

Solutions To Question Bank <Unit-II>

Ques1. Show whether the following grammar is ambiguous or not. Also construct the parse tree using LMD & RMD.

$$E \rightarrow E + E \mid E * E \mid (E) \mid id$$

input string $id_1 + id_2 * id_3$ $\langle *, id_1, id_2 \neq id_3 \text{ are different occurrences of same terminal symbol } id \rangle$

Ambiguity: A grammar G is

said to be ambiguous if there exist a string $X \in L(G)$

such that to generate string X using productions of G there exist more than one left most derivations or more than one right most derivations or more than one parse trees for X .

LMD1 for $id_1 + id_2 * id_3$ LMD2

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow id_1 + E \\ &\Rightarrow id_1 + E * E \\ &\Rightarrow id_1 + id_2 * E \\ &\Rightarrow id_1 + id_2 * id_3 \end{aligned}$$

$$\begin{aligned} E &\Rightarrow E * E \\ &\Rightarrow E + E * E \\ &\Rightarrow id_1 + E * E \\ &\Rightarrow id_1 + id_2 * E \\ &\Rightarrow id_1 + id_2 * id_3 \end{aligned}$$

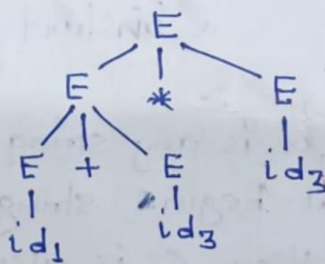
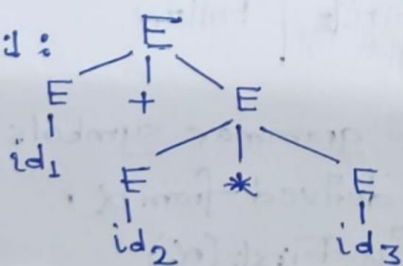
RMD1

$$\begin{aligned} E &\Rightarrow E + E \\ &\Rightarrow E + ~~id_2~~ E * E \\ &\Rightarrow E + E * id_3 \\ &\Rightarrow E + id_2 * id_3 \\ &\Rightarrow id_1 + id_2 * id_3 \end{aligned}$$

RMD2

$$\begin{aligned} E &\Rightarrow E * E \\ &\Rightarrow E * id_3 \\ &\Rightarrow E + E * id_3 \\ &\Rightarrow E + id_2 * id_3 \\ &\Rightarrow id_1 + id_2 * id_3 \end{aligned}$$

Parse Tree1:



Hence the Grammar is ambiguous.

Ques 2: $S \rightarrow iEtss' \mid a$ $\text{First}(S) = \{i, a\}$
 $S' \rightarrow eS \mid E$ $\text{First}(S') = \{e, b\}$
 $E \rightarrow b$ $\text{First}(E) = \{b\}$

↓ LL(1) parsing table

	i	t	a	e	b
S	$S \rightarrow iEtss'$		$S \rightarrow a$		
S'				$S' \rightarrow eS$	$S' \rightarrow E$
E					$E \rightarrow b$

Since each entry in the table has a unique production.

The given grammar is LL(1)

Q3: $S \rightarrow AaBb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

$\text{Follow}(A) = \{a\}$ $\text{Follow}(S) = \{\$ \}$

$\text{Follow}(B) = \{a, b\}$

Remember $A \rightarrow \cdot \epsilon$ is same as $A \rightarrow \epsilon \cdot$ is same as $A \rightarrow \cdot$

State with augmented production

"0"
 $S' \rightarrow \cdot S$
 $S \rightarrow \cdot AaBb$
 $S \rightarrow \cdot BbBa$
 $A \rightarrow \cdot$
 $B \rightarrow \cdot$

Let's number the productions

1. $S \rightarrow AaBb$

2. $S \rightarrow BbBa$

3. $A \rightarrow \epsilon$

4. $B \rightarrow \epsilon$

In the parsing table for state 0 we need to put r3 under Follow(A) and r4 under Follow(B)

	a	b	\$	S	A	B
0	r3/r4	r3				

→ Here we are getting reduce/reduce conflict
 So grammar is not SLR(1)

Q4:

