

DESIGN OF 4 BIT RING COUNTER USING QUANTUM DOT CELLULAR AUTOMATA



A PROJECT REPORT

Submitted by

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BONAFIDE CERTIFICATE

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We jointly declare that the project report on "DESIGN OF 4 BIT RING COUNTER USING QUANTUM CELLULAR AUTOMATA" is the result of original work done by us and best of our knowledge, similar work has not been submitted to "ANNA UNIVERSITY CHENNAI" for the requirement of Degree of BACHELOR OF ENGINEERING. This project report is submitted on the partial fulfillment of the requirement of the award of Degree of BACHELOR OF ENGINEERING.

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ABSTRACT

Moore's Law states that the number of transistors per square inch on integrated circuits has doubled approximately every two years, this is true for CMOS based VLSI circuit design. Quantum-Dot Cellular Automata (QCA) replaces CMOS based VLSI technology. The assembly of quantum dots replaces transistors which is said to be "Quantum Dot Cellular Automata", an emerging nanotechnology in the field of quantum electronics. Such type of circuit can be used in many digital applications and has an advantage of reduced area utilization. Quantum mechanics and cellular automata are together said to be Quantum Dot Cellular Automata. QCA technology has advantages like small size and high speed. CMOS technology uses transistors to create a logic gate but in QCA technology, logic gates and wires are created by using QCA cells. The basic logic gates like AND, OR, inverter, majority gates are implemented. Many combinational and sequential circuits are designed by using these basic gates. This project aims at the design of sequential circuits like 4-bit ring counter using four types of flip flops. The circuit was designed and the functionality of those was verified using QCADesigner tool.

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LIST OF ABBREVIATIONS

QCA - Quantum-Dot Cellular Automata

RC - Ring Counter

FF - Flip Flop

D FF - Delay Flip Flop

JK FF - JK FLip Flop

SR FF - Set-Reset Flip Flop

T FF - Toggle Flip Flop

CLK - Clock

Q(t) - Output at Time 't'

Q(t+1) - Output at Next Clock Cycle

CHAPTER 1

INTRODUCTION

1.1 OVERVIEW OF NANOTECHNOLOGY

Nanotechnology is a science and technology of small things in particular things that are less than 100nm in size. One nanometer is 10-9 meters. Most computer scientists and engineers today are aware of the shrinking transistor sizes, for it has been a continuous process since the advent of vacuum tubes, and the cause of rapid development of computing technologies.

Today, we use CMOS (Complementary Metal Oxide Semiconductor) technology to build our transistors. The advantages of CMOS technology over other technologies are that they have no static power dissipation, logic levels are fully restored, integration levels are high, and rise and fall transition times are of the same order. In the past, we have been using micron technology. In 2001, we began using 0.25µm CMOS technology which is said to be deep sub-micron (DSM) technology.

Some believe that there will be a gradual switch from CMOS technology to molecular electronics technology as we learn more and begin incorporating small molecular components within the existing chip technology. Others believe that a dramatic switch will occur as a next generation "Intel" based on molecular nanoelectronics emerges.

Nanotechnology is already in use in many computing, communications, and other electronics applications to provide faster, smaller, and more portable systems that can manage and store larger and larger amounts of information.

These continuously evolving applications include:

Nanoscale transistors that are faster, more powerful, and increasingly energy-efficient; soon your computer's entire memory may be stored on a single tiny chip.

Magnitude random access memory (MRAM) enabled by nanometer-scale magnetic tunnel junction that can quickly and effectively save even encrypted data

during a system shutdown or crash, enable resume play features, and gather vehicle accident data.

Displays for many new TV's, laptop computers, cell phones, digital cameras and other devices incorporated nanostructured polymer films known as organic light-emitting diodes or OLEDs, OLED screens offer brighter images in a flat format, as well as wider viewing angles, lighter weight, better picture density, lower power consumption, and longer lifetimes.

Other computing and electronic products include Flash memory chips for iPod nanos ultra responsive hearing aids; antimicrobial/antibacterial coatings on mouse/keyboard/cell phone casing; conductive inks for printed electronics for RFID/smart cards/smart packaging; more life-like video games and flexible display for e-book reader.

VLSI (Very Large-Scale Integration) design engineers are beginning to face new problems as the integrated chips increase in density. For example, the electrons are jumping the gap between metal layers. One common solution is to introduce new types of metallic materials into the chip. However, this is not a sufficient and viable solution in the long term.

After more than three decades of research and experience in chip making, VLSI design engineers had developed certain DRC (Design Rule Checking) methods to confirm that a circuit will work with a certain technology. Software tools such as those of Cadence and Synopsis helped designers quickly establish the stability and correctness of a circuit design.

However, with nanotechnology this method of checking a circuit is no longer enough due to quantum effects such as tunneling from one metal layer to another. Therefore, research in applying statistical mechanics to deal with probabilistic behavior of metal to metal jumping electron in the chip is also occurring. This too may lead to the nanoscale electronics of the near future.

Let us introduce the term "nano-VLSI" to discuss this phenomenon as "nanoelectronics" has already been taken. This will allow us to maintain broader scope and also consider the interactions and systems between many nanoscale transistors.

1.2 OBJECTIVES OF QCA

According to Moore's Law, chip increases its size exponentially with time by Gorden Moore in 1965. It is true for CMOS based VLSI circuit design. Hence, to fabricate CMOS transistors into smaller size, it will eventually hit its fundamental physical limitations. By reducing the transistor size, we can achieve high speed, high design, low power dissipation. So many alternatives have been proposed and studied by the scientist to invent new technology which increases the device density.

Very Large-Scale Integration process of creating IC by combining tools of transistors into a single chip. Before the introduction of technology, the most IC's had a limited set of functions they could perform. Electronic circuits consist of CPU, RAM, ROM and glue logic. VLSI designers add all of those onto the chip. Main problem in this technology is size of the circuit.

A complex circuit like computer was dependent on speed. If the component of computer were too large or the wires interconnecting them are too long. The electric signals could not travel fast enough through the circuit, thus making the computer too slow to be effective. Solution for this problem is to make all components and the chip out of the same block of semiconductor material. Number of components and wires has to be assembled manually hence circuit becomes smaller. Integrating all components on a single silicon wafer came into existence, which lead to development in SSI. Later, LSI as well as VLSI with 10,000's transistors on a single chip.

Nanotechnology is a new computing method which provides a possible alternative to overcome these problems. International Technology Roadmap for Semiconductors (ITRS) report summarizes several nanotechnologies with Quantum-Dot Cellular Automata (QCA) as a possible option.

CHAPTER 2

LITERATURE SURVEY

S.Lekashri et al., (2025) present a novel and efficient design for a D-type Flip-Flop (DFF) integrated with a pulse generator using Quantum-Dot Cellular Automata (QCA) technology, aiming to enhance the performance and energy efficiency of sequential digital circuits. QCA, a cutting-edge nanotechnology alternative to conventional CMOS, enables computation without the flow of electric current, instead utilizing Coulomb interactions between quantum dots to represent binary data, which leads to a significant reduction in power consumption and heat generation. The proposed DFF design takes advantage of QCA's inherent benefits by integrating a pulse generator to act as a frequency divider, which plays a critical role in timing control within sequential circuits, particularly in the design of n-bit counters. This integration not only simplifies the architecture but also contributes to minimizing latency and power dissipation, issues that are commonly encountered in traditional flip-flop-based systems. The research outlines the full design and implementation process of the counter architecture, where the DFF governs the frequency division while maintaining synchronization and operational stability. Simulation of the circuit was conducted using the QCA Designer tool, a specialized environment for QCA-based digital logic, and the results demonstrated improved performance in key metrics such as speed, energy efficiency, and reliability when compared to conventional CMOS counterparts. Moreover, the use of majority voter gates—a fundamental logic element in QCA design—further contributed to the reduction of design complexity while maintaining logical robustness and signal integrity. Overall, this work highlights a significant advancement in the domain of high-speed, low-power digital logic, suggesting that QCA-based DFFs with integrated pulse generation could pave the way for future developments in nanoelectronic circuit design, especially in applications where size, energy efficiency, and performance are critical.

Pezhman Kiani Vosta et al., (2024) introduce three innovative and efficient topologies for 4-bit counters using Quantum-Dot Cellular Automata (QCA) technology, presenting a promising alternative to traditional CMOS-based digital

circuit designs. Their study focuses on the development and analysis of a Johnson ring counter, a standard synchronous counter, and a synchronous counter with an added reset function, each optimized for performance, cell economy, and spatial efficiency. These counters were designed with a strong emphasis on leveraging the fundamental strengths of QCA, including its potential for high-speed operation, extremely low power consumption, and ultra-compact layout, which are critical advantages over the conventional CMOS approach that often suffers from higher power dissipation and larger physical footprint. Through detailed simulation and comparison, the authors demonstrate that their proposed QCA-based designs achieve remarkable reductions in the number of cells and the overall occupied layout area—by approximately 25.82% and 35%, respectively—when compared to earlier models, showcasing notable gains in design compactness and circuit optimization. The research not only provides insight into efficient counter implementation using QCA logic but also reinforces the viability of QCA as a future-ready solution for digital system design, especially in domains where miniaturization and energy efficiency are essential. Additionally, the counters were rigorously tested through simulation to evaluate their functional accuracy and performance under typical operating conditions, confirming their capability to address critical challenges faced by CMOS technologies, such as scalability, switching delays, and thermal inefficiencies. These findings support the broader conclusion that QCA technology has the potential to significantly enhance the design and operation of digital counters and similar sequential circuits, paving the way for next-generation advancements in nanoelectronic systems and energy-efficient computing platforms.

Saeid Seyedi and Hatam Abdoli (2024) present a detailed and forward-thinking study on the design and implementation of approximate Full Adder (FA), Full Subtractor (FS), and Full Adder-Subtractor (FAS) circuits optimized for Quantum-Dot Cellular Automata (QCA), a next-generation nanotechnology platform. Recognizing the growing demand for efficient and compact computing architectures, the authors propose these innovative arithmetic designs as an alternative to traditional CMOS circuits, which often face challenges such as increased power consumption, larger chip area, and performance limitations. QCA, with its low power usage, minimal complexity, and fast switching capabilities, serves as a powerful foundation for

realizing advanced computational components. By utilizing XOR logic, the authors construct approximate versions of FA, FS, and FAS circuits, which are especially effective in balancing performance with hardware simplicity in applications that tolerate minor computational inaccuracies. The paper elaborates on the structural intricacies of these circuits and reports impressive outcomes: the approximate FA and FS use only 11 and 12 QCA cells, respectively, with an extremely low delay of 0.5 clock phases and minimal area usage of just 0.01 µm². In addition, the study introduces a 4-bit Ripple Carry Adder (RCA) comprising 64 QCA cells, showing a substantial reduction in resource consumption and enhancement in computational efficiency. Functional simulations conducted using QCADesigner validate the superiority of the proposed designs, with a 21% improvement in both the FA and FS and a 43% reduction in cell count for the RCA when compared to previously reported designs. These findings illustrate that the proposed approximate arithmetic circuits not only meet but exceed current design benchmarks, paving the way for the development of more compact, energy-efficient, and high-speed arithmetic modules. Moreover, the research establishes a strong foundation for further exploration into QCA-based computation, emphasizing the potential of approximate logic in addressing the performance and area constraints of conventional circuit design in the era of nanoscale technology.

