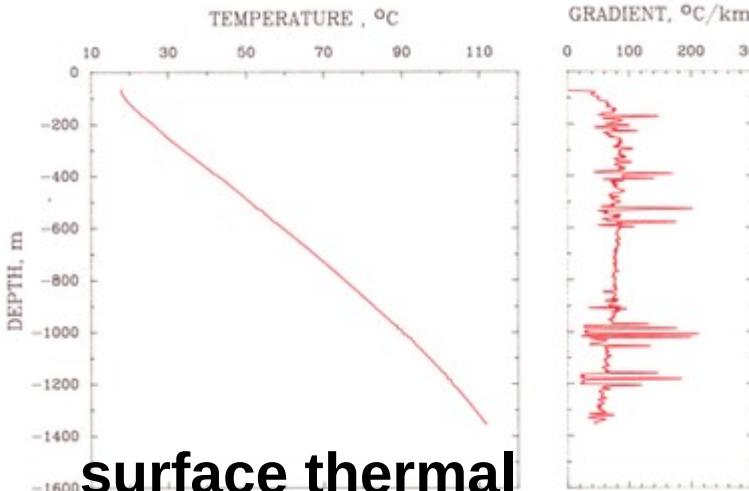


Davies G<sup>3</sup> 2013

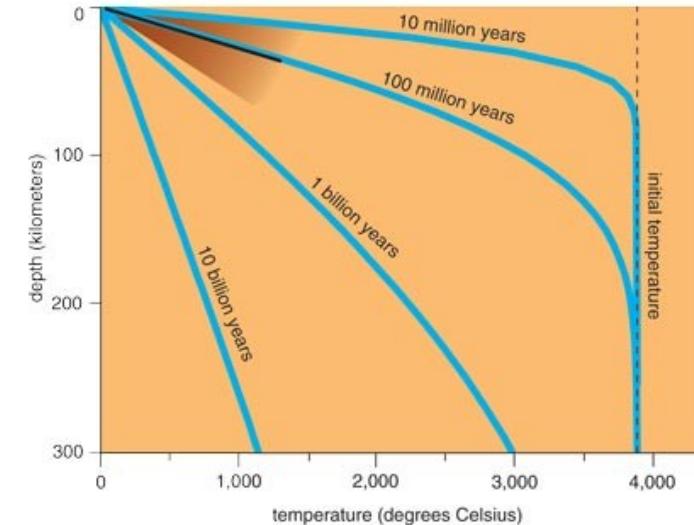
→ need a reduced thermal gradient  
> **convective heat transport**  
and motion of Earth's interior ?

regions of large heat flux :  
magmatism, **hot upwelling** ?

# Argument for solid Earth motions : Earth's internal temperature & surface heat flow



**surface thermal  
gradient ~ 30°C/km**



extrapolation to 6400 km depth  
= 200 000°C ??? gas ?!

**from cooling to Earth's age**  
> **Buffon, Fourier, Kelvin, Perry...**

→ need a reduced thermal gradient  
> **convective heat transport**  
and motion of Earth's interior ?

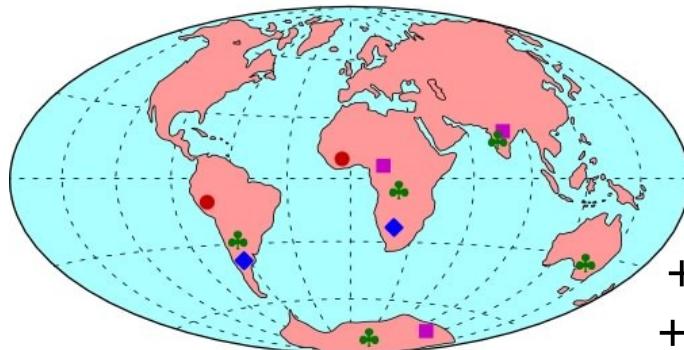
<https://www.americanscientist.org/article/kelvin-perry-and-the-age-of-the-earth>

<https://planet-terre.ens-lyon.fr/ressource/age-Terre-histoire.xml>

# Evidence of surface motions : geological and paleontological records

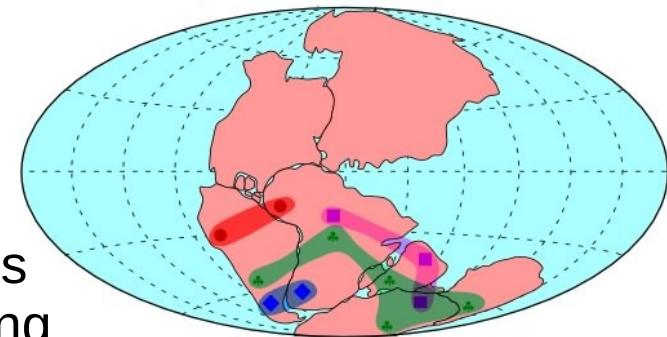


Wegener  
1912



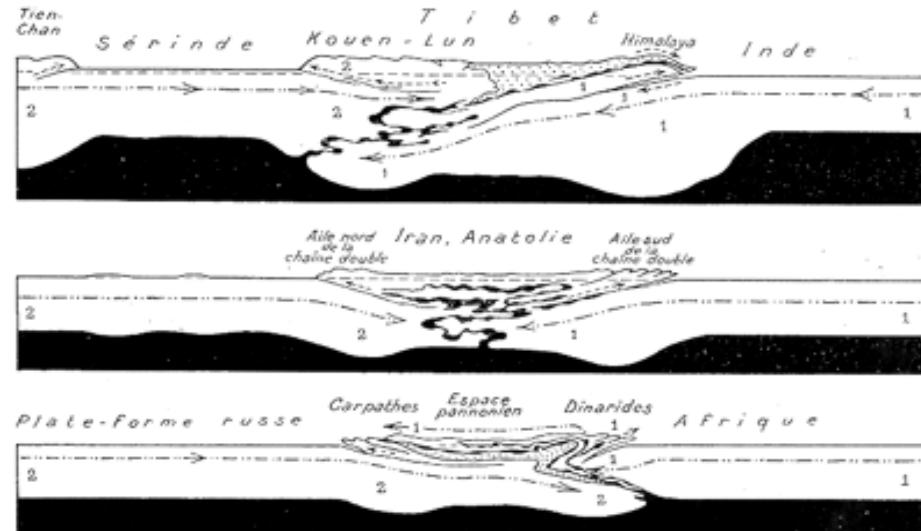
permian fossils  
+ glacial striations  
+ coast interlocking

La solution de Wegener

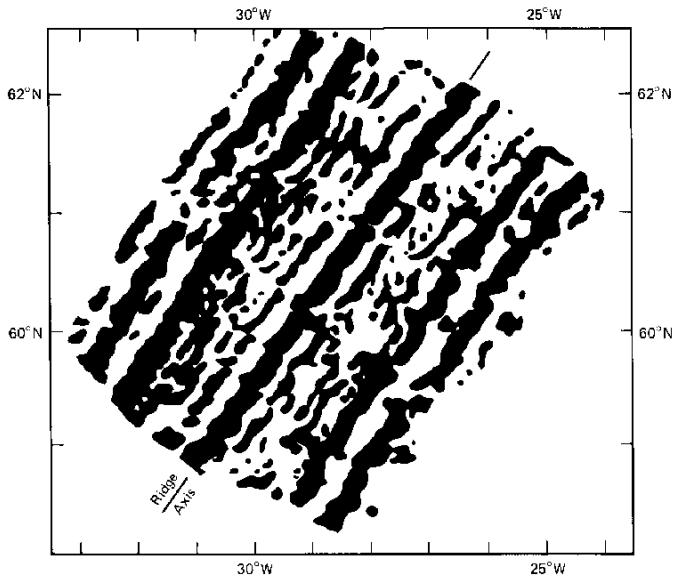


Bertrand + Haug +  
Du Toit + Argand

<https://planet-terre.ens-lyon.fr/ressource/derive-continentes-wegener.xml>



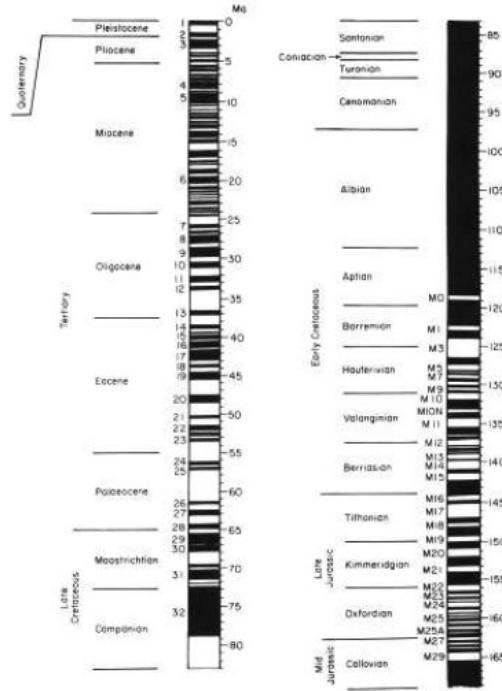
# Evidence of surface motions : paleomagnetism



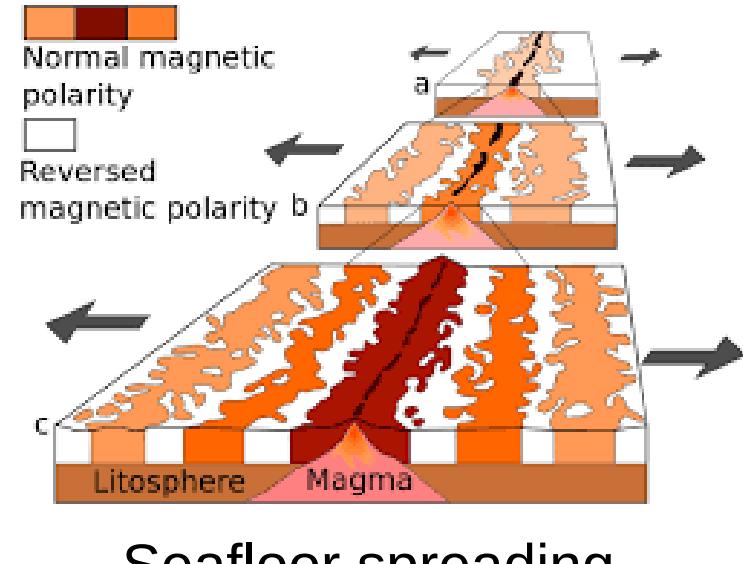
300 geomagnetic  
reversals these  
last 200 Myr



Figure 3.6 Chronométrie des polarités du champ magnétique depuis 165 Ma



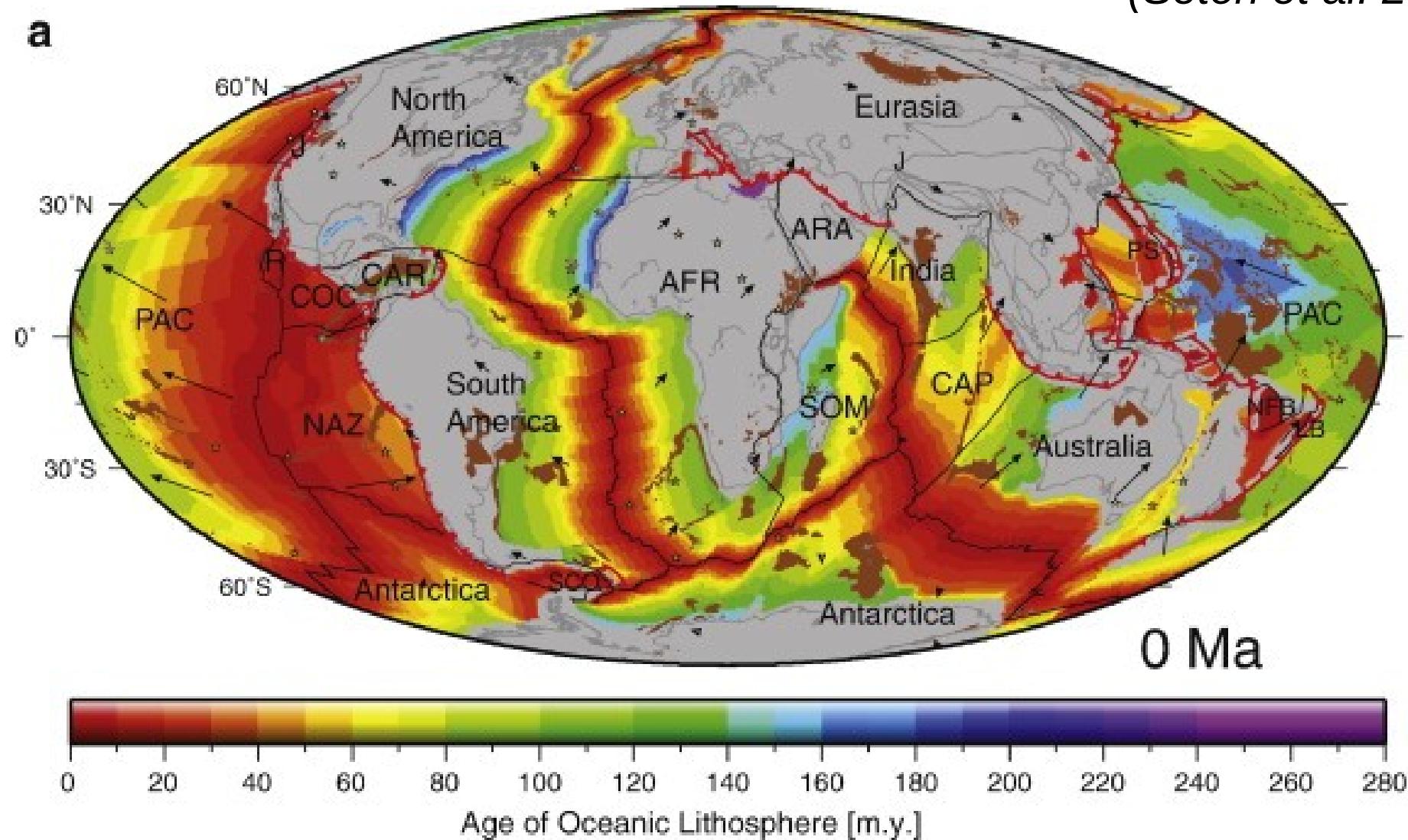
**magnetite ( $\text{Fe}_3\text{O}_4$ ) of basalt  
and gabbro record the  
magnetic field polarity during  
its cooling at ridge  
(magnetization below 730°C)**



Seafloor spreading  
(Morley, Vines, Matthews - 1963)

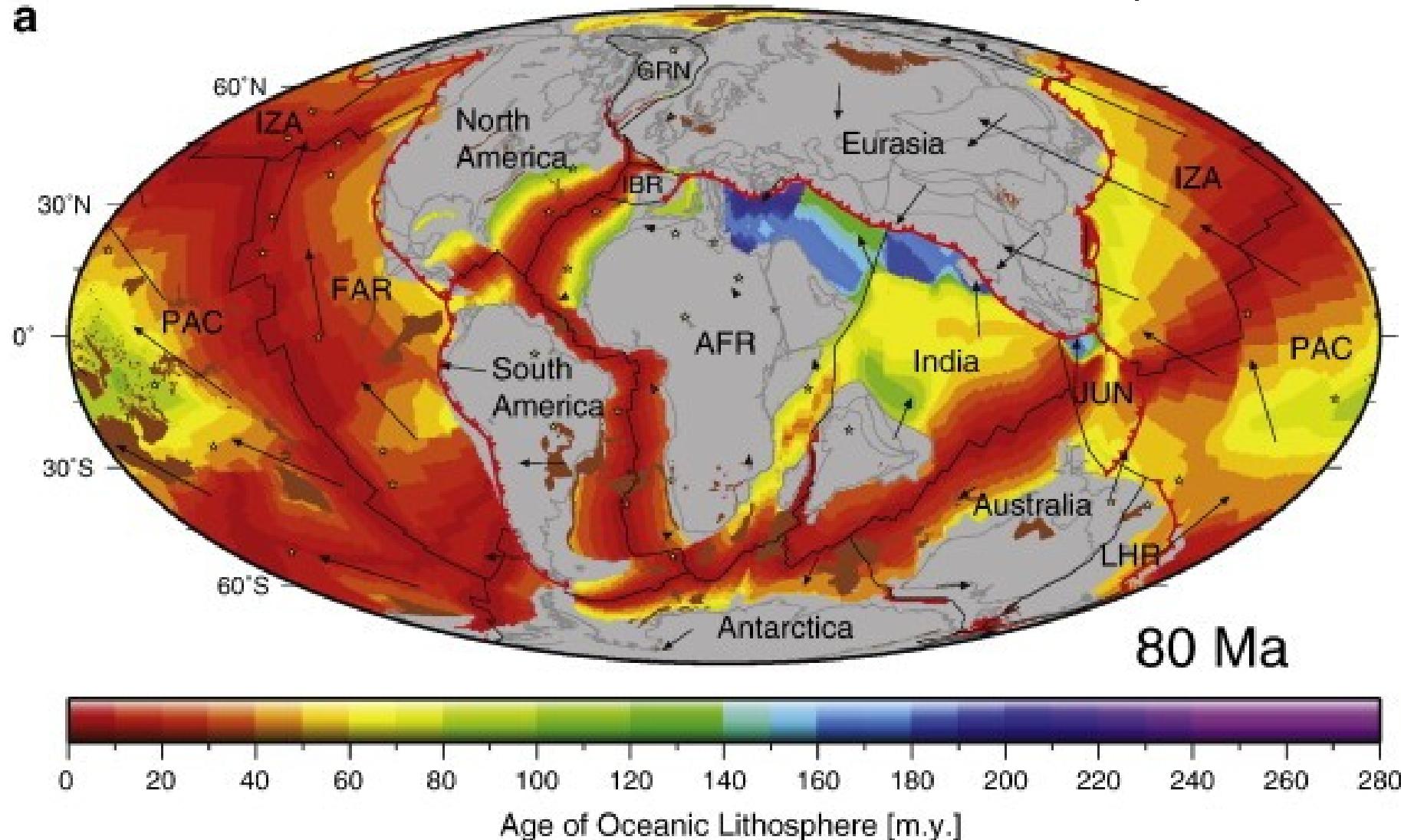
(Seton et al. 2012)

a



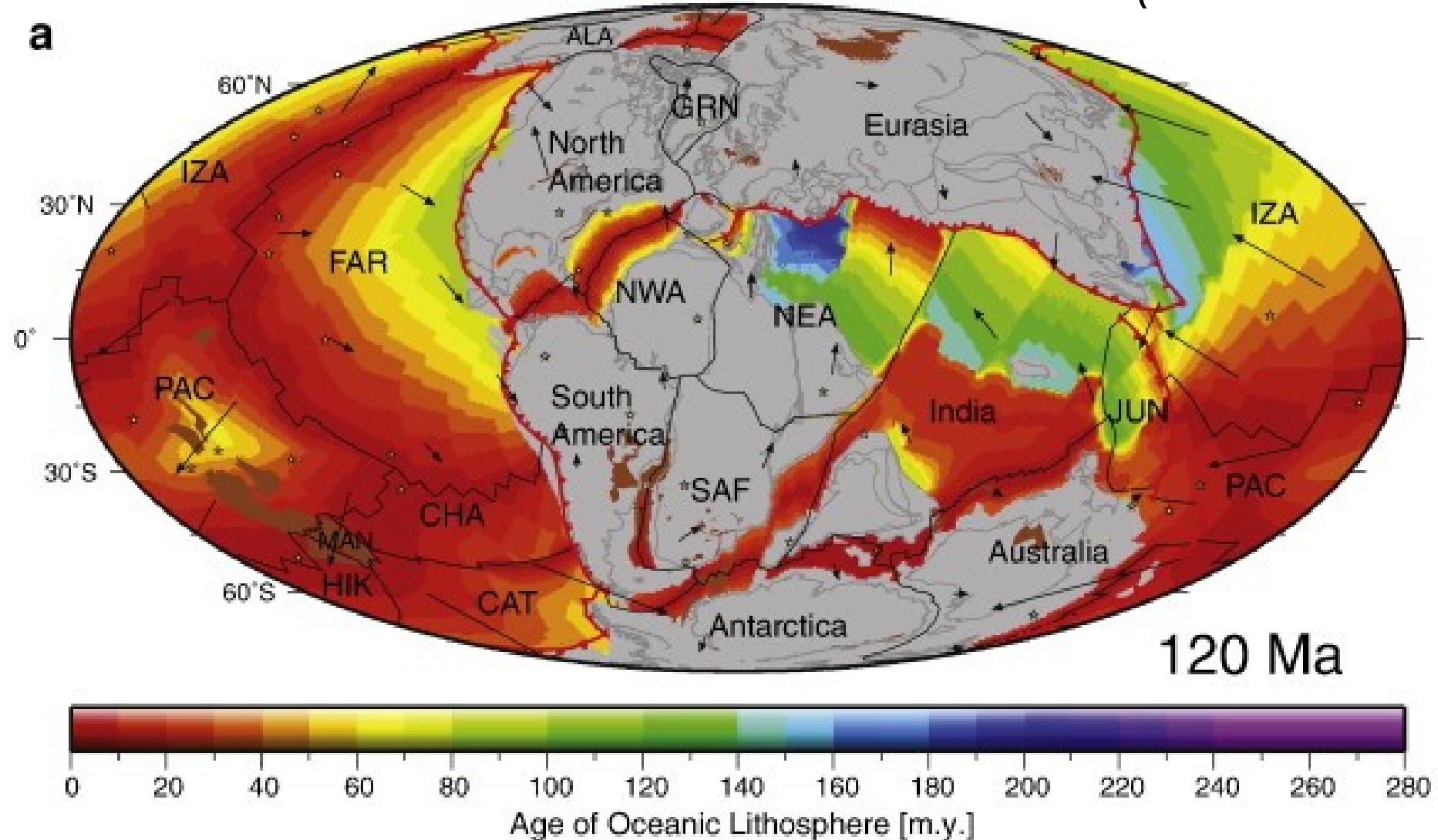
(Seton et al. 2012)

a



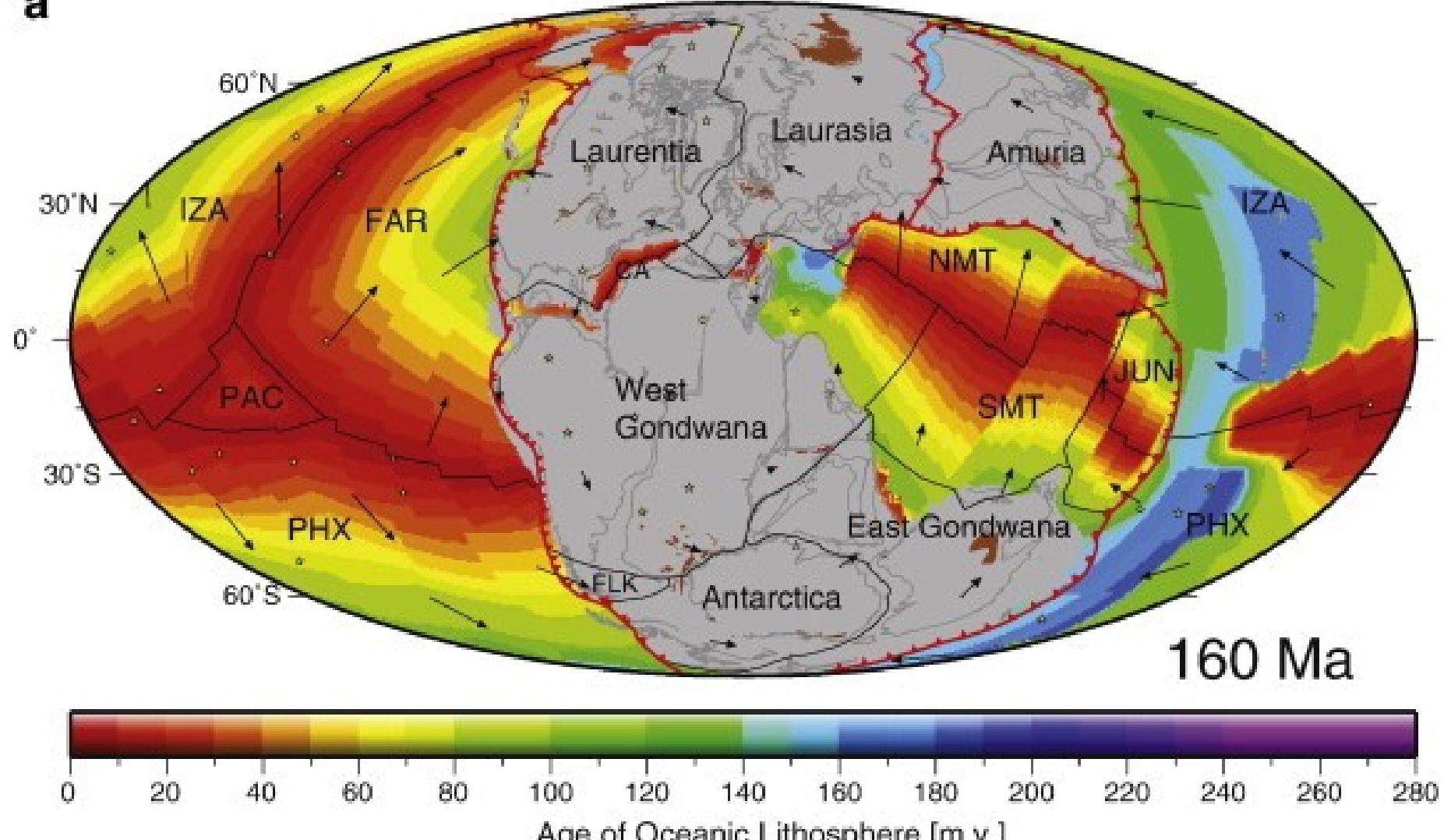
(Seton et al. 2012)

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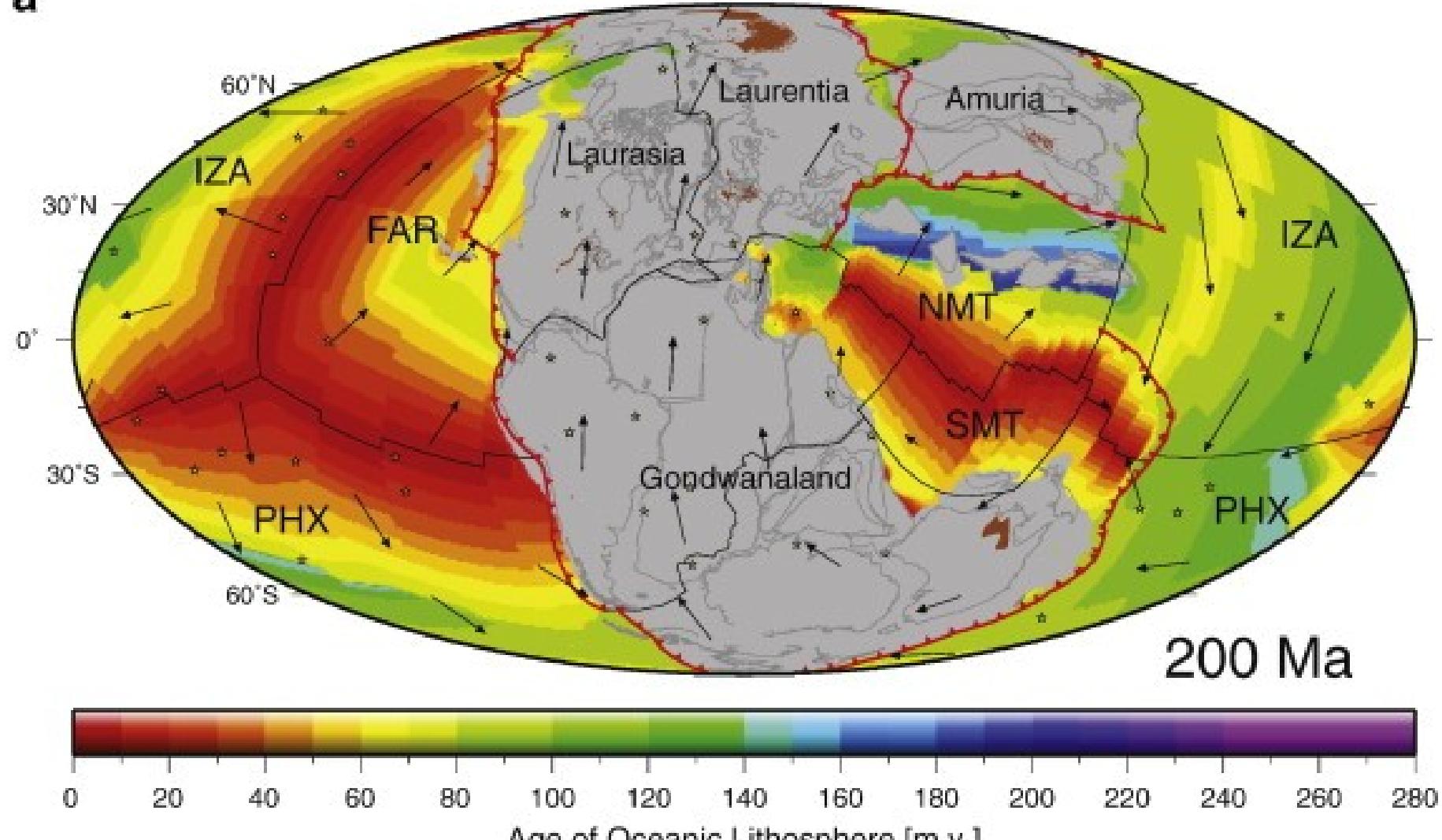
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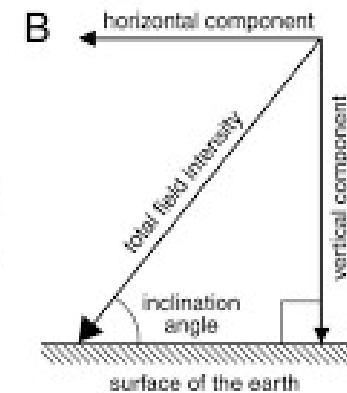
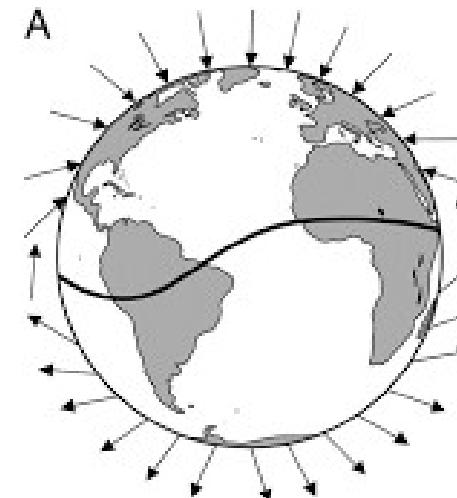
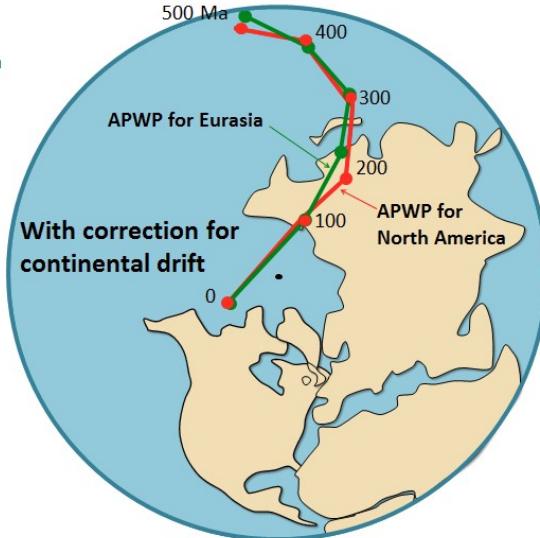
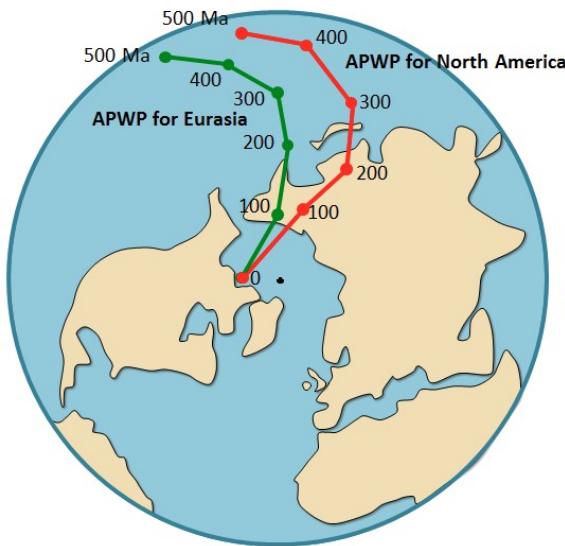


