



**NATIONAL INSTITUTE OF TECHNOLOGY PATNA**  
**DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING**  
**MID SEMESTER EXAMINATION – October, 2022**  
**B. Tech (Computer Science and Engineering) III<sup>rd</sup> Semester**  
**CS34110 – Discrete Mathematics and Graph Theory**  
Full marks:30

Q.no	Question	Marks	CO	BL
1	Determine whether the following functions are one-to-one, onto, or one-to-one onto: N is natural number i. $f: N \rightarrow N$ $f(j) = j^2 + 2$ <i>one-to-one</i> ii. $f: N \rightarrow N$ $f(j) = j \pmod{3}$ <i>3</i>	06	CO1	Application
2	How many different relations are possible on a set of four elements? Determine whether the relation represented by the relation graph shown in Fig. 1 is reflexive, symmetric, antisymmetric and/or transitive.	06	CO1	Application
3	Find the number of bit strings of length 7 that do not have two consecutive 0s. Do not use the recurrence relation to solve the problem.	06	CO2	Analysis <i>34</i>
4	How many positive integers not exceeding 500 are divisible by 3 or 5?	06	CO2	Evaluation <i>233</i>
5	What is the minimum number of students, each of whom comes from one of the 50 states, who must be enrolled in a university to guarantee that there are at least 100 students who come from the same state?	06	CO2	Application <i>4951</i>



Fig. 1

CYB