Mohammed Alharbi et al., (2024) present an innovative hybrid design methodology for Quantum-Dot Cellular Automata (QCA) nanocomputing circuits, offering a compelling solution to the inherent limitations of traditional CMOS-based technologies. Recognizing the performance bottlenecks and energy inefficiencies associated with CMOS, the authors focus on the transistor-less, field-coupled nature of QCA, which facilitates significantly higher clock speeds, minimized chip area, and superior energy efficiency. The paper emphasizes the conventional reliance on irreversible majority gates in QCA circuit designs, which have been favored for their simplicity and functional adequacy. However, with the growing demand for ultra-low power systems, there has been a noticeable transition toward reversible computing techniques. While these reversible methods offer theoretical advantages in terms of zero energy dissipation due to information loss, they often come at the cost of

increased design complexity, longer delay times, and larger chip footprints. In response to this challenge, the authors propose a novel hybrid approach that intelligently combines irreversible, reversible, and partially reversible QCA gates. This flexible design strategy empowers engineers and designers to fine-tune their circuits based on specific performance requirements, balancing trade-offs between power consumption, spatial efficiency, and computational delay. To validate the practicality of this hybrid framework, the study implements and analyzes four different hybrid QCA-based half-adder circuits, each utilizing distinct combinations of majority gates to achieve various levels of performance optimization. These circuits are rigorously evaluated using the QCADesigner-E 2.2 simulation environment, which accurately models QCA behavior and provides detailed performance metrics. The results of the simulations clearly demonstrate the superiority of the hybrid designs over conventional methods, achieving enhanced efficiency across multiple performance parameters. This research not only showcases a viable path forward for energy-efficient digital circuit design but also establishes the hybrid QCA gate approach as a scalable and adaptable solution for future nanoscale computing architectures.

Jun-Cheol Jeon (2024) introduces an innovative Fixed Cell-Based Programmable Logic Gate (FPLG) leveraging Quantum-Dot Cellular Automata (QCA) technology to overcome the inherent constraints of conventional CMOS systems in digital circuit design. The study underscores QCA's significant advantages over traditional technologies, notably its extremely low power consumption, minimal area requirements, and reduced operational latency—factors that make it a strong candidate for next-generation nanoscale computing architectures. The proposed FPLG stands out by offering dynamic functionality through fixed cell arrangements and three enable inputs, which collectively control its operation and allow it to execute seven distinct 2-input logic functions and one 3-input function on a single, compact gate structure. This functional flexibility contributes to simplifying circuit complexity and reducing the total number of logic gates required, which is especially beneficial for medium and large-scale digital systems. The author validates the FPLG design through both physical layout verification and thorough simulation using QCA-specific tools, confirming accurate and reliable performance across all tested functions. Notably, the

proposed logic gate achieves a substantial 130% improvement in design cost efficiency compared to existing programmable logic gate alternatives, making it an attractive solution for scalable, cost-effective circuit designs. Furthermore, the paper explores the broader implications of integrating the FPLG into more complex digital architectures, suggesting that its reconfigurability and space efficiency could play a pivotal role in advancing digital system manufacturing processes. By streamlining logic design and enhancing component versatility, this research contributes significantly to the development of highly efficient, compact, and programmable digital logic solutions within the realm of QCA technology.

Gaurang Tyagi et al., (2024) propose a novel 2-bit Arithmetic Logic Unit (ALU) design based on Quantum Dot Cellular Automata (QCA) technology, aiming to address the persistent limitations of traditional CMOS-based Very Large Scale Integration (VLSI) circuits. The study identifies critical drawbacks in CMOS technology, particularly its relatively slow switching speeds and high power consumption, and positions QCA as a compelling alternative due to its inherent advantages in compactness, energy efficiency, and operational speed. The proposed QCA-based ALU is capable of performing fundamental arithmetic and logical operations, including addition, subtraction, multiplication, and various bitwise logic functions, demonstrating its practical utility in modern digital systems. The authors underscore the merits of QCA in terms of simplified circuit architecture, reduced quantum cost, and high efficiency in both latency and area utilization, making it a suitable candidate for next-generation computational devices. Simulation outcomes, conducted using specialized QCA tools, validate the ALU's effectiveness in surpassing the energy and performance limitations typically associated with CMOS circuits. The research illustrates that the integration of QCA technology into arithmetic processing units can significantly enhance overall system performance while drastically reducing power consumption, which is vital for energy-conscious applications. These findings reinforce QCA's potential to revolutionize digital circuit design, setting a strong foundation for future advancements in low-power, high-speed electronic systems tailored for nanoscale and ultra-efficient computing environments.

Mrinal Goswami et al., (2024) deliver an in-depth review of regular clocking schemes in Quantum Dot Cellular Automata (QCA), emphasizing the technology's growing potential as a superior alternative to conventional CMOS systems. The paper highlights the critical challenges associated with QCA, especially the complications arising from irregular clock zones, which hinder fabrication ease and design efficiency. To address these challenges, the authors promote the adoption of regular and scalable clocking schemes, which are crucial for ensuring reliable data transfer and synchronized timing across QCA circuits. The review underscores QCA's intrinsic advantages, such as significantly reduced energy consumption, faster data processing speeds, and high resilience to radiation—qualities that make it an appealing option for future-generation electronics. By systematically comparing a variety of clocking architectures, the study reinforces the importance of employing regular clocking zones to enhance circuit reliability and performance. These findings support the practical implementation of QCA in developing energy-efficient digital systems and highlight the critical role of optimized clocking in overcoming existing design limitations, ultimately advancing the applicability and effectiveness of QCA technology in nanoscale computing environments.

Birinderjit Singh Kalyan et al., (2024) present a comprehensive and detailed study on the development of flip-flops based on Quantum Dot Cellular Automata (QCA) technology, focusing on their application in the design of Serial-in-Serial-Out (SISO) shift registers. The research underscores the growing importance of nanoelectronics and the role of QCA as a transformative alternative to conventional CMOS circuits. QCA is highlighted for its unique benefits, such as ultra-high-speed computations, minimal energy dissipation, reduced circuit complexity, and significantly lower spatial requirements, which are critical in scaling down electronic components for next-generation devices. The authors employ a systematic and optimized design methodology, using the QCA Designer tool to simulate and analyze the behavior of JK and D flip-flops—core components necessary for constructing sequential logic elements like shift registers. Emphasis is placed on the utilization of five-input majority voter gates, which prove to be highly effective in reducing the total cell count, quantum cost, and area occupied by the flip-flops, ultimately contributing to improved

fabrication feasibility and operational efficiency. Through extensive simulation and verification, the study confirms that the proposed QCA-based flip-flop designs not only maintain functional accuracy but also outperform existing CMOS equivalents in terms of speed, energy consumption, and design compactness. Furthermore, the work highlights the scalability of the designs, making them suitable for larger, more complex circuit architectures required in high-performance computing and embedded systems. The findings affirm the critical role of QCA flip-flops in advancing sequential circuit design and demonstrate their suitability for low-power, high-speed digital applications. As the demand for more efficient and compact technologies increases, this study positions QCA as a strong candidate for the foundation of future nanoscale electronic devices, offering practical solutions to overcome current limitations

Gaurang Tyagi et al., (2024) present a comprehensive and in-depth study on the utilization of Quantum Dot Cellular Automata (QCA) technology in the design and optimization of VLSI circuits, with a particular focus on the development of an innovative NOT gate that significantly enhances performance parameters. The research responds to the persistent limitations of traditional Complementary Metal Oxide Semiconductor (CMOS) technologies, which are increasingly constrained by issues such as slow switching speeds, large device footprints, and excessive power consumption. In contrast, QCA offers a revolutionary alternative by leveraging fieldcoupled nanotechnology that enables high-speed operation, extremely low energy dissipation, and a dramatic increase in circuit density. The study introduces a novel NOT gate design that incorporates key optimization strategies, including Boolean expression simplification and advanced cell layout techniques, resulting in substantial improvements in design metrics. Specifically, the proposed NOT gate achieves an impressive 55% reduction in the number of QCA cells required and an 80.77% decrease in the overall area occupied, highlighting the efficiency gains attainable through intelligent design practices. Moreover, the authors demonstrate the gate's application in XOR circuit design, achieving a notably low delay of just 0.5 clock cycles, further emphasizing the technology's potential for high-speed computing. The results of this study strongly indicate that QCA technology is well-positioned to drive the next wave of innovation in digital electronics by supporting the development of compact, energy-efficient, and scalable logic circuits. The authors conclude that their proposed designs not only outperform existing models but also underscore the long-term promise of QCA in the broader context of nanotechnology and the digital transformation of electronic systems. This research contributes meaningfully to the growing body of knowledge surrounding QCA and sets the stage for future explorations into its practical applications across a wide array of digital and embedded system platforms.

Huanging Cui et al., (2023) introduce a sophisticated programmable synchronous 2-bit counter based on Quantum-Dot Cellular Automata (QCA) technology, tackling one of the more complex aspects of digital system design sequential circuit construction. Unlike conventional CMOS technology, QCA operates through a field-coupling mechanism that alters the fundamental approach to circuit design, introducing both new opportunities and unique challenges. Recognizing these constraints, the authors propose an innovative counter design that integrates combinational logic with falling edge-triggered JK flip-flops to enable dynamic control over counting operations. This design is particularly noteworthy for its programmable functionality, allowing for real-time modifications to the counter's operation mode via dedicated control signals—an essential feature for adaptive digital systems. Furthermore, the study addresses a critical issue in QCA-based sequential circuits: the unpredictability of initial cell polarization. To overcome this, the authors implement a novel initialization method that enables the controlled setting of initial states, thereby improving reliability and performance stability. The counter's functionality and efficiency are rigorously validated using QCADesigner simulation tools, which confirm its correct operation and high potential for integration into advanced nanoscale computing architectures. The findings highlight how QCA technology, with its minimal power requirements, reduced area consumption, and enhanced switching capabilities, can significantly improve the design and implementation of sequential circuits. Ultimately, this research not only underscores the viability of QCA as a robust alternative to CMOS in digital logic design but also paves the way for more intelligent, compact, and energy-efficient systems in future electronics.

Madhavi Repe et al., (2023) present an in-depth investigation into the design and optimization of flip flops using Quantum Dot Cellular Automata (QCA) technology, offering a promising alternative to the long-standing limitations of CMOS-based digital circuits. The study begins by addressing key drawbacks inherent in traditional CMOS technology, including significant leakage currents, increased power dissipation, and scalability challenges as device sizes shrink to the nanoscale. In contrast, the authors advocate for QCA, a novel transistor-less architecture that leverages the principles of Coulombic repulsion between quantum dots to facilitate highly efficient, low-power data transmission without relying on current flow.

The research focuses on the development and simulation of several fundamental flip flop types—namely SR (Set-Reset), D (Data), and T (Toggle) flip flops—using QCADesigner as the primary design and analysis platform. These designs are evaluated based on critical performance parameters such as cell count, area utilization, latency, and energy dissipation. The simulation results indicate that the QCA-based flip flops demonstrate a marked reduction in energy consumption and occupy significantly less physical space compared to their CMOS counterparts, reinforcing their suitability for integration into energy-efficient, high-density nanocircuits.

Furthermore, the authors emphasize the strategic importance of flip flops in constructing complex sequential logic circuits, making their QCA-optimized versions valuable building blocks for future nano communication systems and next-generation computational devices. The study concludes by asserting that the implementation of QCA in flip flop design not only enhances power and area efficiency but also lays a strong foundation for future research in ultra-low-power digital electronics. These advancements position QCA as a transformative technology with far-reaching implications in the ongoing miniaturization and optimization of electronic systems.

