## EE24BTECH11014 - Deepak Ahirwar

## **Question:**

For the Differential Equation  $\frac{dy}{dx} + \sin x = 0$ , verify that  $y = \cos x + C$  is a solution of the differential equation.

**Solution:** : We are given the first-order ordinary differential equation:

$$\frac{dy}{dx} + \sin x = 0 \tag{1}$$

This is a separable differential equation. We can rewrite it as:

$$\frac{dy}{dx} = -\sin x\tag{2}$$

Now, we integrate both sides with respect to x:

$$\int \frac{dy}{dx} dx = \int -\sin x \, dx \tag{3}$$

$$\int dy = -\int \sin x \, dx \tag{4}$$

$$\implies y = \cos x + C \tag{5}$$

where C is the constant of integration.

Therefore, the general solution to the given differential equation is:

$$y(x) = \cos x + C \tag{6}$$

## **Computational Solution:**

Using classical defination of derivative we get,

$$f'(x) = \frac{f(x+h) - f(x)}{h} \tag{7}$$

$$\implies f(x+h) = f(x) + f'(x)h \tag{8}$$

For y = f(x), we can get the points of the required graph by iterating the equation obtained in (8) where values of x increases in each iteration by h and obtaining the y-coordinate of it.

For,

$$x_0 = 0 (9)$$

$$y_0 = 1 \tag{10}$$

$$h = 0.001 \tag{11}$$

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Using Euler Method, we get difference equation,

$$y_{n+1} = y_n + h \frac{dy}{dx} \Big|_{(x_n, y_n)}$$
 (12)

$$x_{n+1} = x_n + h \tag{13}$$

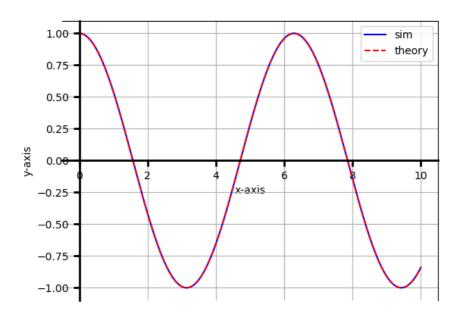


Fig. 0: Verification