Hycon2 Benchmark: Power Network System

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Abstract

As a benchmark exercise for testing software and methods developed in Hycon2 for decentralized and distributed control, we address the problem of designing the Automatic Generation Control (AGC) layer in power network systems. In particular, we present three different scenarios and discuss performance levels that can be reached using Centralized Model Predictive Control (MPC). These results can be used as a milestone for comparing the performance of alternative control schemes. Matlab software for simulating the scenarios is also provided in an accompanying file.

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1 Introduction

An example of a real application that can benefit of decentralized and distributed control schemes is the regulation of a Power Network System (PNS). We consider a PNS as composed by several power generation areas coupled through tie-lines [Saa02]. The aim is to design the Automatic Generation Control (AGC) layer for frequency control with the goal of:

- keeping the frequency approximately at the nominal value;
- controlling the tie-line powers in order to reduce power exchanges between areas. In the asymptotic regime each area should compensate for local load steps and produce the required power.

We consider thermal power stations with single-stage turbines. The dynamics of an area equipped with primary control and linearized around equilibrium value for all variables can be described by the following continuous-time LTI model [Saa02]

$$\Sigma_{[i]}^C: \quad \dot{x}_{[i]} = A_{ii} x_{[i]} + B_i u_{[i]} + L_i \Delta P_{L_i} + \sum_{j \in \mathcal{N}_i} A_{ij} x_{[j]}$$
 (1)

where $x_{[i]} = (\Delta \theta_i, \ \Delta \omega_i, \ \Delta P_{m_i}, \ \Delta P_{v_i})$ is the state, $u_{[i]} = \Delta P_{ref_i}$ is the control input of each area, ΔP_L is the local power load and \mathcal{N}_i is the sets of neighboring areas, i.e. areas directly connected to $\Sigma_{[i]}^C$ through tie-lines. The matrices of system (1) are defined as

For the meaning of constants as well as some typical parameter values we defer the reader to Table 1.

We note that model (1) is input decoupled since both ΔP_{ref_i} and ΔP_{L_i} act only on subsystem $\Sigma^{C}_{[i]}$. Moreover, subsystems $\Sigma^{C}_{[i]}$ are parameter dependent since the local dynamics depends on the quantities $-\frac{\sum_{j\in\mathcal{N}_i}P_{ij}}{2H_i}$.

In the following we introduce three scenarios corresponding to different interconnection topologies of generation areas. The model parameters and constraints on $\Delta\theta_i$ and on ΔP_{ref_i} for systems in all Scenarios are given in Table 2. We highlight that all parameter values are within the range of those used in Chapter 12 of [Saa02]. We define M as the number of areas in the power network. For each scenario, discrete-time models $\Sigma_{[i]}$ with $T_s=1$ sec sampling time are obtained from $\Sigma_{[i]}^C$ using two alternative discretization schemes.

- Exact discretization of the overall system (acronym D);
- Discretization system-by-system, i.e. exact discretization for each area treating $u_{[i]}$, ΔP_{L_i} and $x_{[j]}$, $j \in \mathcal{N}_i$ as exogenous inputs (acronym Dss).

In particular, we note that Dss preserves the input-decoupled structure of $\Sigma_{[i]}^C$ while D does not.

$\Delta \theta_i$	Deviation of the angular displacement of the rotor with respect to the stationary reference axis on the stator					
$\Delta\omega_i$	Speed deviation of rotating mass from nominal value					
ΔP_{m_i}	Deviation of the mechanical power from nominal value (p.u.)					
ΔP_{v_i}	Deviation of the steam valve position from nominal value (p.u.)					
ΔP_{ref_i}	Deviation of the reference set power from nominal value (p.u.)					
$\begin{array}{c} \Delta P_{ref_i} \\ \Delta P_{L_i} \end{array}$	Deviation of the nonfrequency-sensitive load change from nominal value (p.u.)					
H_i	Inertia constant defined as $H_i = \frac{\text{kinetic energy at rated speed}}{\text{machine rating}}$ (typically values in range [1 – 10] sec)					
R_i	Speed regulation					
D_i	Defined as percent change in load change in frequency					
T_{t_i}	Prime mover time constant (typically values in range $[0.2-2]$ sec)					
T_{g_i}	Governor time constant (typically values in range $[0.1 - 0.6]$ sec)					
P_{ij}	Slope of the power angle curve at the initial operating angle between area i and area j					

Table 1: Variables of a generation area with typical value ranges [Saa02]. (p.u.) stands for "per unit".