Mohammad Gholami et al., (2023) conduct a thorough investigation into the design and optimization of sequential circuits using Quantum-Dot Cellular Automata (QCA), with the objective of enhancing energy efficiency, processing speed, and spatial compactness—key limitations in conventional Complementary Metal-Oxide-Semiconductor (CMOS) technologies. The study addresses the growing demand for

ultra-low-power and area-efficient digital systems, particularly as the scaling limitations of CMOS become more pronounced in nanoscale circuit designs. At the core of their research, the authors propose an innovative T-latch architecture optimized through QCA's transistor-less, field-coupled mechanism. Leveraging the unique characteristics of QCA—such as polarization-based information propagation and clocked control—the newly designed T-latch achieves a 6.45% reduction in layout area and a 44.49% decrease in power consumption compared to previously published T-latch designs. This highlights QCA's potential in significantly improving energy efficiency without compromising performance. In addition to the T-latch, the paper presents novel designs for 3-bit and 4-bit counters, two essential components of sequential logic circuits. The 3-bit counter demonstrates a 2.14% reduction in cell count, while the 4-bit counter achieves a 0.51% reduction in total cell number and a 4.16% decrease in cross-sectional area, all of which contribute to the miniaturization and efficiency of digital systems. Moreover, the study introduces selective counters capable of counting within specific ranges—such as 0 to 5 and 2 to 5—showcasing the flexibility and application-specific adaptability of QCA technology. These selective counting circuits are crucial in specialized digital applications where dynamic and programmable counting logic is required. The proposed designs were validated using QCADesigner, a simulation tool specifically tailored for QCA-based circuit design and analysis. The results confirm that QCA circuits not only outperform traditional CMOS counterparts in critical performance metrics like power consumption and area but also provide more scalable and energy-conscious solutions for complex sequential operations.

Orestis Liolis et al., (2022) propose a novel automated design methodology for Quantum-dot Cellular Automata (QCA) circuits, addressing a major challenge in the field— the absence of standardized, scalable design rules for constructing complex QCA systems. As traditional QCA approaches often struggle with the design and integration of large-scale circuits, the authors introduce a generic and modular QCA crossbar architecture that supports a wide range of logic functions, offering significant improvements in design efficiency and flexibility. This architecture facilitates customization and reuse, streamlining the circuit development process. The paper

outlines comprehensive programming principles and an analytical design flow that guide the functioning of the proposed automated design tool, making it applicable to both combinational and sequential logic circuit implementations. The methodology is validated through extensive simulations, which confirm its accuracy, user-friendliness, and practical effectiveness. The results demonstrate that the tool can significantly reduce design time while maintaining high-performance metrics, such as low power consumption and compact circuit layout—key advantages of QCA technology. By unifying the QCA circuit design process and enabling efficient automation, this study highlights the transformative potential of QCA in the development of next-generation nanoelectronic systems and presents a viable path forward for overcoming the limitations of traditional CMOS-based technologies.

Alireza Navidi et al., (2021) present an innovative approach to designing and simulating quaternary logic gates using Quantum-Dot Cellular Automata (QCA), aiming to overcome the limitations posed by traditional CMOS technologies in deep sub-micron regimes. The study introduces QCASim, a custom-built simulator specifically tailored for quaternary QCA (QQCA) systems, allowing for the design, modeling, and verification of key quaternary logic gates, including MIN, MAX, and various inverter configurations. The authors emphasize the benefits of QQCA, such as efficient handling of circuit complexity and reduced area requirements, which are essential in designing compact and high-performance logic systems. In comparison to carbon nanotube field-effect transistor (CNFET)-based quaternary logic designs, the QQCA approach demonstrates superior performance in terms of delay and energy efficiency, positioning it as a strong candidate for future nanoelectronic applications. Additionally, the paper features the design of a 1-to-4 decoder using the proposed gates, illustrating how QQCA supports the representation of two binary bits as a single quaternary digit—enhancing both data density and processing capability. These findings highlight QQCA's potential to revolutionize circuit design for energy-efficient, high-density logic systems, paving the way for scalable next-generation digital technologies.

H. Alamdar et al. (2021) introduce a cutting-edge method for digital circuit design using Quantum-dot Cellular Automata (QCA), centering on a D-type Flip-Flop (D-FF)

that integrates a Nand-Nor-Inverter (NNI) gate. This approach addresses the growing limitations of conventional CMOS technologies, such as short-channel effects, high power consumption, and the rising operational frequencies in modern digital systems. The authors demonstrate that QCA offers compelling advantages—including ultra-low power requirements and the ability to function at terahertz frequencies—positioning it as a promising alternative for next-generation circuit design. Their proposed architecture features a D-latch composed of just 24 cells, boasting an ultra-compact area of 0.02 µm² and a latency of only 0.5 clock cycles, making it highly efficient for high-speed applications. Moreover, the D-FF design includes a reset function, increasing its applicability in critical components like Phase-Frequency Detectors (PFDs). Simulation results obtained via QCADesigner and QCAPro validate the circuit's superior energy efficiency and performance compared to traditional CMOS-based designs. Overall, the study highlights the potential of QCA to address the pressing challenges of current technologies while paving the way for innovative solutions in nano-scale digital systems.

Salma Yaqoob et al., (2021) present an in-depth and comprehensive study on the development of highly efficient N-bit shift registers by employing optimized D flipflops within the framework of Quantum Dot Cellular Automata (QCA) technology. This work aims to address the increasing demand for secure, compact, and ultra-lowpower nano communication systems, which are becoming critical in the era of miniaturized electronics and advanced digital applications. The paper begins by thoroughly examining the fundamental limitations of traditional Complementary Metal Oxide Semiconductor (CMOS) technology, which include excessive power dissipation, limited scalability, and slower processing speeds, making it less viable for future nanoscale device fabrication. In contrast, QCA emerges as a promising solution, offering unique advantages such as high-speed data transmission, reduced area requirements, low energy consumption, and superior device density. The authors propose a novel and robust D flip-flop design specifically tailored for QCA technology, focusing on improving energy efficiency, fault tolerance, and scalability. They perform a meticulous fault tolerance analysis, evaluating the impact of single-cell omission and addition to ensure the reliability and stability of their design under potential fabrication

defects. Using this optimized D flip-flop as a foundational element, the authors construct shift registers of varying bit sizes—including 2-bit, 3-bit, 4-bit, and 8-bit implementations—demonstrating the scalability and flexibility of the design, which can be effortlessly extended to N-bit configurations as required by the application. These shift registers are vital components in sequential circuit design and are essential in applications such as data storage, serial communication, and digital signal validation, conducted processing.For performance simulations were QCADesigner, a specialized tool for modeling QCA circuits, to confirm the functional accuracy of the proposed shift registers. Additionally, the energy dissipation characteristics were thoroughly analyzed using QCAPro, which confirmed that the designs exhibit significantly lower energy consumption compared to conventional approaches. The proposed QCA-based shift registers not only demonstrate superior performance in terms of speed and power but also achieve high reliability and costeffectiveness, making them ideal for future nanoelectronic and communication systems. Overall, this research underscores the transformative potential of QCA in replacing traditional CMOS in nanoscale applications, offering a viable path forward in the design of compact, efficient, and highly reliable digital circuits.

Ziyad Altarawneh et al., (2021) present a comprehensive study on the design and implementation of arbiter circuits based on Quantum Dot Cellular Automata (QCA), emphasizing demand high-performance, energy-efficient the growing for computational systems in the era of nanoscale technology. The paper focuses on the development of both 2-input and 3-input asynchronous arbiter circuits and provides a comparative analysis with conventional majority-based QCA structures. Recognizing the inefficiencies and limitations of traditional approaches, the authors propose novel arbiter architectures that significantly reduce the number of QCA cells, minimize layout area, and lower overall energy dissipation, all while ensuring that the functional integrity and arbitration logic remain uncompromised. A key innovation in their work lies in the strategic incorporation of input prioritization techniques, enabling more intelligent and efficient resource management during arbitration decisions. This is particularly relevant for modern System-on-Chip (SoC) environments, where multiple processing cores compete for shared resources, necessitating fast and power-conscious arbitration mechanisms. The simulation and performance evaluation of the proposed designs, conducted using QCADesigner and QCAPro tools, reveal that the newly introduced 3-input arbiter not only performs the required arbitration tasks effectively but also outperforms majority-gate-based alternatives in terms of efficiency metrics. By addressing both architectural and energy-related challenges, this research underscores the promising role of QCA technology in advancing next-generation SoC architectures. The compactness, low power usage, and scalability of these QCA-based arbiters position them as ideal components for future nanoelectronic systems, capable of meeting the stringent demands of modern digital circuit design and high-performance computing environments.

Amanpreet Sandhu et al., (2021) analyze the energy dissipation characteristics of sequential circuits designed using Quantum-Dot Cellular Automata (QCA) technology, presenting a significant advancement over traditional CMOS-based digital designs. The study highlights the growing limitations of CMOS technology, particularly leakage currents, increased power consumption, and quantum tunneling issues that become more prominent as device dimensions continue to scale down in deep submicron regimes. In contrast, QCA offers a transistor-less and highly compact alternative, capable of mitigating these challenges through its unique data transmission mechanism based on Coulombic interactions. The authors present optimized designs for SR and D latches, showcasing notable improvements in energy efficiency, area consumption, and delay. The proposed SR latch occupies just 0.01 µm² with a delay of 2 clock cycles, while the D latch consumes 0.04 µm² of space with a faster delay of 1 clock cycle. Importantly, both designs exhibit minimal energy dissipation even under varying temperature conditions, underscoring the thermal stability and robustness of QCA-based circuits. Through simulation using QCADesigner and energy evaluation with QCAPro, the paper verifies the practical viability of these designs for low-power applications. The research suggests that QCA technology holds substantial promise for future nanoelectronic systems, particularly in environments where energy efficiency and miniaturization are critical. By effectively addressing several of the major bottlenecks faced by CMOS, the study positions QCA as a forward-looking solution for building next-generation sequential logic circuits that are not only compact and fast but also environmentally sustainable.

Swagata Das et al., (2021) conduct a systematic review on efficient nano circuit structures utilizing Quantum-dot Cellular Automata (QCA) technology, focusing on its potential to overcome the inherent limitations of traditional CMOS VLSI circuits. As CMOS technology approaches its physical and performance limits due to quantum mechanical effects at nanoscale dimensions—such as increased leakage currents and power dissipation—there is an urgent need for alternatives that can support continued device scaling without sacrificing efficiency. The authors position QCA as a compelling candidate, owing to its transistor-less structure and ability to perform Boolean logic using arrays of quantum dots influenced by Coulombic interactions, which drastically reduce power consumption and circuit area. The review highlights various innovative contributions from researchers in the field, such as the development of reversible logic gates, including a reversible priority encoder designed to limit power dissipation, and a novel Phase-Frequency Detector (PFD) structure that showcases QCA's applicability in timing-sensitive systems. These designs illustrate QCA's capabilities in delivering high-performance, compact, and low-energy circuits suitable for a wide range of applications. Simulation outcomes from tools like QCADesigner and QCAPro validate the effectiveness of these proposed structures, confirming QCA's superiority over conventional CMOS in metrics such as energy efficiency, delay, and functional compactness. The authors emphasize that QCA not only meets the increasing demand for high-speed and power-conscious electronic systems but also opens up new possibilities for advancements in wireless communication and nano-computing. The findings underscore QCA's viability as a transformative technology for the future of electronic circuit design, offering both performance enhancements and substantial energy savings.