$S \rightarrow \underline{A}CB \mid C\underline{b}B \mid B\underline{a}$

$A \rightarrow \underline{d}a \mid B\underline{C}$

$B \rightarrow g \mid \epsilon$

$C \rightarrow \underline{h} \mid \epsilon$

$\text{First}(\)$

$\{d, g, h, b, a, \epsilon\}$

$\{d, g, h, \epsilon\}$

$\{g, \epsilon\}$

$\{h, \epsilon\}$

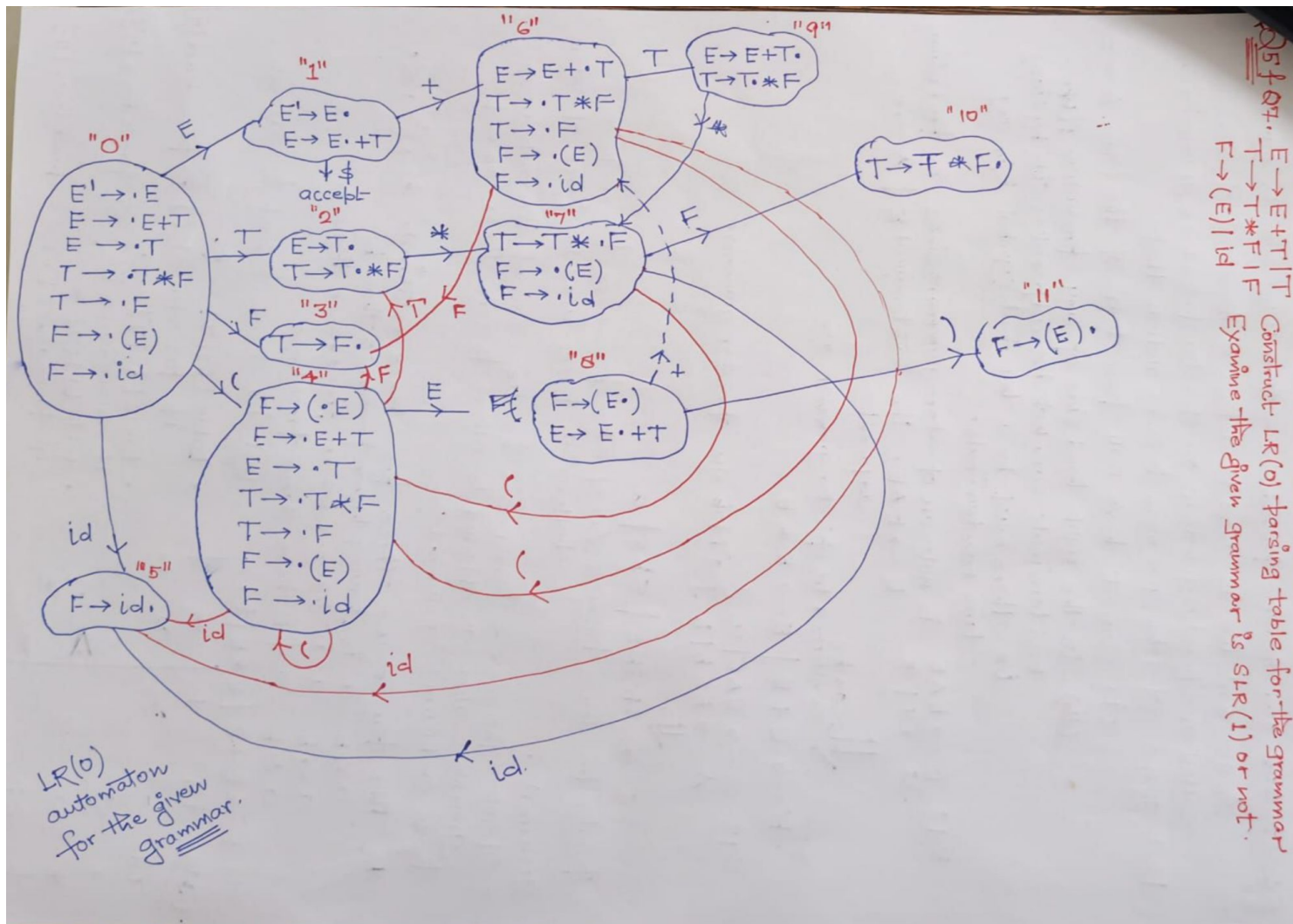
$\text{Follow}(\)$

$\{\$ \}$

$\{h, g, \$ \}$

$\{\$, a, h, g\}$

$\{g, \$, b, h\}$



SLR(1) Parsing Table

state	id	ACTION						GOTO		
		+	*	()	\$		E	T	F
0	S5			S4				1	2	3
1		S6				Acc				
2		r2	S7		r2	r2				
3		r4	r4		r4	r4				
4	S5			S4				8	2	3
5		r6	r6		r6	r6				
6	S5			S4					9	3
7	S5			S4						10
8		S6			S11					
9		r1	S7		r1	r1				
10		r3	r3		r3	r3				
11		r5	r5		r5	r5				

Productions with Number

1. $E \rightarrow E+T$
2. $E \rightarrow T$
3. $T \rightarrow T * F$
4. $T \rightarrow F$
5. $F \rightarrow (E)$
6. $F \rightarrow id$

⇒ Since there is no conflict

⇒ Grammar is SLR(1).

$FOLLOW(E) = \{ \$, +,) \}$

S_i : means shift and stack state i

r_j : reduce by the production numbered j .

blank entries refer to errors.

* To construct the LR(0) Parsing Table.

In the action part under each terminal we need to place the reduce move.

for the states having production with \cdot (dot) at the end of rhs of a production

eg: Consider state 11 contains production $F \rightarrow (E) \cdot$ Number 15
 state 9 " " " $E \rightarrow E+T \cdot$ number 1

State	id	+	*	()	\$	E	T	F
9	r1	r1	S7/r1	r1	r1	r1	-	-	-
11	r5	r5	r5	r5	r5	r5	-	-	-
5	r6	r6	r6	r6	r6	r6	-	-	-
3	r4	r4	r4	r4	r4	r4	-	-	-

