

Tutorial - 5

Any-1

BFS

- 1) Yes queue data structure.
- 2) Stands for breadth first search.
- 3) Can be used to find single source shortest path in an ~~unweighted~~ graph if we reach a vertex with min no. of edges from a source vertex.

- 4) Siblings are visited before the children.

Application:-

- 1) Shortest path & minimum spanning tree for unweighted graph.
- 2) Peer to Peer Networks.
- 3) Social Networking websites
- 4) GPS Navigation systems.

DFS

- 1) Uses stack data structure.
- 2) Stands for depth first search.
- 3) We might traverse through more edges to reach a destination vertex from a source.

- 4) Children are visited before the siblings.

Applications:

- 1) Detecting cycle in a graph.
- 2) Path finding
- 3) Topological sorting
- 4) Solving puzzles with only one soln.

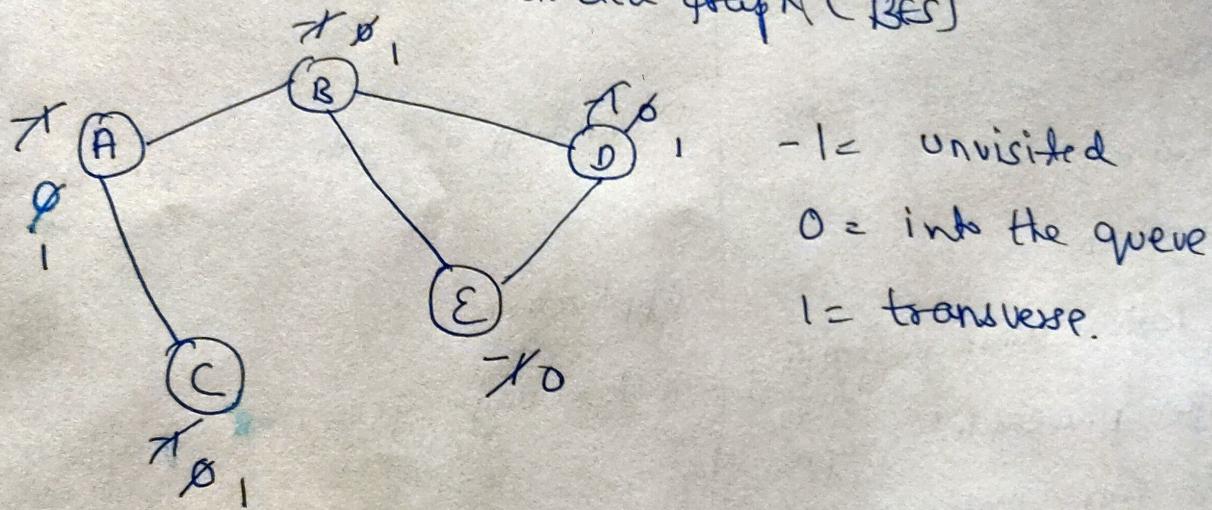
Any-2 In BFS we use queue data structure as queue is used when things don't have to be processed immediately, but have to be processed in FIFO order like BFS.

In DFS stack is used as DFS uses backtracking. For DFS we retrieve it from root to the farthest node as much as possible this is the same idea as LIFO [used by stack].

A₃ Dense graph is a graph in which the no. of edges is close to the maximal no. of edges. Sparse graph is a graph in which the no. of edges is close to the minimal no. of edges. It can be disconnected graph.

* Adjacency lists are preferred for sparse graph & adjacency matrix for dense graph.

A₃₋₄ cycle detection in undirected graph (BFS)

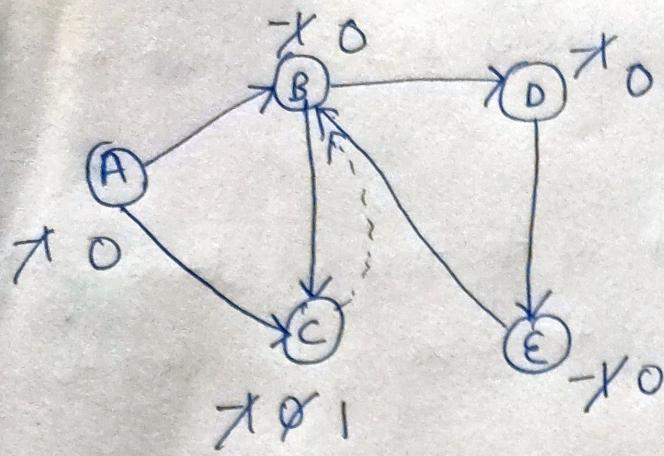


Queue :- [A | B | C | D | E]

Visited set :- [A | B | C | D]

when D checks its adjacent vertex it finds E with 0
⇒ if any vertex finds the adjacency vertex with flag 0, then it contains cycle

cycle detection in directed graph (DFS)



stack :-



visited set

ABCDG

$$\Rightarrow B \rightarrow D \rightarrow E \rightarrow B$$

parent map

vertex	parent
A	-
B	A
C	B
D	B
E	D

these E finds B (adjacent vertex of E) with 0.