Mingliang Zhang et al., (2021) propose a novel design methodology for Line Feedback Shift Registers (LFSRs) utilizing Quantum Dot Cellular Automata (QCA) technology, effectively addressing the inherent complexities of feedback implementation in sequential circuits. Traditional LFSR designs often require multiple components for feedback paths, which can introduce significant delays,

synchronization issues, and increased error susceptibility, especially as circuit complexity scales. To overcome these limitations, the authors introduce a simplified QCA-based LFSR structure that achieves a single clock cycle delay in the feedback loop, thereby enhancing design efficiency and performance. Their approach incorporates clearly defined quantitative criteria for assessing the feasibility of multifeedback LFSRs, demonstrating that all such designs can be transformed into functionally equivalent single-feedback systems without compromising performance. Additionally, the authors propose advanced transformation techniques that mitigate the exponential increase in clock delays typically associated with multi-feedback configurations. These optimizations ensure minimal propagation delay and maintain data integrity throughout the sequential operations. Simulation results validate the proposed methodology, confirming reduced design complexity and improved overall efficiency compared to conventional CMOS-based LFSR architectures. The study not only underscores the practicality of QCA in designing compact and energy-efficient sequential circuits but also highlights its potential in next-generation digital systems requiring high performance and low power consumption. This research reinforces QCA's viability as a cutting-edge solution for addressing the growing demands of nanoelectronic circuit design.

Chunsong Zhu et al., (2021) propose a novel design and implementation of a programmable logic array (PLA) utilizing a crossbar structure within Quantum Dot Cellular Automata (QCA) technology, effectively addressing the scalability and modularity constraints inherent in traditional CMOS circuits. The study delves into the pressing challenges faced by CMOS as device dimensions continue to shrink, particularly the emergence of quantum effects that degrade performance and escalate power consumption. In response, the authors introduce a QCA-based PLA featuring multiple programmable units, where majority gates are leveraged to function flexibly as AND/OR gates, thus enabling greater versatility in logic design. The PLA incorporates a programmable clocking scheme along with an N-bit latch, allowing dynamic control and reconfiguration of logic states, which enhances adaptability in circuit behavior. This architecture not only supports stable operation and ultrafast

speed but also ensures significantly reduced energy consumption—hallmarks of QCA technology. To validate their approach, the authors implement and simulate four distinct digital circuits: a full adder, a 2-to-1 multiplexer, a D flip-flop, and a 1-bit memory. All demonstrate reliable and accurate logic functionality under the proposed system, showcasing the robustness and practicality of the design. The results affirm that this crossbar-based QCA PLA design successfully overcomes limitations of current QCA implementations by introducing programmability and scalability in a compact form. It represents a significant advancement in the pursuit of programmable, low-power nanoelectronic systems, and highlights the broader potential of QCA in next-generation digital circuit applications.

Behrouz Safaiezadeh et al., (2021) present a novel design and simulation of a 3-bit binary to Gray code converter utilizing Quantum Dot Cellular Automata (QCA), exploring both reversible and non-reversible modes to overcome the limitations of traditional CMOS-based designs. The paper underscores the critical challenges posed by CMOS technology, particularly its high power consumption, increased heat generation, and inefficiency at nanoscale dimensions. In contrast, QCA emerges as a highly promising alternative, offering substantial benefits such as ultra-low energy consumption, minimal area requirements, and greater circuit density. To advance the field of low-power computation, the authors introduce a reversible Arithmetic Logic Unit (ALU) that incorporates fundamental reversible logic blocks along with a newly proposed component named the BS1 block. This addition significantly enhances the functional efficiency of the ALU, particularly in executing arithmetic and logic operations in a reversible manner, which is crucial for minimizing energy dissipation. The design methodology emphasizes the importance of reversibility in reducing information loss, aligning with Landauer's principle of energy conservation in computing systems. Simulation results validate the effectiveness of the proposed architecture, showing a 35% reduction in quantum cost, a 27% decrease in the number of QCA cells, and a 30% reduction in occupied area when compared to prior state-ofthe-art designs. These improvements not only affirm the viability of the proposed QCA-based converter and ALU for future digital systems but also highlight the broader applicability of reversible computing in enhancing energy efficiency. This

study marks a significant step toward the realization of high-performance, energy-efficient nanoelectronic systems. It reinforces the potential of QCA technology as a sustainable replacement for conventional CMOS, particularly in applications requiring compact, fast, and low-power digital circuit solutions.

Z.Amirzadeh et al., (2021) introduce a novel design for bi-directional counters utilizing Quantum-dot Cellular Automata (QCA) technology, aiming to effectively address the increasing challenges of power consumption and scalability in modern compact integrated circuits. The study emphasizes the limitations of traditional MOSFET-based technologies, particularly in terms of their growing inefficiency and complexity at nanoscale dimensions. In contrast, QCA emerges as a forward-looking alternative, offering benefits such as a simplified circuit structure, reduced number of cells, and significantly lower power dissipation—making it a strong candidate for next-generation digital systems. Central to the paper is the development and optimization of a T-Latch circuit, a critical component widely used in the construction of sequential elements and Arithmetic Logic Units (ALUs). The authors propose an improved T-Latch design that outperforms existing solutions by achieving a 6.45% reduction in cross-sectional area and an impressive 44.49% decrease in power consumption. These enhancements are crucial for the development of highly efficient nanoelectronic components that maintain functionality while minimizing energy usage. Building on this optimized T-Latch, the researchers design a 3-bit bi-directional up-down counter that consists of 204 quantum cells, occupies a compact area of only 0.26 µm², and operates with a delay of 5.25 clock cycles. This counter is capable of incorporating both reset and set terminals, adding versatility to its operation and making it suitable for more complex logic control systems. The proposed architecture demonstrates reliable functionality and efficient performance through extensive simulation using QCADesigner, validating the feasibility of the design for practical nanoelectronic implementations. The results of the study highlight the potential of QCA-based designs to significantly outperform conventional CMOS approaches in terms of both energy efficiency and spatial compactness. This work not only advances the development of energy-aware digital systems but also contributes to the growing body of research positioning QCA as a viable and scalable technology for future integrated circuit design.

Orestis Liolis et al., (2020) tackle the intricate issue of signal synchronization in large-scale Quantum-dot Cellular Automata (QCA) circuits, a persistent challenge that stems from the inherent limitations of QCA technology, such as the lack of a global clock and strict timing dependencies. As circuits scale in complexity and size, ensuring reliable and synchronized signal propagation becomes increasingly difficult, often resulting in timing mismatches and design inefficiencies. To address this, the authors propose an innovative synchronization methodology inspired by the classical Firing Squad Synchronization Problem (FSSP), adapting the well-known Mazoyer algorithm to the unique requirements of QCA-based systems. This approach facilitates coordinated signal transmission across the entire circuit by initiating simultaneous signal activation after a predetermined number of clock cycles. One of the key contributions of the paper is the introduction of a novel freezing technique, which allows signals to be held temporarily until the appropriate synchronization moment, thereby improving overall timing control without introducing additional complexity into the circuit design. The study critically evaluates existing QCA clocking mechanisms, noting their inefficiency in handling feedback loops and the excessive area they consume, which limits the scalability of complex systems. In contrast, the proposed methodology provides a universal, scalable solution that enhances synchronization across a broad range of QCA circuits. The authors demonstrate its applicability and effectiveness through simulation and implementation in various design scenarios, underscoring its practical viability. The findings reveal that this synchronization technique not only improves timing accuracy and coordination in QCA circuits but also lays the groundwork for developing more robust and scalable nanoelectronic systems. By bridging the gap between theoretical synchronization models and practical QCA implementations, the research significantly contributes to advancing the reliability and performance of future QCA-based digital architectures.

Mohsen Hayati et al., (2019) introduce an innovative and highly optimized design of a Universal Logic Gate (ULG) tailored for Quantum-Dot Cellular Automata (QCA), offering a compelling solution to the fundamental limitations of traditional CMOS

technologies. As CMOS continues to face challenges related to excessive power consumption, performance degradation, and scaling constraints at the nanoscale, QCA emerges as a viable alternative due to its inherently low power requirements, high operational speed, and minimal physical footprint. In this study, the authors present a novel ULG architecture that supports the implementation of 13 essential logic functions—such as AND, OR, NAND, NOR, XOR, XNOR, and others—without the need for auxiliary gates or additional components. The design is notably efficient, requiring only a single clock phase delay, which significantly enhances signal propagation speed and reduces circuit complexity. This optimization not only simplifies the logic design process but also minimizes the number of QCA cells, thereby improving energy efficiency and area utilization. An additional contribution of the paper lies in the integration of an Artificial Neural Network (ANN) model specifically developed for the ULG. This ANN-based model allows the proposed gate to be simulated within widely used circuit analysis platforms like HSPICE and MATLAB Simulink, offering improved modeling accuracy and facilitating seamless integration into broader digital system simulations. Such compatibility greatly aids in performance evaluation and prototyping, bridging the gap between theoretical design and practical implementation. Simulation results confirm the superiority of the proposed ULG in terms of reduced delay, lower power dissipation, and compactness compared to existing logic gate configurations. These findings underscore the gate's potential to become a foundational building block in the design of future QCA-based digital circuits, paving the way for more efficient, scalable, and high-performance nanoelectronic systems.

CHAPTER 3

QUANTUM DOT CELLULAR AUTOMATA

3.1 QCA SURVEY

The foundation of nanotechnology can be traced back to 1959, when Nobel laureate Richard P. Feynman delivered his famous lecture titled "There's Plenty of Room at the Bottom." In it, he envisioned manipulating individual atoms and molecules to build incredibly small devices, essentially planting the seeds for what would become the field of nanotechnology.

Building upon this vision, the concept of Quantum Cellular Automata (QCA) emerged as a potential paradigm for future computing architectures. The term "Quantum Cellular Automata" was first introduced in 1988 by Gerhard Grössing and Anton Zeilinger. Their initial model was more theoretical and only loosely aligned with the quantum computing model previously proposed by David Deutsch in 1985, which laid the groundwork for the field of quantum computation.

The first significant theoretical framework for QCA was presented by John Watrous, who provided a comprehensive study of the principles behind quantum cellular automata in computational models. Later, Craig S. Lent and Paul Tougaw revolutionized the field by proposing a practical implementation of QCA using quantum dots—nanoscale structures that can confine and manipulate individual electrons. Their work laid the foundation for QCA as a promising successor to traditional CMOS (Complementary Metal-Oxide-Semiconductor) technology, which is facing scalability challenges at nanometer nodes.

In the QCA model, information is encoded in the arrangement of charges within a cell composed of quantum dots. Each cell contains four or five quantum dots and two mobile electrons that tend to occupy opposite corners due to Coulomb repulsion. The two resulting stable charge configurations represent binary logic states 0 and 1. Unlike CMOS, QCA does not rely on current switching but rather on electrostatic interactions, enabling potentially lower power consumption and faster operation.

Craig S. Lent and Paul Tougaw proposed using quantum dots for QCA as a successor to CMOS technology. In QCA, binary operations are performed by cells with bi-stable charge configurations, where two charge states represent 0 and 1. With clocking schemes, QCA enables general-purpose computing. While early QCA devices functioned only at cryogenic temperatures, ongoing research aims to achieve room-temperature operation using molecular or magnetic dot technologies.

Leading research groups include University of Notre Dame, which has led QCA research for over a decade, and University of Pisa, led by Massimo Macucci, through the QUADRANT project. The ATIPS lab at University of Calgary developed QCADesigner, the first and most widely used QCA design and simulation tool.

QCA research is primarily focused on device fabrication and architectural improvements, with global efforts advancing this innovative nanotechnology.

3.2 QCA BASIC CONCEPTS

According to Moore's Law, the capacity of computer chip would grow exponentially with time. Device size decreases to an order of 0.05 microns. CMOS transistors eventually hits the fundamental limitations. Hence, several alternatives have been proposed and invented a new technology that allow the continued growth of device density. Nanotechnology, a new computing method provides an alternative to overcome this problems. International Technology Roadmap of Semiconductor (IRTS) report summarizes several nanotechnology with QCA as option.