Complete LR(0) parsing table by your own.

Q6: Operator Precedence Parser :

- A grammar that is used to define mathematical operators is called an operator grammar with restrictions.

1. Operator grammar can not have null productions of the form $A \rightarrow \epsilon$

2. In the right hand side of the production rules ; Two non terminals can not be adjacent (side by side)

eg: $E \rightarrow EAE$
 $A \rightarrow + | *$ } \rightarrow This is not an operator grammar since in the production $E \rightarrow EAE$, The non terminals E & A are adjacent to each other.

\Downarrow can be converted to operator grammar as

$$E \rightarrow E + E \mid E * E$$

eg: $S \rightarrow SAS \mid a$
 $A \rightarrow bSb \mid b$ } \rightarrow Not an operator grammar as in $S \rightarrow SAS$ S & A are side by side (adjacent to each other)

\Downarrow operator grammar

$$S \rightarrow sbSbS \mid sbS \mid a.$$

- An operator precedence parser is a bottom up parser used to parse operator grammars.
- Operator precedence parser is capable of parsing some of the ambiguous grammar.

- $a \succ b \Rightarrow a$ is having higher precedence than b

- $a \prec b \Rightarrow a$ is having lower precedence than b

- Uses operator relation table.

eg: $E \rightarrow E + E \mid E * E \mid id$

- Rows & columns have terminals

Rules: id has highest precedence

$$table[i][j] = \succ$$

if $precedence(i) > precedence(j)$

$$table[i][j] = \prec$$

if $precedence(i) < precedence(j)$

table	id	+	*	\$
id	-	\succ	\succ	\succ
+	\prec	\succ	\prec	\succ
*	\prec	\succ	\succ	\succ
\$	\prec	\prec	\prec	-