\Rightarrow it contains a cycle.

Ans - S The disjoint set data structure is also known as union-find data structure & merge-find set. It is a data structure that contains a soln. of disjoint or non-overlapping sets. The disjoint set means that when the set is partitioned into the disjoint subsets, various op's can be performed on it.

In this case, we can add new sets, we can merge the sets, & we can also find the representative members of a set. It also allows to find out whether the two elements are in the same set or not efficiently.

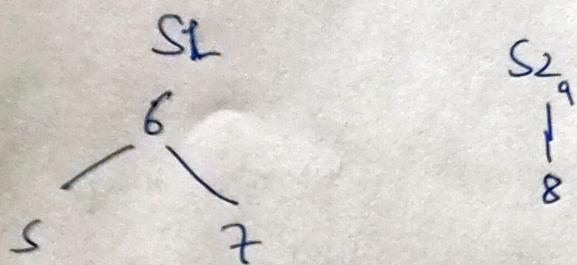
operations on disjoint set :-

1) Union

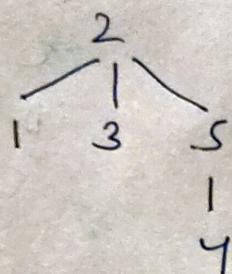
\Rightarrow if S_1 & S_2 are two disjoint sets, their union $S_1 \cup S_2$ is a set of all elements x such that x is in either S_1 or S_2 .

- As the sets should be disjoint $S_1 \cup S_2$ replaces $S_1 \& S_2$ which no longer exists.
- Union is achieved by simply making one of the trees a subtree of other i.e. to set parent field of one of the roots of the trees to other root.

Ex:

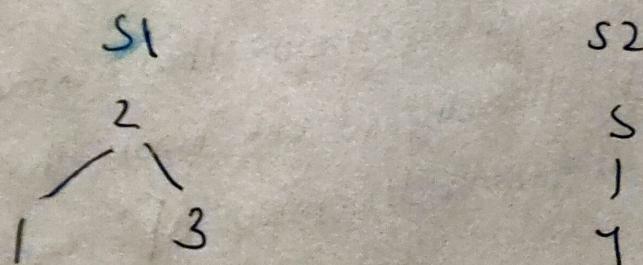


$S_1 \cup S_2$



2) find

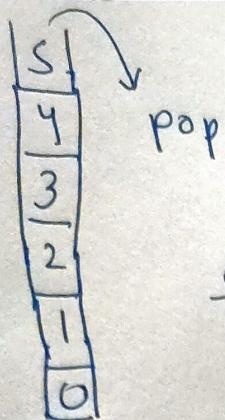
Given an element X , to find the set containing it ex:-



$\text{find}(3) \Rightarrow S_1$

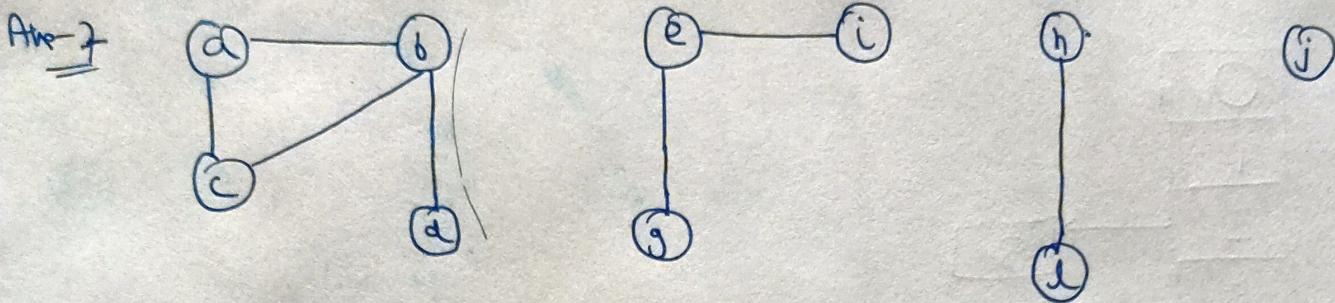
~~$\text{find}(5) \Rightarrow S_2$~~

~~Ans~~ go to node 5, all the adjacent nodes are already visited
push node 5 into the stack & mark it visit.



