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Search in Rotated Array

(without duplicate)

arr = [3, 4, 5, 6, 7, 0, 1, 2]
 asc desc asc
 Pivot

- Find pivot in Rotated array
- Search in first half \Rightarrow single BS
 $(0, pivot)$
- otherwise, Search in Second half \Rightarrow
 $(pivot + 1, length - 1)$

Finding pivot

 Pivot
 [3, 4, 5, 6, 7, 0, 1, 2]
 Desc

*

\Rightarrow Case-1

```
if (arr[mid] > arr[mid+1]) {
    // We found pivot (ans = mid)
    return mid;
}
```

\Rightarrow Case-2

```
if (arr[mid] < arr[mid-1]) {
    // We found pivot (ans = mid-1)
    return mid-1;
}
```


Notes:

below cases (3 & 4) are for without duplicates

=> Case-3

if (arr[start] \geq arr[mid]) {

// In this case all elements from middle

// will be \leq start.

// Hence, we can ignore all these

// elements and look for peak in left

// side of arr.

end = mid - 1;

}

=> Case-4

if (arr[start] < arr[mid]) {

start = mid + 1; // ignore ^{all} elements of
left side from middle
and look for pivot in right
side of arr.

}

=> // Now we have found a peak element
so we can apply binary search in
rotated array

For Binary Search there are three cases:

=> Case 1:-

if (arr[pivot] == target) {

ans = pivot

}

$t > s$ lies in here
 \Rightarrow Case-2 $[s \text{ // // // // } p \text{ // // // } e]$

if (target > arr[start]) {

Search (s, Pivot-1)

start

}

$t < s$ lies in here
 \Rightarrow Case-3 $[s \text{ // // // } p \text{ // // // } e]$

if (target < arr[start]) {

Search (Pivot+1, end)

}

* With duplicates find ~~best~~ Pivot

We can use case 2 & case 3 of finding pivot

\Rightarrow Case-3

$[2, 2, 2, 2, 9]$

rotate twice

$s \quad m \quad e$
 $[2, 9, 2, 2, 2]$

Here

start, middle and end all are equal. So we can not use past cases (3, 4) for finding pivot


```
if (arr[mid] == arr[start] && arr[mid] == arr[end])
```

```
{
```

```
// if all are equal we skip the start  
and end and update by 1.
```

```
=> // but before updating check if start  
is pivot
```

```
if (start < end && arr[start] > arr[start+1])  
{
```

```
    return start; // ans
```

```
}
```

```
// if start is not pivot increment it by 1.  
start++;
```

```
=> // check if end is pivot
```

```
if (end > start && arr[end] < arr[end-1])  
{
```

```
    return end; // ans
```

```
}
```

```
// if end is not pivot decrement by 1.
```

```
end--;
```

```
}
```


=> case 4:

```
if (arr[start] < arr[mid] ||  
    arr[start] == arr[mid] &&  
    arr[mid] > arr[end]) {  
    start = mid + 1;  
}  
else {  
    end = mid - 1;  
}
```

* Let's code:

// without duplicates

```
FindPivot (int[] arr) {
```

```
    int start = 0;
```

```
    int end = arr.length - 1;
```

```
    while (start <= end) {
```

```
        int mid = start + (end - start) / 2;
```

```
        if (mid < end && arr[mid] > arr[mid + 1])  
        {
```

```
            return mid;
```

```
        }
```

```
        if (mid > start && arr[mid] < arr[mid - 1])  
        {
```

```
            return mid - 1;
```

```
        }
```



```
if (arr[start] >= arr[mid]) {
```

```
    end = mid - 1;
```

```
}
```

```
else {
```

```
    start = mid + 1;
```

```
}
```

```
return -1;
```

```
}
```

// With duplicates

```
FindPivotWithDuplicates (int[] arr) {
```

```
    int start = 0;
```

```
    int end = arr.length - 1;
```

```
    while (start <= end) {
```

```
        int mid = start + (end - start) / 2;
```

```
        if (mid < end && arr[mid] > arr[mid + 1])
```

```
        {
```

```
            return mid;
```

```
        }
```

```
        if (mid > start && arr[mid] < arr[mid - 1])
```

```
        {
```

```
            return mid - 1;
```

```
        }
```


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```
// if start, end and mid are equal  
if (arr[mid] == arr[start] &&  
    arr[mid] == arr[end])  
{
```

```
    // check if start is pivot
```

```
    if (start < end && arr[start] arr[start] > arr[start+1]  
        && arr[start] > arr[start-1])  
    {  
        return start;  
    }
```

```
    // if start is not pivot  
    start++;
```

```
    // check if end is pivot
```

```
    if (end > start && arr[end] < arr[end-1]  
        && arr[end] > arr[end+1])  
    {  
        return end;  
    }
```

```
    // if end is not pivot  
    end--;
```

```
    }
```

```
    else if (arr[start] < arr[end] &&  
        (arr[start] == arr[mid] &&  
        arr[mid] > arr[end])) {  
        start = mid + 1;
```

```
    } else {
```

```
        end = mid - 1;
```

```
    }  
    return -1;
```


Now, after Finding pivot apply binary search

```
Search (int[] arr, int target) {
```

```
    // if without duplicates
```

```
    int pivot = Find FindPivot(arr);
```

or

```
    // if duplicates are available
```

```
    int pivot = FindPivotWithDuplicates(arr);
```

```
    if (pivot == -1) {
```

```
        // if you did not find pivot means,  
        arr is not rotated.
```

```
        // so apply simple normal binary search
```

```
        return binarySearch(arr, target, 0,  
                               arr.length - 1);
```

```
    }
```

```
    if (arr[pivot] == target) {
```

```
        return pivot;
```

```
    }
```

```
    // target lie in left from pivot
```

```
    if (target < arr[0]) {
```

```
        return binarySearch(arr, target, 0, pivot - 1);
```

```
    } // target lie in right from pivot
```

```
    return binarySearch(arr, target, pivot + 1,  
                          arr.length - 1);
```

```
}
```


binarySearch (int[] arr, int target, int start,
int end)

{

~~int~~

while (start <= end)

{

int mid = start + (end - start) / 2;

if (target > arr[mid]) {

start = mid + 1;

}

else if (target < arr[mid]) {

end = mid - 1;

} else {

return mid;

}

}

return -1;

}