Nowadays, those CMOS circuits has a limitations in design such as tunneling current, subthreshold leakage, quantum effects, fabrication cost, interconnection delay. To overcome this, researchers found a new technology that uses both quantum mechanics and cellular automata. Hence, the best replacement of CMOS based VLSI technology is QCA (Quantum dot Cellular Automata).

Transistors may be replaced by assemblies of quantum dots called QCA (Quantum dot Cellular Automata). QCA is an emerging Nanotechnology in the field of quantum electronics for low power consumption and high speed by reducing size. QCA operates at quantum level. This circuits can be used in many digital applications QCA circuits

offers an advantages of very high device density, high speed, high fan-out and low circuit complexity.

3.3 ELEMENTS OF QCA

3.3.1 QCA CELLS

The basic device in QCA is a "QCA cell" which enables both the computation and transmission of the information. A QCA cell consists of a hypothetical square space with four electronic sites and two electrons. The electronics sites, called "Dots", represent the locations which the electrons can occupy. The dots are coupled through quantum mechanical tunneling barriers and electrons can tunnel through them depending on the state of the system. Due to their Coulombic repulsion, the electrons tend to occupy the farthest dots in a cell which corresponds to the lowest energy state of the system. The relative positions of the electrons in a cell are used to represent the "cell-polarization" which can then be used to encode binary states 0 or 1.

There are two types of QCA cells namely 90° and 45° cells. Figure 3.3.1 shows 90° cells with polarization of P = -1 which represents binary 0 and Figure 3.3.2 shows a polarization of P = +1 representing binary 1. These two states are called the cell's ACTIVE states. A cell is driven into a particular polarization due to an external field or adjacent polarized cells. Thus a completely isolated cell would have a polarization of P = 0 which is called NULL state. Other types of cells are shown in Figure 3.3.4. These cells have same properties as 90° cells except that the dots have been rotated by 45° thus called as 45° cells or symmetric cell. The cell in Figure 3.3.3 represents a binary state and its polarization.

QCA cells do not operate in isolation; rather, their behavior is influenced by the polarization of adjacent cells. Through Coulombic interaction, the polarization of one cell can induce polarization in neighboring cells, thereby enabling signal transmission and logic computation across a QCA circuit.

Additionally, external electric fields applied through the QCA clocking system can guide the cell from NULL to active states, determining the direction and timing of information flow. This makes clocking crucial not just for timing but also for energy transfer and pipeline control.

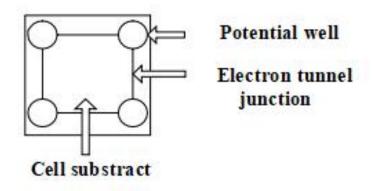


Figure 3.3.1 Basic QCA cell

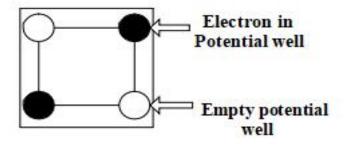


Figure 3.3.2 Electrons in QCA

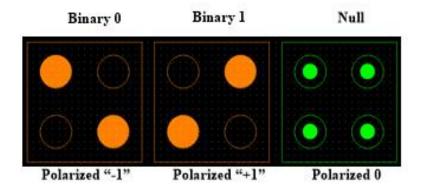


Figure 3.3.3 QCA cell Polarization

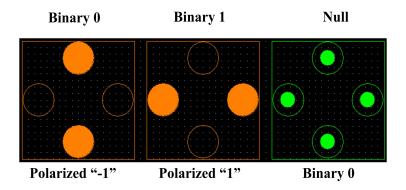


Figure 3.3.4 Symmetric (rotated 45°) cells and its polarization

3.3.2 QCA DOTS

A basic QCA cell is shown in figure 3.3.1 It is a square cell consisting of 4-dots. These dots are known as quantum dots or qdots. The function of this dot is to localize the charge of the electron. The dot is essentially a region of space with potential barriers surrounding it which are sufficiently high and wide so that the charge within it is quantized to a multiple elementary charge. This barrier, however, must be controlled such that the electrons could tunnel through them at the time of switching. The bistability of QCA is nothing but the quantization of charge and hence it is important to know the relationship between the energy levels of a single particle and the energy levels of the dot. Quantum dots can be either metallic, or molecular, or a semiconductor.

The metallic irmplementation of quantum dots consists of metal islands on an insulating substrate. In this type, a single dot consists of billions of free electrons. But the Coulomb cost of one electron, tunneling the dot would be large. The charging of the dot is established by this electrostatic effect. The single particle energy of these dots exists very close together in energy and is in significant during tunneling.

The molecular implantation of quantum dots are simply based on redox centers, areas in a molecule that accepts (reduced) or donates (oxidize) an electron without breaking the bonds that hold the molecule together, within the molecule. These types of dots have very large single particle energy level spacing unlike metallic dots, and a high Coulomb cost for adding additional charge and hence both effects are strong. The

semiconductor based dots are formed by electrostatically depleting a 2- dimensional electron gas. The metallic patterns on the surface are typically used to shape the confining potential. Dots can also be formed from self-assembled structures such as pyramids. Dot sizes and separation are in the order of tens ofnanometers. The single particle energy level distances could be varied by constricting the confining potential. However they are extremely sensitive to variations in geometry.

3.3.3 QCA WIRE

QCA wire can be formed by placing the QCA cells in a linear fashion. The Columbic interaction between the adjacent cells causes the polarization of a cell to alignto its neighboring cells thus allowing the transmission of information along the array of cells. Figure 3.3.5 shows QCA wires transmitting 0 and 1 using 90° cells. In both Figures, the input cell is driven by an external source and is strongly polarized in one direction. The input cell then acts as a driver to the other cells in the NULL state which align themselves to the input cell polarization to reach the systems ground state. In Figure 3.3.5, the input cell IN is strongly polarized to +1 and to bring the system of the first two cells to the ground state, the electrons in first adjacent green cell would tend to align in an orientation with the least electrostatic repulsive forces of the electrons in the cells. This is only possible if the top electron in green cell moves to the top-right dot of the cell. The same theory applies to the rest of the green cells and finally the output cell in yellow polarizes to binary 1 as well. Similarly, a binary 0 is transmitted from input to output cell OUT in Figure 3.3.6.

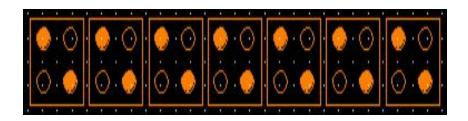


Figure 3.3.5 QCA Wire

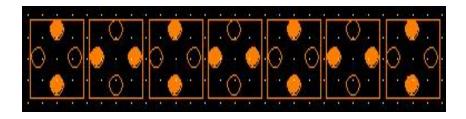


Figure 3.3.6 QCA Wire Symmetric (rotated 45°) cells and its polarization

3.3.4 QCA CLOCKING

The clocking in the QCA circuits controls the information flow and the synchronization in the circuit. It also provides the power gain and avoids the metastable states. In case of a QCA-cell, the meta-stable state corresponds to polarization of a cell that cannot be distinctively identified as logic 1 or logic 0. In other words, the cell polarization is neither strongly -1 (logic 0) nor +1 (logic 1).

The clock in QCA technology, which is different than the conventional definition of clock in CMOS, consists of four phases: switch (unpolarized cells are driven by some input and get polarized depending on their neighbors" polarization), hold (cells are held in some definite polarization representing a binary state), release (cells lose their polarization) and relax (when cells lose their polarization in release phase, the remain unpolarized or null in this state). Each of these phases is a quarter of cycle apart from the previous phase which can be implemented by generating four clocks each with $\pi/2$ phase difference from previous one. The four phases of a QCA clock are shown in Figure 3.3.7 and Figure 3.3.8.

A metastable state in a QCA cell refers to a condition where the cell's polarization is ambiguous or weak, meaning the cell does not clearly represent a binary 0 (P = -1) or 1 (P = +1). This instability typically arises when cells are left to settle without a controlled input or when there's an improper balance in the electrostatic influence from neighboring cells. Clocking prevents this by guiding cells through a strict sequence of controlled phases.

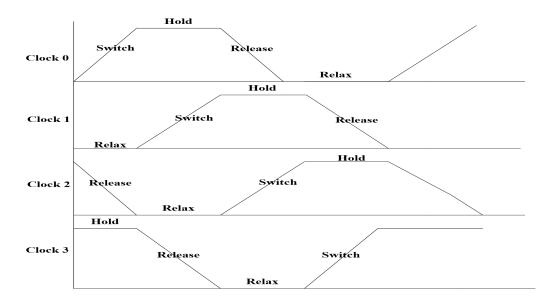


Figure 3.3.7 Four clock zones in QCA

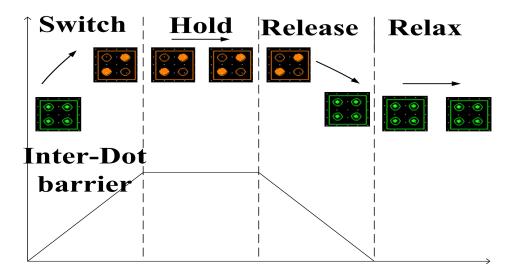


Figure 3.3.8 Four clock zones states in QCA

3.4 BASIC LOGIC GATES IN QCA

The QCA cells can be arranged in a particular fashion to easily create traditional logic gates. The basic gates in QCA technology are the inverter and the majority gate

3.4.1 INVERTER

Figure 3.4.1 and Figure 3.4.2 shows two ways of creating inverters. In Figure 3.4.1 the inverter uses only two cells which are displaced with respect to each other. It can be observed that the gate cells reach the ground state when they have opposite polarities as the electrons are farthest apart. This inverter suffers from signal integrity issues because the displaced cell does not get highly polarized in opposite direction than previous cell. Figure 3.4.2 shows a different type of inverter which is bigger in size but is more robust when compared of two-cell inverter. Another advantage of this inverter is that the negated output is aligned to the input. This would be helpful, for instance, in a bigger QCA circuits when a signal needs to be inverted and still connected to an input of a QCA-gate.

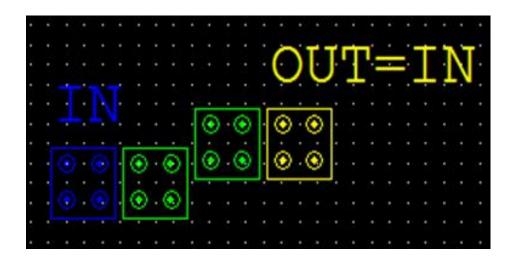


Figure 3.4.1 QCA Simpler 2 cell inverter

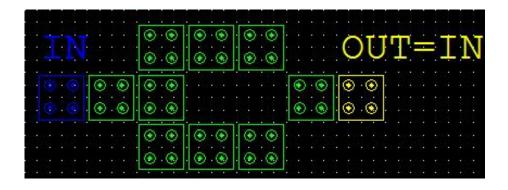


Figure 3.4.2 QCA Larger inverter

3.4.2 MAJORITY, AND, OR GATES

The majority gate is illustrated in Figure 3.4.3. The output F is defined as F = AB+AC+BC. The output cell of the gate polarizes to the computation cell in the center of the gate. The output F can be propagated using a QCA wire which can then act as an input to other gates. The majority gate can be used to build the AND and OR gates. If one of the inputs is fixed to 0/1, the resulting function F is the AND/OR of remaining two inputs.