5 4 2 3 1 0

output.



$$V = \{a, b, c, d, e, f, g, h, i, j, l\}$$

$$E = \{(a,b), (a,c), (b,d), (b,e), (b,g), (d,e), (e,i), (f,g), (h,i), (j,l)\}$$

	$\{a\} \subset \{b\} \subset \{c\} \subset \{d\} \subset \{e\} \subset \{g\} \subset \{h\} \subset \{i\} \subset \{j\} \subset \{l\}$
(a,b)	$\{a, b\} \subset \{c\} \subset \{d\} \subset \{e\} \subset \{g\} \subset \{h\} \subset \{j\} \subset \{i\} \subset \{l\}$
(a,c)	$\{a, b\} \subset \{c\} \subset \{d\} \subset \{e\} \subset \{g\} \subset \{h\} \subset \{i\} \subset \{j\} \subset \{l\}$
(b,d)	$\{a, b, c\} \subset \{d\} \subset \{e\} \subset \{g\} \subset \{h\} \subset \{i\} \subset \{j\} \subset \{l\}$
(b,d)	$\{a, b, c, d\} \subset \{e\} \subset \{g\} \subset \{h\} \subset \{i\} \subset \{j\} \subset \{l\}$
(e,i)	$\{a, b, c, d\} \subset \{e, i\} \subset \{g\} \subset \{h\} \subset \{j\} \subset \{l\}$
(e,g)	$\{a, b, c, d\} \subset \{e, i, g\} \subset \{h\} \subset \{j\} \subset \{l\}$
(h,l)	$\{a, b, c, d\} \subset \{e, i, g\} \subset \{h, l\} \subset \{j\}$
(j)	$\{a, b, c, d\} \subset \{e, i, g\} \subset \{h, l\} \subset \{j\}$

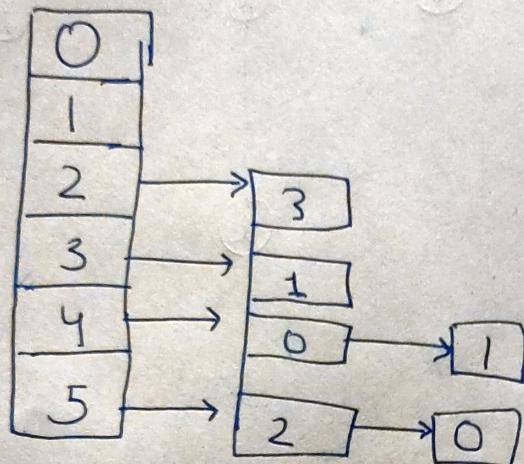
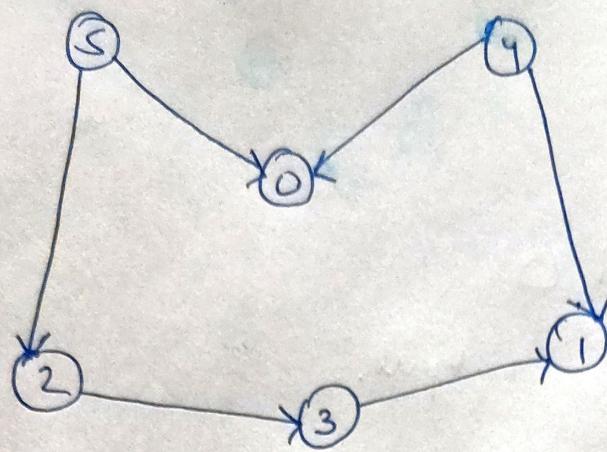
we have

$$\{a, b, c, d\}$$

$$\{e, i, g\}$$

$$\{h, l\}$$

$$\{j\}$$



Ans = Heap is generally preferred for priority queue implementation because heaps provide better performance compared to arrays or linked list.

Algorithm where priority queue is used:-

- 1) Dijkstra's shortest path algorithm:- When the graph is stored in the form of adjacency list or matrix priority queue can be used to extract minimum efficiently when implementing Dijkstra's Algo.
- 2) Prim's algorithm :- to store keys of nodes & extract minimum key node at every step.

Min Heap

- 1) for every pair of the parent & descendant child node, the parent node always has lower value than descendant child node.
- 2) The value of nodes increase as we traverse from root to leaf node.
- 3) Root node has the lowest value.

Max Heap

- 1) for every pair of the parent & descendant child node, the parent node has greater value than descendant child node.
- 2) The value of nodes decrease as we traverse from root to leaf node.
- 3) Root node has the greatest value.