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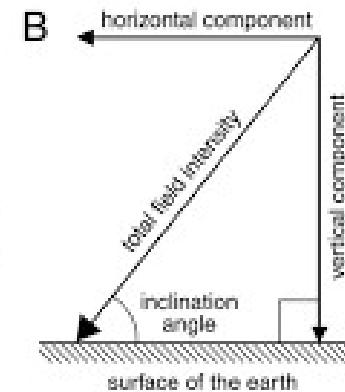
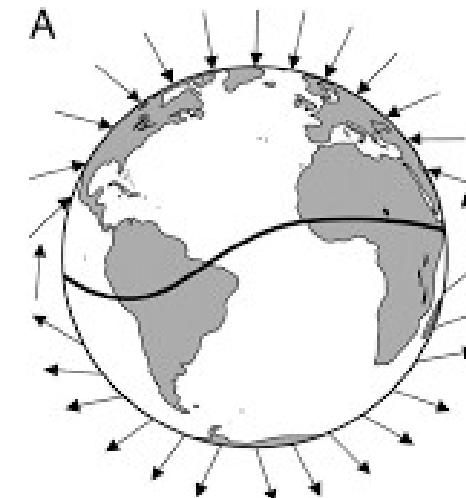
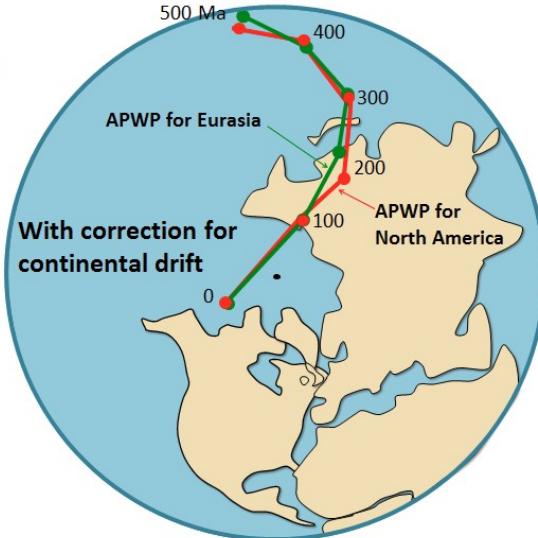
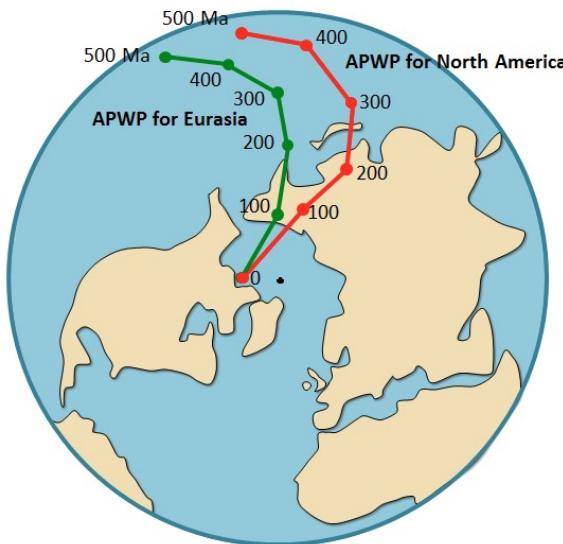
# Evidence of surface motions : paleomagnetism



Apparent polar wander  
path (APWP) due to  
continents motion



# Evidence of surface motions : paleomagnetism



Apparent polar wander path (APWP) due to continents motion

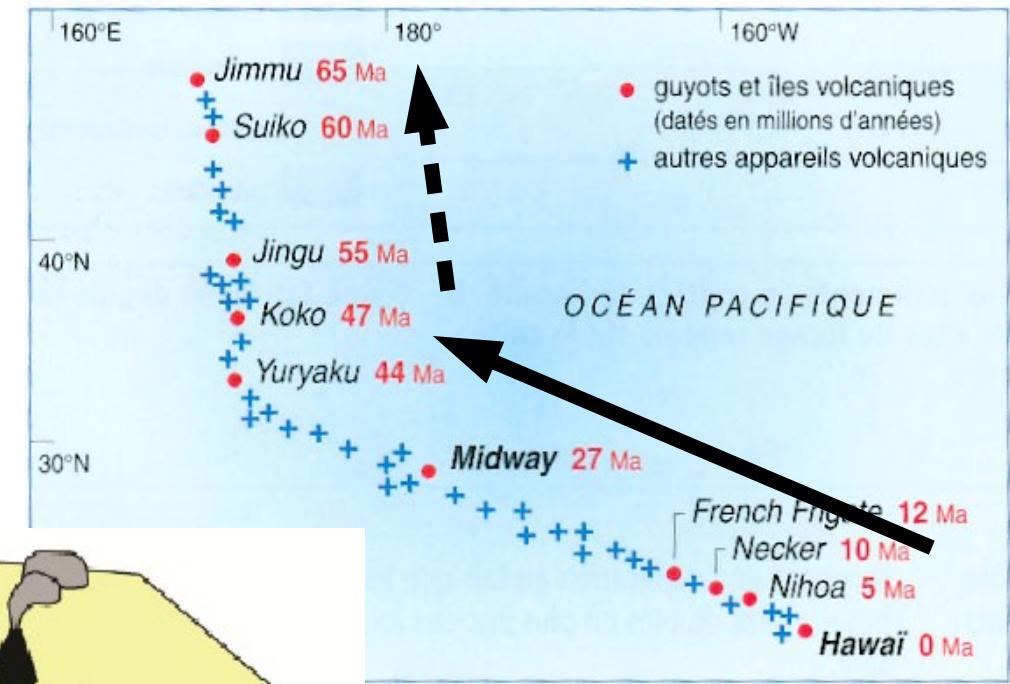
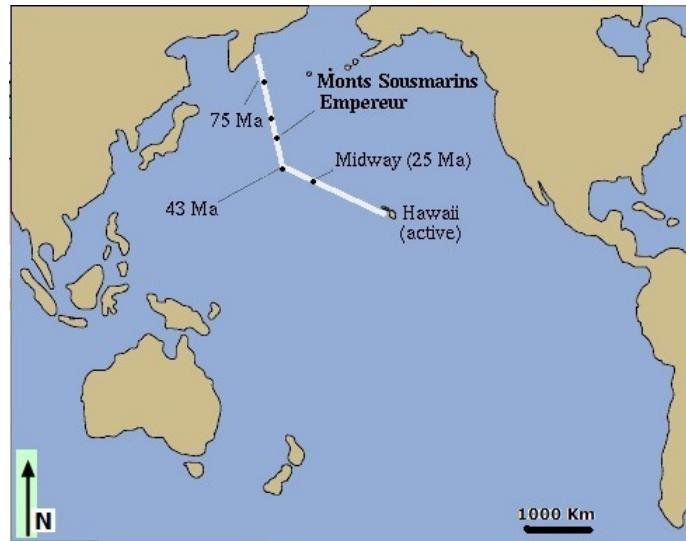


paleolatitude  
deduced from  
**paleo-magnetic  
inclination**

*Rodina  
supercontinent ?*

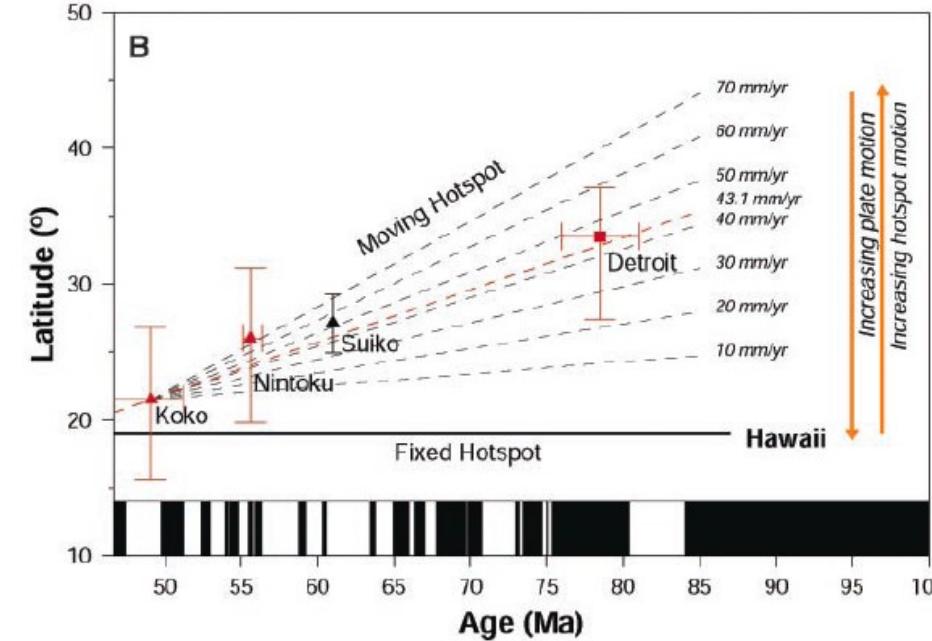
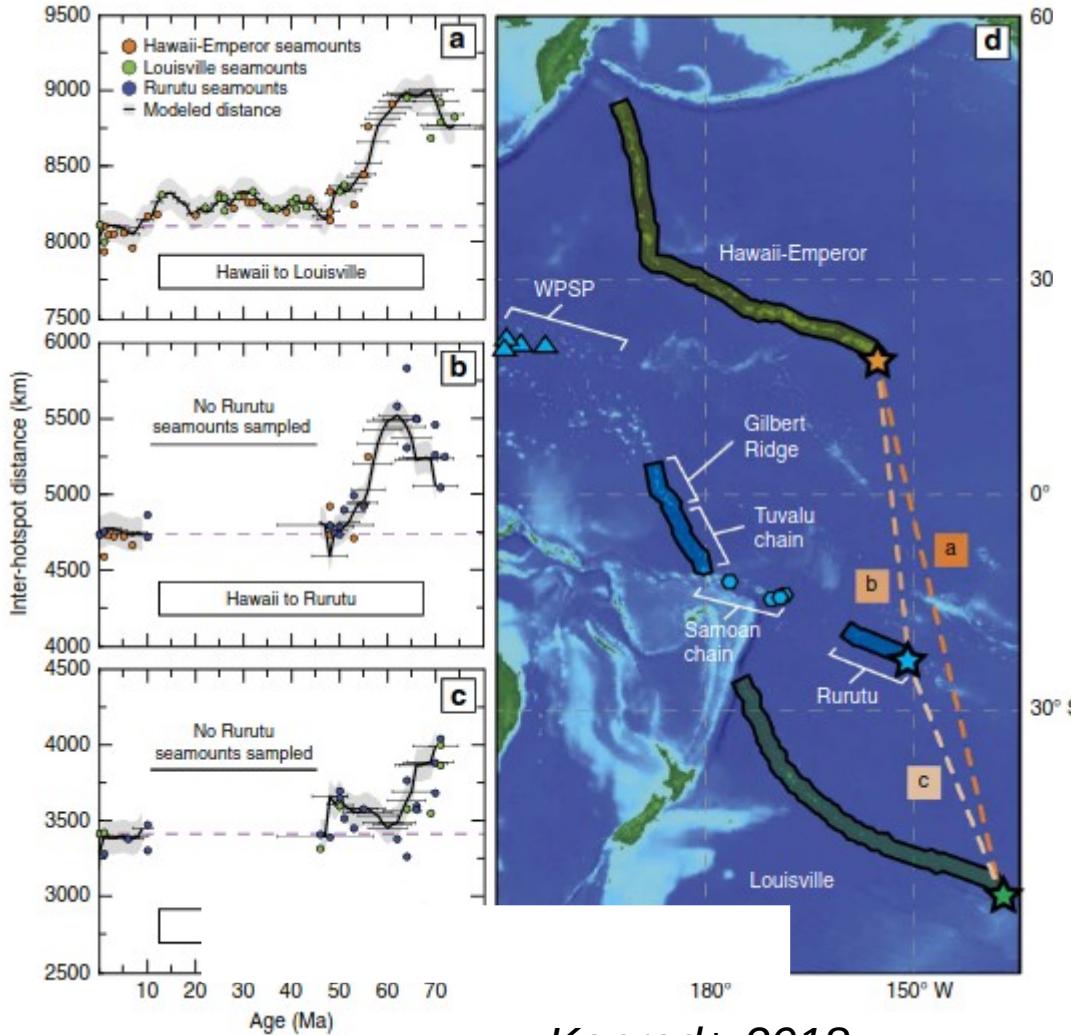


# Evidence of surface motions : hotspot volcanic alignment



**Fixed plume and moving plate** >  
reconstruction of velocity magnitude  
and direction back in time

# Evidence of surface motions : hotspot volcanic alignment



Tarduno+ Science 2003

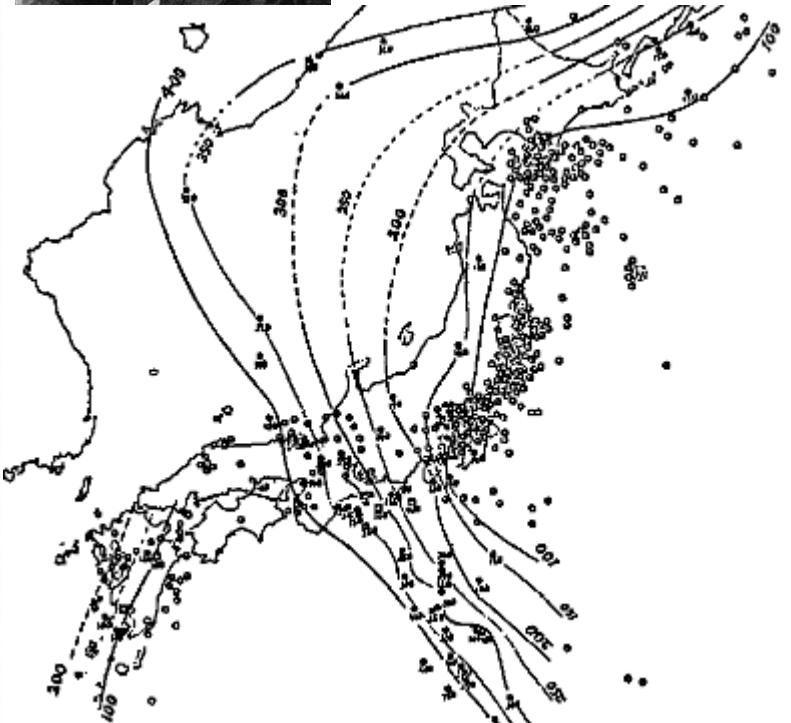
Not so fixed plumes... ?



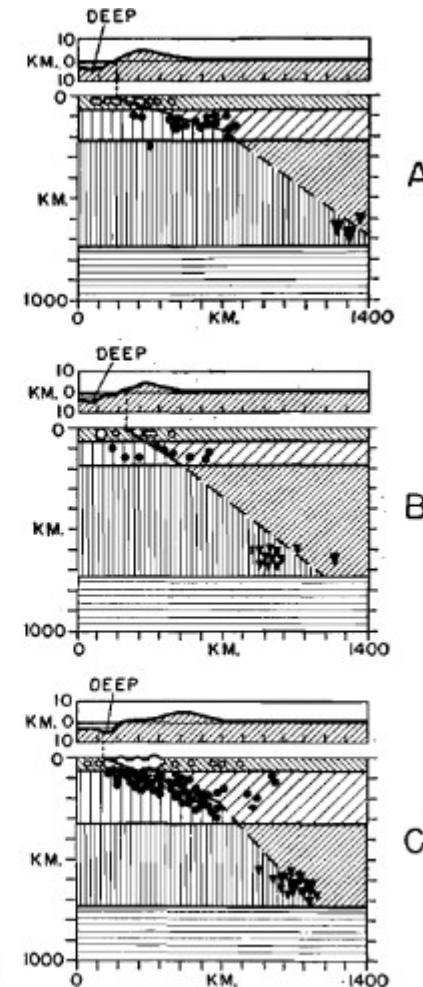
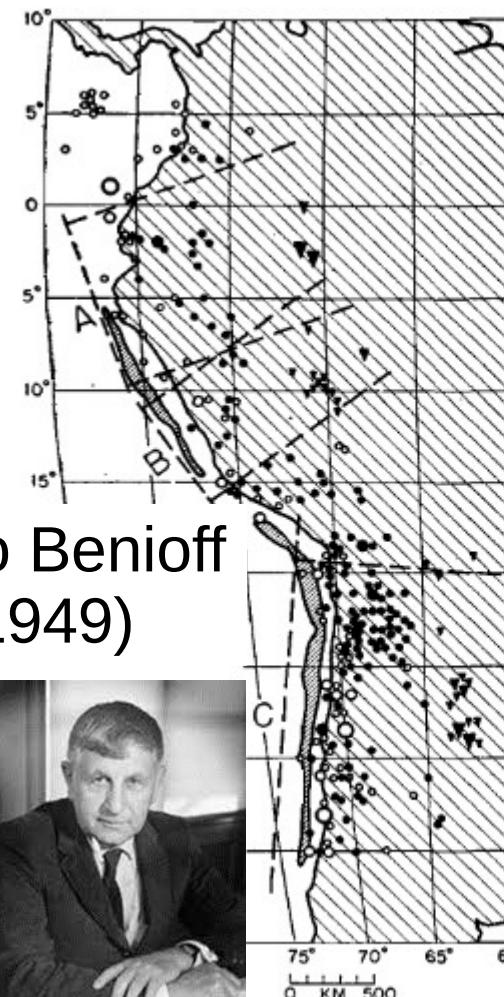
# Evidence of surface motions : faults and earthquakes



Kiyoo Wadachi  
(1928-1935)

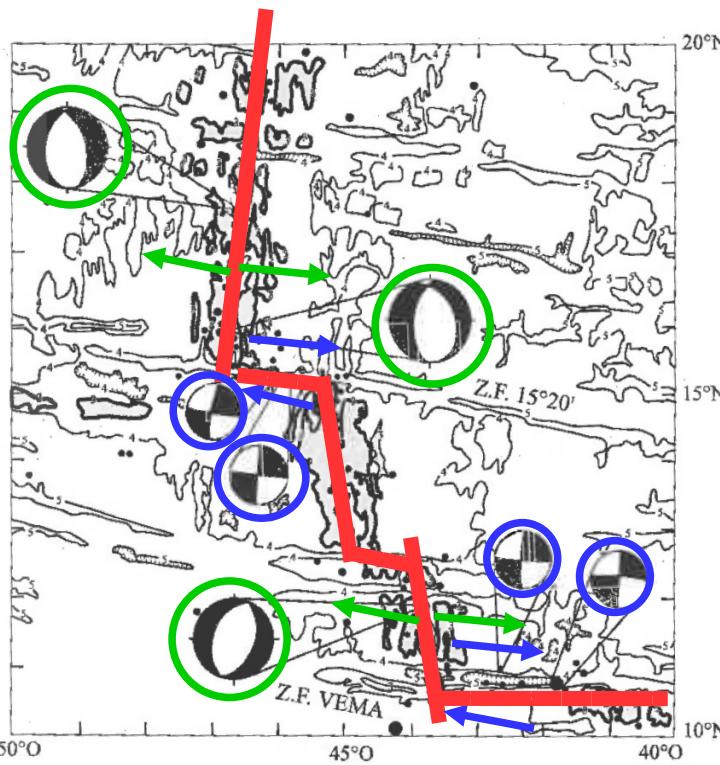


Hugo Benioff  
(1949)

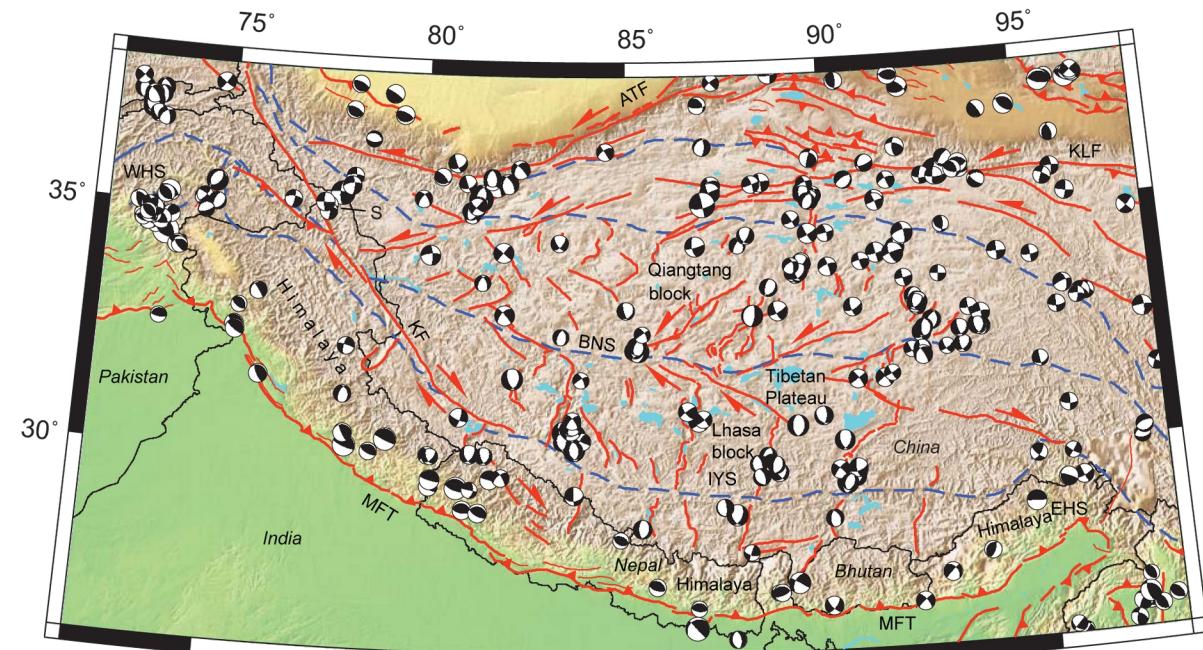


# Evidence of surface motions : faults and earthquakes

*Focal mechanisms of large (plate boundary) faults*



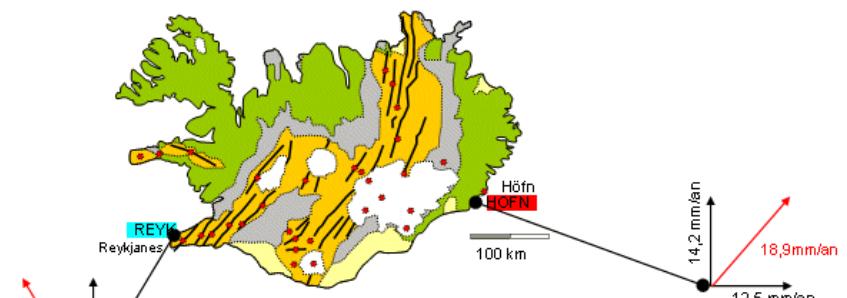
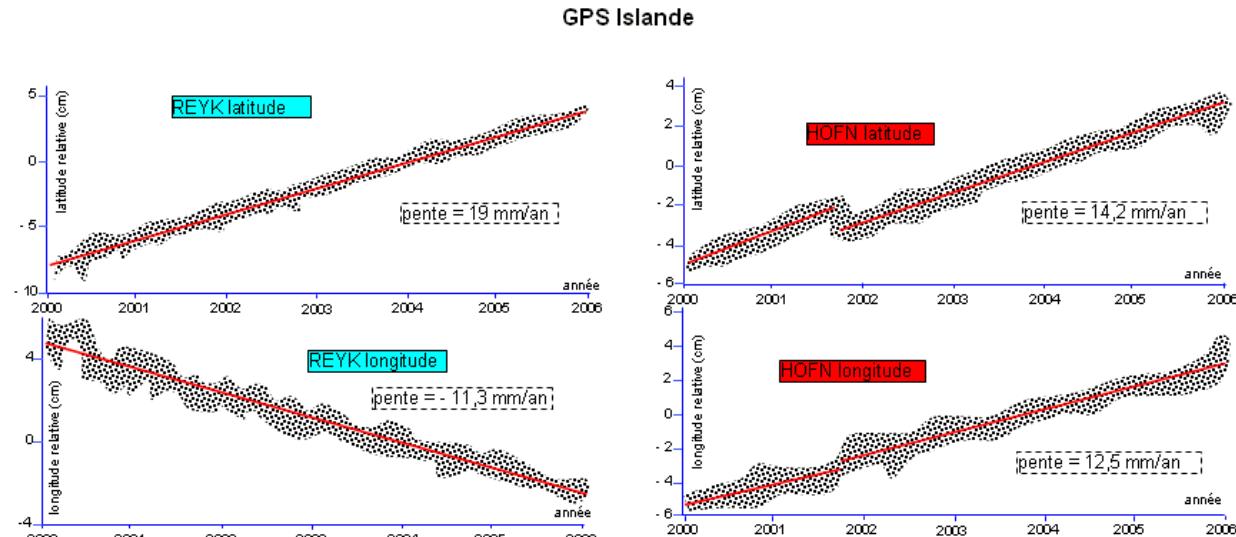
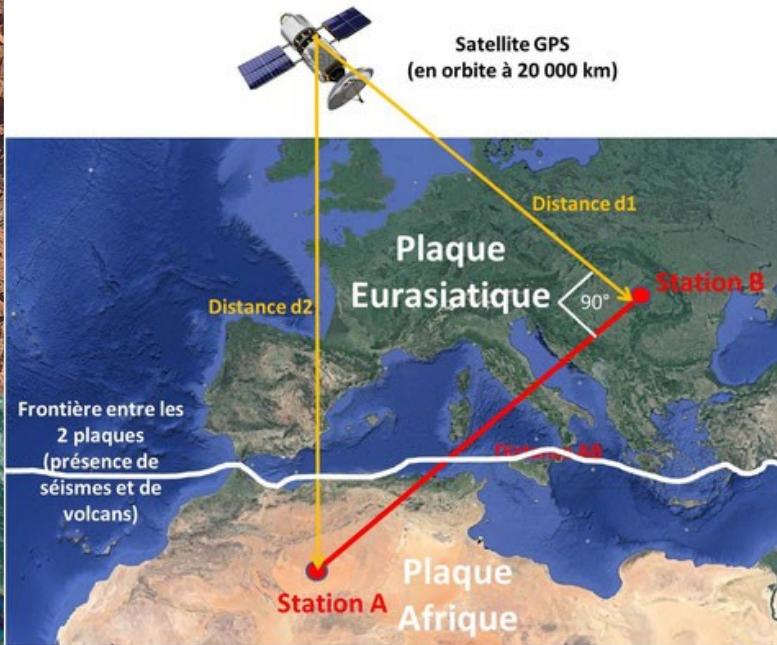
Normal and transform  
faults at mid-Atlantic ridges



Inverse (thrust) faults in Himalaya +  
intraplate deformations  
(plates are not fully rigid)

# Evidence of surface motions : geodesy

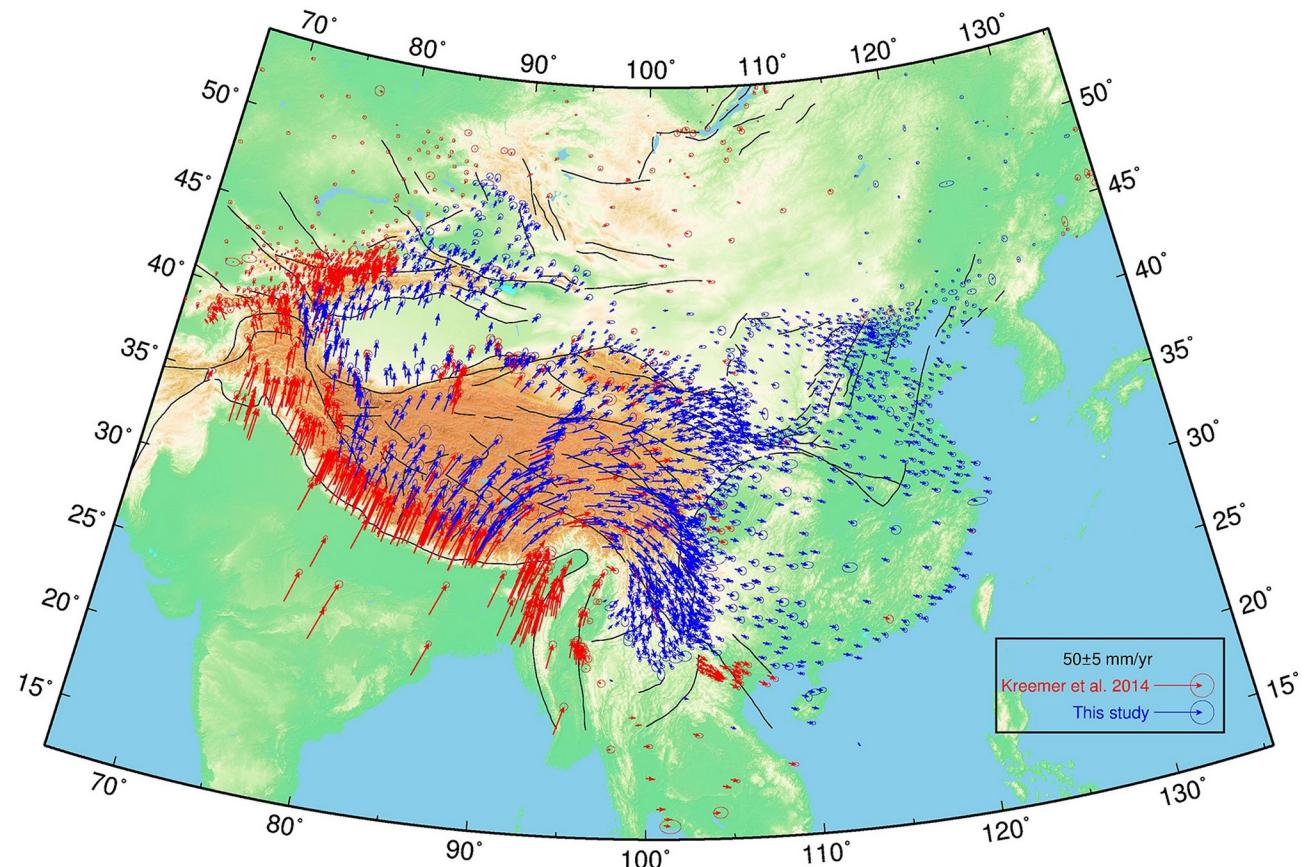
GPS, DORI, VLBI > displacements inferred at human time scales  
(10s years)



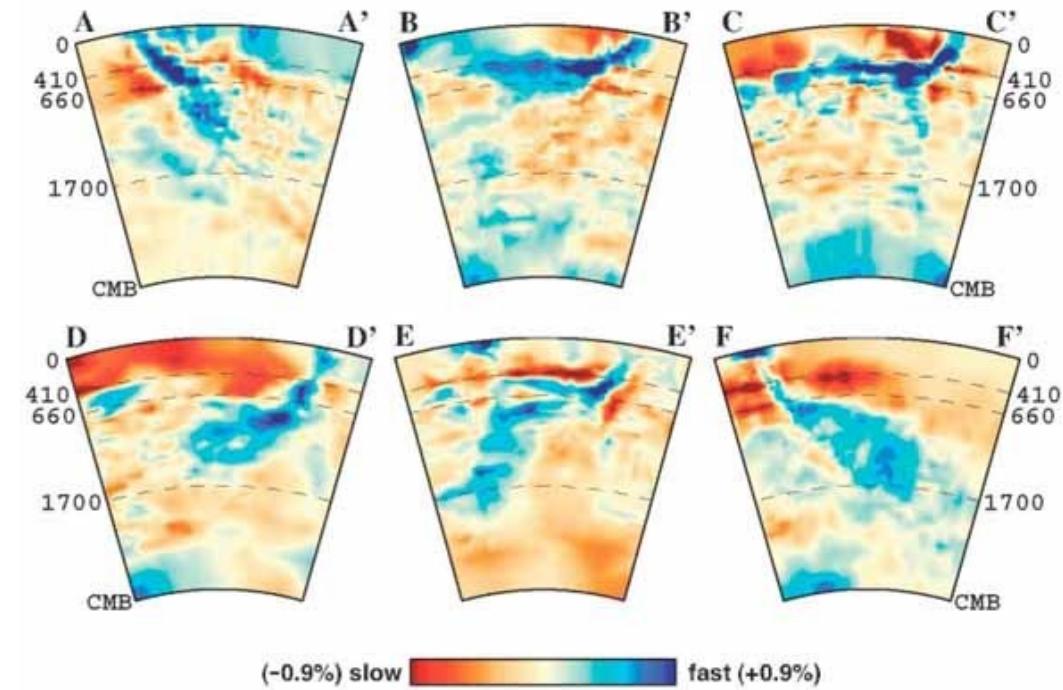
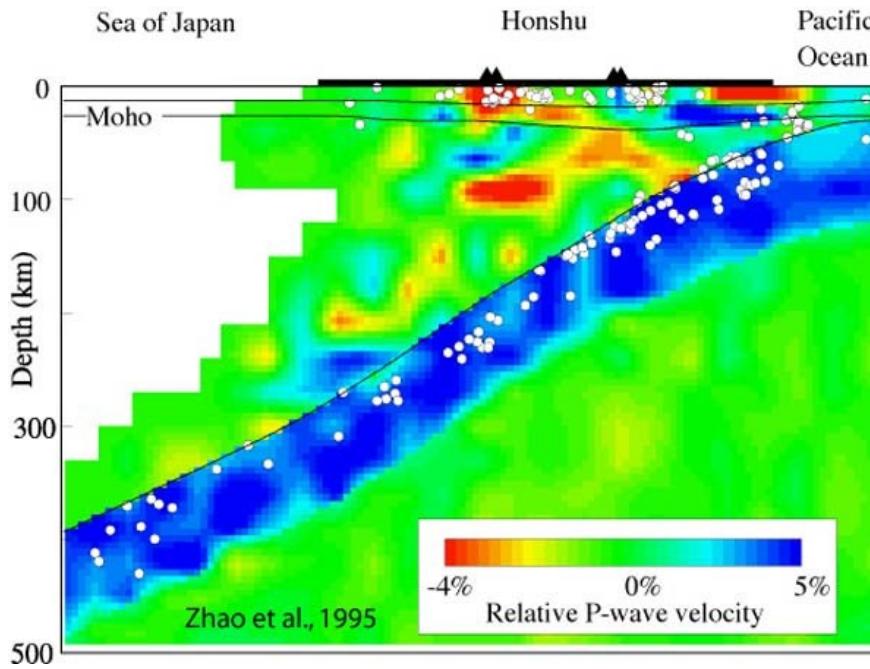
# Evidence of surface motions : geodesy

GPS, DORI, VLBI > displacements inferred at human time scales  
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differential surface motions  
→ **intraplate deformation !**



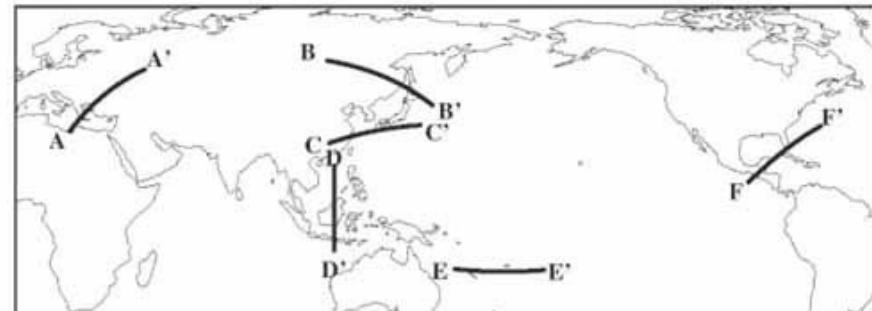
# Argument for deep motions : slabs in seismic tomography