* if any operator is left associative

eg: consider $+$ is left-associative

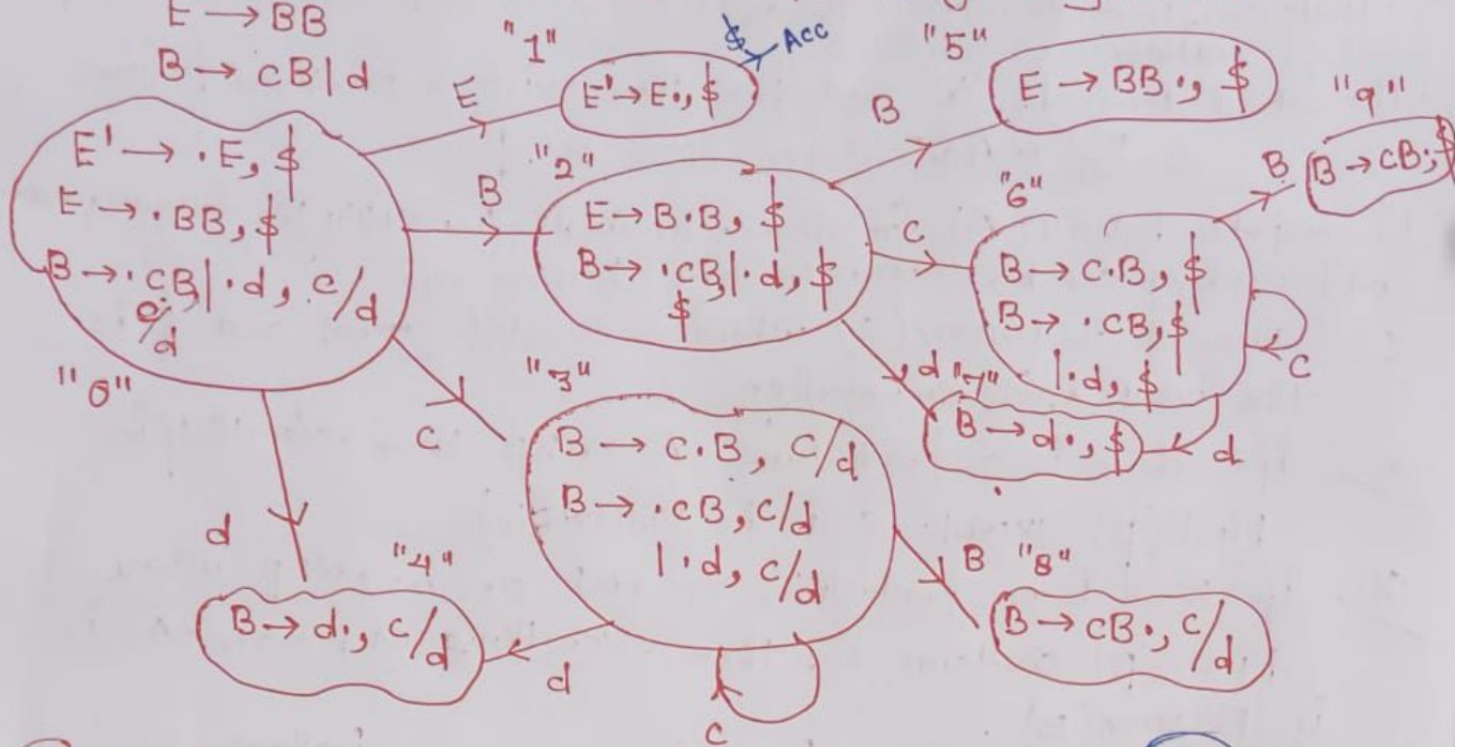
$$table[+][+] = \succ \text{ since left-side}$$

$+$ is having higher precedence than right side $+$

Q9 Construct the CLR(1) parser for the given grammar

S → AB
A → aA | b

$E \rightarrow BB$
 $B \rightarrow cB \mid d$



Construction of CLR(1) Parsing Table.