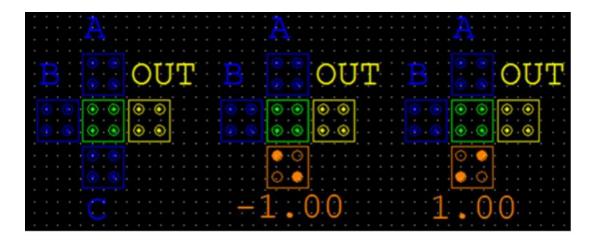


Figure 3.4.3 QCA Majority, AND, OR gates

3.4.3 UNIVERSAL GATES NAND, NOR GATES

In addition to AND, OR, and NOT gates, other logic gates like NAND and NOR are also used in the design of digital circuits shown in Figure 3.4.4 and Figure 3.4.5. The NAND and NOR gates are universalgates. A universal gate is a gate which can implement any Boolean function without need to use any other gate type.

The NAND gate represents the complement of the AND operation. Its name is an abbreviation of NOT AND. The graphic symbol for the NAND gate consists of an AND symbol with a bubble on the output, denoting that a complement operation is performed on the output of the AND gate

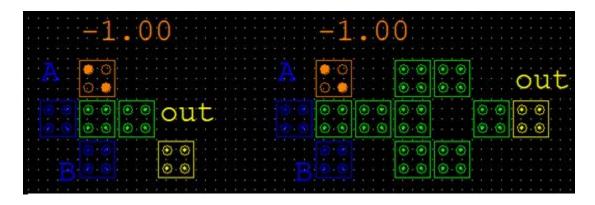


Figure 3.4.4 QCA NAND gate

The NOR gate represents the complement of the OR operation. Its name is an abbreviation of NOT OR. The graphic symbol for the NOR gate consists of an OR symbol with a bubble on the output, denoting that a complement operation is performed on the output of the OR gate.

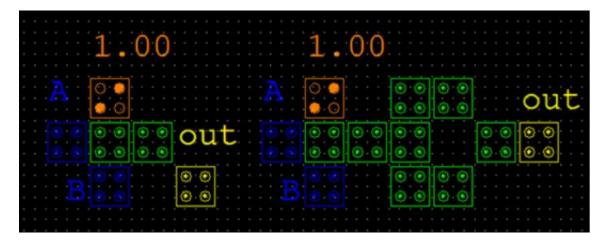


Figure 3.4.5 QCA NOR gate

CHAPTER 4

RING COUNTER USING FLIP FLOP

4.1 RING COUNTER

A ring counter is a type of counter composed of flip-flops connected into a shift register, with the output of the last flip-flop fed to the input of the first, making a "circular" or "ring" structure shown in Figure 4.1.4.

There are two types of ring counters:

- A straight ring counter, also known as a one-hot counter, connects the output of the last shift register to the first shift register input and circulates a single one (or zero) bit around the ring.
- A twisted ring counter, also called switch-tail ring counter, walking ring counter, Johnson counter, or Mobius counter, connects the complement of the output of the last shift register to the input of the first register and circulates a stream of ones followed by zeros around the ring.

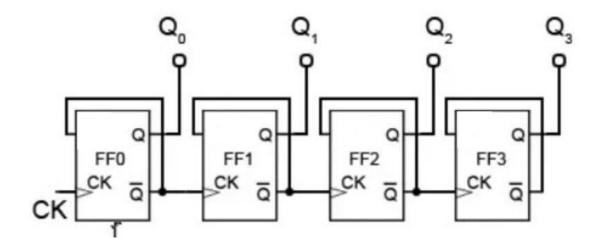


Figure 4.1 4 bit Ring Counter Logic Diagram

Design of ring counter using following flip flops

- SR-Flip Flop
- JK- Flip Flop

- T- Flip Flop
- D- Flip Flop

4.2 SR-FLIP FLOP

The SR flip-flop, also known as a SR Latch Figure 4.2, can be considered as one of the most basic sequential logic circuit possible. This simple flip-flop is basically a one-bit memory bistable device that has two inputs, one which will "SET" the device (meaning the output ="1"), and is labelled S and one which will "RESET" the device (meaning the output="0"),labelled R. Then the SR description stands for "Set-Reset". The reset input resets the flip-flop back to its original state with an output Q that will be either at a logic level "1" or logic "0" depending upon this set/reset condition shown in Table 4.1. The characteristic equation of SR Flip Flop is Qn+1 = S + QnR"

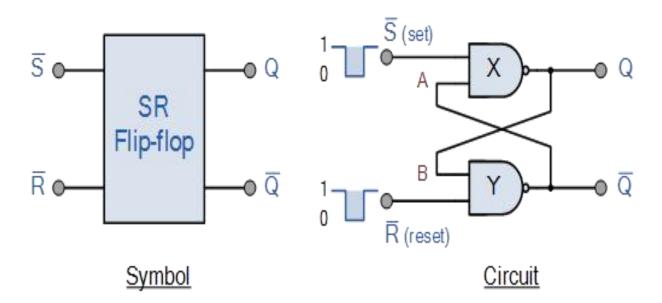


Figure 4.2 Symbol and Circuit of SR-FF

Table 4.1 SR-FF Excitation Table

Qn	Qn+1	S	R
0	0	0	X
0	1	1	0
1	0	0	1
1	1	X	0

4.3 JK- FLIP FLOP

JK flip Flop is the most widely used of all the flip-flop designs and is considered to be a universal flip-flop circuit. The two inputs labelled "J" and "K" are not shortened abbreviated letters of other words, such as "S" for Set and "R" for Reset, but are themselves autonomous letters chosen by its inventor Jack Kilby to distinguish the flip-flop design from other types. The sequential operation of the JK flip flop is exactly the same as for the previous SR flip-flop with the same "Set" and "Reset" inputs.

The difference this time is that the "JK flip flop" has no invalid or forbidden input states of the SR Latch even when S and R are both at logic "1". The JK flip flop is basically a gated SR flip-flop with the addition of a clock input circuitry that prevents the illegal or invalid output condition that can occur when both inputs S and R are equal to logic level "1". Due to this additional clocked input, a JK flip-flop has four possible input combinations, "logic 1", "logic 0", "no change" and "toggle"shown in Table 4.2.

The symbol for a JK flip flop (Figure 4.3) is similar to that of an SR Bistable Latch as seen in the previous tutorial except for the addition of a clock input. The characteristic equation of JK Flip Flop is Qn+1 = Qn (JK + JK') + Qn (J'K' + JK')

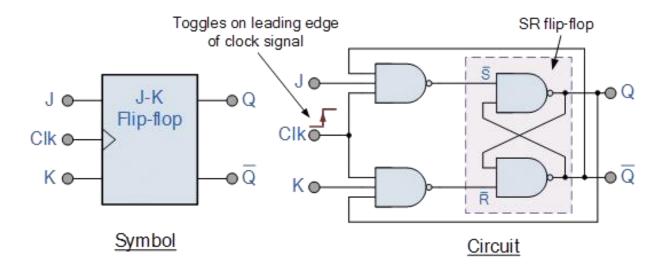


Figure 4.3 Symbol and Circuit of JK-F

Table 4.2 JK-FF Excitation Table

Qn	Qn+1	S	R
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

4.4 T-FLIP FLOP

The T or "toggle" flip-flop changes its output on each clock edge, giving an output which is half the frequency of the signal to the T input shown in Figure 4.4. It is useful for constructing binary counters, frequency dividers, and general binary addition devices. It can be made from a J-K flip-flop by tying both of its inputs high. The characteristic equation of T Flip Flop is $Q(t+1) = T'(t)Q(t) + T(t)Q'(t) = T(t) \oplus Q(t)$. The excitation table of T flip flop is shown in Table 4.3.

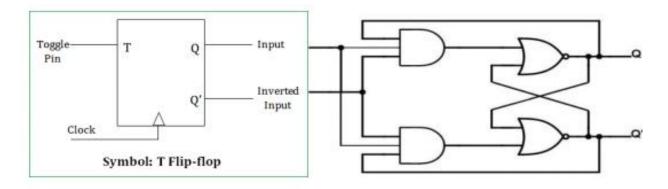


Figure 4.4 Symbol and Circuit of T-FF

Table 4.3 T-FF Excitation Table

5	Input	
Present	Next	Т
0	0	0
0	1	1
1	0	1
1	1	0

4.5 D-FLIP FLOP

The D-type flip-flop in Figure 4.5 is a modified Set-Reset flip-flop with the addition of an inverter to prevent the S and R inputs from being at the same logic levelOne of the main disadvantages of the basic SR NAND Gate Bistable circuit is that the indeterminate input condition of SET = "0" and RESET = "0" is forbidden. This state will force both outputs to be at logic "1", over-riding the feedback latching action and whichever input goes to logic level "1" first will lose control, while the other input still at logic "0" controls the resulting state of the latch. But in order to prevent this from happening an inverter can be connected between the "SET" and the "RESET" inputs to produce another type of flip flop circuit known as a Data Latch, Delay flip flop, D-type pistable, D-type flip flop or just simply a D flip flop as it is more generally called.

The D Flip Flop is by far the most important of the clocked flip-flops as it ensures that ensures that inputs S and R are never equal to one at the same time. The D-type flip flop are constructed from a gated SR flip-flop with an inverter added between the S and the R inputs to allow for a single D (Data) input. Then this single data input, labelled "D" and is used in place of the "Set" signal, and the inverter is used to generate the complementary "Reset" input thereby making a level-sensitive D-type flip-flop from a level-sensitive SR-latch as now S = D and R = not D as shown. The characteristic equation of D Flip Flop is Q(t+1) = D(t). The excitation table of D flip flop is shown in Table 4.4.

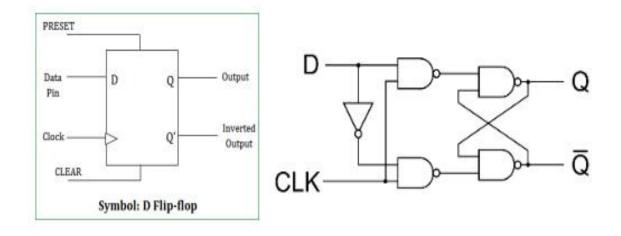


Figure 4.5 Symbol and Circuit of D-FF

Table 4.4 D-FF Excitation Table

Q(t+1)	Q(t)	D
0	0	0
0	1	1
1	0	0
1	1	1

CHAPTER 5

EXISTING METHOD

The QCA-based 4-bit ring counter presents a significant improvement in terms of area efficiency and power consumption compared to traditional CMOS-based implementations. In CMOS design, the 4-bit ring counter requires multiple transistors, interconnections, and routing layers, leading to higher area utilization and complex circuit layouts. The presence of interconnect parasitics and leakage currents in CMOS technology further contributes to higher power dissipation, making it less suitable for ultra-low-power applications. In contrast, QCA technology eliminates the need for transistors, replacing them with quantum-dot cells that rely on electron tunneling for state transitions. This results in significantly reduced area requirements due to minimal interconnect complexity and compact cell-based designs.

In terms of area efficiency, CMOS-based designs require larger chip space due to the presence of metal routing and additional control circuitry. For example, a 4-bit ring counter implemented in CMOS typically occupies a larger silicon footprint when synthesized in Microwind or Cadence, primarily due to the presence of individual transistors for each flip-flop, along with clocking and interconnect logic. On the other hand, the QCA-based counter, when simulated in QCADesigner, demonstrates a much smaller circuit layout, with an optimized majority gate and inverter-based design. The reduction in physical circuit complexity allows QCA to offer higher integration density, making it an ideal candidate for future nanoelectronic circuit design.