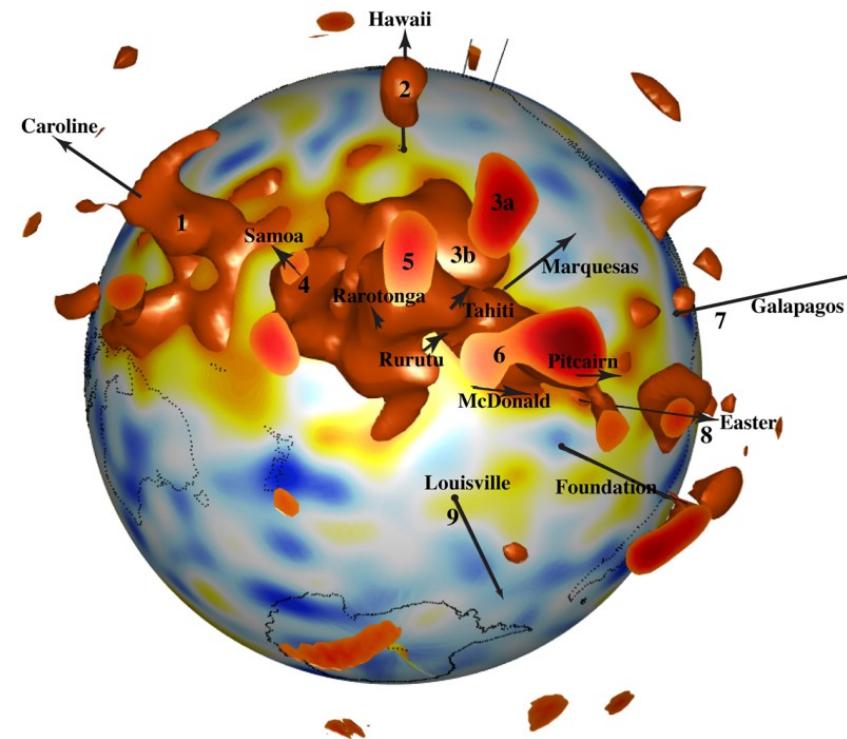
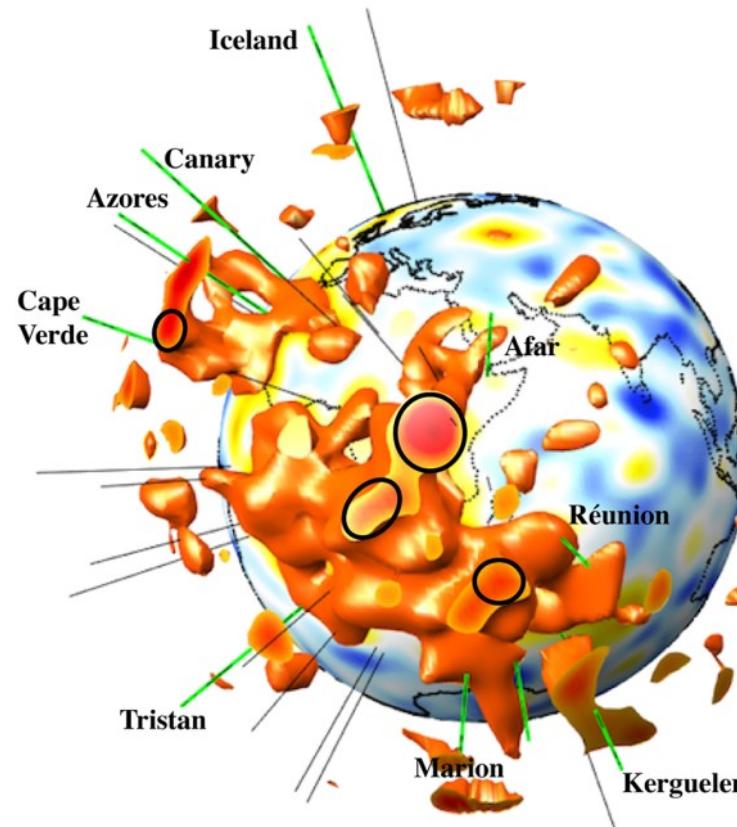
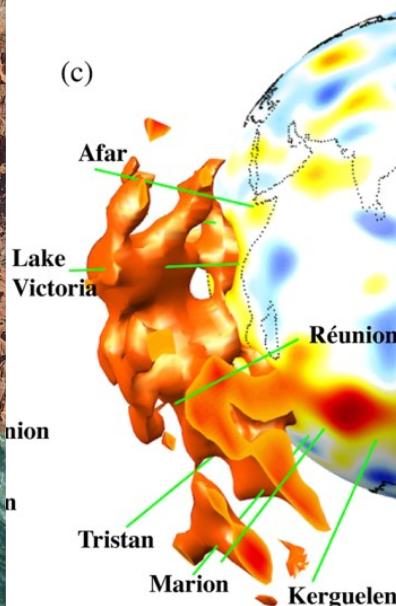
wave velocity anomaly

> density anomaly (motion)  
> temperature anomaly

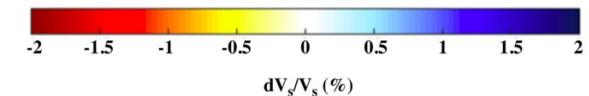
Karason & van der Hilst, 2000



# Argument for deep motions : plumes in seismic tomography



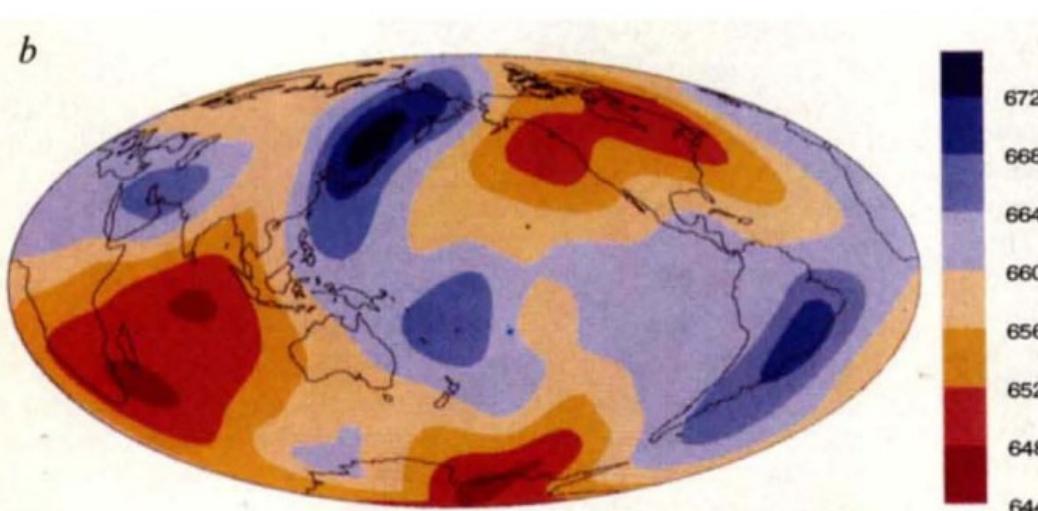
-0.8 to -1 % isosurface



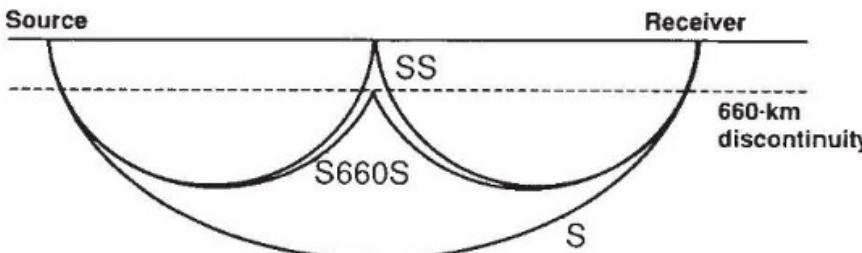
**bundles** of mantle (thermochemical) plumes  
between 1500 and 2800 km depth

# Argument for deep motions : deflection of seismic discontinuities

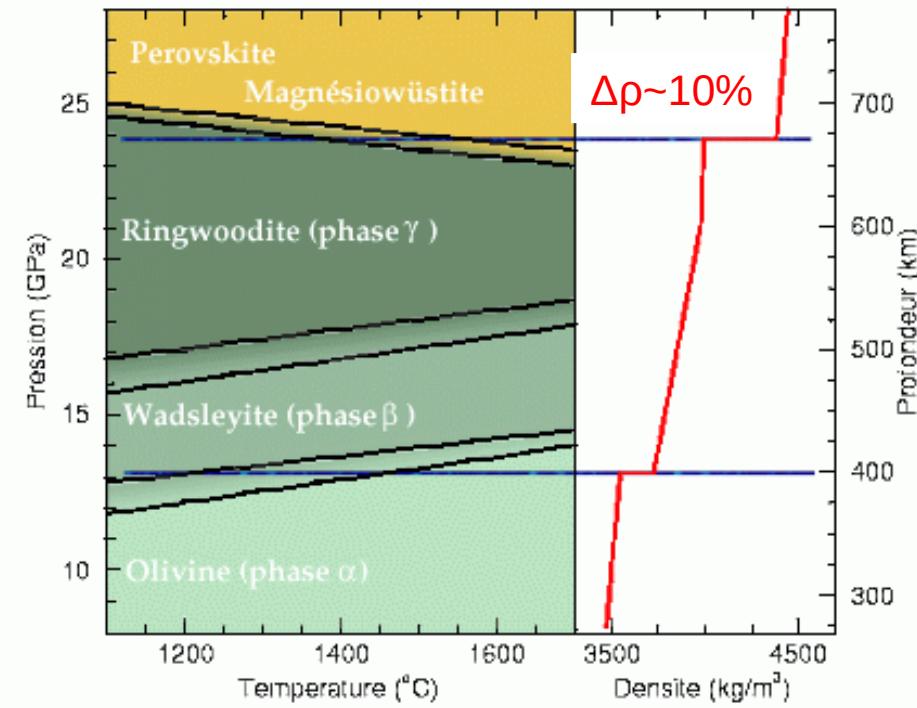
b



Shearer & Masters, Nature, 1992

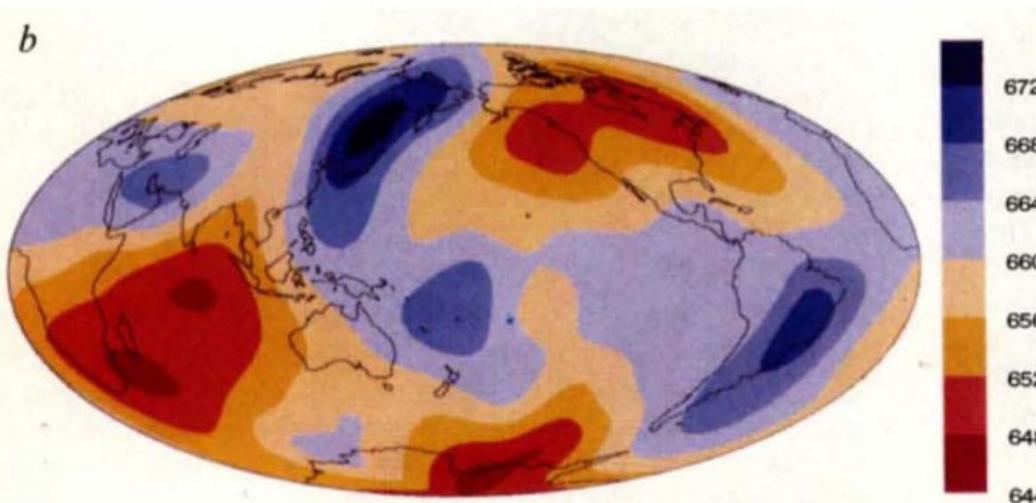


topography of phase transitions  
> temperature anomalies

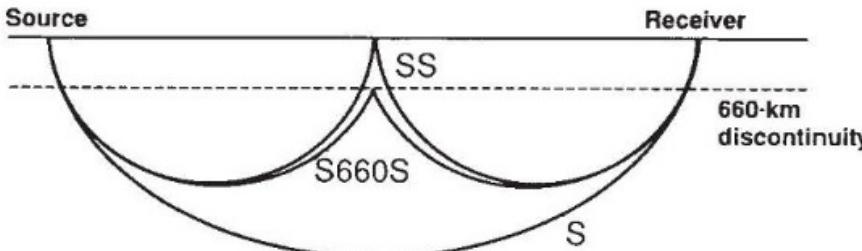


# Argument for deep motions : deflection of seismic discontinuities

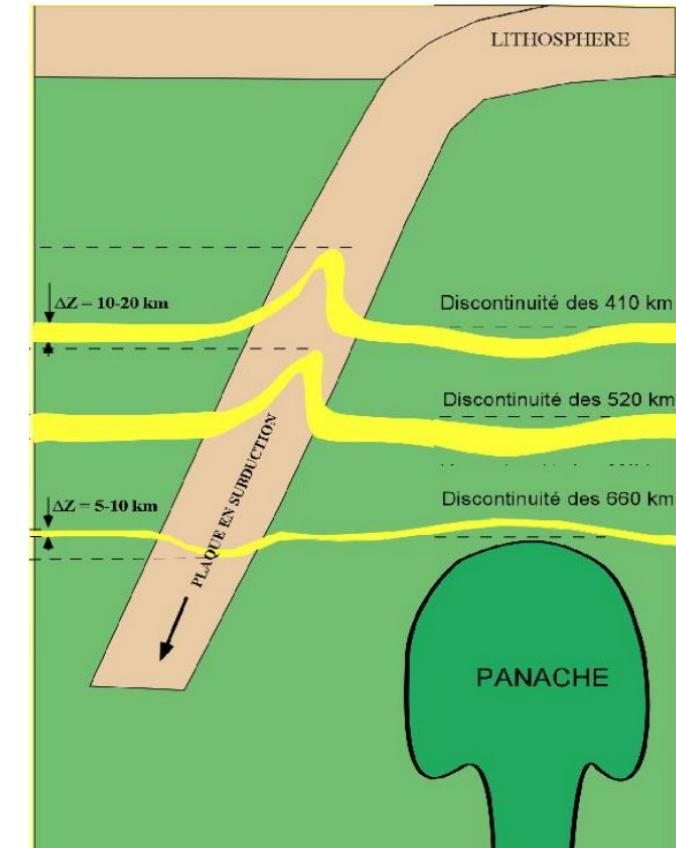
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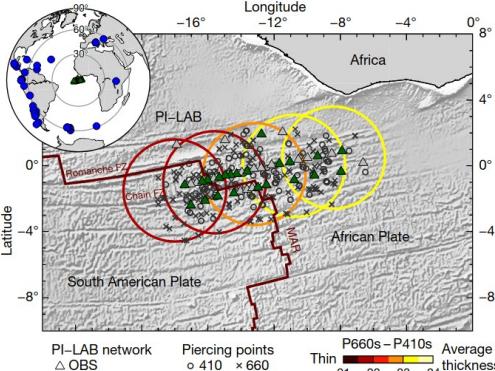


Shearer & Masters, Nature, 1992

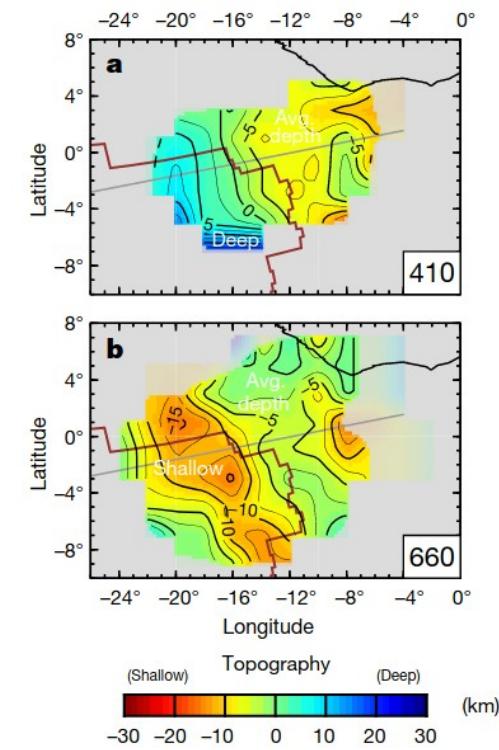
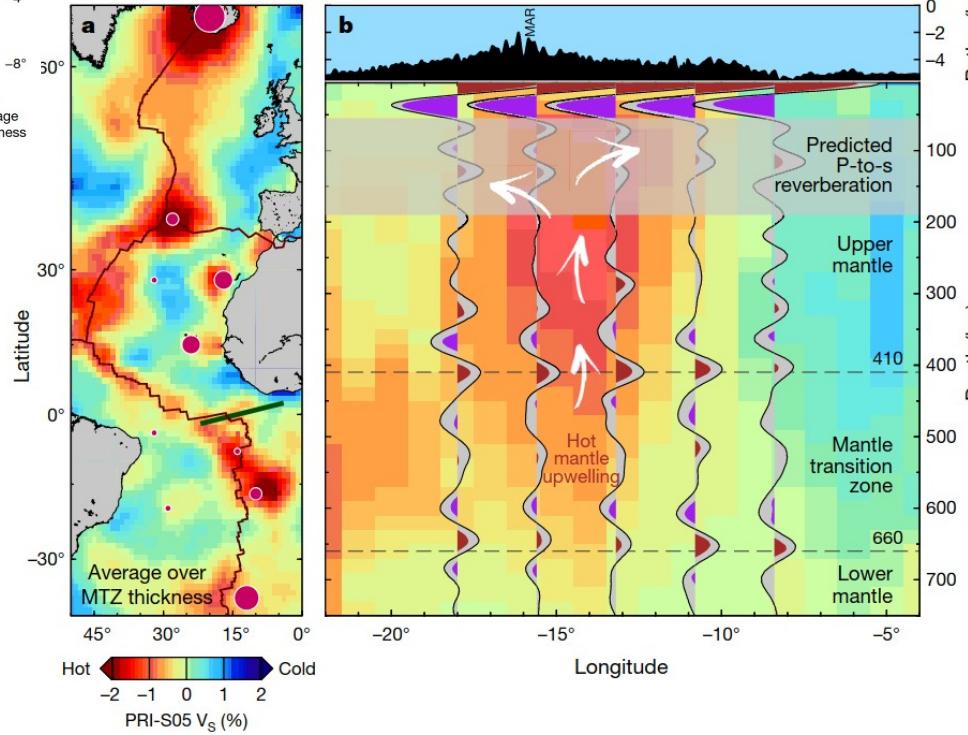


topography of phase transitions  
> temperature anomalies

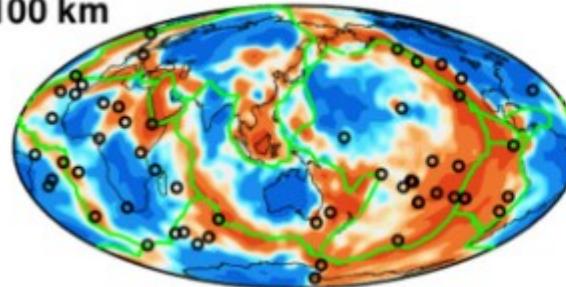




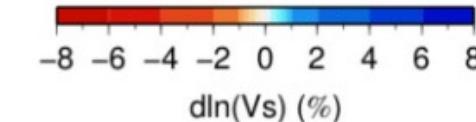
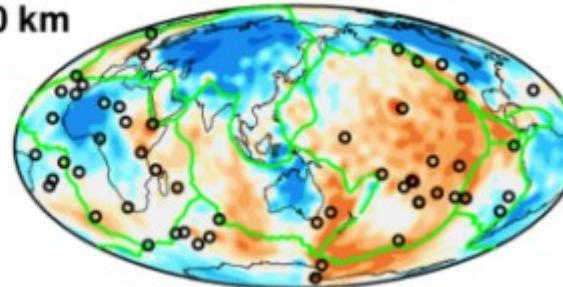
# Deep motions also below mid-ocean ridges ?!



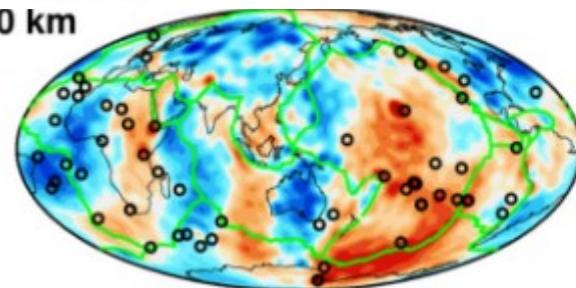
100 km



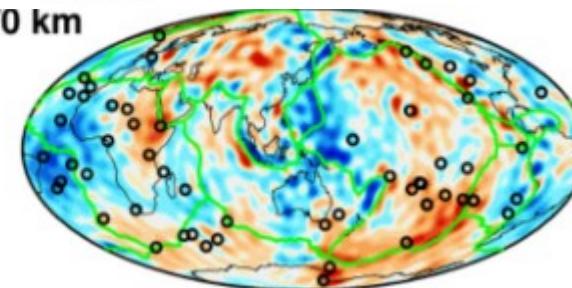
300 km



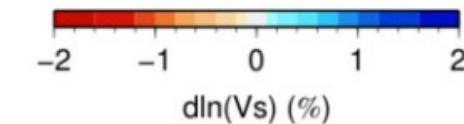
410 km



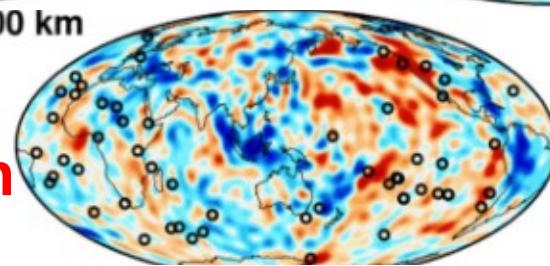
670 km



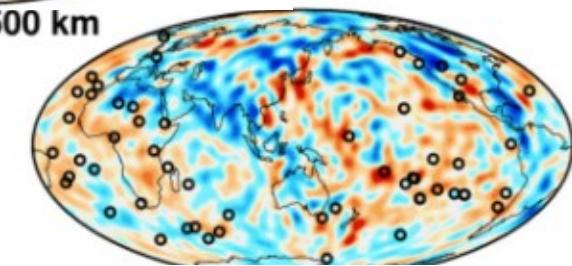
**SEISGLOB2**  
Durand+ GJI 2017



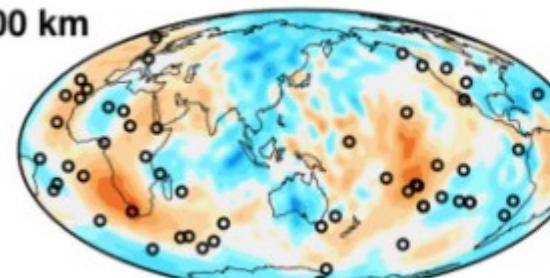
1000 km



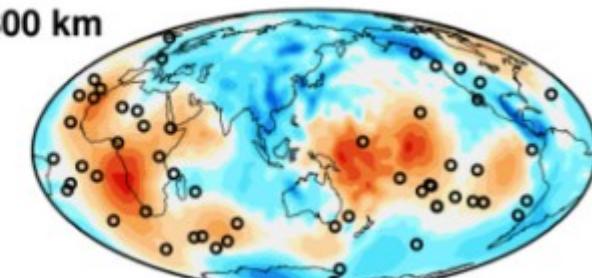
1500 km



2200 km



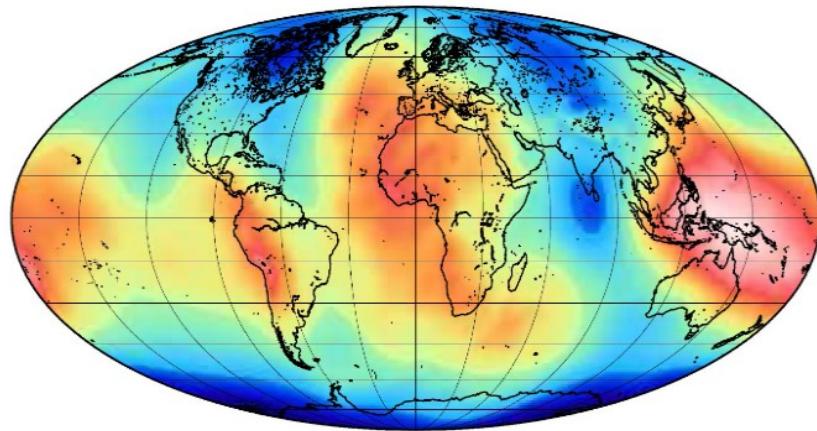
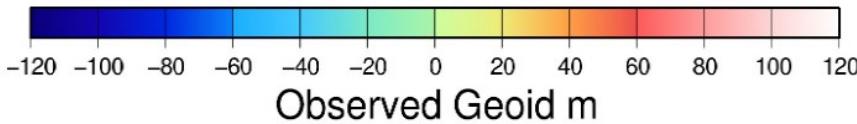
2800 km



**Several scales  
of mantle convection**

what happens around  
1000 km depth ?  
(short wavelengths)

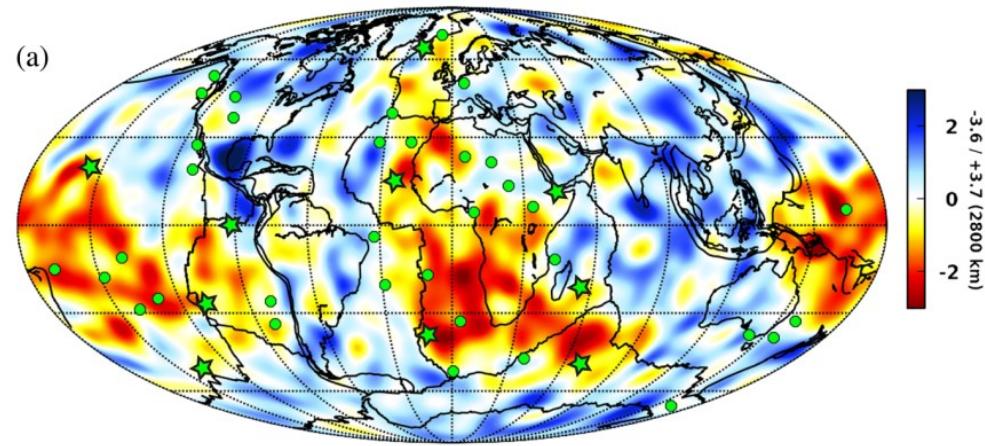
# Argument for deep motions : geoid vs. seismic tomography



F. Chambat

Shear velocity relative anomaly  
at 2800 km depth

(a)



French & Romanowicz GJI 2014

Why does lighter material induces a geoid high ?

Why does denser material induces a geoid low ?

## MOTION

> “flow-induced” deformation  
of density interfaces (surface,  
mantle phase transitions, CMB)

# Argument for deep motions : geoid vs. seismic tomography

## Geoid Anomalies

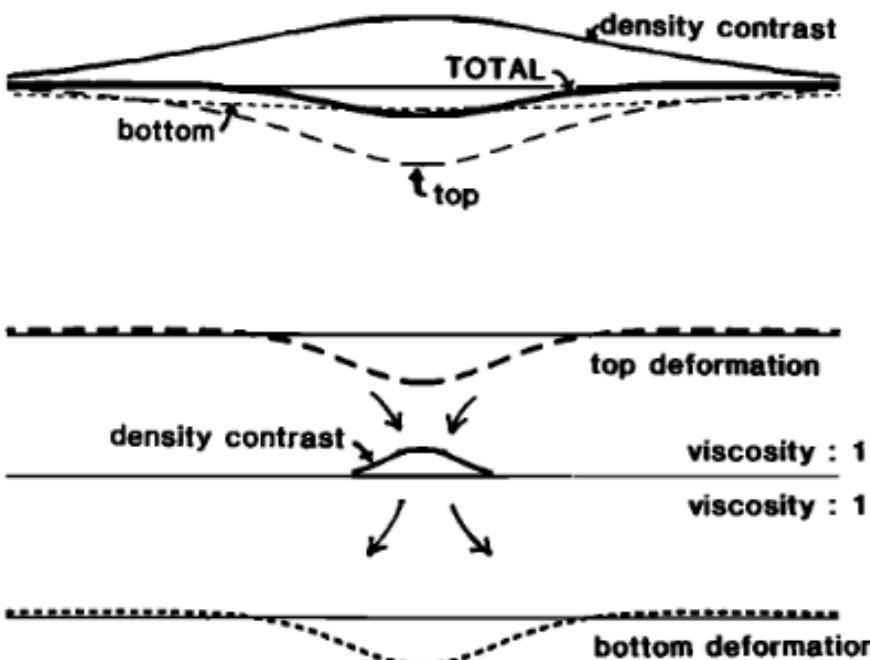


Fig. 1. Illustration of the components of the geoid anomaly from a cosine bell density contrast at the midpoint of a layer of uniform viscosity  $\eta$ . The total anomaly (heavy solid line) is the sum of the contributions from the density contrast itself (light solid line), from dynamic deformation of the upper boundary (long dashes), and from dynamic deformation of the lower boundary (short dashes). The total geoid anomaly is negative for a positive density anomaly.

## Geoid Anomalies

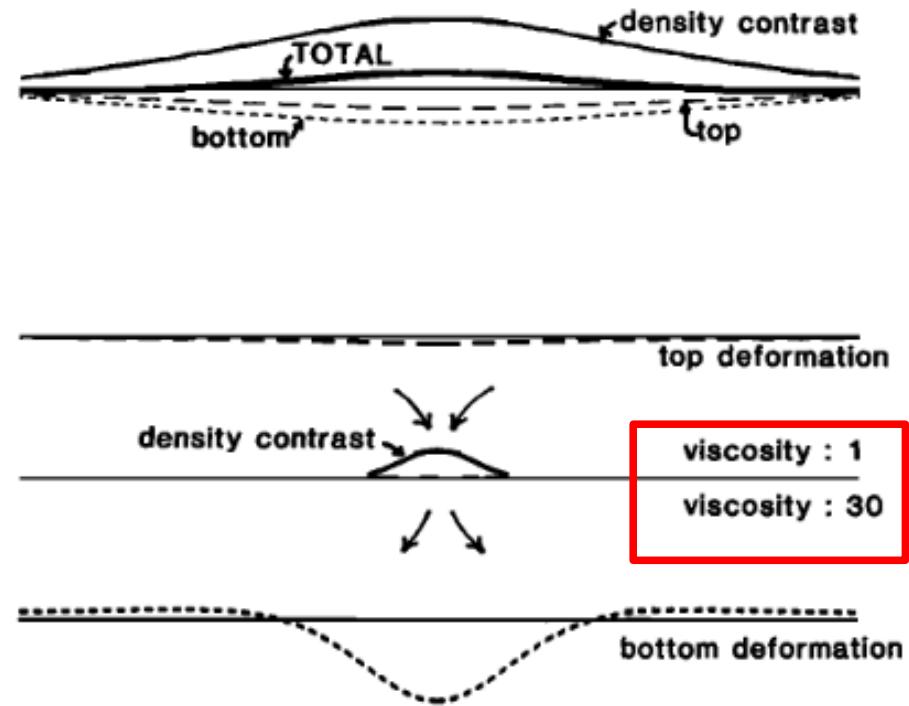
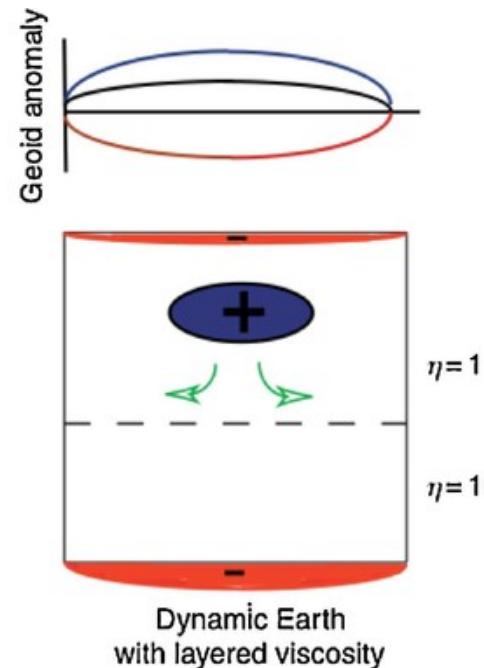
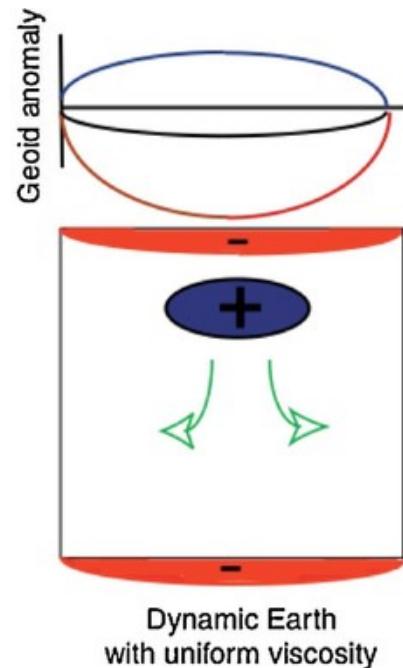
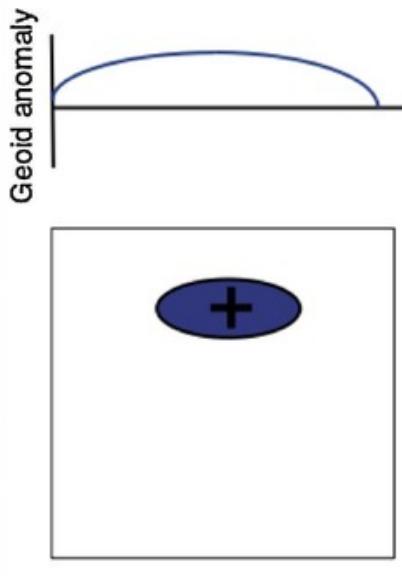


Fig. 2. As in Figure 1, but now the bottom half of the layer has a viscosity  $\eta$  a factor of 30 larger than the upper half. The sign of the total geoid anomaly is now positive.

