HPIPM reference guide

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Chapter 1

Introduction

HPIPM - High-Performance Interior Point Method.

HPIPM is a library providing a collection of quadratic programs (QP) and routines to manage them. Aim of the library is to provide both stand-alone IPM solvers for the QPs and the building blocks for more complex optimization algorithms.

At the moment, three QPs types are provided: dense QPs, optimal control problem (OCP) QPs, and tree-structured OCP QPs. These QPs are defined using C structures. HPIPM provides routines to manage the QPs, and to convert between them.

HPIPM is written entirely in C, and it builds on top of BLASFEO [**?**], that provides high-performance implementations of basic linear algebra (LA) routines, optimized for matrices of moderate size (as common in embedded optimization).

Chapter 2

Dense QP

Chapter 3

OCP QP

The OCP QP is a QP in the form

$$
\begin{aligned}
\min_{x,u,s} \quad & \sum_{n=0}^{N} \frac{1}{2} \begin{bmatrix} u_n \\ x_n \\ 1 \end{bmatrix}^T \begin{bmatrix} R_n & S_n & r_n \\ S_n^T & R_n & q_n \\ r_n^T & q_n^T & 0 \end{bmatrix} \begin{bmatrix} u_n \\ x_n \\ 1 \end{bmatrix} + \frac{1}{2} \begin{bmatrix} s_n^l \\ s_n^u \\ 1 \end{bmatrix}^T \begin{bmatrix} Z_n^l & 0 & z_n^l \\ 0 & Z_n^u & z_n^u \\ (z_n^l)^T & (z_n^u)^T & 0 \end{bmatrix} \begin{bmatrix} s_n^l \\ s_n^u \\ 1 \end{bmatrix} \\
s.t. \quad & x_{n+1} = A_n x_n + B_n u_n + b_n && n = 0, \dots, N-1 \\
& \begin{bmatrix} \underline{u}_n \\ \underline{x}_n \\ \underline{d}_n \end{bmatrix} \leq \begin{bmatrix} J_{u,n} & 0 \\ 0 & J_{x,n} \\ D_n & C_n \end{bmatrix} \begin{bmatrix} u_n \\ x_n \end{bmatrix} + \begin{bmatrix} J_{s^l,u,n} \\ J_{s^l,x,n} \\ J_{s^l,g,n} \end{bmatrix} s_n^l && n = 0. \dots, N \\
& \begin{bmatrix} J_{u,n} & 0 \\ 0 & J_{x,n} \\ D_n & C_n \end{bmatrix} \begin{bmatrix} u_n \\ x_n \end{bmatrix} - \begin{bmatrix} J_{s^u,u,n} \\ J_{s^u,x,n} \\ J_{s^u,g,n} \end{bmatrix} s_n^u \leq \begin{bmatrix} \overline{u}_n \\ \overline{x}_n \\ \overline{d}_n \end{bmatrix} && n = 0. \dots, N
\end{aligned}
$$

Chapter 4

Tree OCP QP