	Area 1	Area 2	Area 3	Area 4	Area 5
H_i	12	10	8	8	10
R_i	0.05	0.0625	0.08	0.08	0.05
D_i	0.7	0.9	0.9	0.7	0.86
T_{t_i}	0.65	0.4	0.3	0.6	0.8
T_{g_i}	0.1	0.1	0.1	0.1	0.15

		Area 1	Area 2	Area 3	Area 4	Area 5
Ī	$\Delta \theta_i$	$ x_{[1,1]} _{\infty} \le 0.1$	$ x_{[2,1]} _{\infty} \le 0.1$	$ x_{[3,1]} _{\infty} \le 0.1$	$ x_{[4,1]} _{\infty} \le 0.1$	$ x_{[5,1]} _{\infty} \le 0.1$
ſ	ΔP_{ref_i}	$ u_{[1]} _{\infty} \le 0.5$	$ u_{[2]} _{\infty} \le 0.65$	$ u_{[3]} _{\infty} \le 0.65$	$ u_{[4]} _{\infty} \le 0.55$	$ u_{[5]} _{\infty} \le 0.5$

$$P_{12} = 4$$
 $P_{23} = 2$ $P_{34} = 2$ $P_{45} = 3$ $P_{25} = 3$

Table 2: Model parameters and constraints for systems $\Sigma_{[i]}, i \in 1, \dots, 5$.

1.1 Scenario 1

We consider four areas interconnected as in Figure 1. We will simulate Scenario 1 using the load

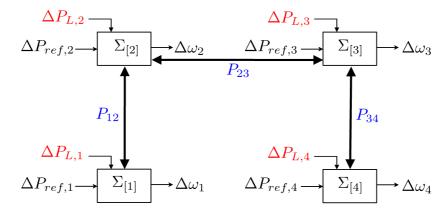


Figure 1: Power network system of Scenario 1

steps specified in Table 3.

Step time	Area i	ΔP_{L_i}
5	1	+0.15
15	2	-0.15
20	3	+0.12
40	3	-0.12
40	4	+0.28

Table 3: Load of power ΔP_{L_i} (p.u.) for simulation in Scenario 1. $+\Delta P_{L_i}$ means a step of required power, hence a decrease of the frequency deviation $\Delta \omega_i$ and therefore an increase of the power reference ΔP_{ref_i} .

1.2 Scenario 2

We consider the power network proposed in Scenario 1 and add a fifth area connected as in Figure 2. We will simulate Scenario 2 using the load steps specified in Table 4.

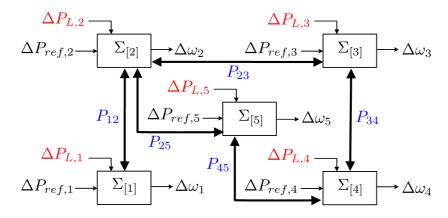


Figure 2: Power network system of Scenario 2

Step time	Area i	ΔP_{L_i}
5	1	+0.10
15	2	-0.16
20	1	-0.22
20	2	+0.12
20	3	-0.10
30	3	+0.10
40	4	+0.08
40	5	-0.10

Table 4: Load of power ΔP_{L_i} (p.u.) for simulation in Scenario 2. $+\Delta P_{L_i}$ means a step of required power, hence a decrease of the frequency deviation $\Delta \omega_i$ and therefore an increase of the power reference ΔP_{ref_i} .

1.3 Scenario 3

We consider the power network described in Scenario 2 and disconnect the area 4, hence obtaining the areas connected as in Figure 3. We will simulate Scenario 3 using load steps specified in Table 5.

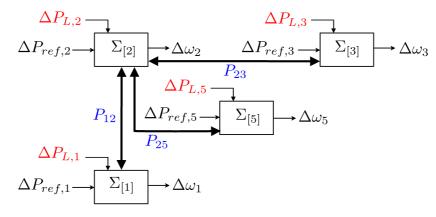


Figure 3: Power network system of Scenario 3

Step time	Area i	ΔP_{L_i}
5	1	+0.12
15	2	-0.15
20	5	+0.20
40	2	+0.15
40	3	+0.13
40	5	-0.20

Table 5: Load of power ΔP_{L_i} (p.u.) for simulation in Scenario 3. $+\Delta P_{L_i}$ means a step of required power, hence a decrease of the frequency deviation $\Delta \omega_i$ and therefore an increase of the power reference ΔP_{ref_i} .