# Argument for deep motions : geoid vs. seismic tomography



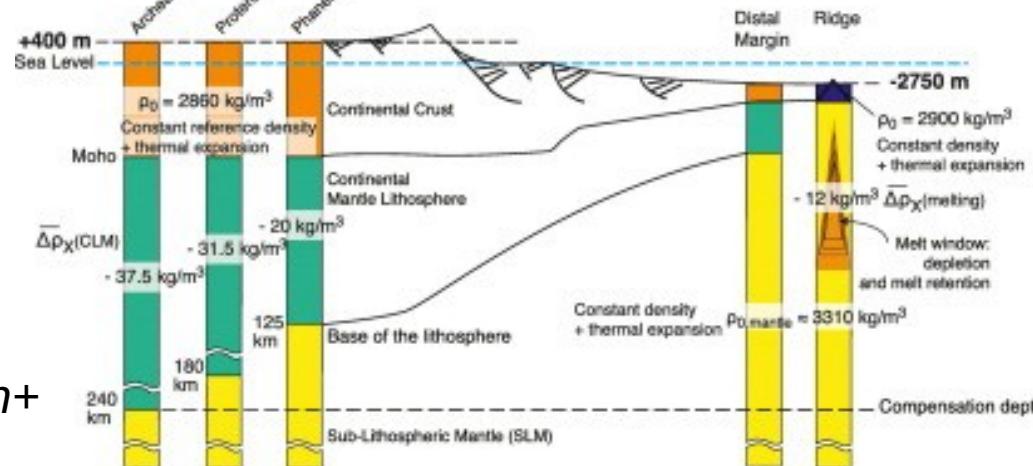
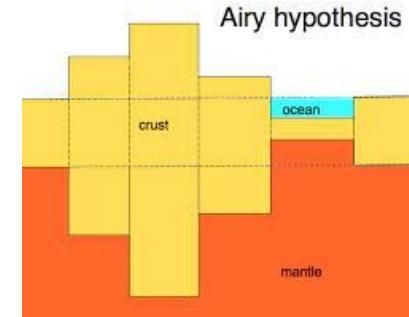
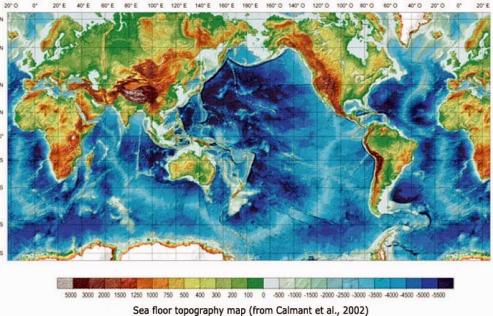
Reconciling geoid  
and seismic  
tomography gives  
constraints on the  
**viscosity**  
**variation with**  
**depth**

(e.g. Ricard+ JGR  
1993)



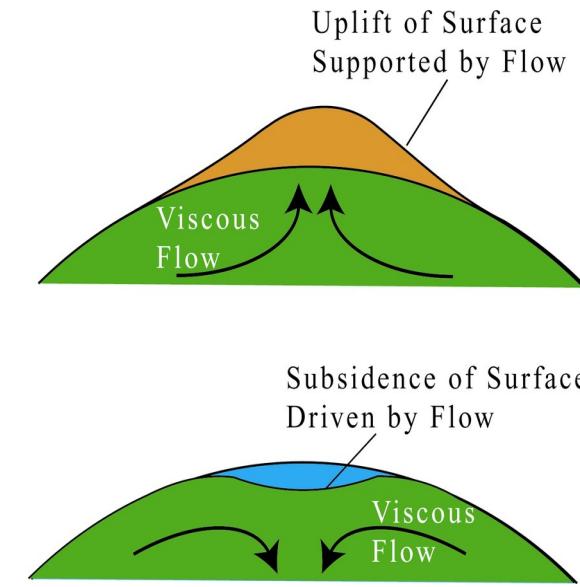
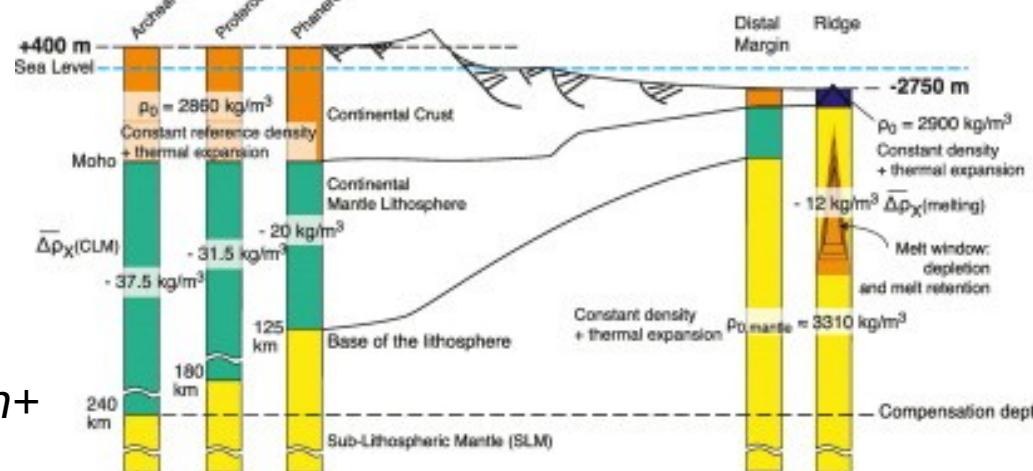
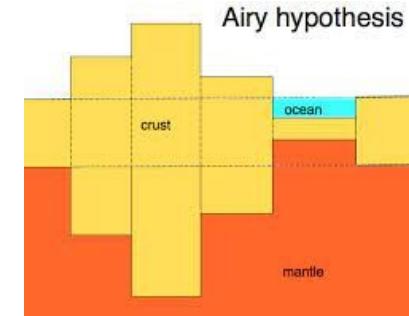
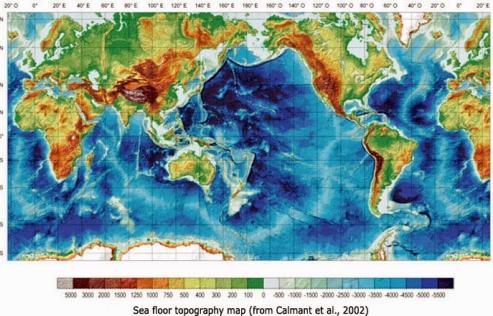
# Argument for deep motions : dynamic (non-isostatic) topography

Topography = statically-equilibrated density distribution + “residual”  
(dynamic component ?)

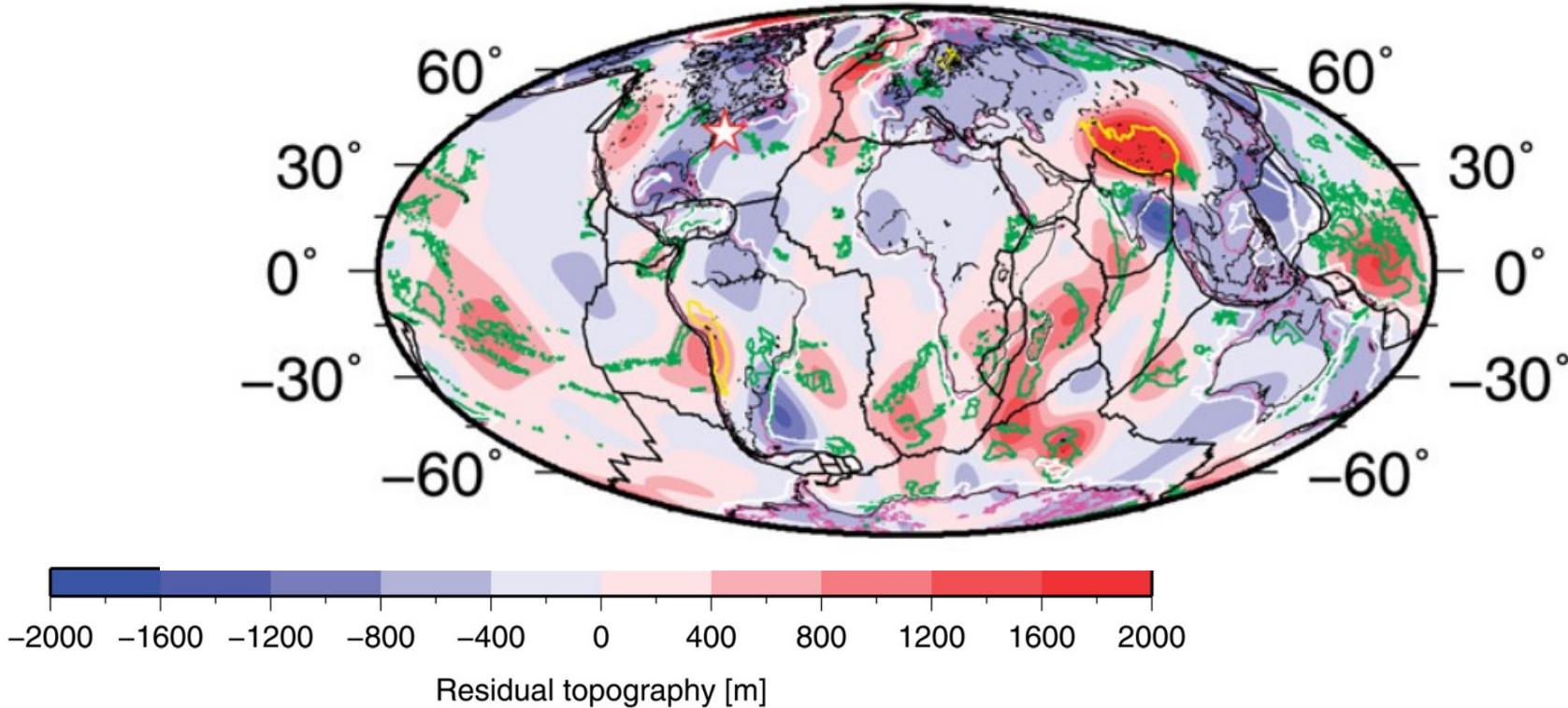


# Argument for deep motions : dynamic (non-isostatic) topography

Topography = statically-equilibrated density distribution + “residual”  
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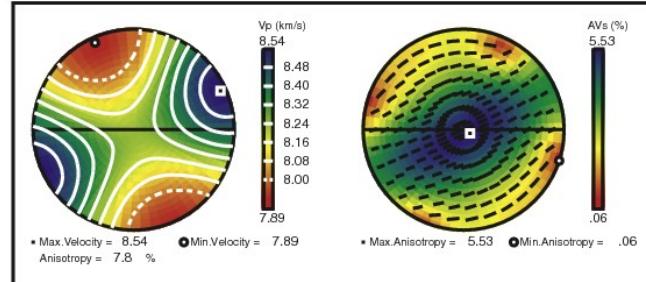
# Argument for deep motions : dynamic (non-isostatic) topography



- green > large igneous provinces
- yellow > continental crust thicker than 50 km

# Argument for deep motions : seismic anisotropy (UM + D")

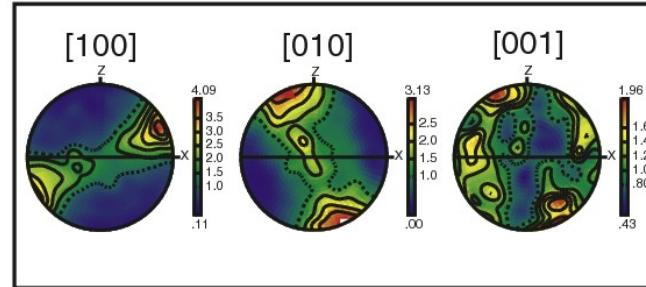
(a) seismic anisotropy magnitude and orientation



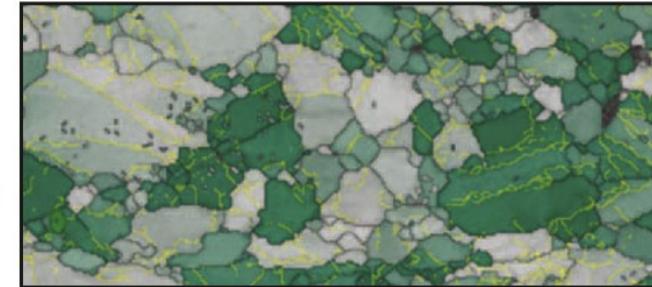
(d) mantle flow



(b) CPO development



(c) rock deformation

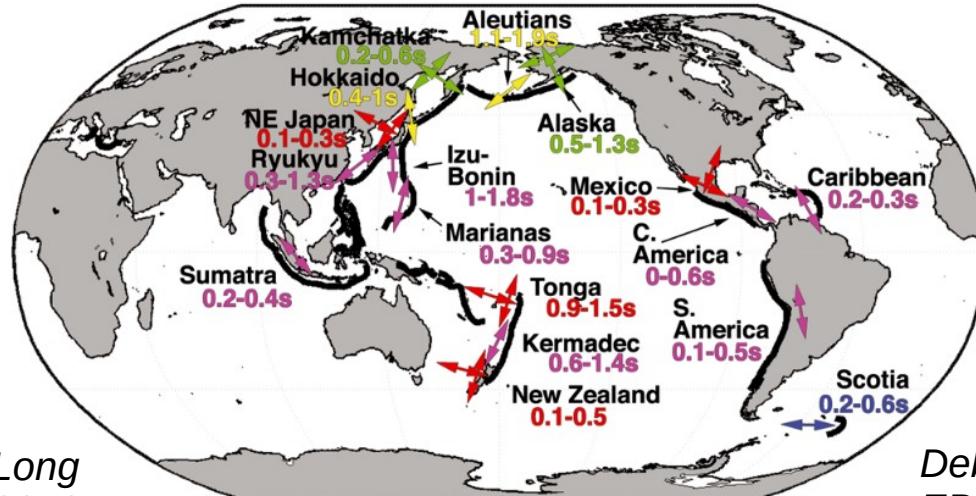


inverse approach (a) → (d)

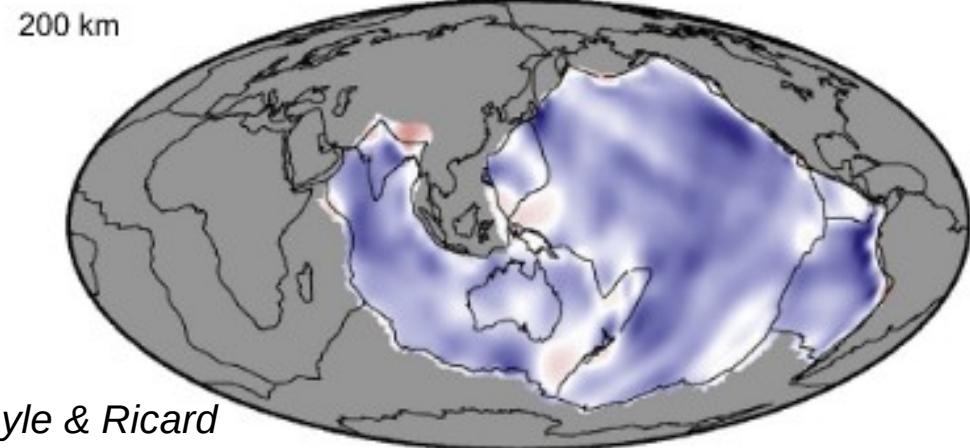
forward approach (d) → (a)

# Argument for deep motions : seismic anisotropy (UM)

## Fast direction in subduction wedges



agreement between fast direction  
and present-day plate motion

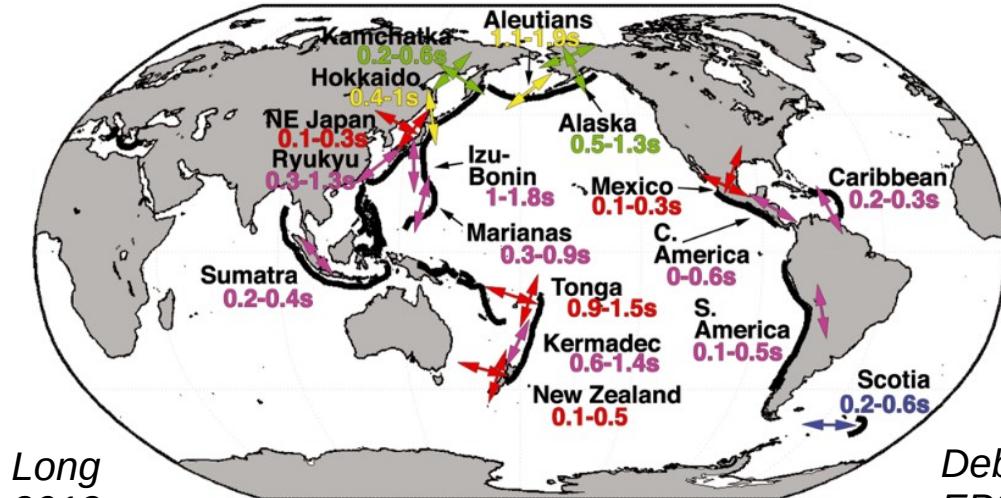


Debayle & Ricard  
EPSL 2013

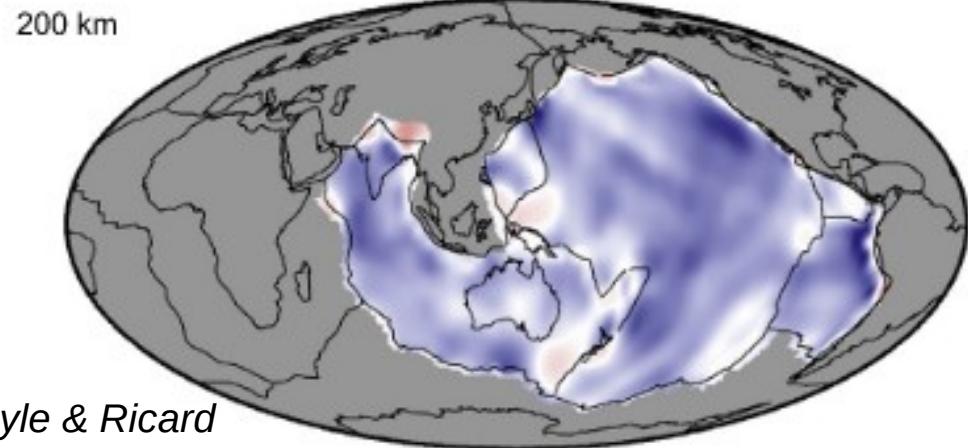


# Argument for deep motions : seismic anisotropy (UM)

## Fast direction in subduction wedges

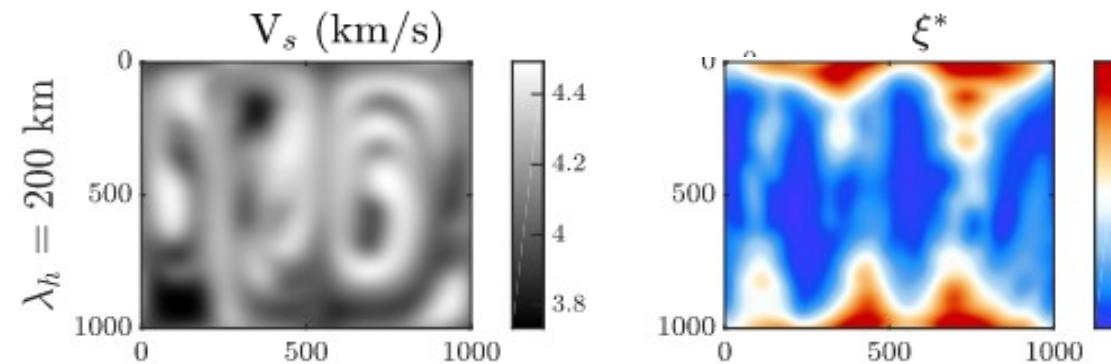


agreement between fast direction and present-day plate motion



Debayle & Ricard  
EPSL 2013

... but **small-scale heterogeneities**  
> “caution should be taken  
when interpreting observed  
anisotropy in terms of LPO  
and mantle deformation”

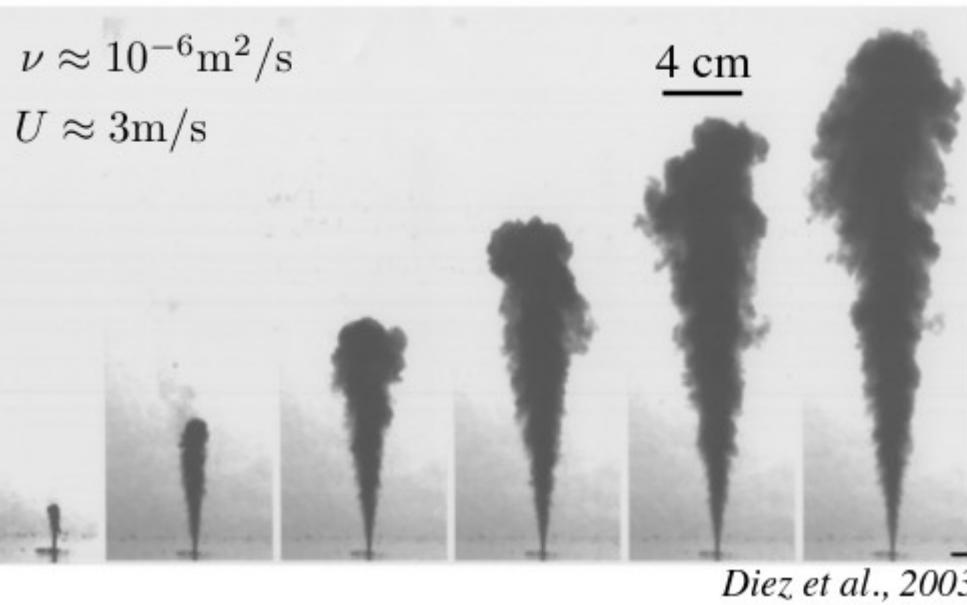


Alder+ GJI 2017

# Dimensionless numbers

- Reynolds number  $Re = \frac{\text{inertia}}{\text{viscous forces}} = \frac{\text{viscous time}}{\text{advective time}} = \frac{UL}{\nu}$

$Re \approx 9000$  Turbulent plume



# Dimensionless numbers for mantle dynamics

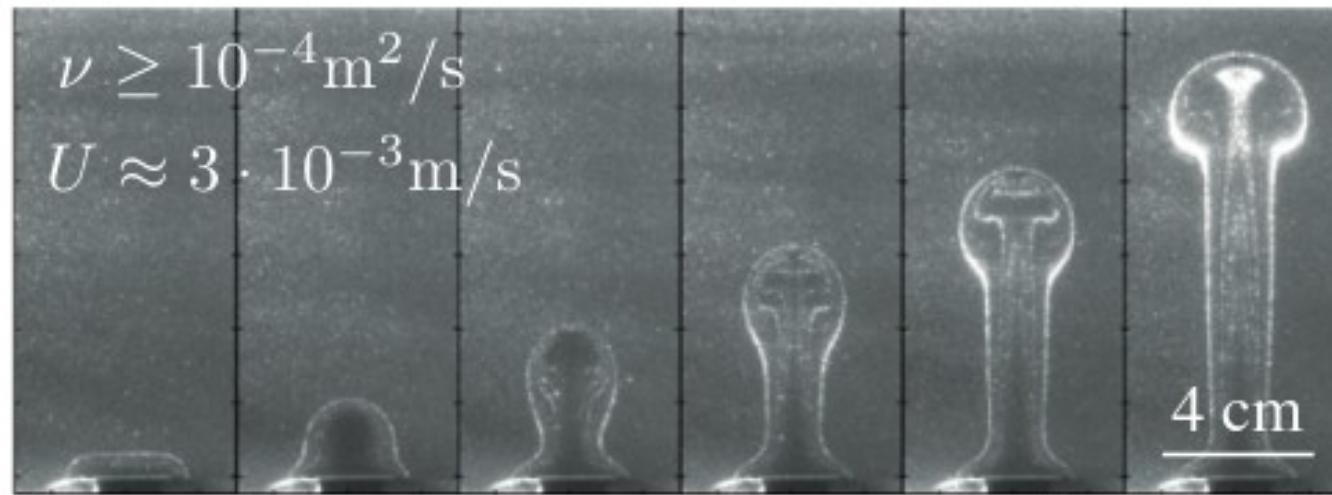
- Reynolds number  $Re = \frac{\text{inertia}}{\text{viscous forces}} = \frac{\text{viscous time}}{\text{advective time}} = \frac{UL}{\nu}$  Re << 1 laminar flow  
kinematic viscosity  $\nu \sim 10^{18} \text{ m}^2/\text{s}$

$$Re \approx 1$$

Laminar plume

$$\nu \geq 10^{-4} \text{ m}^2/\text{s}$$

$$U \approx 3 \cdot 10^{-3} \text{ m/s}$$



Davaille et al., 2011

# Dimensionless numbers for mantle dynamics

- Reynolds number  $Re = \frac{\text{inertia}}{\text{viscous forces}} = \frac{\text{viscous time}}{\text{advective time}} = \frac{UL}{\nu}$  Re << 1  
kinematic viscosity  $\nu \sim 10^{18} \text{ m}^2/\text{s}$  laminar flow

- Rayleigh number  $Ra = \frac{\alpha \Delta T g H^3}{\nu k}$  - buoyancy vs. momentum + thermal diffusivities  
- time scales : thermal diffusion vs. convection

upper mantle viscosity  $\sim 10^{20} \text{ Pa.s}$

lower mantle viscosity  $\sim 10^{22} \text{ Pa.s}$

sub-plate low viscosity layer (?)  $\sim 10^{18} \text{ Pa.s}$

$H = 200 \text{ km}$  (sub-plate SSC ?)

$H = 660 \text{ km}$  (upper mantle)

$H = 2900 \text{ km}$  (whole mantle)

$$\Delta T_{\text{subplate-surface}} \sim 1000 \text{ K}$$

$$\Delta T_{660\text{-surface}} \sim 2000 \text{ K}$$

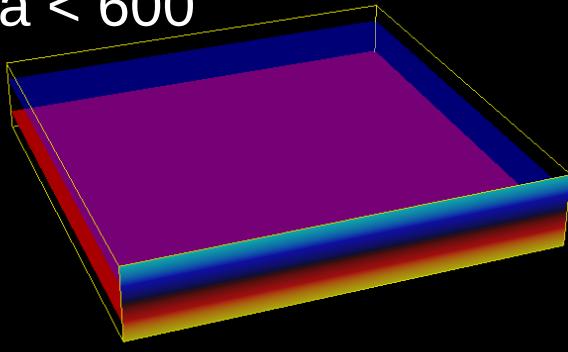
$$\Delta T_{\text{CMB-surface}} \sim 3000 \text{ K}$$

$Ra \sim 10^6 - 10^8$   
convecting mantle

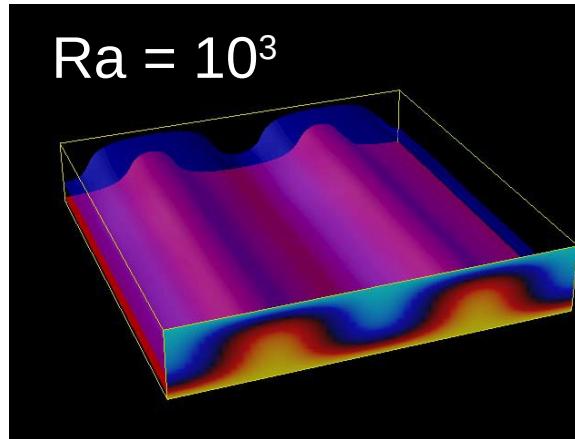


# Increasing the Rayleigh number and changing the pattern of convection

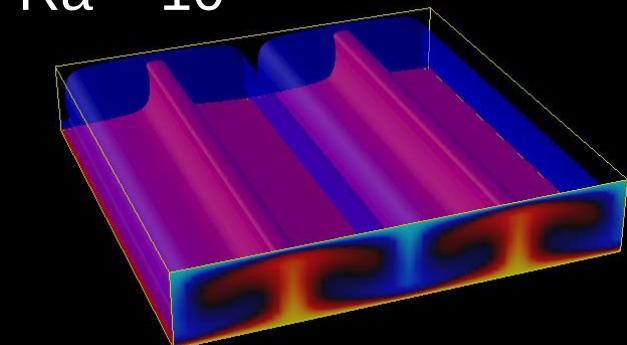
$\text{Ra} < 600$



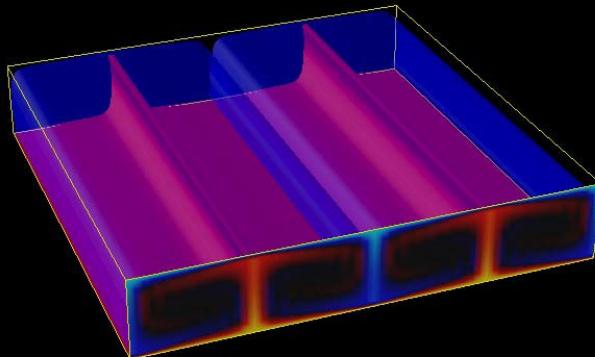
$\text{Ra} = 10^3$



$\text{Ra} = 10^4$

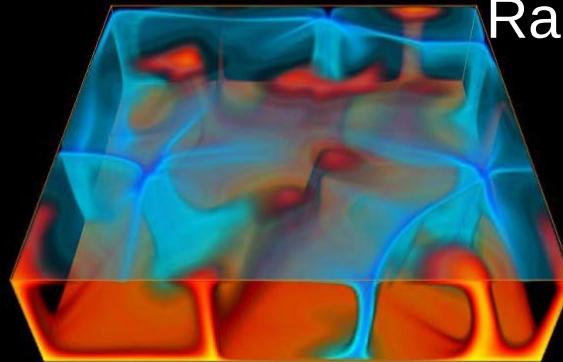


$\text{Ra} = 10^5$

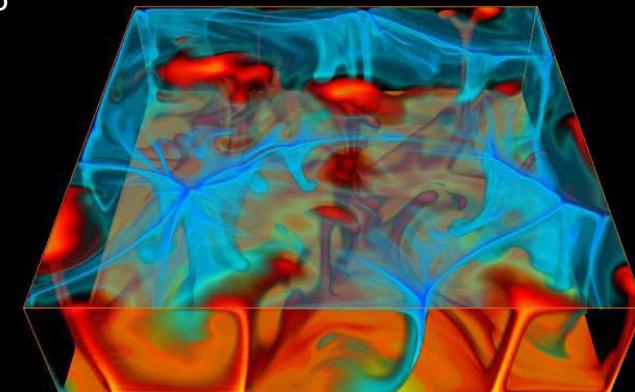


Dubuffet, 2005

$\text{Ra} = 10^6$



$\text{Ra} = 10^7$



# Dimensionless numbers for mantle dynamics

- Reynolds number  $Re = \frac{\text{inertia}}{\text{viscous forces}} = \frac{\text{viscous time}}{\text{advective time}} = \frac{UL}{\nu}$  Re << 1  
kinematic viscosity  $\nu \sim 10^{18} \text{ m}^2/\text{s}$  laminar flow

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$$\Delta T_{\text{CMB-surface}} \sim 3000 \text{ K}$$

$Ra \sim 10^6 - 10^8$   
convecting mantle

- Prandtl number  $Pr = \frac{\nu}{k}$  momentum diffusivity  
to thermal diffusivity

$Pr > 10^{23}$  - “*infinite*”  
thermal anomalies trigger motions



# Dimensionless numbers for mantle dynamics

- Reynolds number  $Re = \frac{\text{inertia}}{\text{viscous forces}} = \frac{\text{viscous time}}{\text{advective time}} = \frac{UL}{\nu}$  Re << 1  
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$$\Delta T_{\text{CMB-surface}} \sim 3000 \text{ K}$$

$Ra \sim 10^6 - 10^8$   
convecting mantle

**large Ekman number**  
viscous/creeping flow  
(no Earth's rotation effect)

- Prandtl number  $Pr = \frac{\nu}{k}$  momentum diffusivity  
to thermal diffusivity

$Pr > 10^{23}$  - "infinite"  
thermal anomalies trigger motions

# Orders of magnitude : 0-D mantle dynamics

- Surface plate motions  $\sim 0.1\text{-}10 \text{ cm/yr}$  - Deep mantle motions  $\sim 1 \text{ cm/yr}$   
**time to travel through the mantle** (plume up, slab down)  $\sim ???$
- Ratio between surface ( $R=6400 \text{ km}$ ) and CMB ( $R=2800 \text{ km}$ )  $\sim ???$   
*surface of a sphere =  $4\pi R^2$* 
  - **Strain rate** in the upper mantle  $\sim ???$  *2 cm/yr plate shearing the upper mantle (Couette)*
- Thermal anomalies  $\sim +300 / -1000 \text{ K}$   $\rightarrow$  **relative density anomalies**  $\sim ???$   
*thermal expansivity  $\alpha \sim 3 \cdot 10^{-5} \text{ K}$*
- Length scale of **thermal diffusion** over 100 Myr  $\sim ???$  1 yr  $\sim 3 \cdot 10^7 \text{ s}$
- Length scale of **chemical diffusion** over 100 Myr  $\sim ???$
- Diffusive time to transport heat through a 10 or 100-km lithosphere  $\sim ???$   
 $d = (\kappa t)^{1/2}$  - *thermal diffusivity  $\sim 10^{-6} \text{ m}^2/\text{s}$  - chemical diffusivity  $10^{-9}\text{-}10^{-13} \text{ m}^2/\text{s}$*
- **Heat flux** advected by slabs :  $Q = \delta x L \rho C_p w \delta T \sim ???$   
 $L_{\text{trench}} \sim 50\,000 \text{ km}$  -  $\delta T \sim 600 \text{ K}$  -  $w \sim 10 \text{ cm/yr}$  – slab thickness  $\delta x \sim 100 \text{ km}$   
density  $\rho \sim 3300 \text{ kg/m}^3$  – specific heat  $C_p \sim 1000 \text{ J/K/kg}$