When considering power consumption, CMOS circuits exhibit higher dynamic and static power dissipation due to switching transients, leakage currents, and short-circuit power losses. Asynchronous counters in CMOS require constant clocking and power delivery, further increasing energy consumption. Conversely, the QCA-based design benefits from near-zero leakage current and ultra-low switching energy, making it significantly more power-efficient. The use of localized clocking zones in QCA also ensures that only specific regions of the circuit are active at a time, further reducing unnecessary energy dissipation. While CMOS circuits suffer from voltage scaling

limitations, QCA-based architectures operate efficiently at the nanoscale, making them well-suited for low-power computing applications.

Overall, the QCA-based 4-bit ring counter offers a highly compact and energy-efficient alternative to traditional CMOS implementations. Its transistor-free design, combined with optimized clocking mechanisms, ensures minimal area usage and lower power dissipation. As CMOS technology approaches scalability and efficiency limitations, QCA presents itself as a viable next-generation alternative for designing low-area, high-speed sequential circuits.

CHAPTER 6

PROPOSED METHOD

In this project, we have designed and analyzed 4-bit Ring Counters using different types of flip-flops, namely D Flip-Flop, JK Flip-Flop, SR Flip-Flop, and T Flip-Flop, using QCA Designer. Our main objective is to minimize the area and reduce the number of QCA cells compared to traditional designs. Among all the proposed designs, the 4-bit Ring Counter using D Flip-Flop has achieved the lowest QCA cell count and the smallest circuit area.

6.1 DESIGN OF 4-BIT RING COUNTER USING D FLIP-FLOP

The D Flip-Flop-based 4-bit Ring Counter Figure 6.2 exhibits superior performance in terms of area and QCA cell count. The design follows the characteristic equation of the D Flip-Flop:

$$Q(t+1)=DQ(t+1)=D$$

Since a Ring Counter is a shift register with feedback, the first flip-flop receives an initial logic "1", while the remaining flip-flops receive "0". With each clock pulse, the logic "1" shifts through the flip-flops in a cyclic manner.

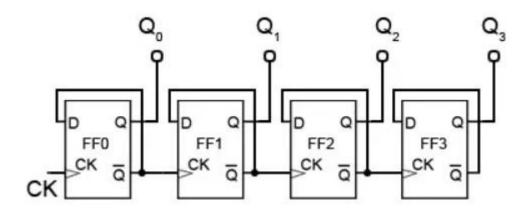


Figure. 6.1. 4 Bit Ring Counter Using D Flip Flop

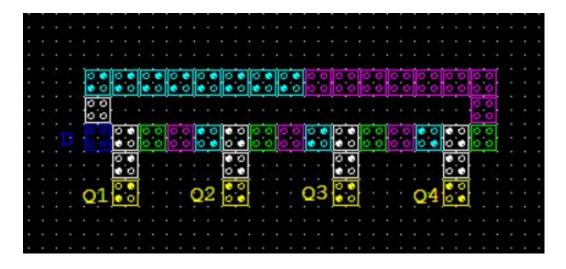


Figure. 6.2. QCA Design Of 4 Bit Ring Counter Using D Flip Flop

6.2 DESIGN OF 4-BIT RING COUNTER USING JK FLIP-FLOP

In the second approach, we implemented a 4-bit Ring Counter using JK Flip-Flop in Figure 6.4. The excitation table of a JK Flip-Flop determines its behavior in response to different input combinations. The characteristic equation of the JK Flip-Flop is:

$$Q(t+1)=JQ'+K'Q$$

For a Ring Counter, we configure the JK Flip-Flops in such a way that the circuit shifts the logic "1" across flip-flops in a cyclic manner.

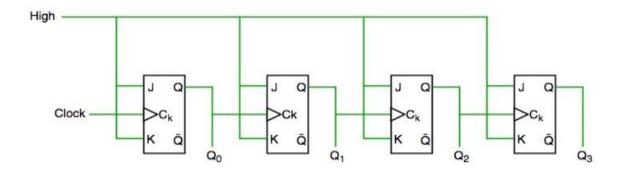


Figure. 6.3. 4 Bit Ring Counter Using JK Flip Flop

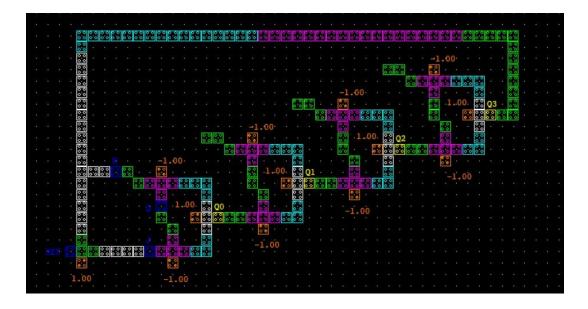


Figure. 6.4. QCA Design Of 4 Bit Ring Counter Using JK Flip Flop

6.3 DESIGN OF 4-BIT RING COUNTER USING SR FLIP-FLOP

For the third design, we utilized SR Flip-Flop to implement the 4-bit Ring Counter (Figure 6.6). The characteristic equation of the SR Flip-Flop is:

$$Q(t+1)=S+R'Q$$

To ensure proper shifting behavior in the Ring Counter, we configured the Set (S) and Reset (R) inputs appropriately.

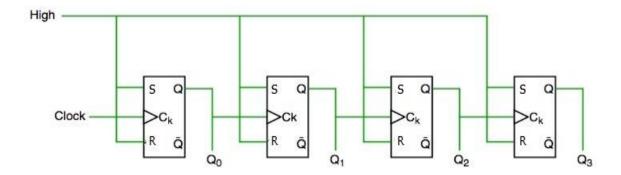


Figure. 6.5. 4 Bit Ring Counter Using SR Flip Flop

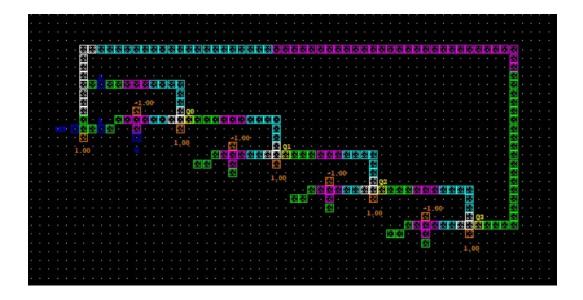


Figure. 6.6. QCA Design Of 4 Bit Ring Counter Using SR Flip Flop

6.4 DESIGN OF 4-BIT RING COUNTER USING T FLIP-FLOP

The final design utilizes T Flip-Flops to construct the 4-bit Ring Counter. The characteristic equation of the T Flip-Flop is:

$$Q(t+1)=T \oplus Q$$

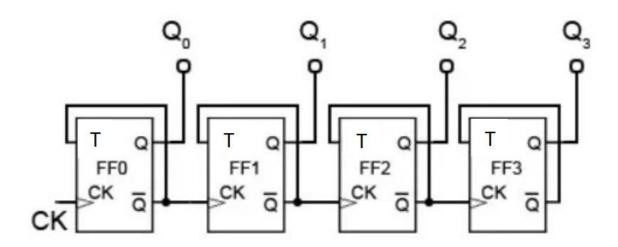


Figure. 6.7. 4 Bit Ring Counter Using T Flip Flop

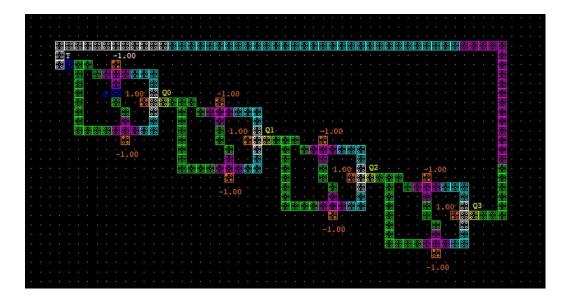


Figure. 6.8. QCA Design Of 4 Bit Ring Counter Using T Flip Flop

For a Ring Counter, the T Flip-Flops must be triggered in such a way that the "1" bit shifts through each stage sequentially.

The D Flip-Flop-based 4-bit Ring Counter is the most area-efficient design, requiring only 40 QCA cells and occupying 0.03 µm². The JK Flip-Flop-based Ring Counter is a moderately efficient design with 167 QCA cells and 0.35 µm² area. The SR Flip-Flop-based Ring Counter requires 173 QCA cells and occupies 0.44 µm². The T Flip-Flop-based Ring Counter has the highest resource consumption, requiring 200 QCA cells and 0.47 µm². Through our analysis, we conclude that choosing D Flip-Flop for the 4-bit Ring Counter leads to significant area reduction, making it the best candidate for implementation in QCA-based circuits.

CHAPTER 7

SOFTWARE REQUIRED

7.1 QCA DESIGNER

QCA Designer (Figure 7.1) is a specialized simulation tool developed for designing, testing, and analyzing Quantum-Dot Cellular Automata (QCA) circuits. It serves as a fundamental platform for researchers and engineers exploring QCA-based nanotechnology, offering layout design, logic verification, and circuit optimization capabilities. Unlike traditional transistor-based simulators, QCA Designer allows the visualization and simulation of quantum-dot interactions, enabling precise modeling of sequential and combinational logic circuits. The tool provides multiple simulation engines, including the Bistable Approximation and Coherence Vector Model, which help analyze state transitions, polarization effects, and stability in QCA circuits. It supports the design of fundamental logic gates (majority gate, inverter, XOR, AND, OR, NAND, NOR) and complex sequential elements (flip-flops, latches, shift registers, and counters). One of the key features of QCA Designer is its clocking mechanism, which allows users to define the four-phase clock zones, ensuring proper data propagation and synchronization in QCA circuits.

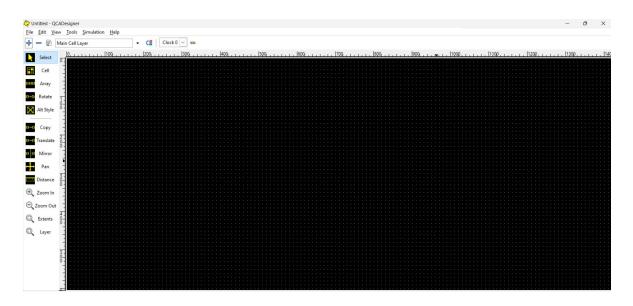


Figure. 7.1. QCA Designer tool

CHAPTER 8

RESULT & DISCUSSION

In this section, we present the simulation outputs, QCA cell counts, and area analysis for the 4-bit asynchronous ring counter implemented using D Flip-Flop, JK Flip-Flop, SR Flip-Flop, and T Flip-Flop. The performance of each design is compared based on cell count and circuit area to identify the most optimized configuration.

8.1 SIMULATION OUTPUT – 4-BIT RING COUNTER USING D FLIP-FLOP

The D Flip-Flop-based ring counter demonstrates the lowest cell count and smallest area among all designs. The D flip-flop, with the next state Q(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+1)=DQ(t+



Figure. 8.1. Simulation of 4 bit Ring Counter Designs using D Flip Flop

Table 8.1 Output table for 4 bit Ring Counter using D Flip Flop

Clock Cycle	Q3	Q2	Q1	Q0	D Input(Next State)
0	0	0	0	1	1 0 0 0
1	1	0	0	0	0100
2	0	1	0	0	0 0 1 0
3	0	0	1	0	0 0 0 1

8.2 SIMULATION OUTPUT – 4-BIT RING COUNTER USING JK FLIP-FLOP

The JK Flip-Flop-based ring counter requires more QCA cells and area compared to the D Flip-Flop. The output of the JK flip-flop-based ring counter is shown in Figure 8.2, with the characteristic equation Q(t+1) = JQ' + K'Q. This design requires 167 QCA cells and occupies $0.35~\mu m^2$ of circuit area. While the design is functionally accurate, it consumes significantly more QCA cells and area compared to the D flip-flop-based ring counter, making it less optimized in terms of resource efficiency. The increased complexity arises from the additional input conditions (J and K) and the need to manage both set and reset states, leading to higher spatial requirements and more computational elements.