(Q9)

State	ACTION			GOTO	
	c	d	\$	E	B
0	s3	s4		1	2
1			Accept		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2			
9			r2		

Q10: $S \rightarrow AB|d$
 $A \rightarrow aA|b$
 $B \rightarrow bB|c$

$\text{First}(B) = \{b, c\}$

$\text{Follow}(S) = \{\$ \}$

$\text{First}(A) = \{a, b\}$

$\text{Follow}(A)$

$\text{First}(S) = \{a, b, d\}$

$= \text{First}(B) \cup \text{Follow}(A)$

$= \{b, c\}$

$\text{Follow}(B) = \text{Follow}(S)$

$\cup \text{Follow}(B)$

$= \{\$ \}$

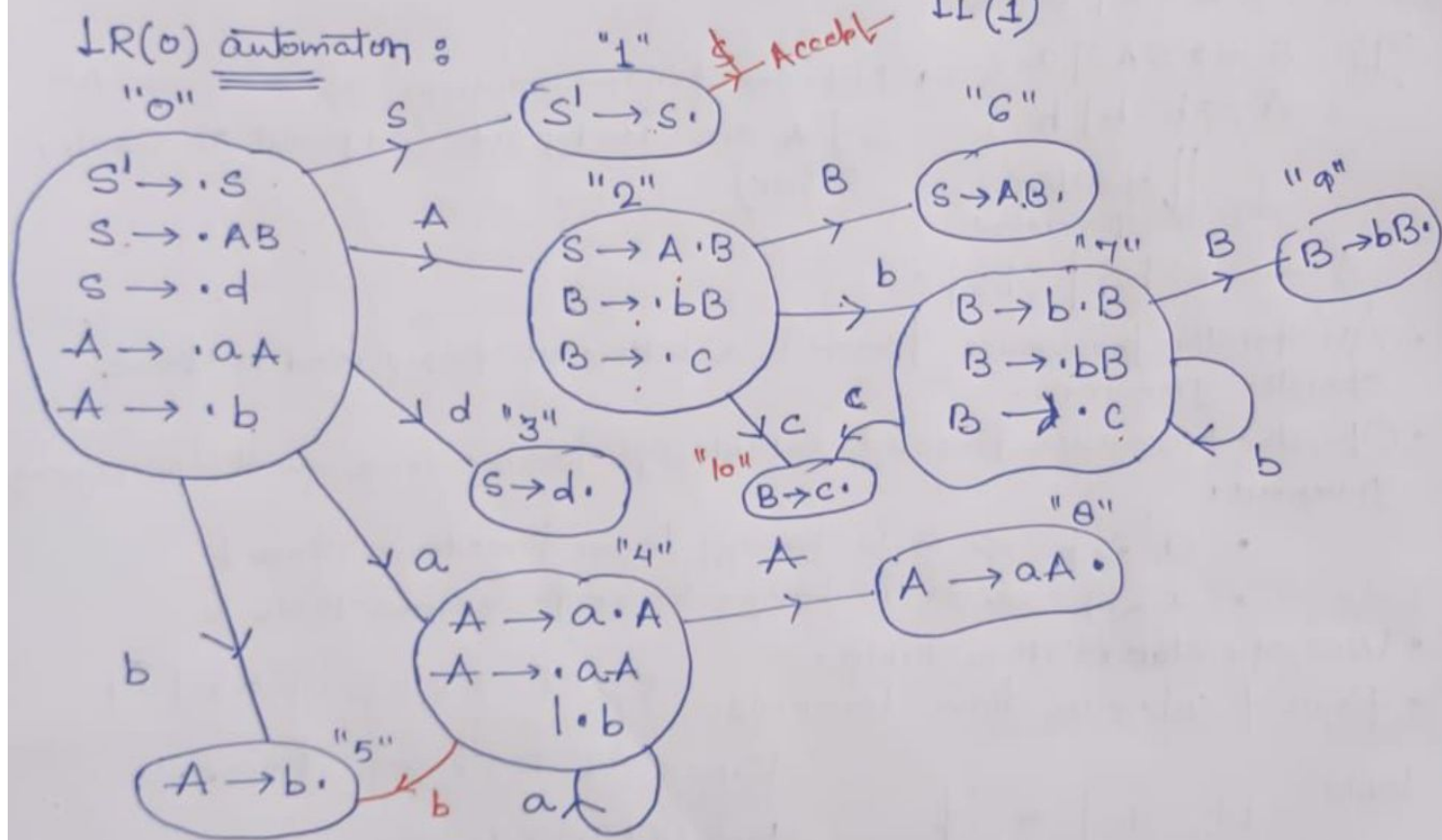
Each entry has single production \Rightarrow Grammar is

LL(1)

LL(1) Parsing Table

	a	b	c	d	\$
S	$S \rightarrow AB$	$S \rightarrow AB$		$S \rightarrow d$	
A	$A \rightarrow aA$	$A \rightarrow b$			
B		$B \rightarrow bB$	$B \rightarrow c$		

LR(0) automaton:



Consider, the states having final items

State no. (5) only one production with final item,

(1) \neq (3) \neq (6) \neq no shift,

(9) \neq (8) \neq (10)

No conflict - Grammar is LR(0)

Q12: Explain translation rule for expression 2+5*4.