# Orders of magnitude : 0-D mantle dynamics

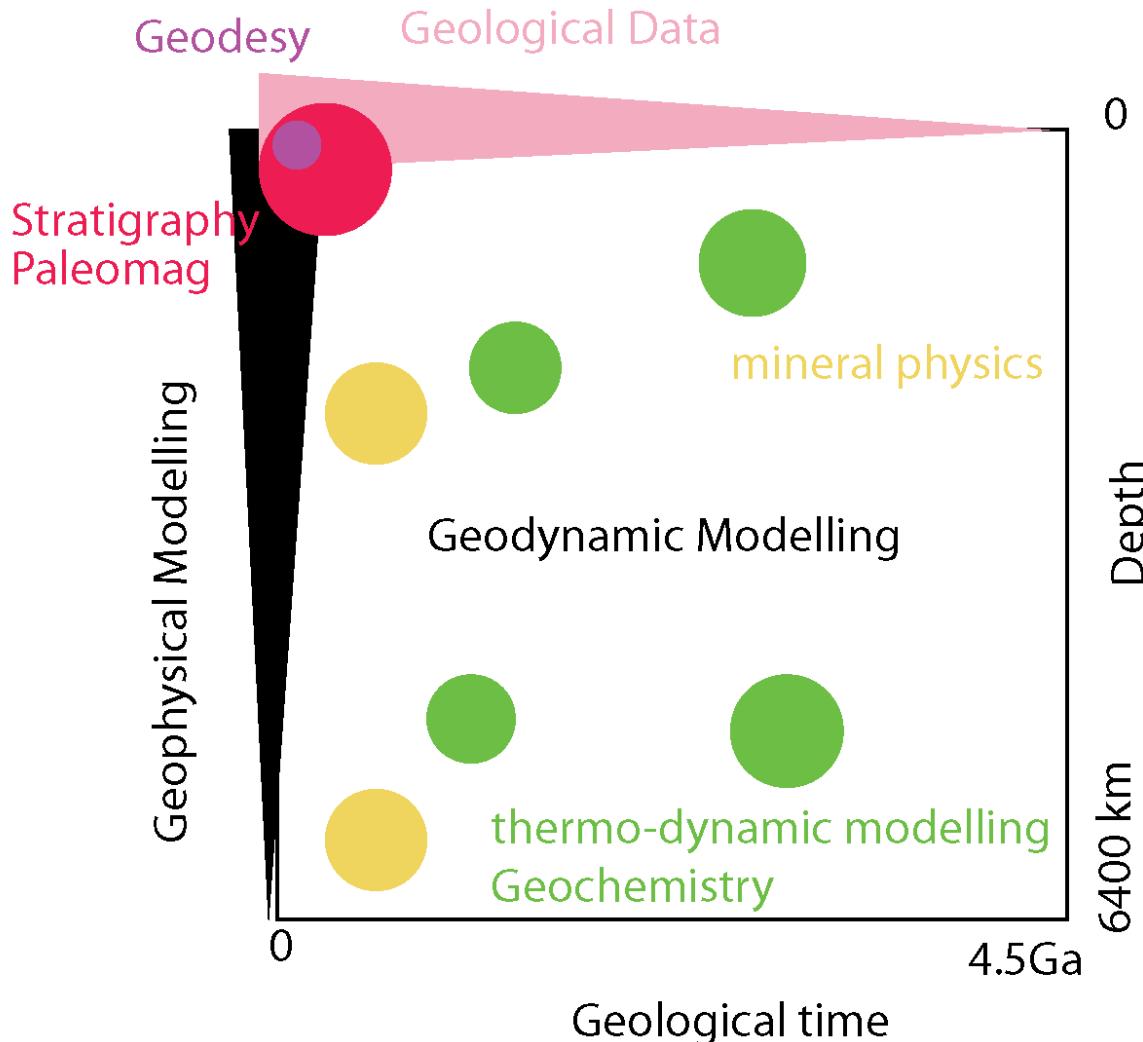
- Surface plate motions  $\sim 0.1\text{-}10 \text{ cm/yr}$  - Deep mantle motions  $\sim 1 \text{ cm/yr}$   
**time to travel through the mantle** (plume up, slab down)  $\sim 300 \text{ Myr}$
- Ratio between surface ( $R=6400 \text{ km}$ ) and CMB ( $R=2800 \text{ km}$ )  $\sim 5$   
*surface of a sphere =  $4\pi R^2$* 
  - **Strain rate in the upper mantle**  $\sim 10^{-15} \text{ s}^{-1}$  *2 cm/yr plate shearing the upper mantle (Couette)*
- Thermal anomalies  $\sim +300 / -1000 \text{ K}$   $\rightarrow$  **relative density anomalies**  $\sim 1\text{-}3 \%$   
*thermal expansivity  $\alpha \sim 3 \cdot 10^{-5} \text{ K}$*
- Length scale of **thermal diffusion** over 100 Myr  $\sim 60 \text{ km}$  1 yr  $\sim 3.10^7 \text{ s}$
- Length scale of **chemical diffusion** over 100 Myr  $\sim 20 \text{ m} - 2 \text{ km}$
- Diffusive time to transport heat through a 10 or 100-km lithosphere  $\sim 3 / 300 \text{ Myr}$   
 $d = (\kappa t)^{1/2}$  - *thermal diffusivity  $\sim 10^{-6} \text{ m}^2/\text{s}$  - chemical diffusivity  $10^{-9}\text{-}10^{-13} \text{ m}^2/\text{s}$*
- **Heat flux advected by slabs** :  $Q = \delta x L \rho C_p w \delta T \sim 30 \text{ TW}$  (plumes  $\sim 2 \text{ TW}$ )  
 $L_{\text{trench}} \sim 50\,000 \text{ km}$  -  $\delta T \sim 600 \text{ K}$  -  $w \sim 10 \text{ cm/yr}$  – slab thickness  $\delta x \sim 100 \text{ km}$   
density  $\rho \sim 3300 \text{ kg/m}^3$  – specific heat  $C_p \sim 1000 \text{ J/K/kg}$



# Mantle geodynamics

- 1. Evidence for surface (plate) and deep (mantle) motions  
+ *orders of magnitude***
- 2. Dynamic models to understand the mantle (past & present)**
- 3. Mantle and plate dynamics : modelling diversity and recipes**
- 4. Progress and perspectives**

# Discrete data in time and space



- Measurement  
(displacement, geol. history)  
≠ physical state  
(stress, temperature,  
strength, fluid pressure)
- A pure “data-driven”  
approach not based on  
physics has little chance  
to help us understand  
past or deep earth

after Taras Gerya  
& Laëtitia le Pourhiet



# **Models** (simplified representation of reality) **of solid Earth dynamics**

- **Conceptual models** – “cartoons” (intuition + data)



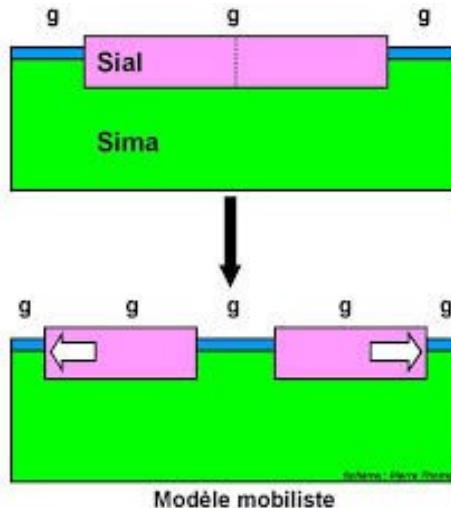
# **Models** (simplified representation of reality) of solid Earth dynamics

## - Conceptual models – “cartoons” (intuition + data)

**continental drift**  
(Wegener – 1912)



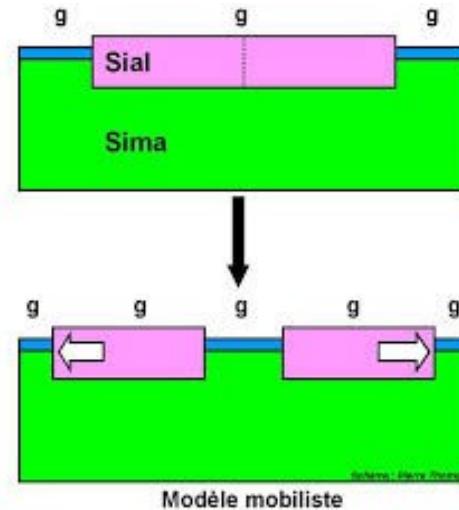
*physical explanation :*  
tidal force



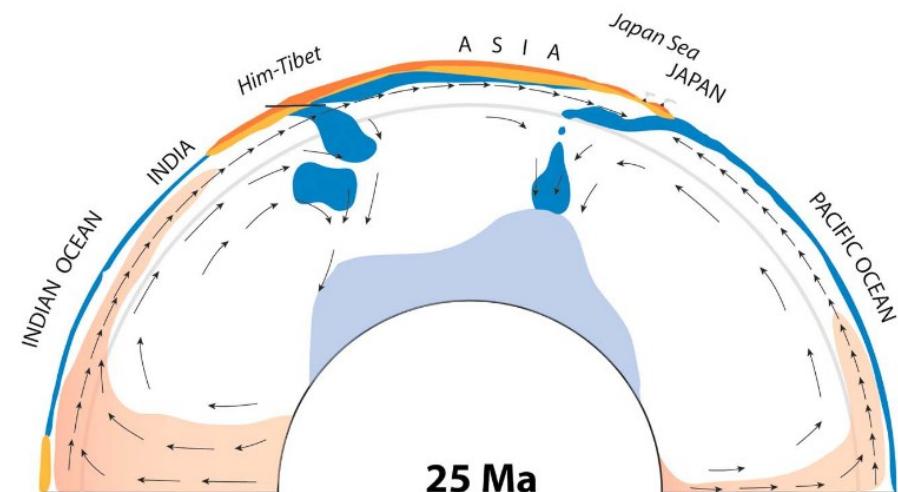
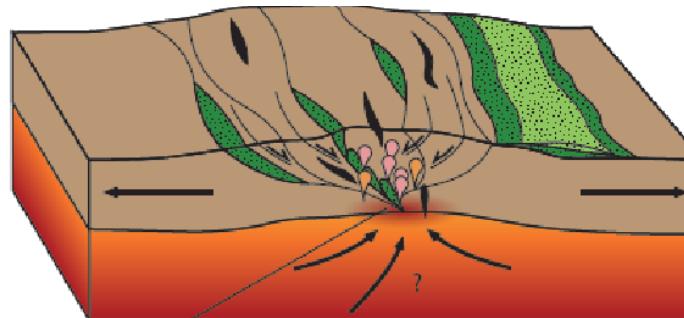
# Models (simplified representation of reality) of solid Earth dynamics

## - Conceptual models – “cartoons” (intuition + data)

continental drift  
(Wegener – 1912)



physical explanation :  
tidal force



Scenario of past mantle flow from geology  
+ seismic tomography/anisotropy

Jolivet+ 2018

Craton evolution from isotope geochemistry  
Albert+ 2016

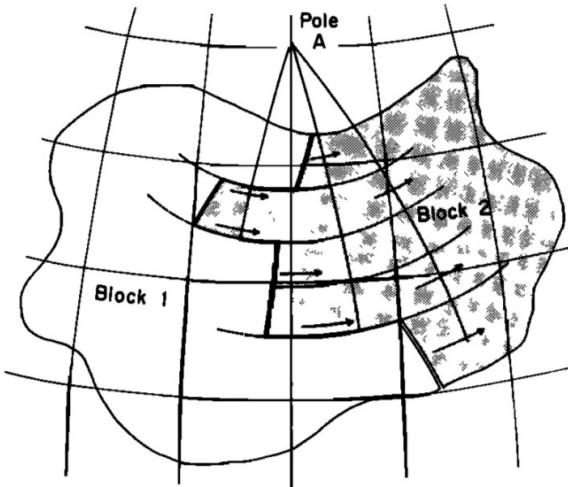
# Models (simplified representation of reality) of solid Earth dynamics

- Conceptual models – “cartoons” (intuition + data)

- Quantitative models

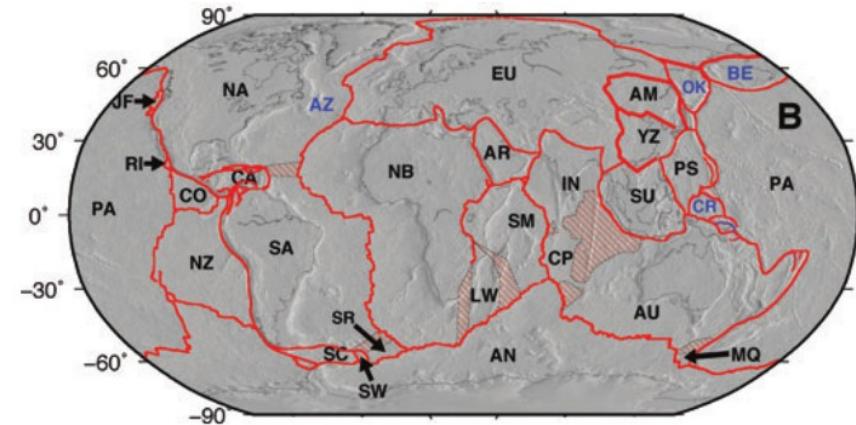
- > instantaneous models

- \* plate tectonics models



Morgan, 1968

- rigid blocks moving at the surface of a sphere
- eulerian formalism
- minimizing surface variations
- oceanic expansion rates since 3 Ma
- + focal mechanisms (+GPS)



25 plates' model MORVEL  
(DeMets+ 2010)

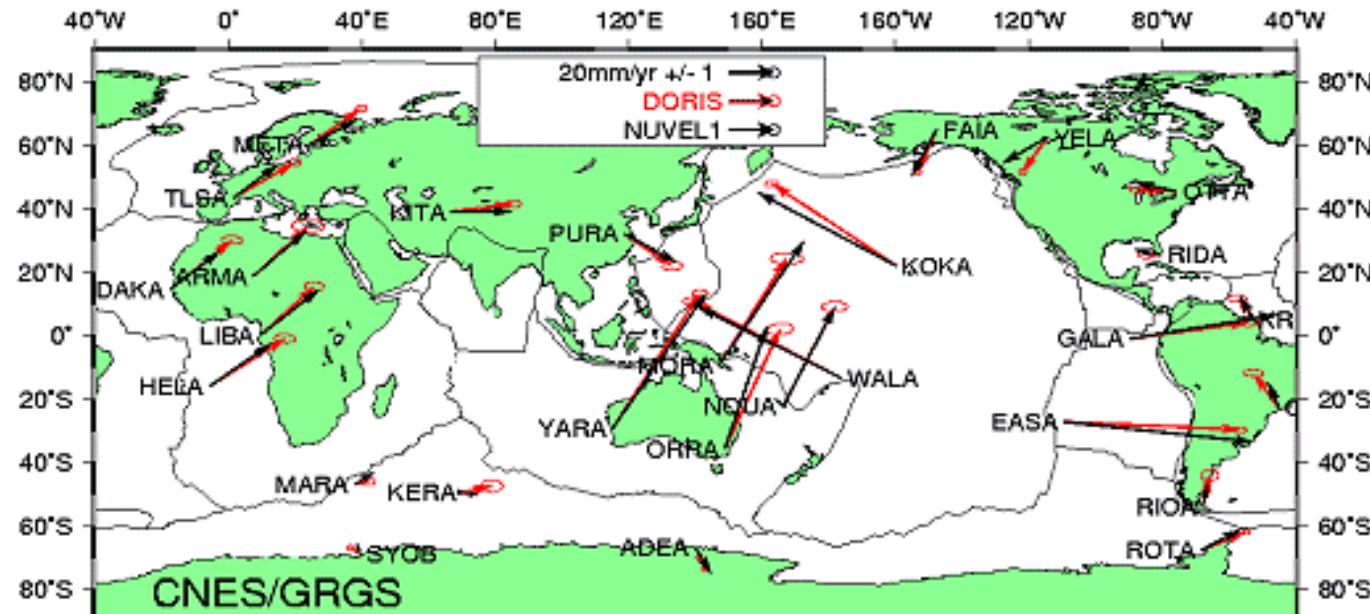
# Models (simplified representation of reality) of solid Earth dynamics

- Conceptual models – “cartoons” (intuition + data)

- Quantitative models

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# **Models** (simplified representation of reality) of solid Earth dynamics

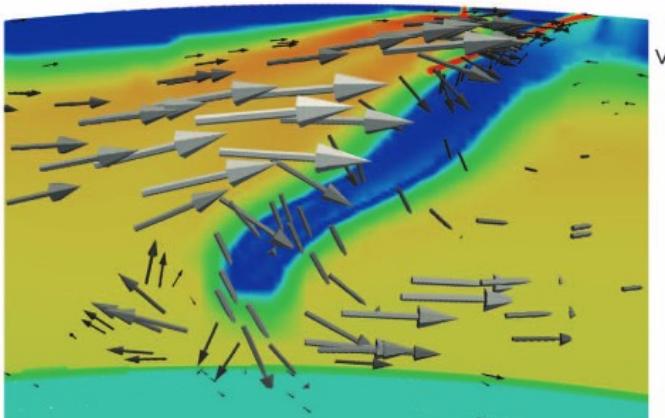
- Conceptual models – “cartoons” (intuition + data)

- Quantitative models

- > instantaneous models

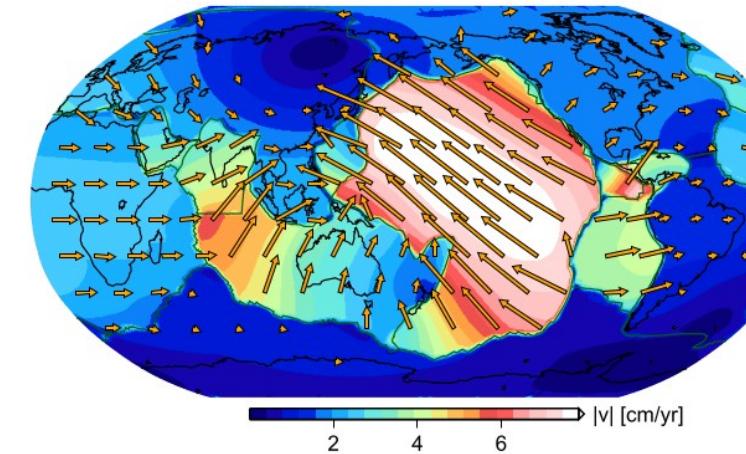
- \* plate tectonics models

- \* instantaneous mantle flow models



Stadler+ Science 2010

**instantaneous  
Stokes solution**  
from present-day  
density anomalies  
(seismology)  
+ viscosity model  
+ plate boundaries...



Becker G<sup>3</sup> 2017



# Models (simplified representation of reality) of solid Earth dynamics

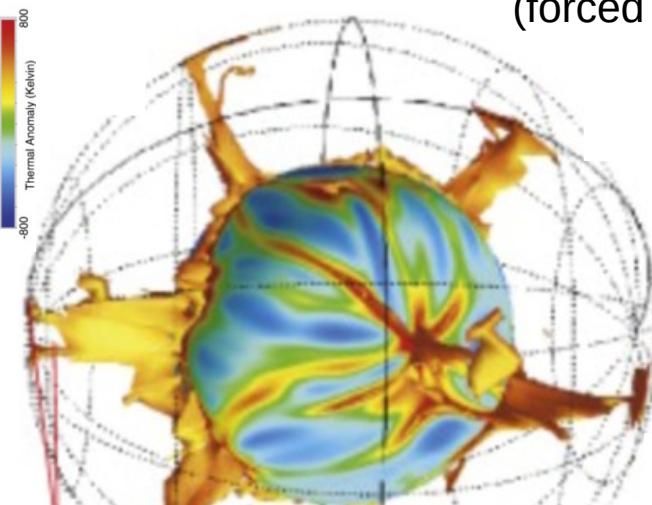
- Conceptual models – “cartoons” (intuition + data)

- Quantitative models

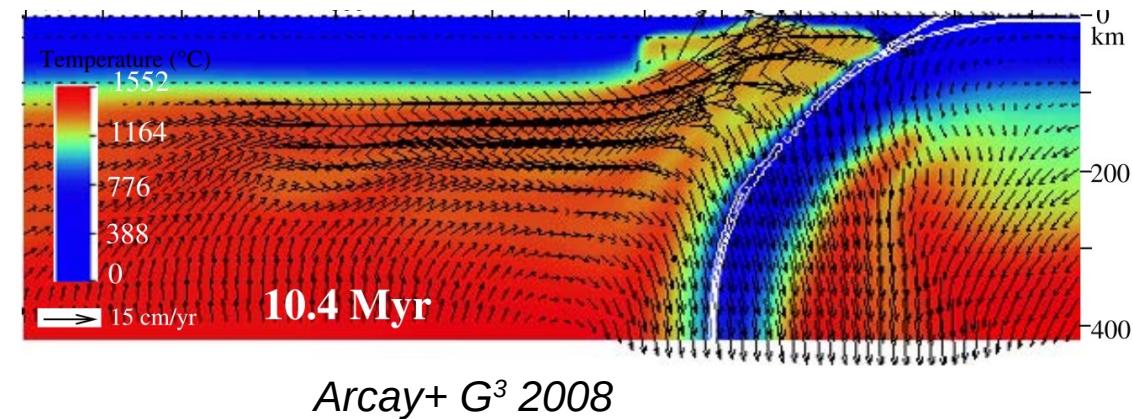
  - > instantaneous models

  - > **time-dependent models**

= evolution in space and time starting from an initial state outside equilibrium  
(forced flow, density anomalies, basal heat...)



Davies &  
Davies  
EPSL  
2009

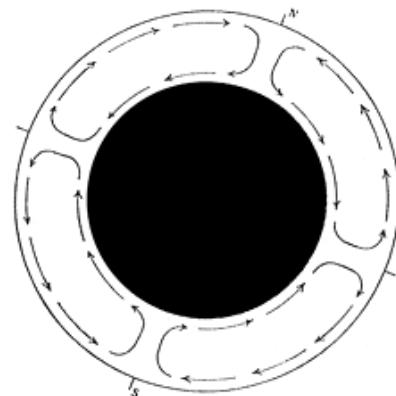


# Mantle geodynamics

- 1. Evidence for surface (plate) and deep (mantle) motions**  
*+ orders of magnitude*
- 2. Dynamic models to understand the mantle** (past & present)
- 3. Mantle and plate dynamics : modelling diversity and recipes**
- 4. Progress and perspectives**

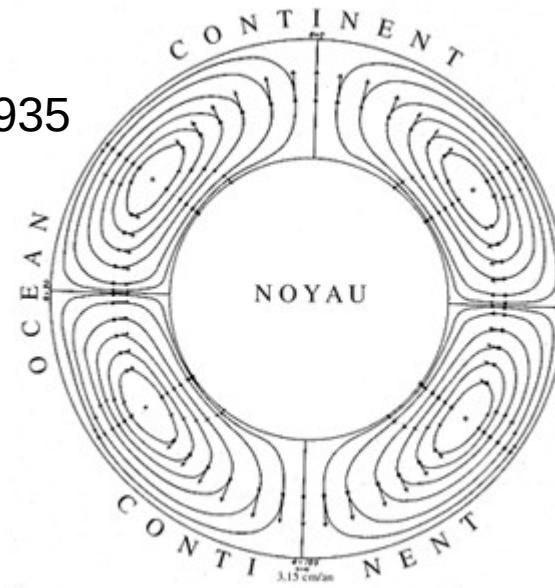
# Thermal convection to explain mantle and surface dynamics

Models of mantle convection have been around for a long time... before plate tectonics theory !

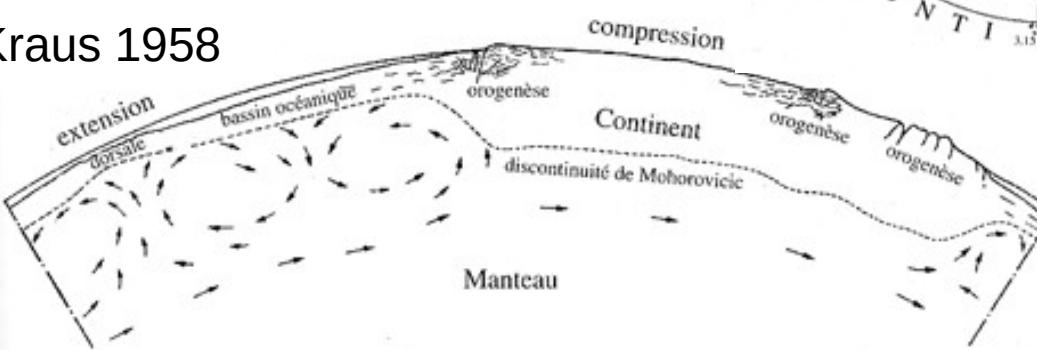


Holmes 1931

Pekeris 1935

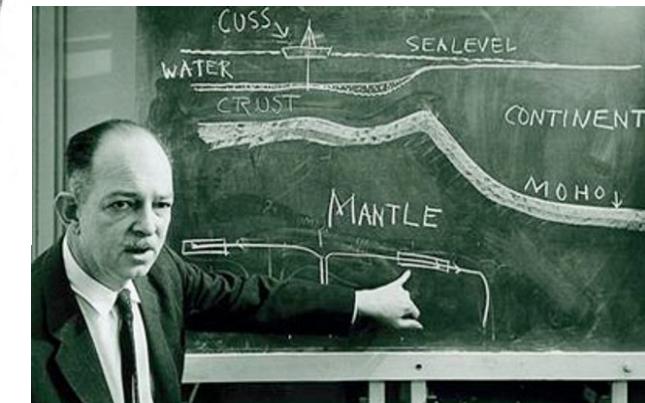


Kraus 1958



+ Vening Meinesz  
+ Griggs + Urey...

<https://planet-terre.ens-lyon.fr/res/source/histoire-convection.xml>



Hess, 1962

# Temperature-dependent mantle viscosity



$$\text{mantle viscosity } \eta \propto \exp\left(\frac{E}{RT}\right)$$

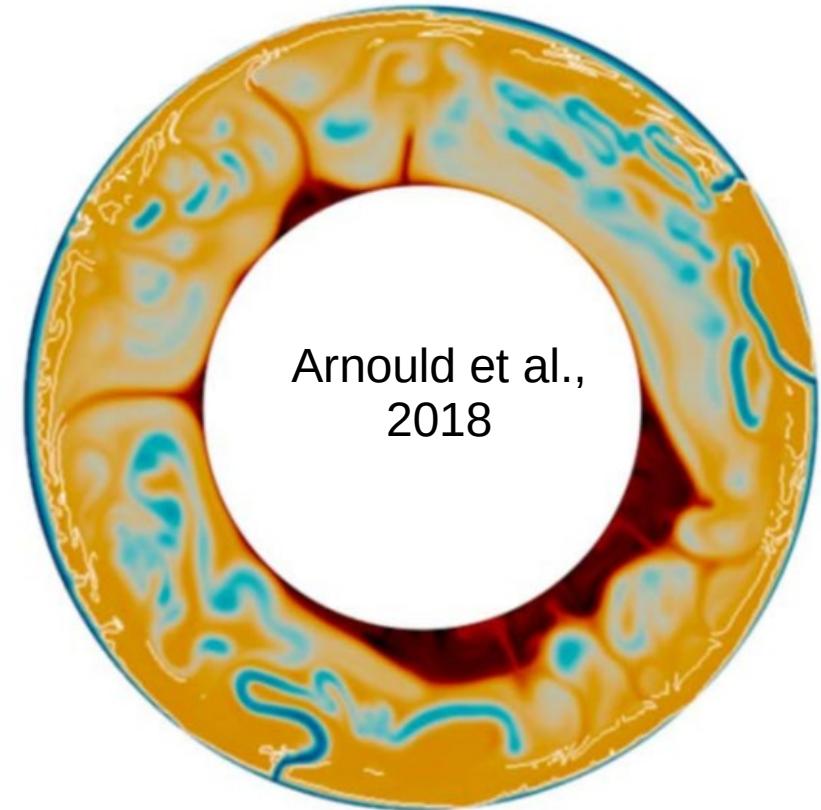
*Arrhenius law*



(cold) lithosphere 1000x more  
viscous than (hot) asthenosphere

# How does the mantle convect ?

- Spherical shell
- Secular cooling
- **temperature-dependent viscosity**
- $\text{Ra} > 10^6$  : “chaotic” convection  
at several scales



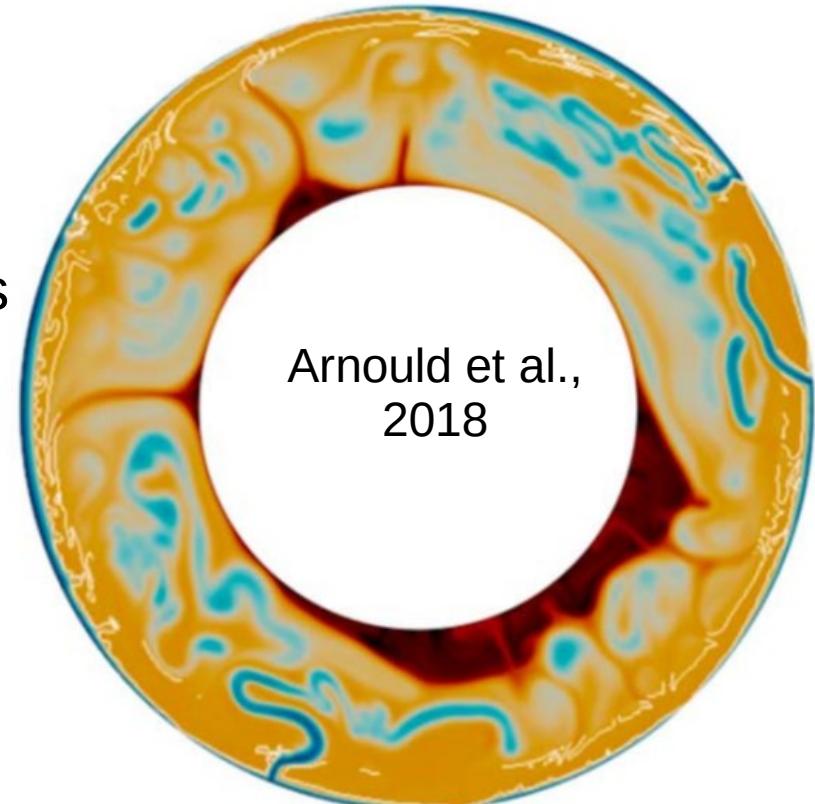
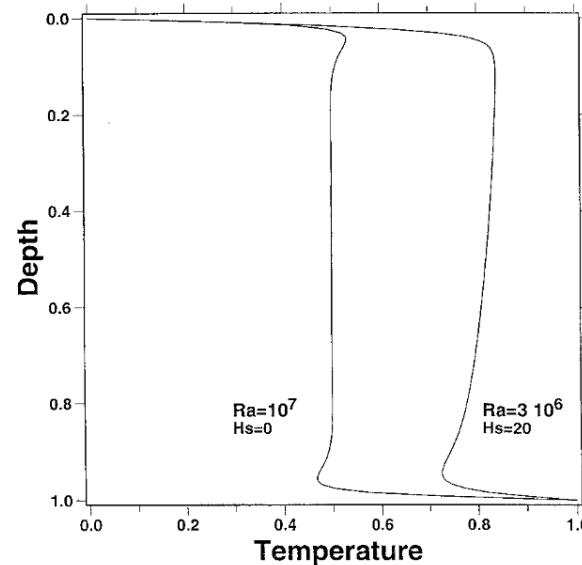
# How does the mantle convect ?

- Spherical shell
- Secular cooling
- temperature-dependent viscosity
- $\text{Ra} > 10^6$  : “chaotic” convection at several scales
- Internal heating from radioactive elements

$$\frac{\partial T}{\partial t} + u \nabla T = \nabla^2 T + H_s$$

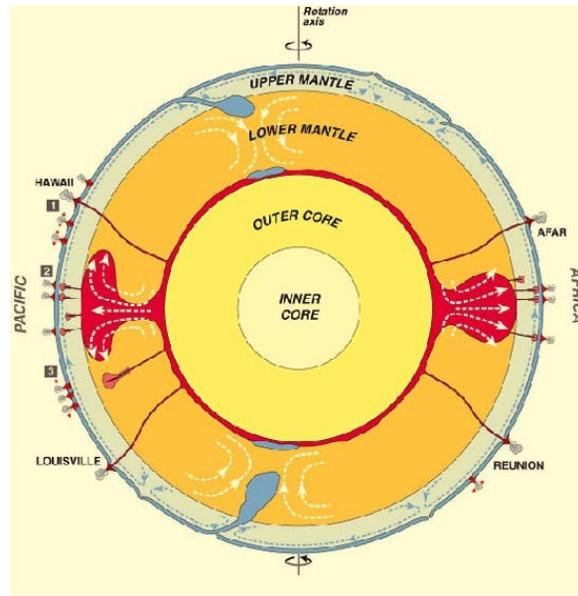
prominent cold boundary layer (lithosphere)

Sotin & Labrosse  
PEPI 1999

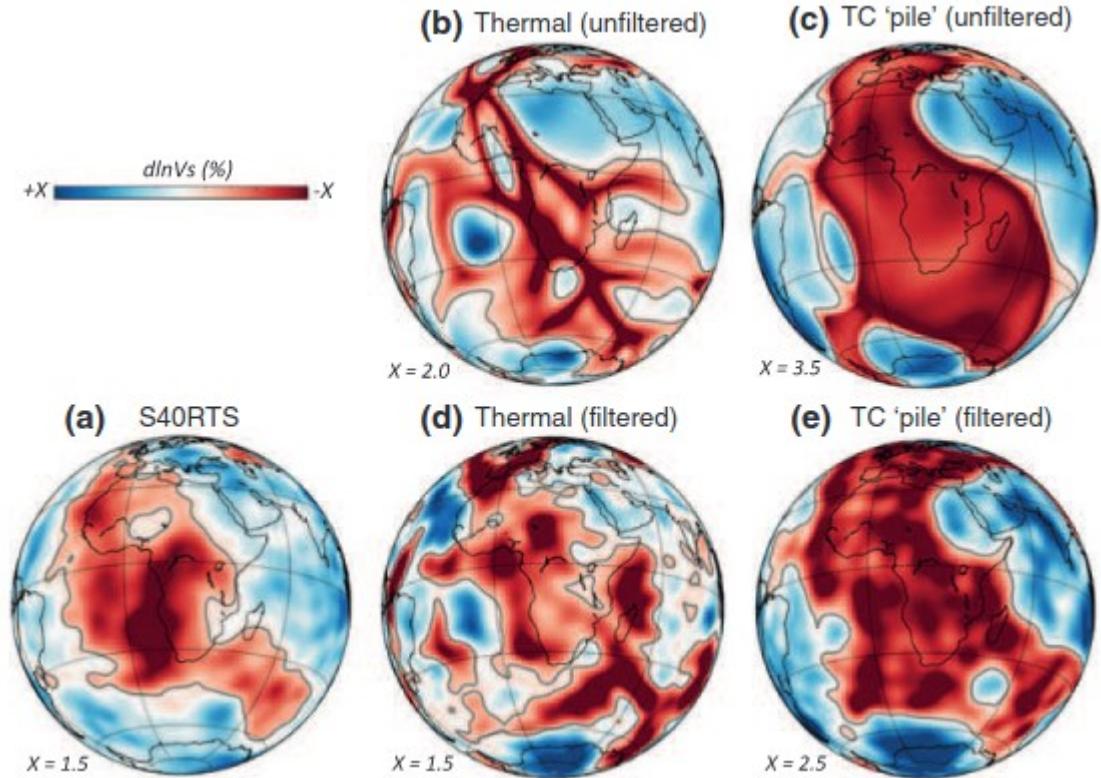


# Persistence of degree-2 mantle convection ?

Stability of degree-2 throughout Earth's history ?



two antipodal denser equatorial regions > stable configuration for Earth's moments of inertia  
(Dziewonski+ EPSL 2010)

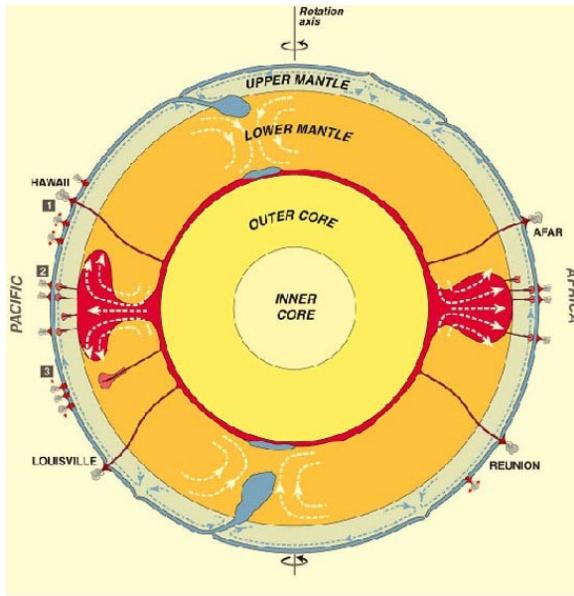


... what is the density anomaly of LLSVP ?