Table 8.2 Output table for 4 bit Ring Counter using JK Flip Flop

Clock Cycle	Q3	Q2	Q1	Q0	J	K
0	0	0	0	1	1000	0 1 1 1
1	1	0	0	0	0100	1 0 1 1
2	0	1	0	0	0 0 1 0	1 1 0 1
3	0	0	1	0	0 0 0 1	1110

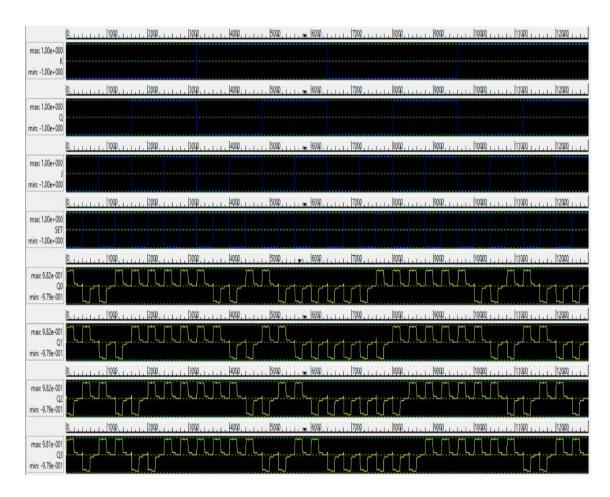


Figure. 8.2. Simulation of 4 bit Ring Counter Designs using JK Flip Flop

8.3 SIMULATION OUTPUT – 4-BIT RING COUNTER USING SR FLIP-FLOP

The SR Flip-Flop-based ring counter also demonstrates increased resource consumption. The output of the SR flip-flop-based ring counter follows the characteristic equation Q(t+1) = S + R'Q, requiring 173 QCA cells and occupying 0.44 μm^2 of circuit area. This design is slightly less optimized than the JK flip-flop-based ring counter due to its higher cell count and larger area consumption. The increased resource usage stems from the need to manage both the set (S) and reset (R) inputs, which adds complexity to the circuit. While it maintains functional accuracy, the higher spatial and structural requirements make it less efficient compared to both D and JK flip-flop-based designs.

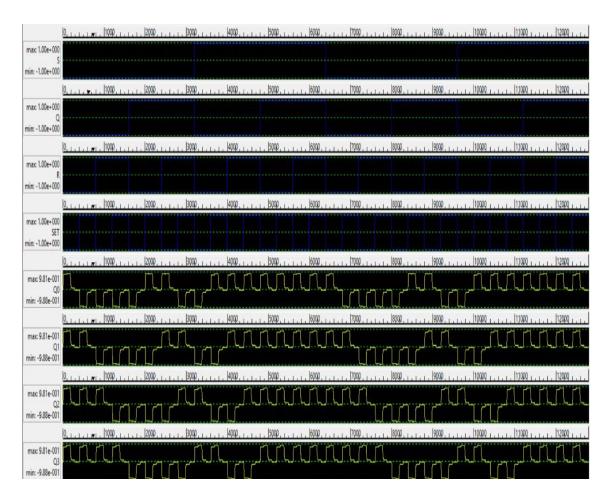


Figure. 8.3 Simulation of 4 bit Ring Counter Designs using SR Flip Flop

Table 8.3 Output table for 4 bit Ring Counter using SR Flip Flop

Clock Cycle	Q3	Q2	Q1	Q0	S	R
0	0	0	0	1	1 0 0 0	0 1 1 1
1	1	0	0	0	0 1 0 0	1011
2	0	1	0	0	0 0 1 0	1 1 0 1
3	0	0	1	0	0 0 0 1	1110

8.4 SIMULATION OUTPUT – 4-BIT RING COUNTER USING T FLIP-FLOP

The T flip-flop-based ring counter, shown in Figure 7.4, follows the characteristic equation $Q(t+1) = T \oplus Q$, where the next state toggles with each clock cycle. This design requires 200 QCA cells and occupies 0.47 μm^2 of circuit area, making it the least optimized in terms of resource consumption. The higher complexity arises from the toggle operation (XOR logic), which demands more structural components and increased spatial allocation. Compared to the D, JK, and SR flip-flop-based designs, the T flip-flop consumes the most QCA cells and circuit area, making it the least efficient choice for implementing the ring counter.



Figure. 8.4. Simulation of 4 bit Ring Counter Designs using SR Flip Flop

Table 8.4 Output table for 4 bit Ring Counter using T Flip Flop

Clock Cycle	Q3	Q2	Q1	Q0	T Input(Next State)
0	0	0	0	1	1 0 0 0
1	1	0	0	0	0 1 0 0
2	0	1	0	0	0 0 1 0
3	0	0	1	0	0 0 0 1

Table 8.5. Comparative Analysis of Flip-Flop Based Ring Counters

Design	FLip-Flop Used	QCA Cells	Circuit Area(µm²)
Proposed Ring Counter	D Flip-Flop	40	0.03
Proposed Ring Counter	T Flip-Flop	167	0.35
Proposed Ring Counter	SR Flip-Flop	173	0.44
Proposed Ring Counter	JK Flip-Flop	200	0.47

The D flip-flop-based ring counter is the most area-efficient and cell-efficient configuration, utilizing only 40 QCA cells and occupying $0.03~\mu m^2$ of circuit area. In contrast, the JK, SR, and T flip-flop designs exhibit higher resource consumption, with the T flip-flop being the most resource-intensive, requiring 200 QCA cells and $0.47~\mu m^2$ of area. This performance analysis clearly demonstrates that the D flip-flop is the optimal choice for implementing 4-bit ring counters in QCA circuits, offering minimal resource consumption and superior efficiency compared to other flip-flop configurations.

CONCLUSION

The design and implementation of a 4-bit ring counter using Quantum-Dot Cellular Automata (QCA) demonstrate significant improvements in circuit area efficiency compared to traditional CMOS-based implementations. By leveraging QCA's majority gate-based logic and minimal interconnect complexity, the proposed design successfully reduces circuit footprint and layout congestion, making it a promising alternative for nanoelectronic applications. Unlike CMOS-based designs, which require transistors, metal interconnections, and clock distribution networks, the QCA-based counter eliminates transistor-related limitations, resulting in a highly compact and scalable architecture.

Simulation results obtained using QCADesigner confirm the correct functionality and optimized layout of the ring counter, ensuring stable state transitions while minimizing area overhead. Compared to CMOS implementations in Microwind or Vivado, the QCA-based design provides higher integration density, allowing for efficient realization of sequential circuits at the nanoscale. The study also highlights the advantage of localized clocking mechanisms in QCA, further contributing to circuit optimization.

Overall, this research establishes QCA as a viable alternative to CMOS technology for designing low-area, high-speed digital circuits. Future work can focus on expanding the design to higher-bit counters, improving fault tolerance, and exploring hybrid QCA-CMOS integration to further enhance scalability and practical implementation in VLSI and nanoelectronics.

FUTURE ENHANCEMENTS

1.ADVANCED SYNCHRONIZATION MECHANISMS

One of the pressing challenges in large-scale QCA systems is ensuring accurate signal synchronization. Traditional clocking schemes often struggle with loops, feedback circuits, and global synchronization issues, leading to timing mismatches and signal degradation.

- Firing Squad Synchronization Problem (FSSP)-based strategies have shown promise, but further research is needed to generalize and optimize them for different QCA topologies.
- Future enhancements should focus on developing global and hierarchical clocking architectures that allow precise control over signal propagation.
- Implementing adaptive clocking techniques could minimize latency, enhance throughput, and avoid glitches in feedback-heavy sequential circuits.

2.INTEGRATION OF REVERSIBLE LOGIC FOR ENERGY EFFICIENCY

Reversible logic is essential for low-power computation as it theoretically produces no heat due to information loss.

- Incorporating reversible gates and logic blocks in QCA circuits—such as reversible encoders, ALUs, and memory units—can significantly reduce energy dissipation.
- Designs like the BS1 block and reversible ALUs demonstrate early success, and future work should focus on universal reversible building blocks that support modular circuit development.

3.SCALABLE AND FLEXIBLE PROGRAMMABLE ARCHITECTURES

Traditional programmable logic structures often face limitations in scalability and reconfigurability

- Advanced QCA-based Programmable Logic Arrays (PLAs) using crossbar structures and majority gate logic offer promising alternatives.
- Future improvements could include multi-layered PLAs, dynamic logic reconfiguration, and programmable memory units to allow versatile digital processing within a compact form.

4.IMPROVED CAD AND SIMULATION TOOLS

Current QCA design and simulation tools like QCADesigner lack the flexibility and intelligence required for complex circuit design.

- Developing AI-powered CAD environments that suggest optimal layouts, reduce redundant cells, and detect logic conflicts will greatly enhance productivity.
- Integration with tools like MATLAB, HSPICE, and Simulink, especially through ANN-based logic models, can improve simulation accuracy and circuit modeling.
- Future tools should support automatic clock zone allocation, cell placement optimization, and thermal-aware layout analysis.

5.HYBRID QCA AND CMOS SYSTEMS

While QCA shows great promise, full replacement of CMOS in near-term applications may not be feasible.

- Hybrid systems that combine QCA modules for high-speed, low-power functions with CMOS for I/O and memory can offer practical interim solutions.
- Research can focus on seamless interfacing techniques and signal conversion circuits between QCA and CMOS domains.

6.ENERGY, AREA, AND DELAY OPTIMIZATION TECHNIQUES

The minimization of power, space, and delay is critical for efficient nanoelectronic design.

- Novel layouts should aim to reduce quantum cell count, eliminate wire crossings, and minimize occupied area without compromising logic integrity
- Enhanced T-latch and shift register designs already show reduced delay and power usage, and future work could optimize these further using evolutionary algorithms or machine learning

7.SECURE AND FAULT-TOLERANT QCA CIRCUITS

As QCA circuits become more complex, ensuring their reliability and security is vital.

- Future enhancements should include redundancy techniques like triple modular redundancy (TMR), parity checkers, and self-repairing architectures.
- QCA can also be explored for low-power cryptographic circuits, including QCAbased AES or SHA units, which are ideal for embedded security systems

8.DEVELOPMENT OF COMPLEX ARITHMETIC UNIT

For QCA to become viable in general-purpose computing, it must support complex arithmetic and control functionalities.

- Research should focus on designing efficient multipliers, dividers, barrel shifters, and floating-point units in QCA.
- Additionally, optimized control units for QCA-based processors can pave the way for complete nanoscale CPUs.

9.THERMAL AND ENVIRONMENTAL STABILITY

Given QCA's sensitivity to environmental fluctuations, it is important to assess thermal reliability

- Future work should analyze thermal behavior under high-frequency operations and integrate heat dissipation strategies in dense layouts.
- Designing circuits that are tolerant to temperature variations, electromagnetic interference, and manufacturing defects is essential for commercial viability.

10. STANDARDIZATION AND BENCHMARKING OF QCA DESIGNS

A lack of standardized performance metrics often hinders fair comparison and progress tracking in QCA research.

- Establishing benchmarking standards for energy, delay, area, fault-tolerance, and scalability will improve the consistency and evaluation of designs.
- Developing open-source libraries of optimized QCA building blocks (e.g., gates, flip-flops, ALUs) can accelerate research and development in academic and industrial settings.

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