Grammar to generate given string

$$E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow \text{num}$$

Translation Rules : By giving the attribute equations and order of evaluation.

$$E \rightarrow E + T \quad \{ E.\text{value} = E.\text{value} + T.\text{value} \}$$

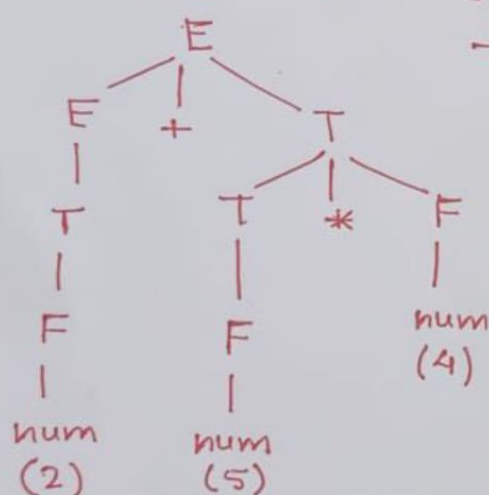
$$E \rightarrow T \quad \{ E.\text{value} = T.\text{value} \}$$

$$T \rightarrow T * F \quad \{ T.\text{value} = T.\text{value} * F.\text{value} \}$$

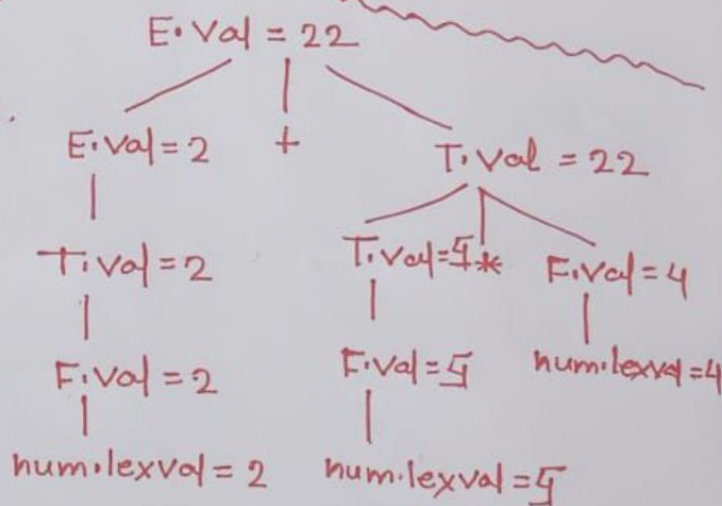
$$T \rightarrow F \quad \{ T.\text{value} = F.\text{value} \}$$

$$F \rightarrow \text{num} \quad \{ F.\text{value} = \text{num}.\text{lexicalvalue} \}$$

Parse Tree for the string 2+5*4



Annotated
Parse tree.



Evaluation with bottom up parsing stack : Use of value stack.

$$E \rightarrow E + T \quad \{ \text{stack}[\text{top}-2].\text{val} = \text{stack}[\text{top}-2].\text{val} + \text{stack}[\text{top}].\text{val}; \text{top} = \text{top}-2; \}$$

$$E \rightarrow T$$

$$T \rightarrow T * F \quad \{ \text{stack}[\text{top}-2].\text{val} = \text{stack}[\text{top}-2].\text{val} * \text{stack}[\text{top}].\text{val}; \text{top} = \text{top}-2; \}$$

$$T \rightarrow F$$

$$F \rightarrow (E) \quad \{ \text{stack}[\text{top}-2].\text{val} = \text{stack}[\text{top}-1].\text{val}; \text{top} = \text{top}-2; \}$$

$$F \rightarrow \text{num}$$