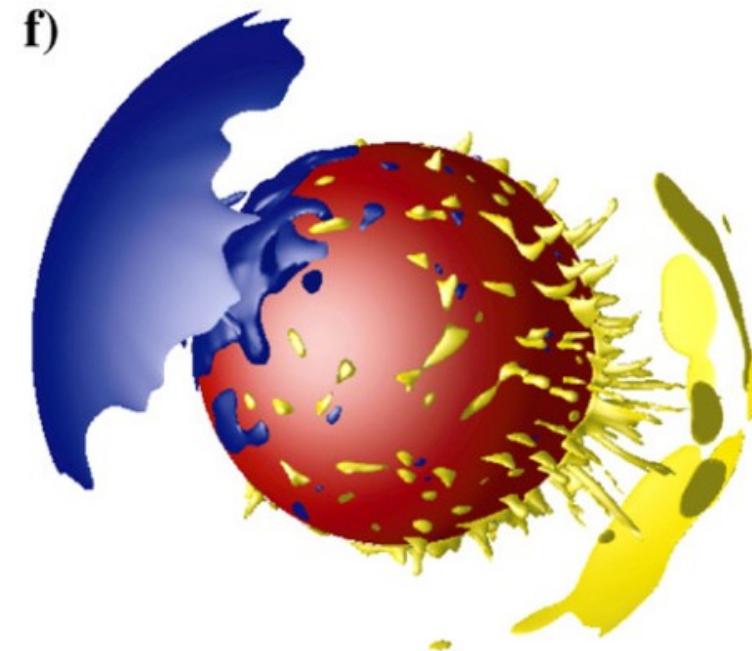
Davies + 2015

# Persistence of degree-2 mantle convection ?

Stability of degree-2  
throughout Earth's history ?



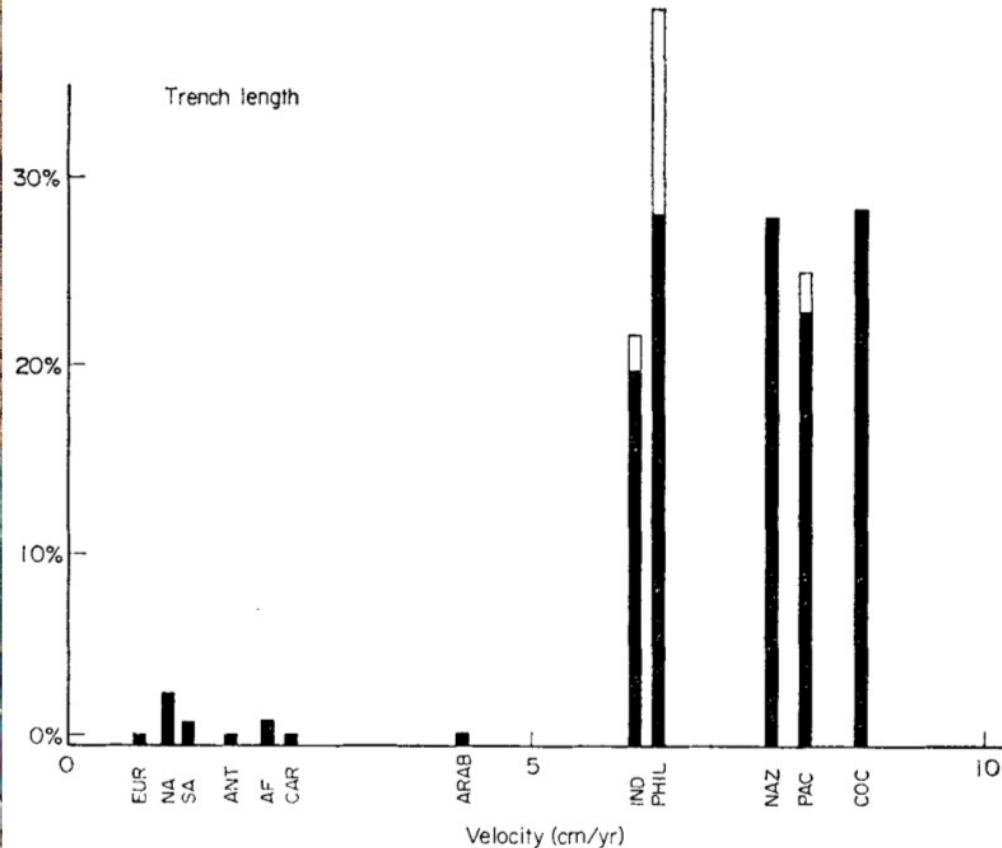
two antipodal denser  
equatorial regions > stable  
configuration for Earth's  
moments of inertia  
(Dziewonski+ EPSL 2010)



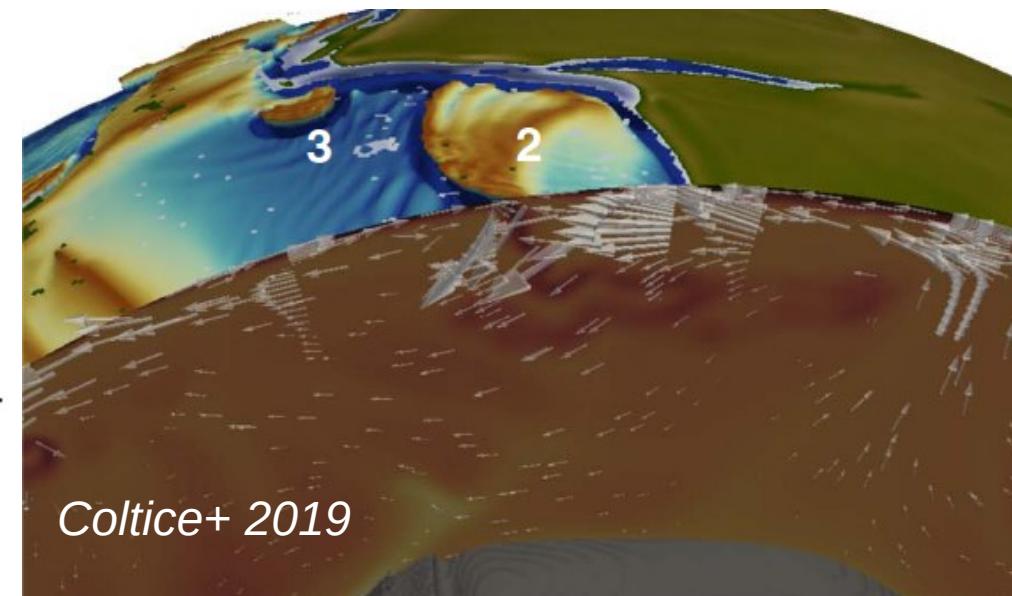
Stable degree-1 configuration with  
supercontinent assembly  
(Zhong+ EPSL 2007)

# Driving forces of plates motions

**Slab pull** is a major driving force of surface plate motions



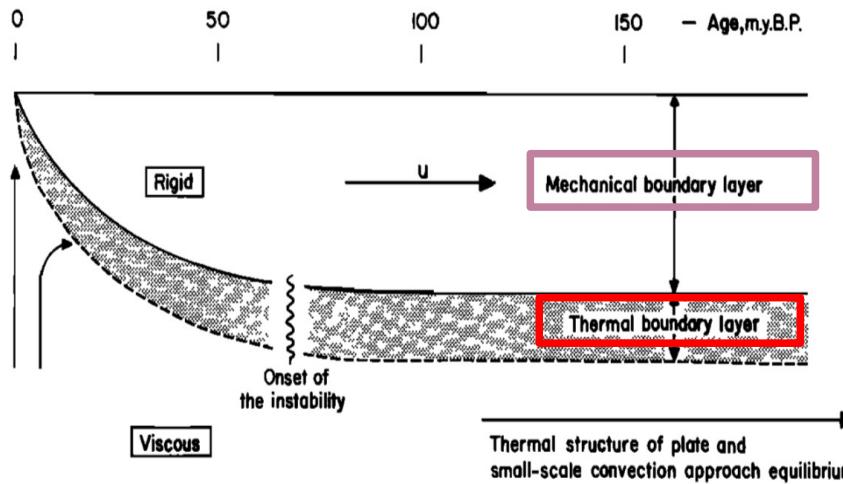
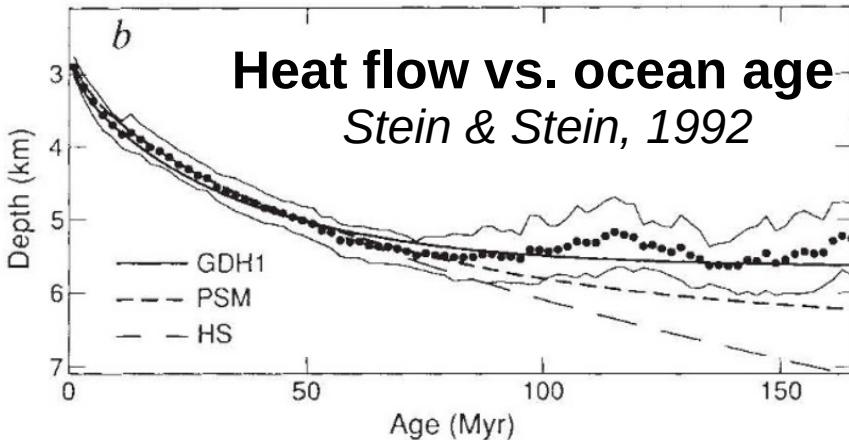
... but **basal drag from asthenosphere** can also play a role (“conveyor belt”)



Coltice+ 2019

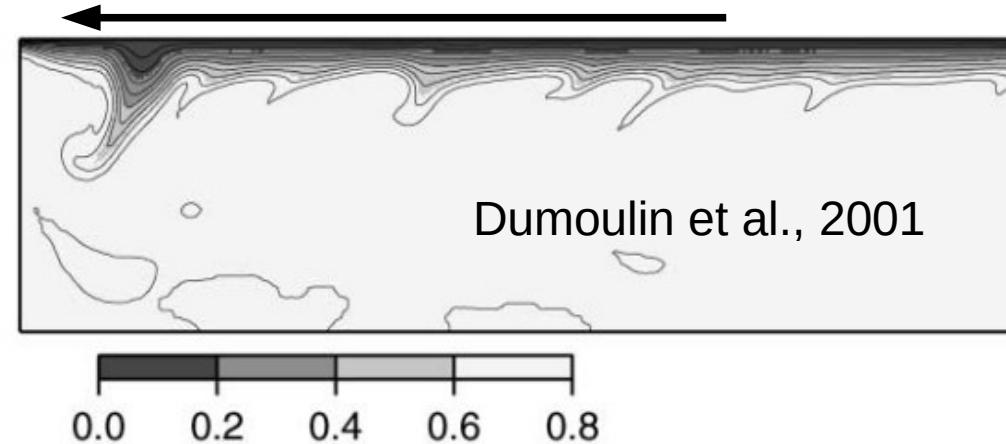
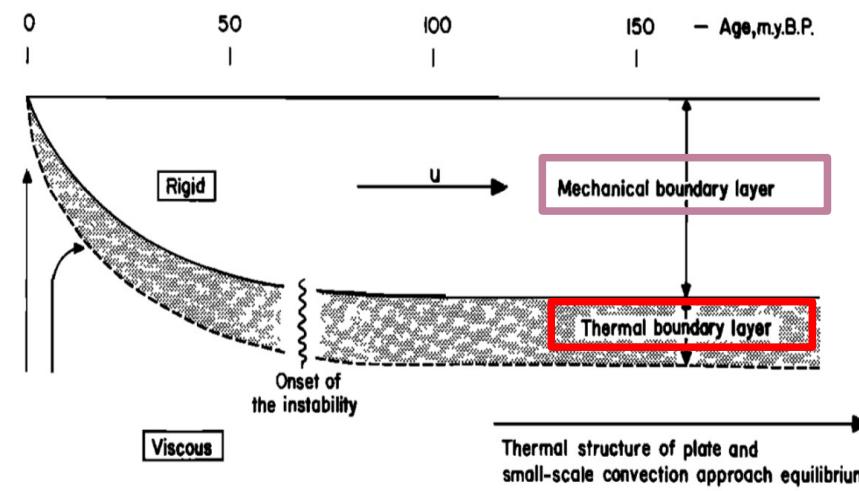
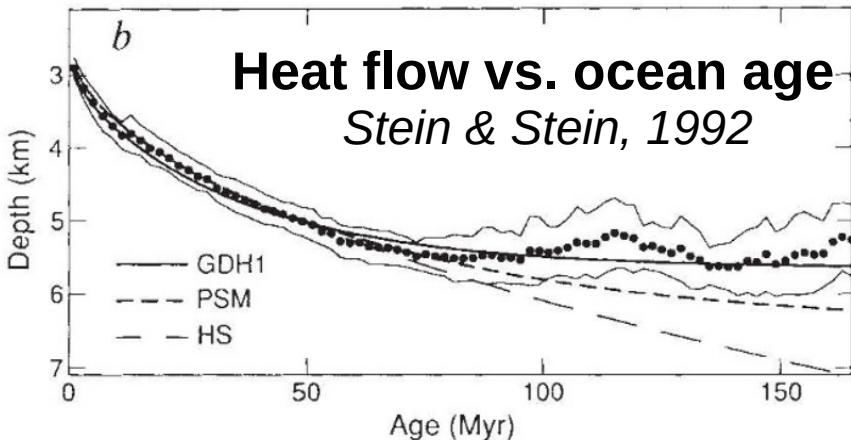
Forsythe & Uyeda, GJI, 1975

# Several scales of convection

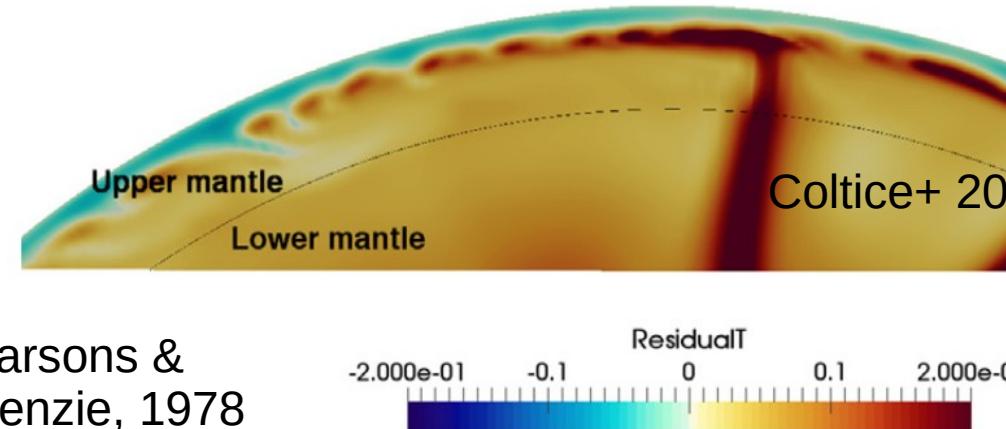


Parsons &  
McKenzie, 1978

# Several scales of convection

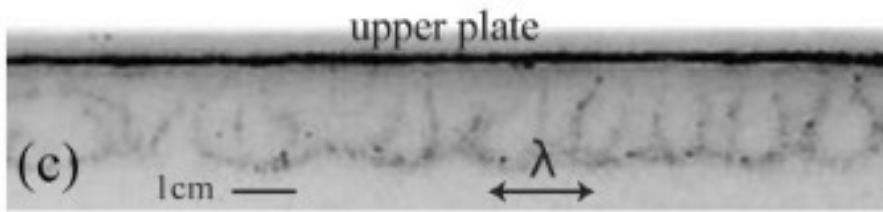
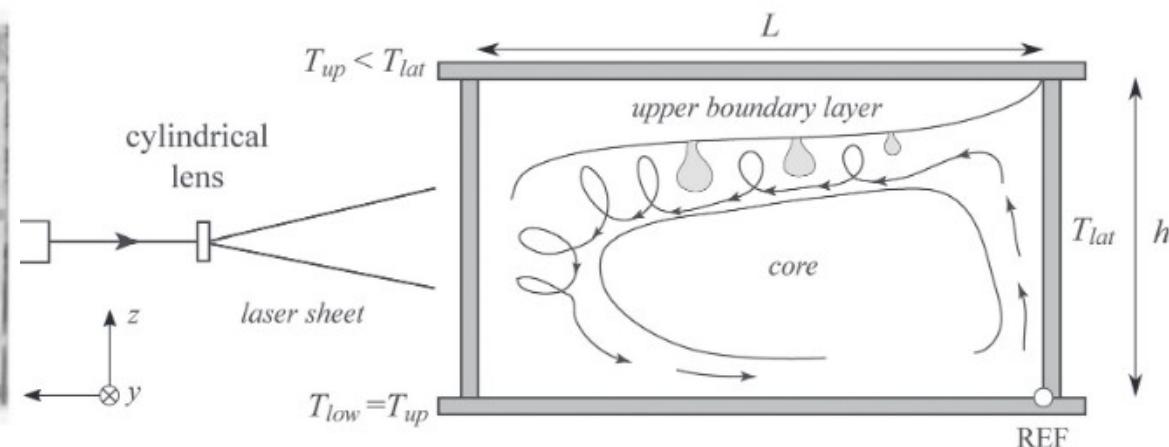
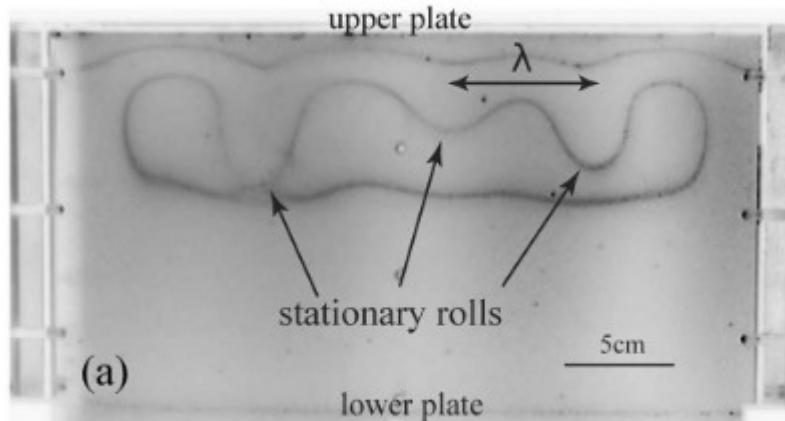


small-scale convection ?

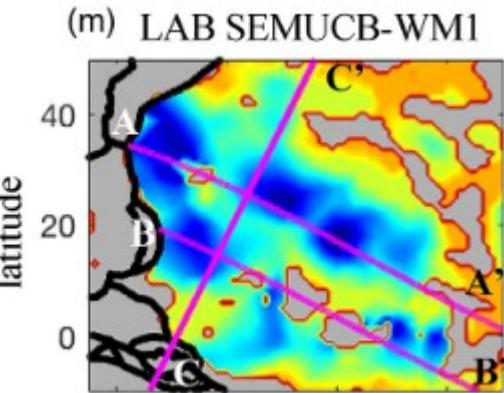
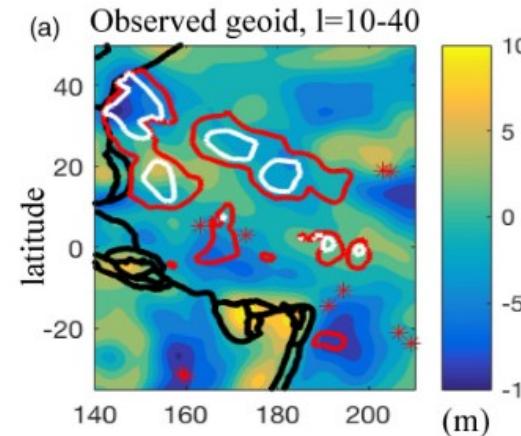


Parsons &  
McKenzie, 1978

# Several scales of convection – 1000-km scale cells ?

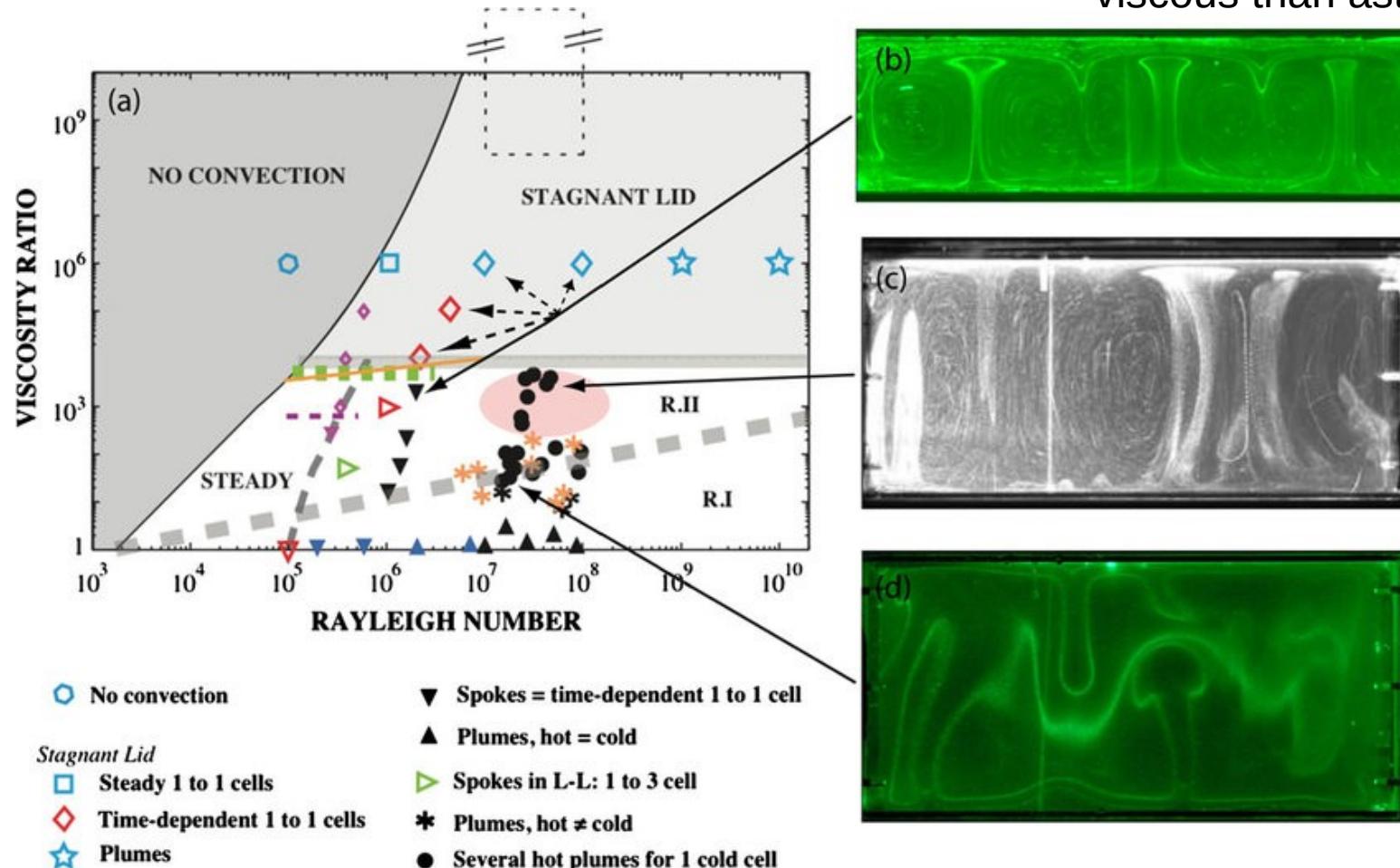


Analogue experiment (glucose syrup)  
+ geoid & seismic data



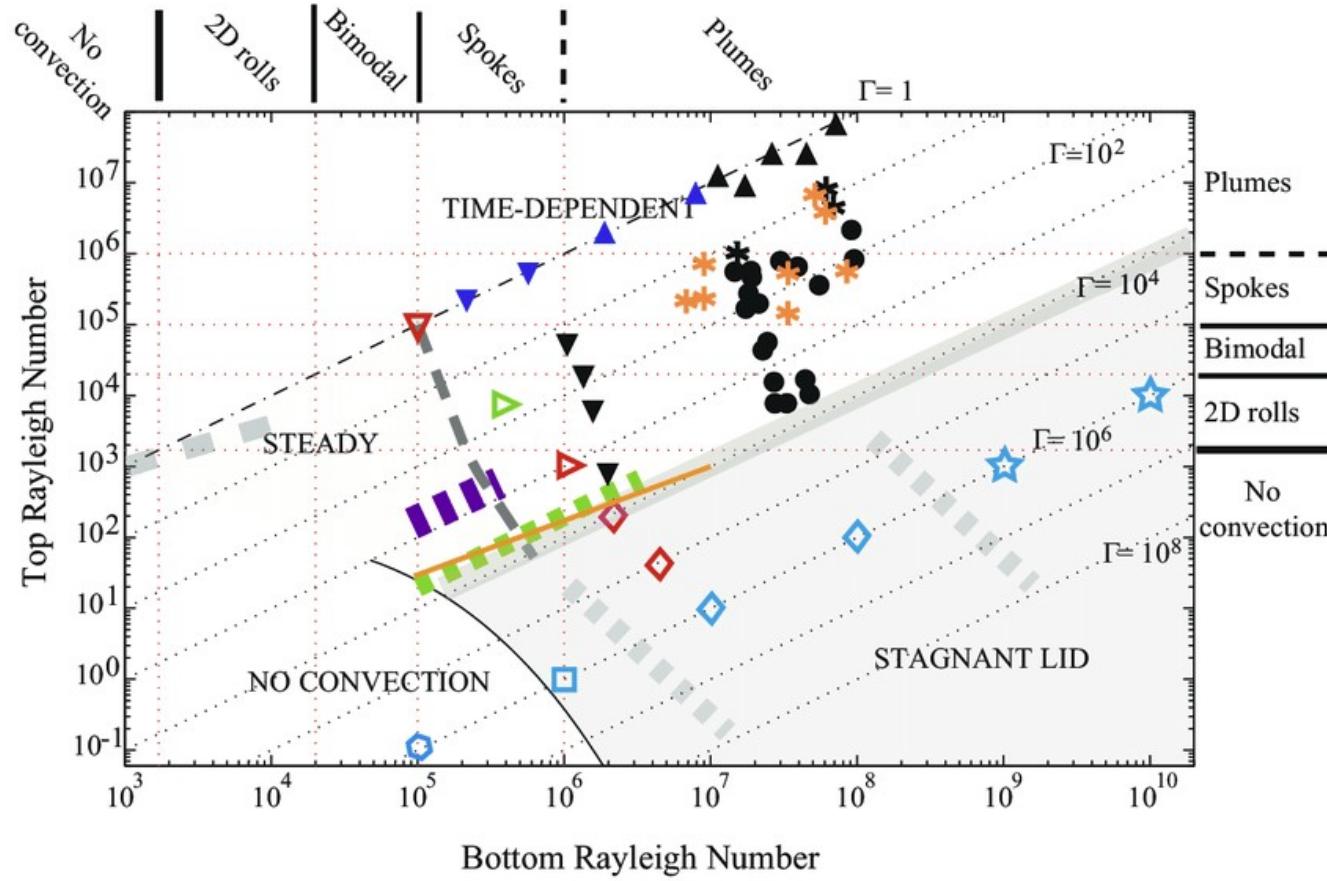
# How does the mantle convect ?