2 Design of the AGC layer for a power network using MPC

The goal of the Benchmark is to design the AGC layer for the scenarios introduced in Section 1. Different control schemes will be compared with the centralized MPC scheme described next. For a given Scenario, at time t we solve the centralized optimization problem

$$\mathbb{P}^{N}(x(t)): \tag{3a}$$

$$\min_{u(t:t+N-1)} \sum_{k=t}^{t+N-1} (||x(k) - x^{O}||_{Q} + ||u(k) - u^{O}||_{R}) + ||x(t+N) - x^{O}||_{S})$$
(3b)

$$x(k+1) = Ax(k) + Bu(k) + L\Delta P_L(t)$$
 $k \in 0: N-1$ (3c)

$$x(k) \in \mathbb{X}$$
 $k \in 0: N-1$ (3d)

$$u(k) \in \mathbb{U}$$
 $k \in 0: N-1$ (3e)

$$x(N) \in \mathbb{X}_f$$
 (3f)

and then apply $\Delta P_{ref} = u(0)$. We note that the cost function depend upon x^O and u^O that are defined as $x_{[i]}^O = (0, 0, \Delta P_{L_i}, \Delta P_{L_i})$ and $u_{[i]}^O = \Delta P_{L_i}$. The constraints \mathbb{X} and \mathbb{U} in (3d) and (3e) are obtained from constraints listed in Table 2. In the cost function (3b) we set N = 15, $Q = \operatorname{diag}(Q_1, \ldots, Q_M)$ and $R = \operatorname{diag}(R_1, \ldots, R_M)$, where

$$Q_i = \begin{bmatrix} 500 & 0 & 0 & 0 \\ 0 & 0.01 & 0 & 0 \\ 0 & 0 & 0.01 & 0 \\ 0 & 0 & 0 & 10 \end{bmatrix} \text{ and } R_i = 10.$$

Weights Q_i and R_i have been chosen in order to penalize the angular displacement $\Delta \theta_i$ and to penalize slow reactions to power load steps. Since the power transfer between areas i and j is given by

$$\Delta P_{tie_{ij}}(k) = P_{ij}(\Delta \theta_i(k) - \Delta \theta_j(k)) \tag{4}$$

the first requirement also penalizes huge power transfers.

In order to guarantee the stability of the closed loop system, we design the matrix S and the terminal constraint set X_f in three different ways.

- S is full (MPCfull): we compute the symmetric positive-definite matrix S and the static state-feedback auxiliary control law $K_{aux}x$, by maximizing the volume of the ellipsoid described by S inside the state constraints while fulfilling the matrix inequality $(A+BK_{aux})'S(A+BK_{aux}) S \leq -Q K'_{aux}RK_{aux}$.
- S is block diagonal (MPCdiag): we compute the decentralized symmetric positive-definite matrix S and the decentralized static state-feedback auxiliary control law $K_{aux}x$, $K_{aux} = \operatorname{diag}(K_1, \ldots, K_M)$ by maximizing the volume of the ellipsoid described by S inside the state constraints while fulfilling the matrix inequality $(A + BK_{aux})'S(A + BK_{aux}) S \leq -Q K'_{aux}RK_{aux}$.
- Zero terminal constraint (MPCzero): we set S=0 and $\mathbb{X}_f=x^O$.

2.1 Performance criteria

We propose the following performance criteria for evaluating different control schemes.

• η -criterion

$$\eta = \frac{1}{T_{sim}} \sum_{k=0}^{T_{sim}-1} \sum_{i=1}^{M} (||x_{[i]}(k) - x_{[i]}^{O}(k)||_{Q_i} + ||u_{[i]}(k) - u_{[i]}^{O}(k)||_{R_i})$$
 (5)

where T_{sim} is the time of the simulation. From (5), η is a weighted average of the error between the real state and the equilibrium state and between the real input and the equilibrium input.

• Φ-criterion

$$\Phi = \frac{1}{T_{sim}} \sum_{k=0}^{T_{sim}-1} \sum_{i=1}^{M} \sum_{j \in \mathcal{N}_i} |\Delta P_{tie_{ij}}(k)| T_s$$
 (6)

where T_{sim} is the time of the simulation and $\Delta P_{tie_{ij}}$ is the power transfer between areas i and j defined in (4). This criterion gives the average power transferred between areas. In particular, if the η -criterion is equal for two regulators, the best controller is the one that has the lower value of Φ .