- Strongly **temperature-dependent viscosity** > lithosphere 1000x more viscous than asthenosphere



Smrekar+ 2018





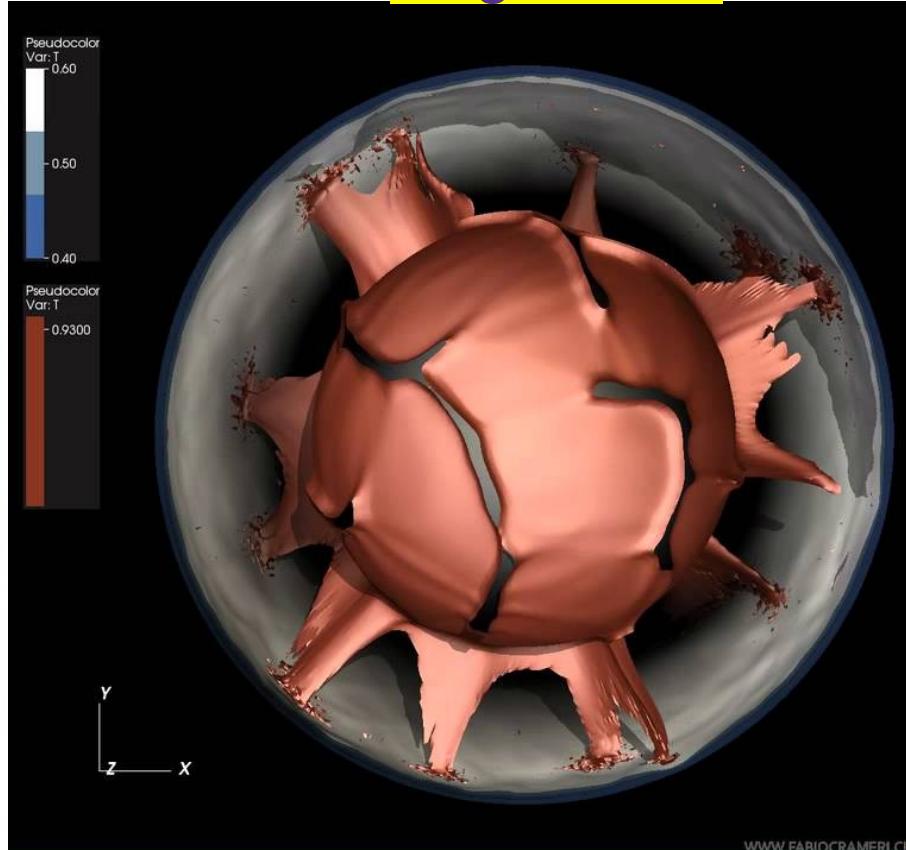
Davaille+ 2011



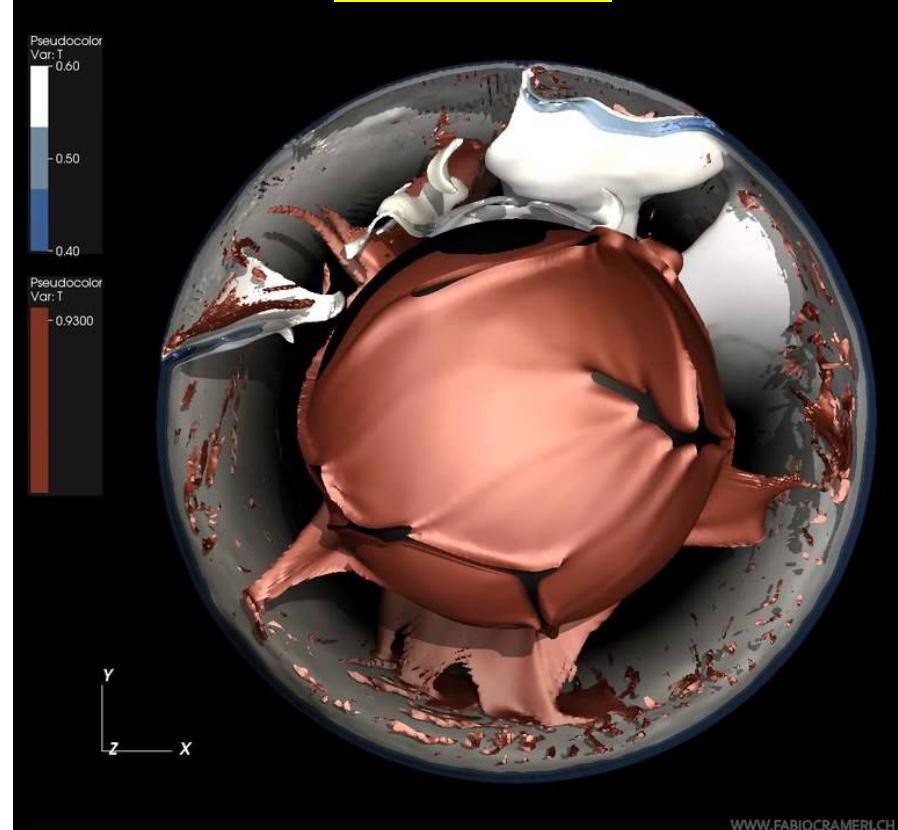
# Importance of viscosity parameterization

- Strongly temperature-dependent viscosity

stagnant-lid



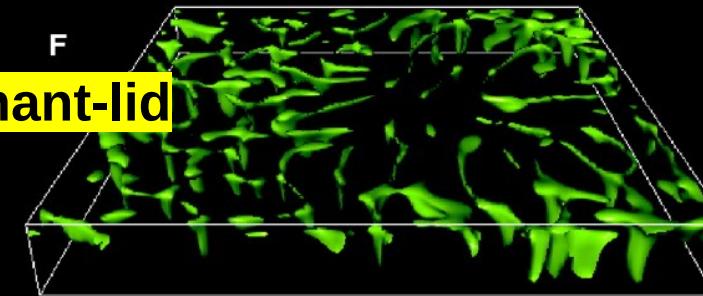
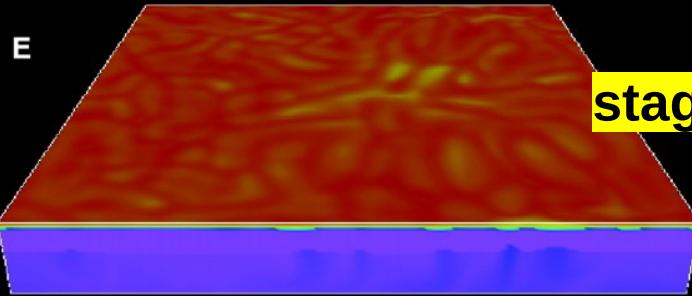
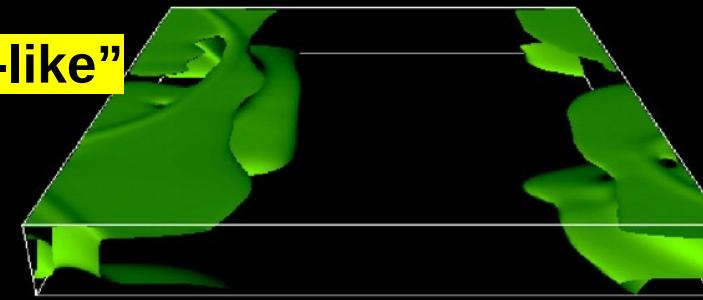
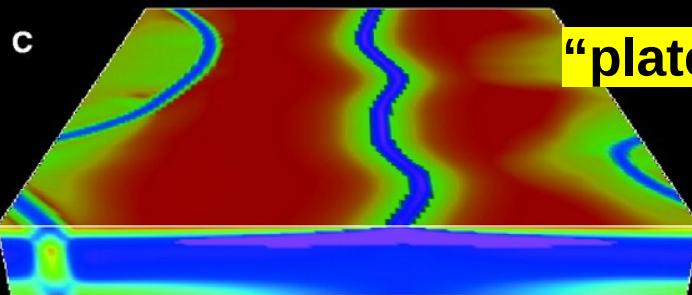
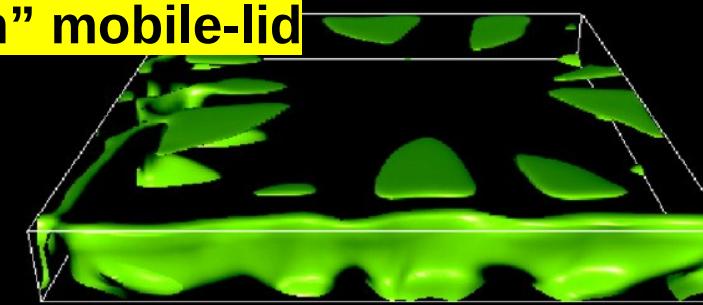
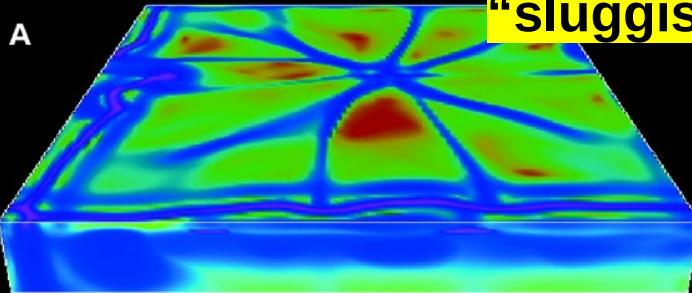
mobile-lid



increasing yield strength

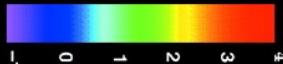
log(Viscosity)

cold temperature (downwellings)



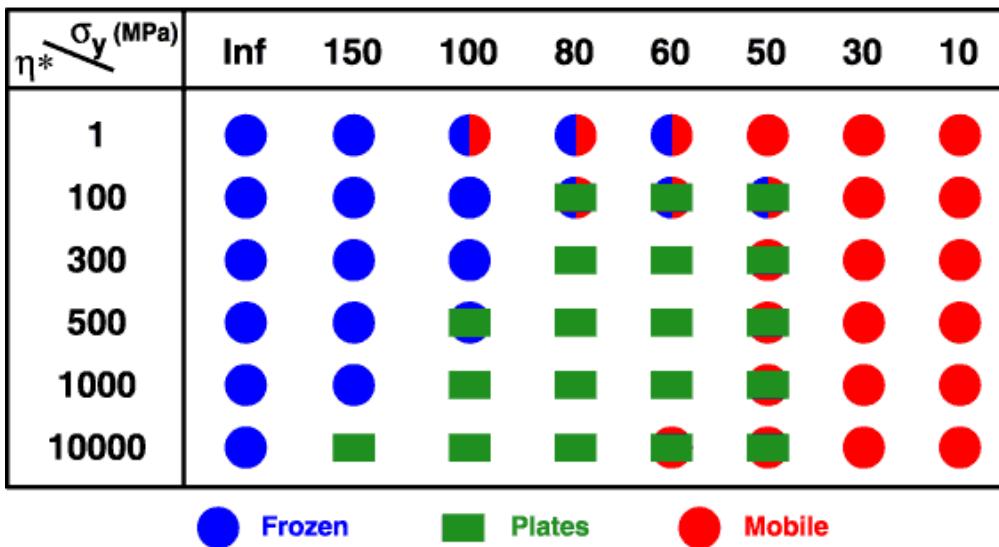
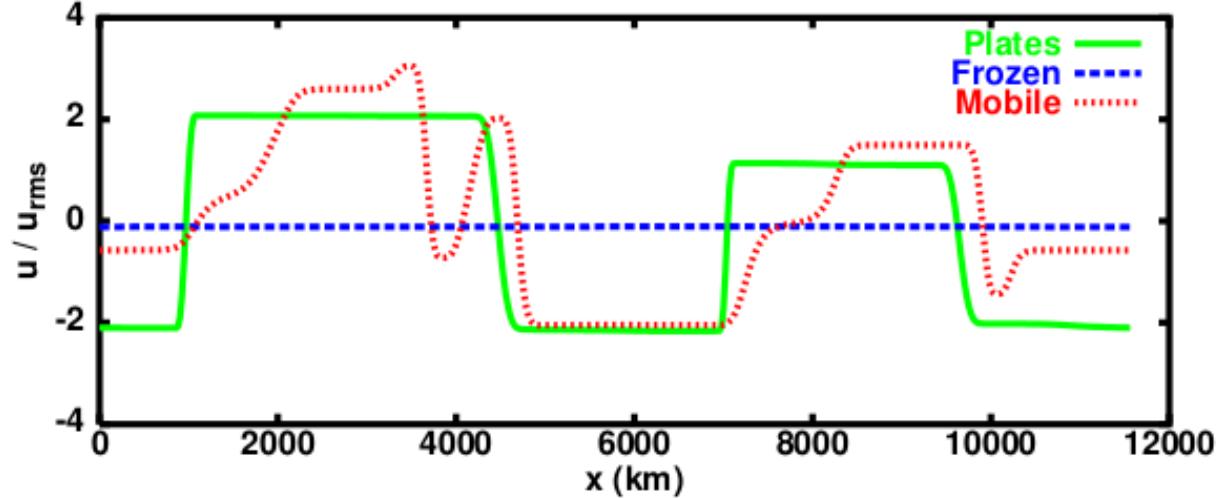
**yield strength =**  
mechanical  
resistance of the  
cold lithospheric  
boundary layer

Tackley  
Science  
2000



# Importance of viscosity parameterization

localizing  
deformation at  
plate boundary

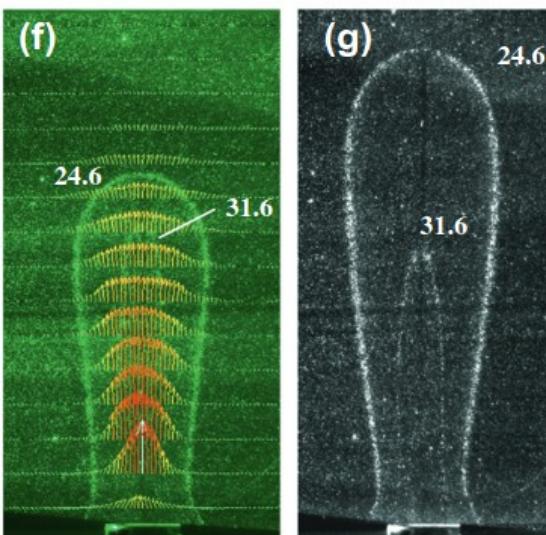
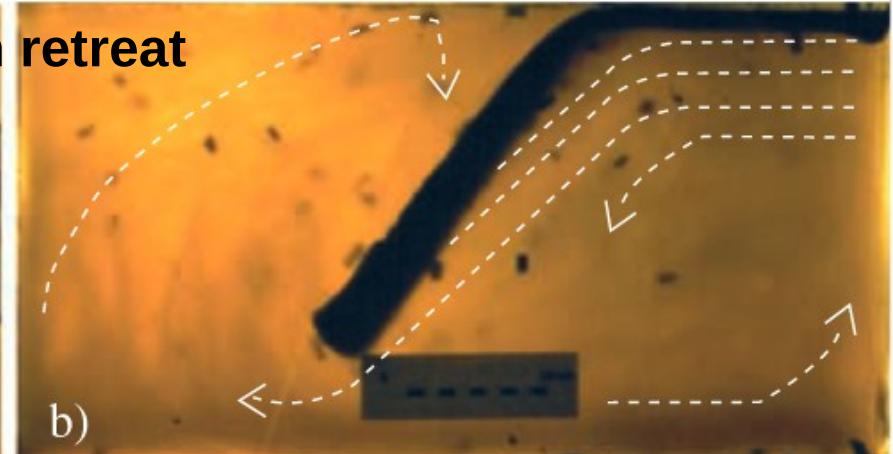
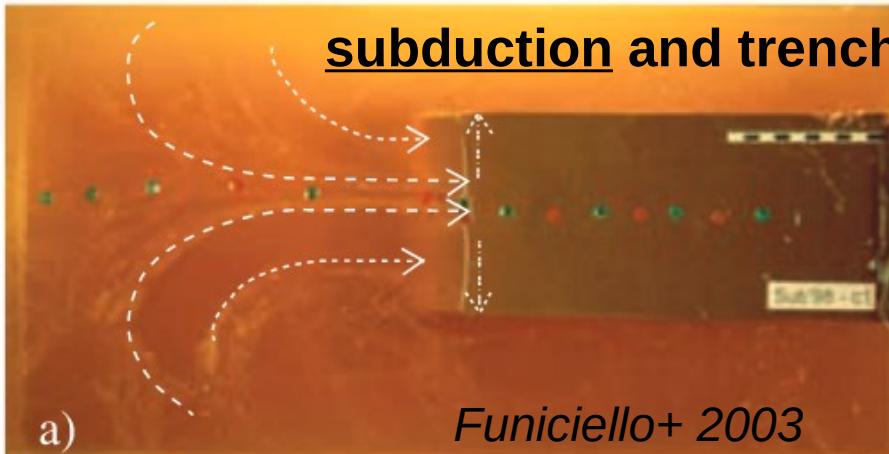


lithosphere mobility as a function of **yield stress**  $\sigma_y$  and viscosity contrast  $\eta^*$  for a **sub-plate low-viscosity layer**

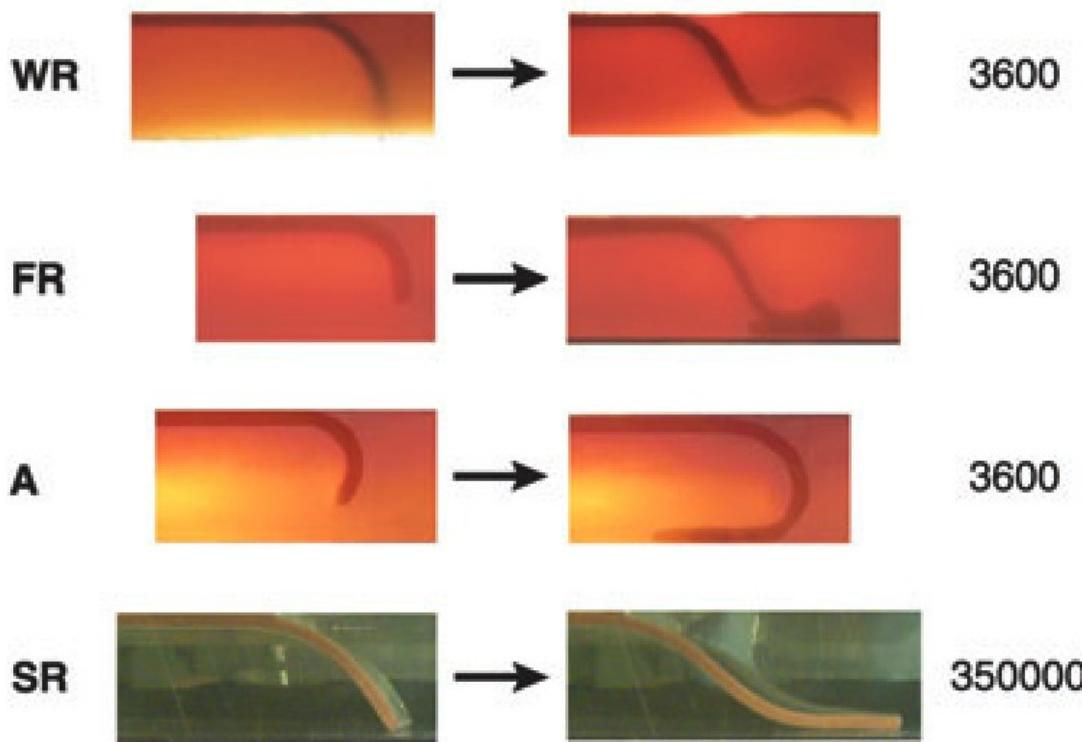
Richards G<sup>3</sup> 2001



# Ingredients of numerical/analogue experiments

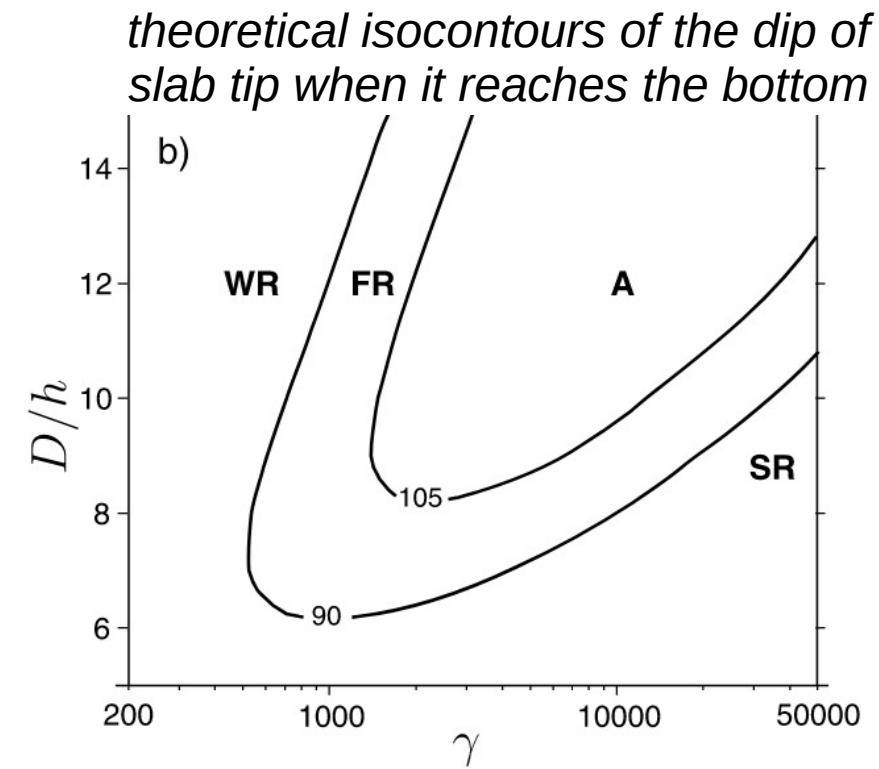


# Slab shape : influence of viscosity contrast



WR: weak retreating mode.  
FR: folding retreating mode.  
A: advancing mode.  
SR: strong retreating mode.

Ribe  
GJI 2010



**modes of free subduction** as a function of the viscosity contrast  $\gamma$  and the ratio  $D/h$  of the layer depth to the sheet thickness



# Mantle convection layering : radial viscosity profile ?

## Geoid Anomalies

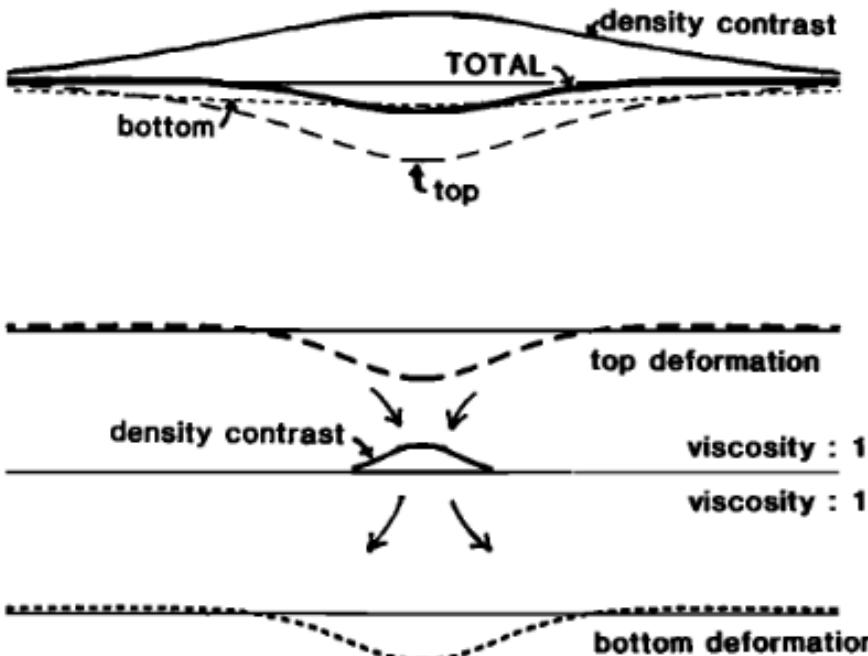


Fig. 1. Illustration of the components of the geoid anomaly from a cosine bell density contrast at the midpoint of a layer of uniform viscosity  $\eta$ . The total anomaly (heavy solid line) is the sum of the contributions from the density contrast itself (light solid line), from dynamic deformation of the upper boundary (long dashes), and from dynamic deformation of the lower boundary (short dashes). The total geoid anomaly is negative for a positive density anomaly.

## Geoid Anomalies

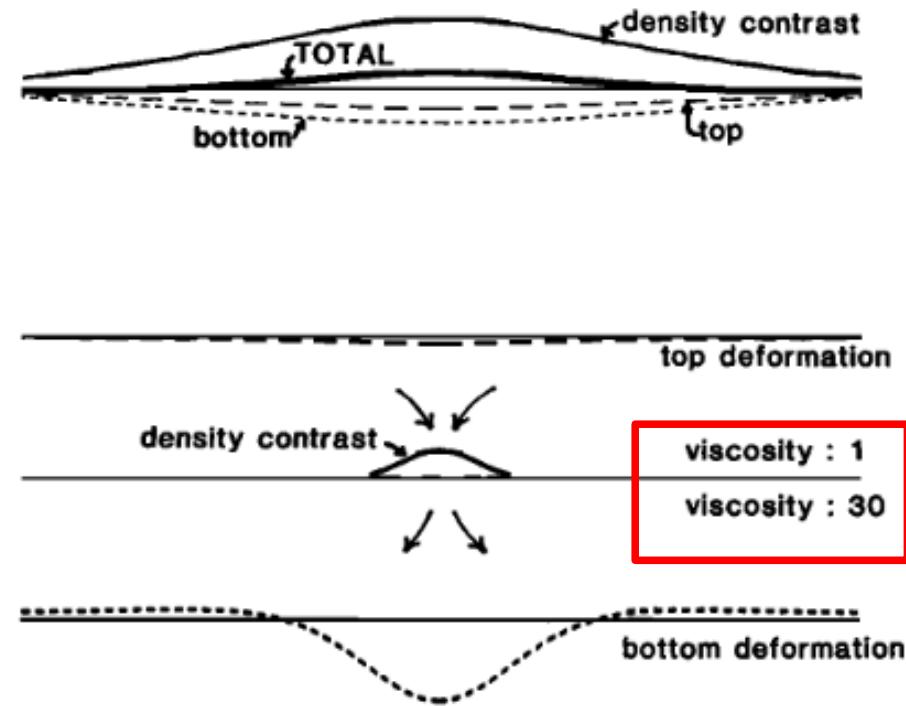
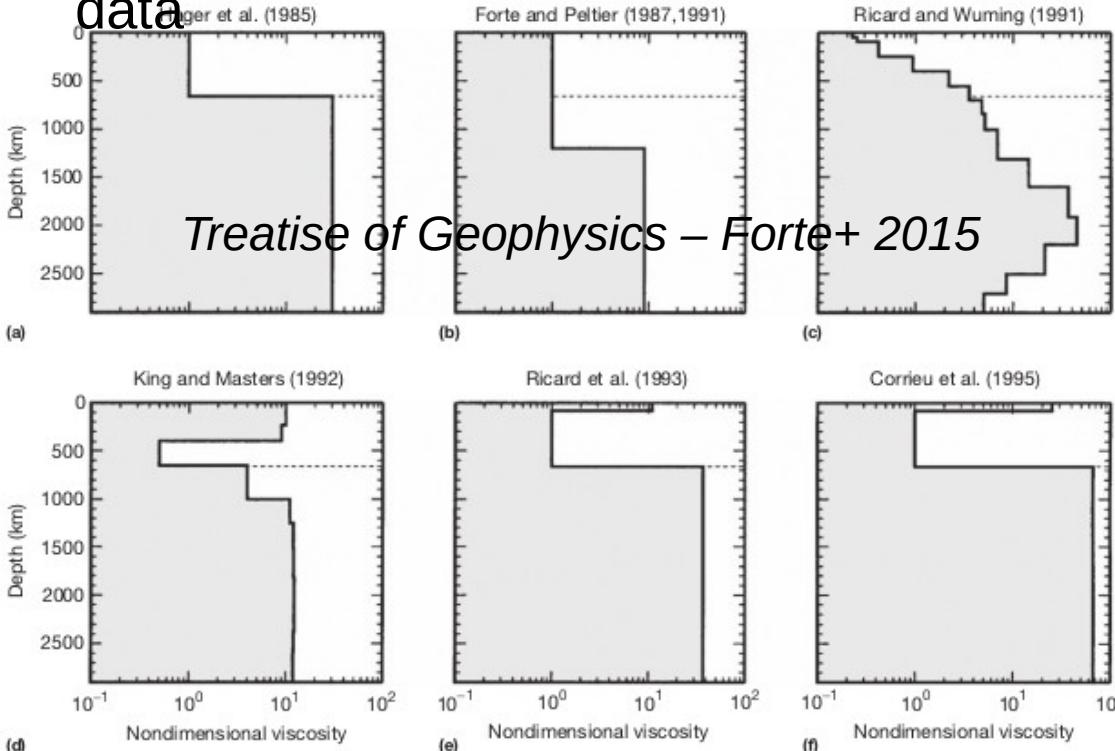


Fig. 2. As in Figure 1, but now the bottom half of the layer has a viscosity  $\eta$  a factor of 30 larger than the upper half. The sign of the total geoid anomaly is now positive.

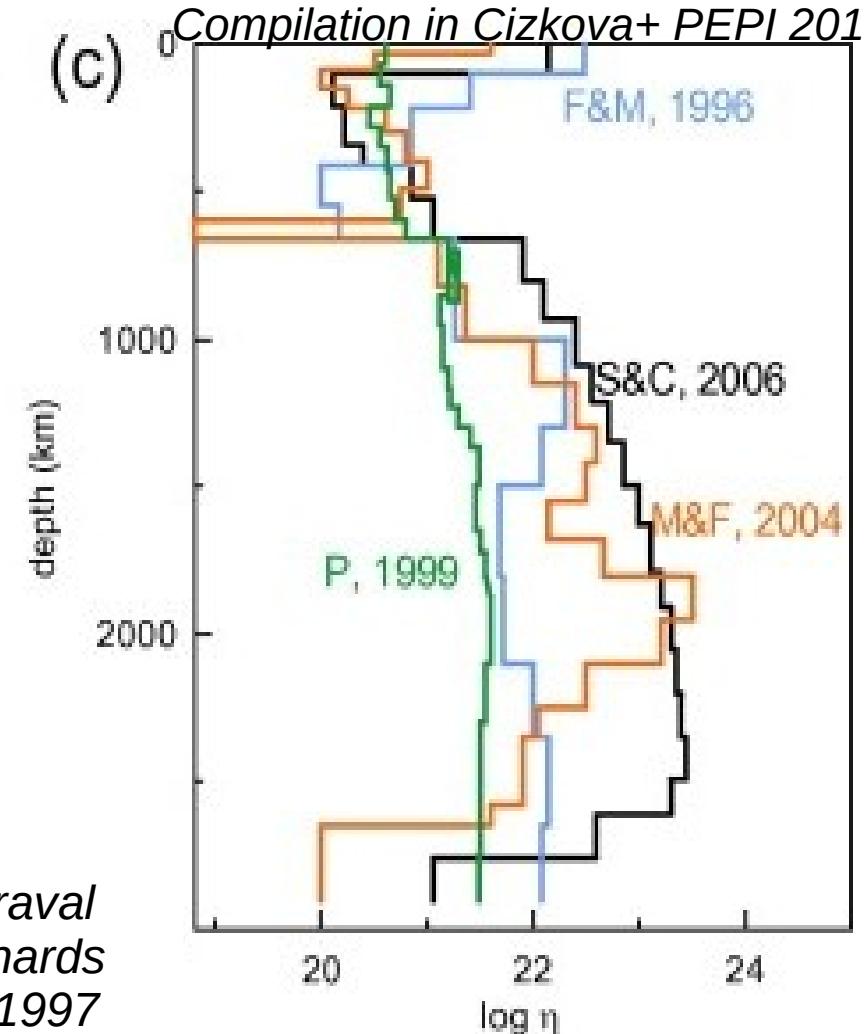
# Mantle convection layering : radial viscosity profile ?

inversion of geoid, postglacial rebound data



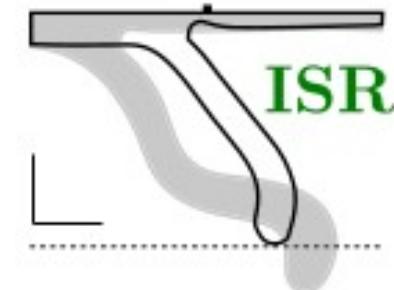
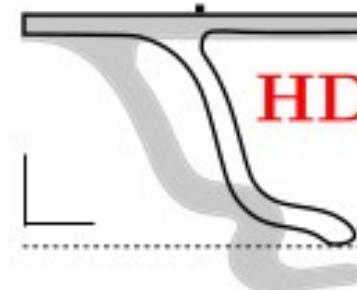
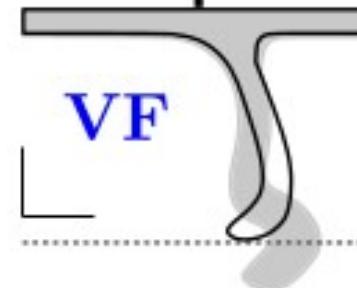
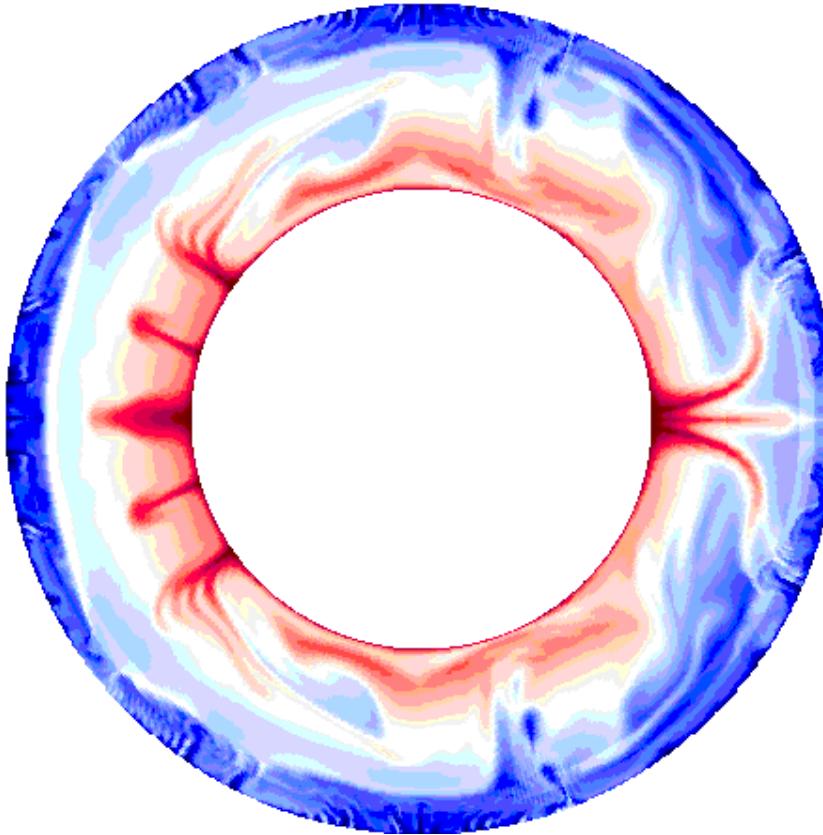
... but large uncertainties on Bcs =  
→ can we solve for more than 3 layers ?

Thoraval  
&Richards  
GJI 1997



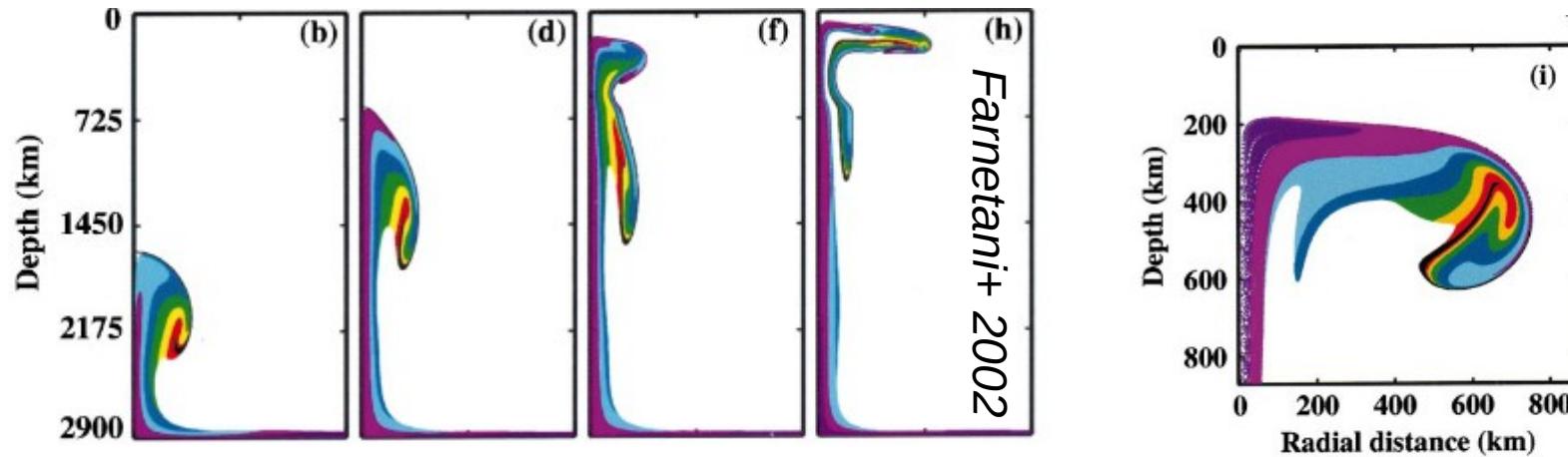
# Mantle convection layering and slab deformation

1.5-layer ?

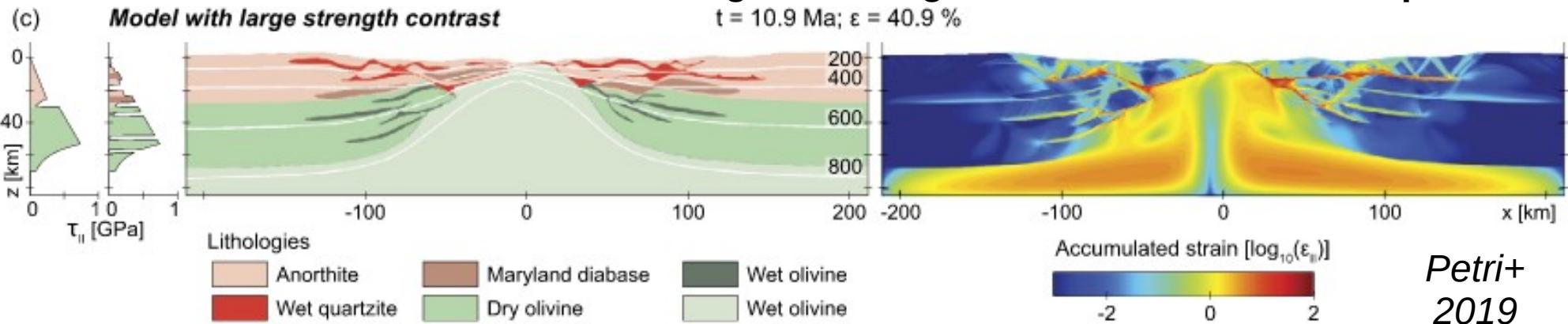


# Ingredients of numerical/analogue experiments

## mixing and deformation in mantle plumes



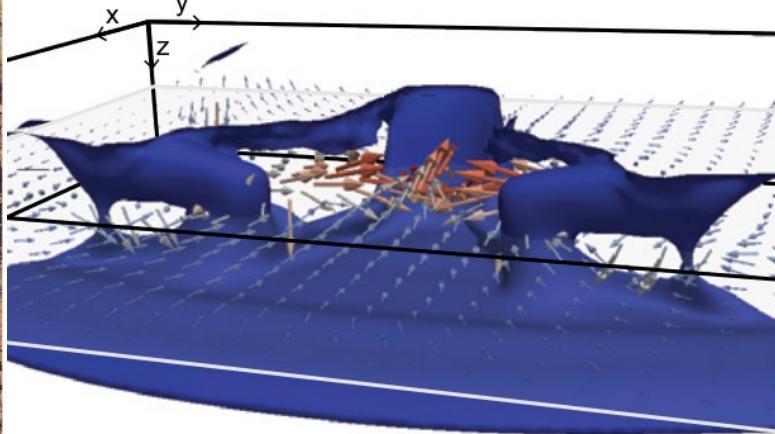
## ripping of heterogeneous continental lithosphere



Petri+  
2019

# Ingredients of numerical/analogue experiments

## 3-D toroidal flow through slab tear

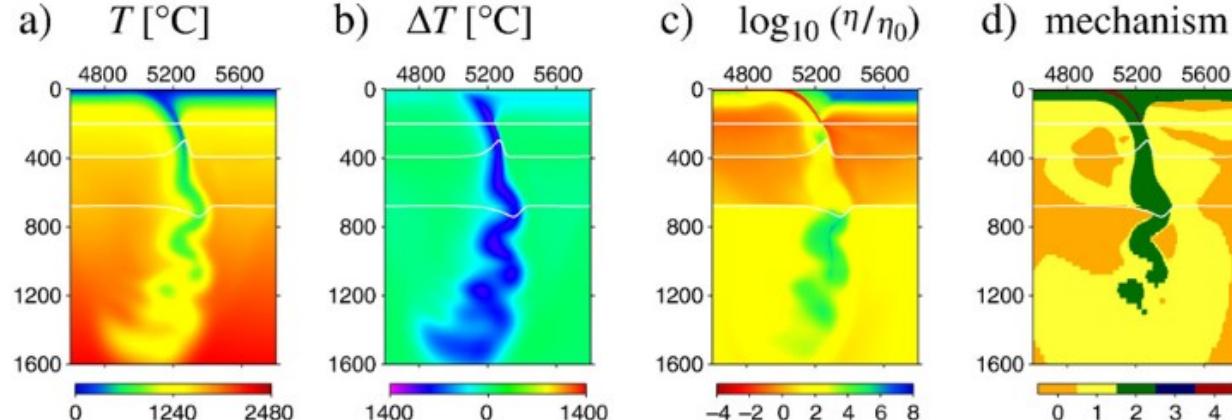


Magni+ Geology 2014

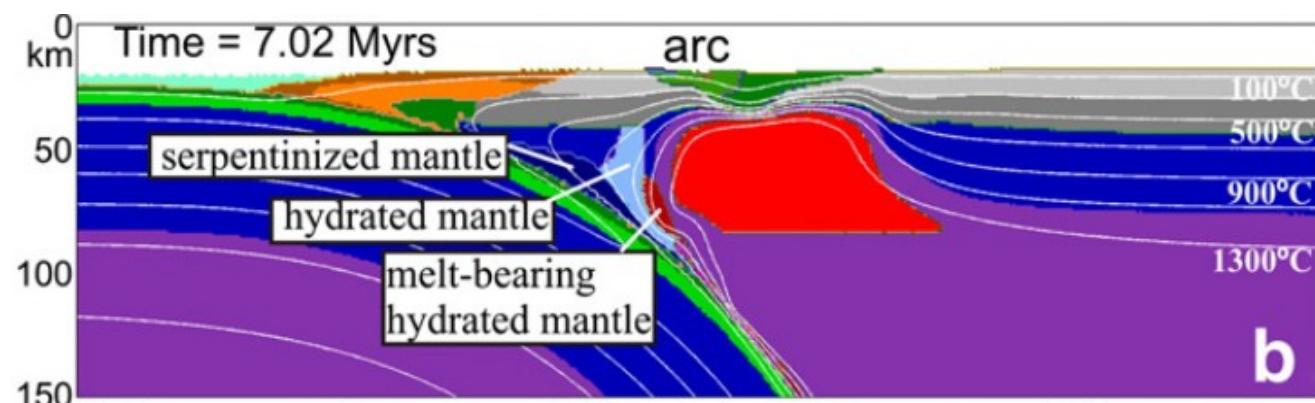
**subduction**  
+ water transfer  
+ partial melting  
+ erosion & sedimentation

Sizova, Gerya+ 2010

## slab piling (viscosity jump + phase transitions)

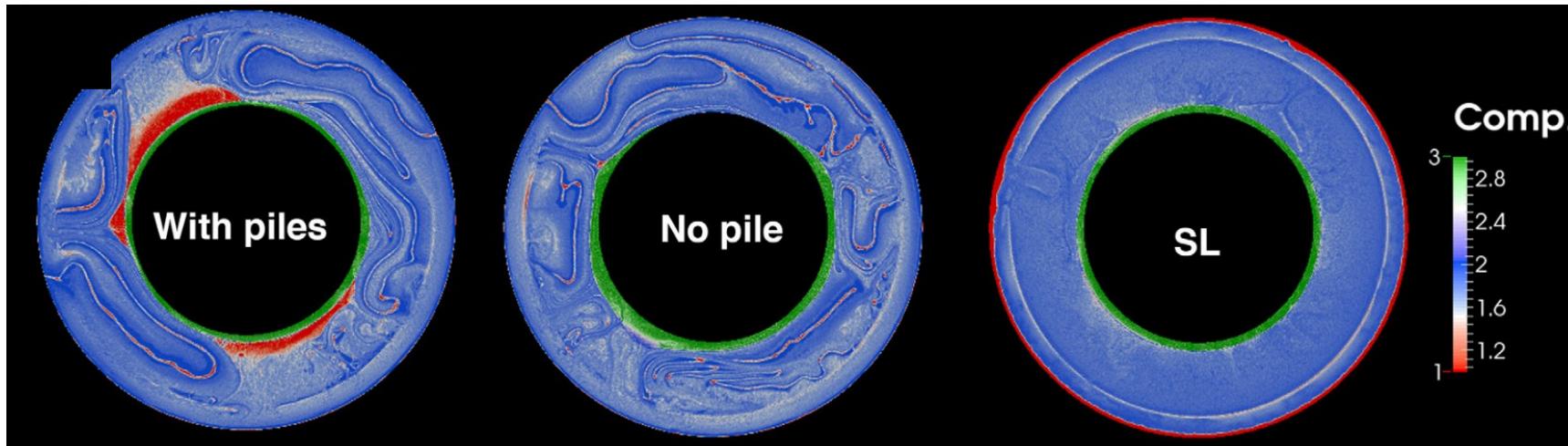


Cizkova & Behoukova EPSL 2008



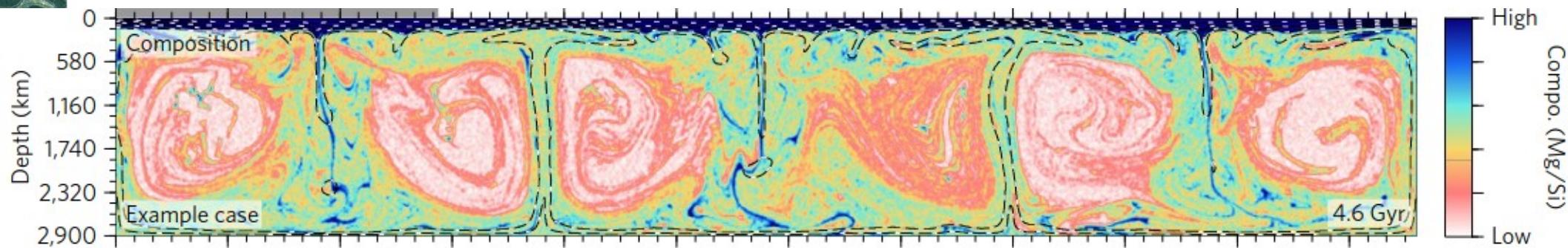
b

# Ingredients of numerical/analogue experiments



Nagakawa  
& Tackley  
G3 2015

Chemical differentiation + various yield strength



persistent **BEAMS** (bridgmanite-enriched ancient mantle structures)  
if viscosity contrast > 30

Ballmer+  
NatGeo 2017

# Ingredients of numerical/analogue experiments

## DOMAIN - A + N

- **dimension** > 2-D (no toroidal flow), 3-D
- domain geometry > cartesian, spherical / upper mantle only vs. whole mantle
- **boundary conditions** : closed (no-slip, free-slip, free-surface, surface-driven)  
or open (periodic, imposed) - heat flux, temperature
- **initial conditions**: thermal field ; continents, chemical reservoirs

Analogue models,  
numerical models

## PROPERTIES – A + N

- **state equation**  $\rho = f(T, z, \text{chemistry, material})$   $\Rightarrow$  density anomalies
- **viscosity**  $\eta = f(T, z, \text{chemistry, material, grain size, strain rate, CPO...})$
- parameters and dependencies (rad. heat production, thermal cond., thermal expansivity...)
- chemical partitioning coefficients

## EQUATIONS - N

- **conservation equations** : mass, momentum (energy) - simplifications : Boussinesq  
+ infinite Pr

## NUMERICAL RESOLUTION - N

## Recipes for solving the conservation equations

- Finite difference, finite-element or finite-volume approximations
- Marker in cells (e.g. evolutive composition, grain size) or passive tracers
- Possible auto-adaptive meshing

*examples of thermo-mechanical codes :*

Citcom & **ASPECT** (US-CIG community codes), **StagYY** (Tackley, Coltice),  
**I3/I2ELVIS** (Gerya+), pTatin (May & Le Pourhiet), **Underworld** (Moresi+),  
**LaMEM** (Kaus+), Fluidity (Davies+)...



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LaMEM (Kaus+), Fluidity (Davies+)...

## Coupling to other codes for other processes

- PerpleX, MAGEMIN - **mineral assemblage evolution**
- Badlands, Fastscape – **erosion, incision & sedimentation**
- D-REX – **evolution of anisotropy...**



# The “good use” of models



**“All models are wrong but some are useful”**



G. Box, *Robustness in the strategy  
of scientific model building*, 1979



# The “good use” of models



**“All models are wrong but some are useful”**



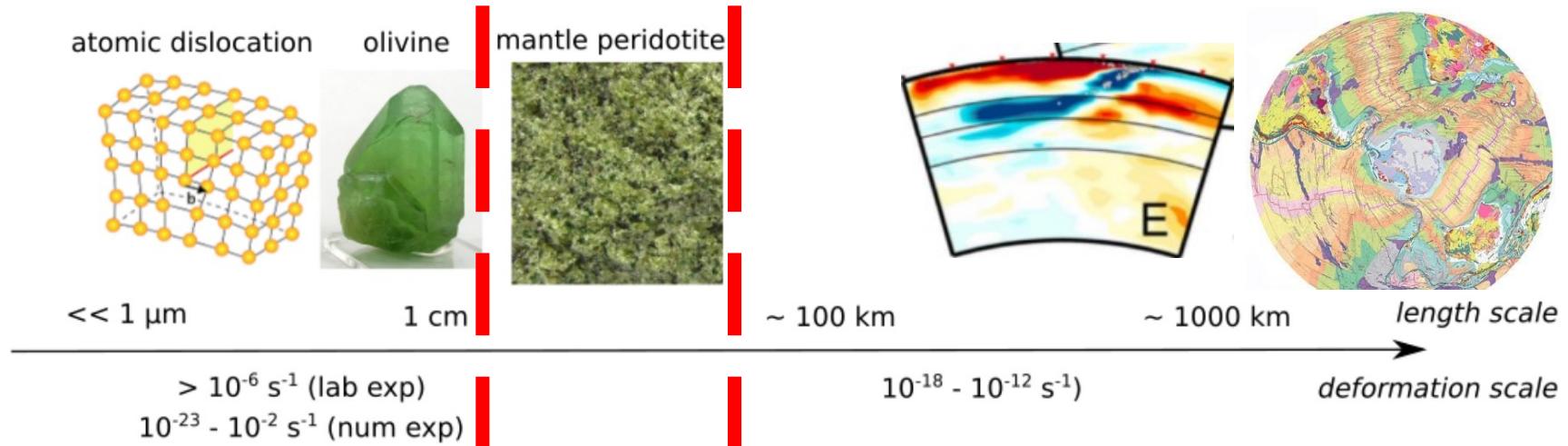
G. Box, *Robustness in the strategy  
of scientific model building*, 1979

→ *of course the model is not the truth*

→ *but the model can be “illuminating and useful”*

A lot of different models can be useful – even simple ones,  
even very complex ones – depending on the science question  
and the data to compare !

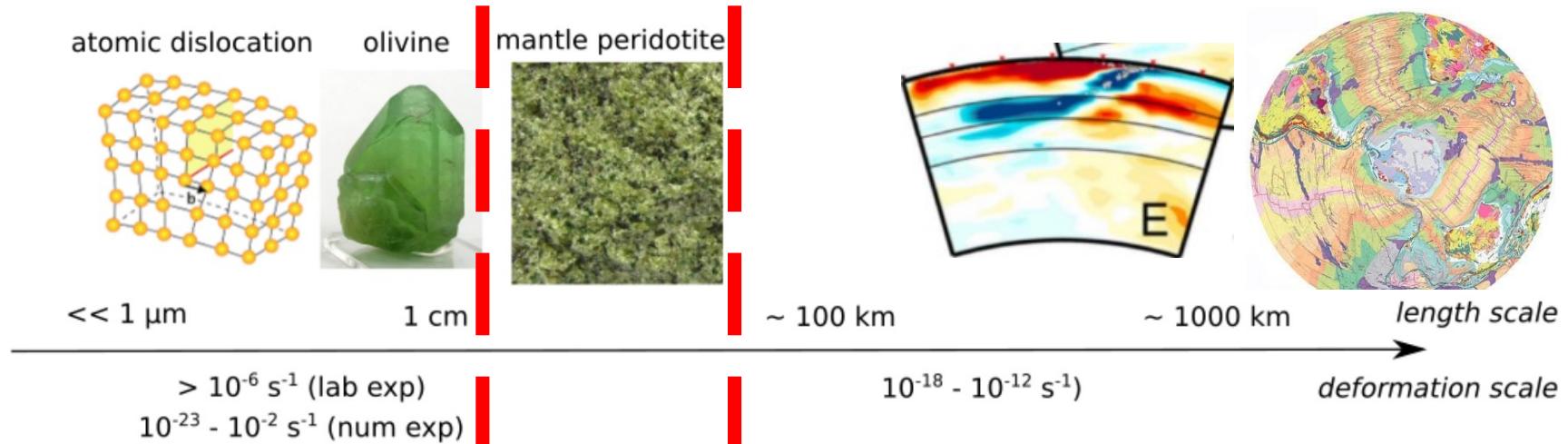
# Dynamical models : input and outputs relative to data



**Small-scale data  
Acquiring / Upscaling**



# Dynamical models : input and outputs relative to data

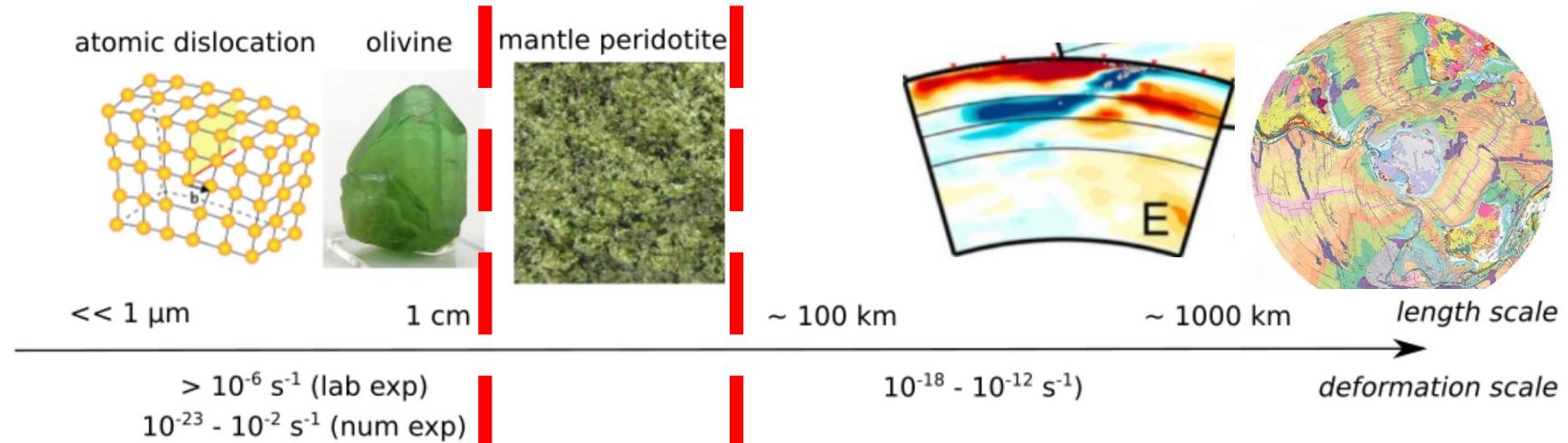


**Small-scale data  
Acquiring / Upscaling**

**INPUT** ↓ **Parameterizing**

**Numerical models**  
- dynamical evolution  
- self-consistent feedbacks

# Dynamical models : input and outputs relative to data



**Small-scale data  
Acquiring / Upscaling**

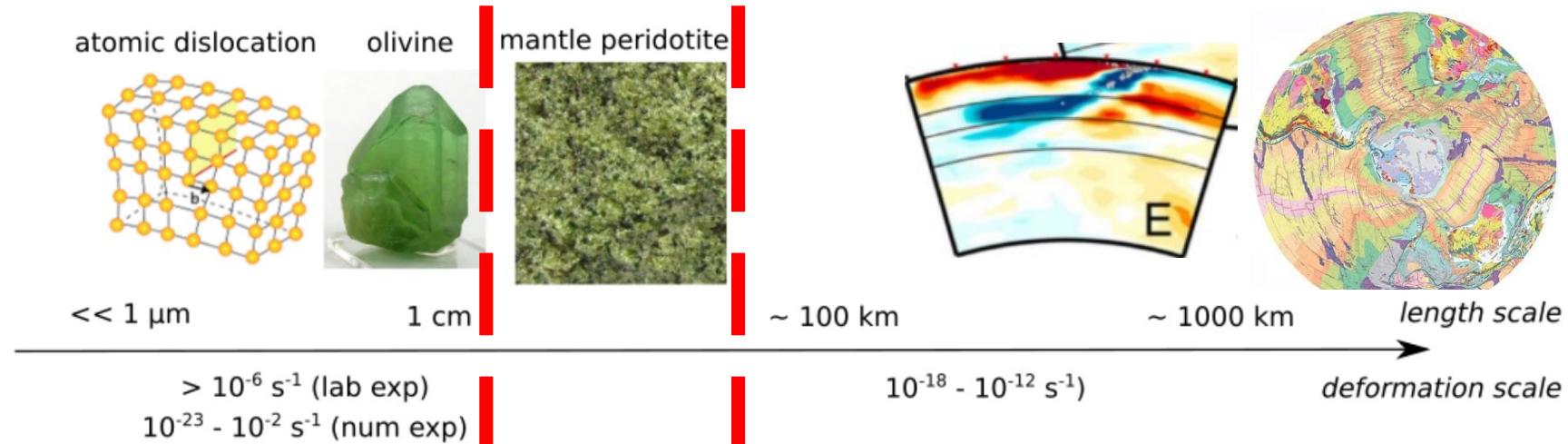
**INPUT** ↓ **Parameterizing**

**Geological and  
geophysical DATA**

**Numerical models**  
- dynamical evolution  
- self-consistent feedbacks

**PREDICTIONS  
SYNTETICS**

# Dynamical models : input and outputs relative to data



**Small-scale data  
Acquiring / Upscaling**

**INPUT** ↓ **Parameterizing**

**Numerical models**  
- dynamical evolution  
- self-consistent feedbacks

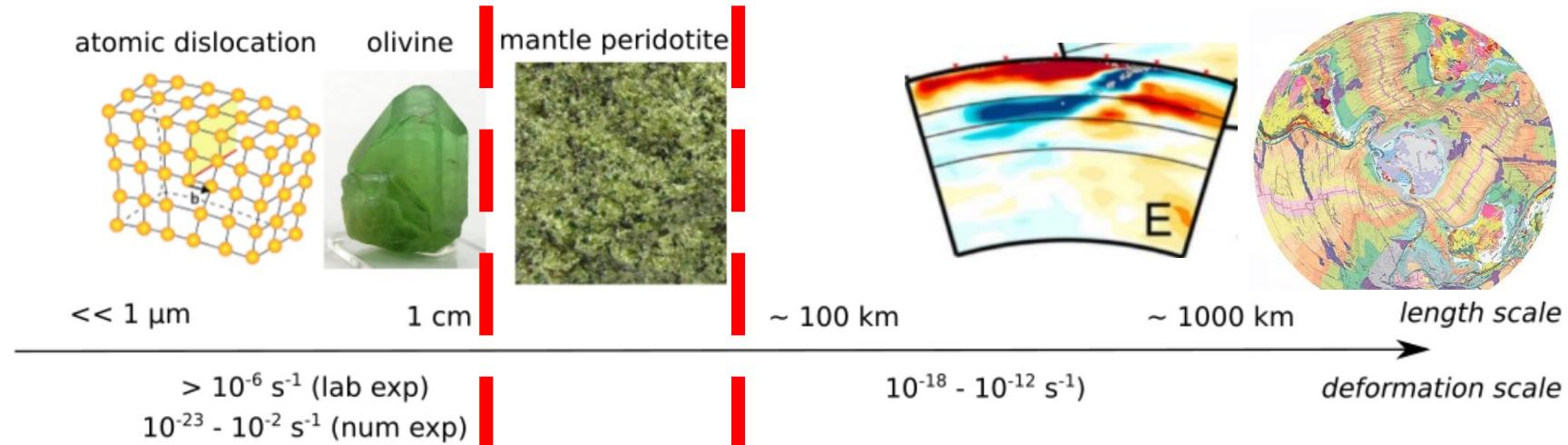
**PREDICTIONS  
SYNTETICS**

**Geological and  
geophysical DATA**

**COMPARISON**

- inversion: what for ? a priori ?
- probabilistic input (uncertainties)
- **data can integrate a long history of mantle evolution**  
(e.g. anisotropy, thermal structure)

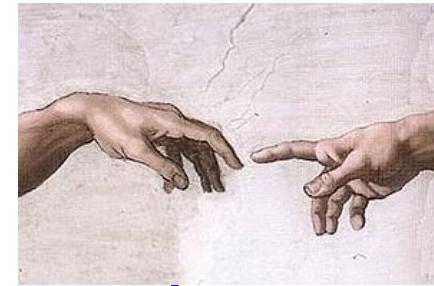
# Dynamical models : input and outputs relative to data



**Small-scale data**



**Geological and geophysical DATA**



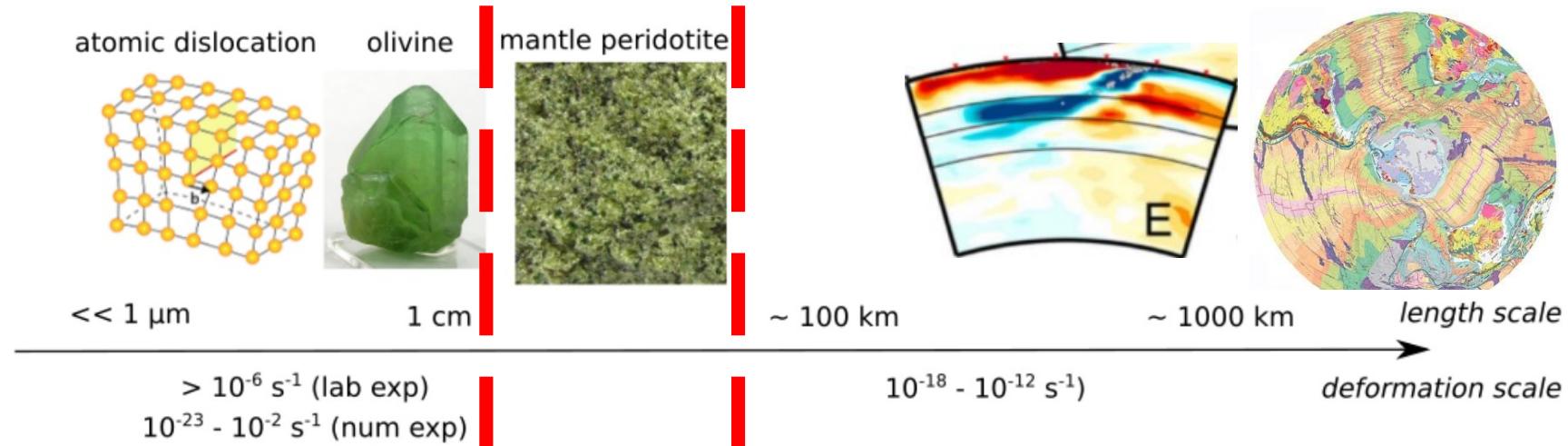
**Numerical models**

- dynamical evolution
- self-consistent feedbacks

**PREDICTIONS  
SYNTETICS**

- inversion: what for ? a priori ?
- probabilistic input (uncertainties)
- **data can integrate a long history of mantle evolution**  
(e.g. anisotropy, thermal structure)

# Dynamical models : input and outputs relative to data



Small-scale data

Geological and geophysical DATA

INPUT

effective  
parameterization

COMPARISON

Numerical models

- dynamical evolution
- self-consistent feedbacks

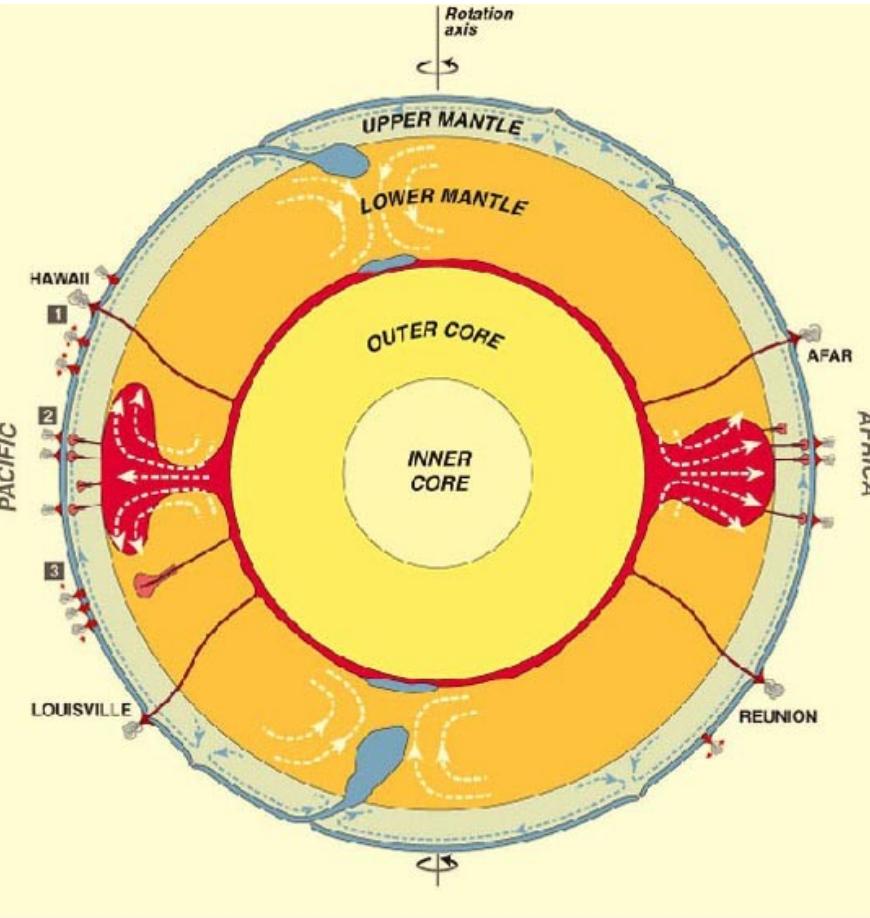
PREDICTIONS  
SYNTETICS

constraints on physical fields and their temporal evolution : viscosity, stress state, velocity, deformation rate

# Mantle geodynamics

- 1. Evidence for surface (plate) and deep (mantle) motions**  
*+ orders of magnitude*
- 2. Dynamic models to understand the mantle** (past & present)
- 3. Mantle and plate dynamics : modelling diversity and recipes**
- 4. Progress and perspectives**

# Mantle convection

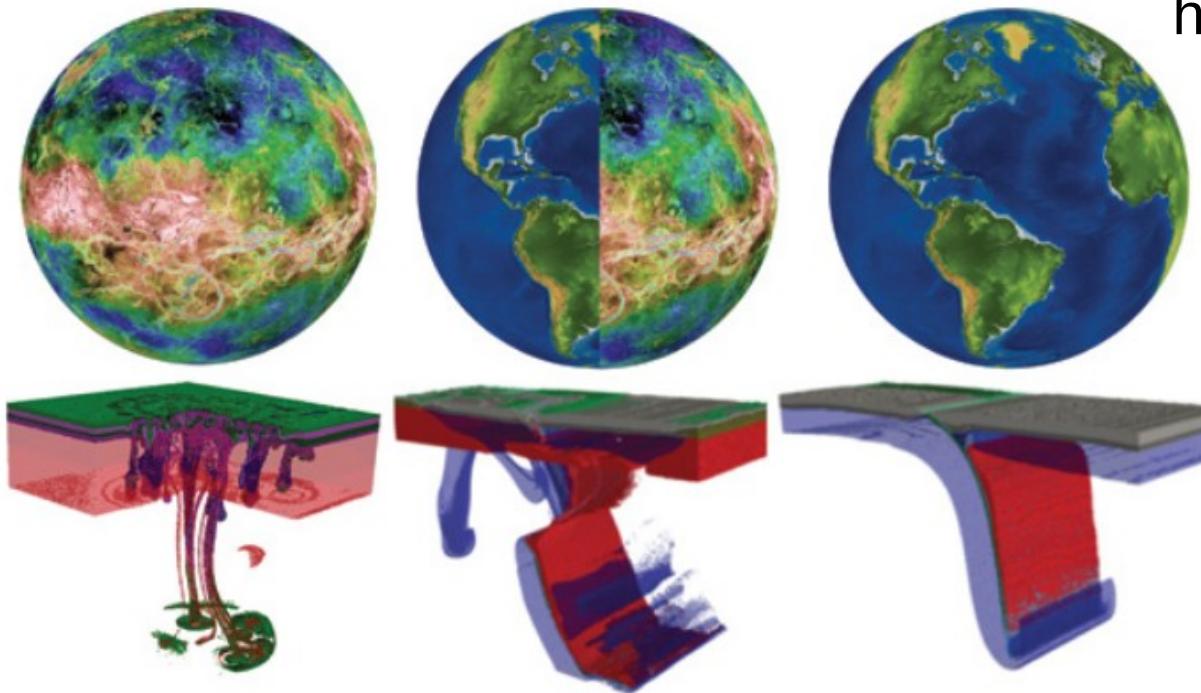


- The mantle convects, with **several** coexisting **length scales**
- Conv. models can exhibit self-consistent plate tectonics : one-sided subduction, subd. initiation, strike-slip faulting, continental break-up...
- Mantle convection is **time-dependent**, with possible “catastrophic events” : slab avalanching, drastic change in plate direction (Hawaiian bend), resurfacing of Venus
- mantle convection influences Earth secular cooling + heat flux at CMB (> core dynamics)



# A big challenge

How did the mantle convect in the **hot early Earth** ?



Squishy-lid tectonics

Transitional tectonics

Modern-style plate tectonics

Gerya 2019

- higher temperature
  - > lower viscosity
  - > higher Ra number
  - > more plumes
  - > Venus-like ?
- > faster microplates ?
- > weak slabs ?
- > ++ partial melt
- > **plutonic-squishy-lid ?**

Lourenço+ G<sup>3</sup> 2020

# Future challenges

- what happens in the **outer zone / transition zone** above 1800 km ?  
water, melt, oc.crust ?
  - what is the **rheology** of the lithospheric mantle ? of the lower mantle ?  
*1-D effective viscosity* of the mantle?
  - where/how are **chemical anomalies** still preserved after 4.5 Gyr of convection ?
  - how did a basal magma ocean transition to a solid convective mantle ?  
*Chemical signatures at D''* ?
  - when did “modern” plate tectonics start ?
  - coupling btn external Earth (**atmosphere/hydrosphere**) and solid Earth for water and carbon cycles ?  
for paleoclimate periodicity ?
  - convection of super-Earths ?
  - multiphysics models, scale transfers
- ....
- $$\text{disappointment} = \frac{\text{hope}}{\text{reality}}$$