3 Control Experiments

We applied the centralized MPC schemes introduced in the previous section to scenarios 1, 2 and 3. Furthermore, for each scenario we discretized the continuos system with both discretization schemes D and Dss. At time t we solve the optimization problem (3) and then apply the control action to the continuos-time system, keeping the value constant between time t and t+1. If at time t the power load increases or decreases, we assume the controller can use this information at time t. This means at time t the controller knows exactly the value of ΔP_L hence can use it. We highlight that violation of this assumption can impact considerably on the index η . In all experiments we use $T_{sim} = 100$. In Table 6 and 7 the values of the performance parameters η and Φ , respectively, are reported for each control experiment.

	Scenario 1		Scenario 2		Scenario 3	
	D	Dss	D	Dss	D	Dss
MPCfull	0.0249	0.0249	0.0346	0.0347	0.0510	0.0511
MPCdiag	0.0249	0.0249	0.0346	0.0347	0.0510	0.0511
MPCzero	0.0249	0.0249	0.0346	0.0347	0.0510	0.0511

Table 6: Values of the performance parameter η using different centralized MPC schemes for the AGC layer.

	Scenario 1		Scenario 2		Scenario 3	
	D	Dss	D	Dss	D	Dss
MPCfull	0.0030	0.0029	0.0063	0.0060	0.0060	0.0058
MPCdiag	0.0030	0.0029	0.0063	0.0061	0.0060	0.0058
MPCzero	0.0030	0.0028	0.0063	0.0059	0.0059	0.0058

Table 7: Values of the performance parameter Φ using different centralized MPC schemes for the AGC layer.

4 Supporting Matlab files

We provide the Matlab files for the parameters in Table 2 (parameters.m) and for all control experiments. Each file .mat of the control experiments contains

- the matrices of the continuos linear system (Ac, Bc, Cc, Dc, Lc);
- the matrices of the discretized linear system (A, B, C, D, L, Ts);
- parameters of the controller (Q, R, S, N, xO, uO);
- parameters of the control experiment Tsim and deltaPload, where deltaPload corresponds to ΔP_L ;
- the results of the control experiment x, deltaPref, η and Φ , where deltaPref corresponds to ΔP_{ref} .

For each Scenario we included also a Simulink model. In particular, one can load the file .mat of a control experiment and simulate the power network system given the power load steps and the power reference computed through centralized MPC.

4.1 Example of simulation

In the following we illustrate how to use the files .mat and the Simulink models through an example. Assume we want to simulate Scenario 2 using the discretization Dss and centralized MPC with zero terminal constraint (MPCzero). In the folder of each scenario there are six folders labeled as [discretization scheme]-[mpc type]. Hence, we have to use files in folder Dss_MPCzero. In this folder we can find the data of the required control experiment as dataSim.mat. The previous operations are performed with the Matlab commands:

```
cd scenario2
load Dss_MPCzero/dataSim
```

We can simulate different scenarios using the Simulink models present in the folder of each scenario. For Scenario 2 we then open the file *simulatorPNS_AGC_2.mdl*. Start a simulation from Simulink will produce the results of the control experiments. These steps are performed with the Matlab commands:

```
open('simulatorPNS_AGC_2')
sim('simulatorPNS_AGC_2')
```

5 Benchmark exercise

The aim is to design decentralized/distributed controllers for the scenarios described in Section 1. Depending on the control technique adopted either D or Dss discretization schemes can be chosen.

The first goal of a distributed AGC layer is to have performance in terms of η similar to centralized MPC. Matching also the values of Φ can be seen as a secondary objective.

Alternative control schemes will be also ranked according to the degree of decentralization of the design process. Ideally, the controller of each area should be designed independently of the others and using information from a limited number of other areas. Decentralized design is important in PNS because if an area needs to be isolated or a new area is plugged into the network one would like to avoid the redesign the whole AGC layer and rather retune just a limited number of local controllers in order to guarantee asymptotic stability and constraints satisfaction for the whole network.

References

[Saa02] H. Saadat. *Power System Analysis*. McGraw-Hill Series in Electrical and Computer Engineering, New York. NY, USA, 2 edition, 2002.