

Homework 11.1

following is the inorder traversal for multi way search tree

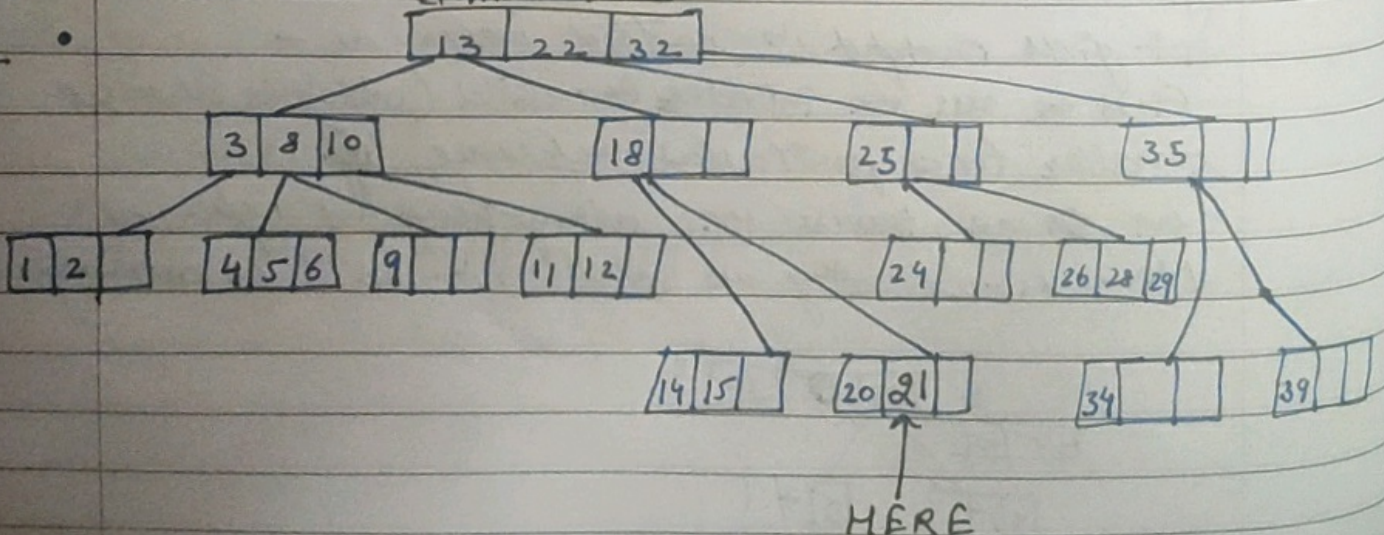
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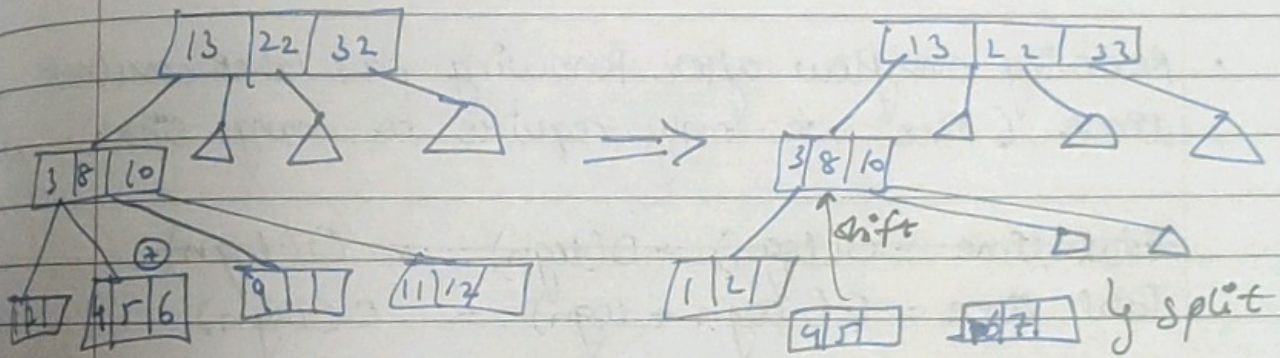
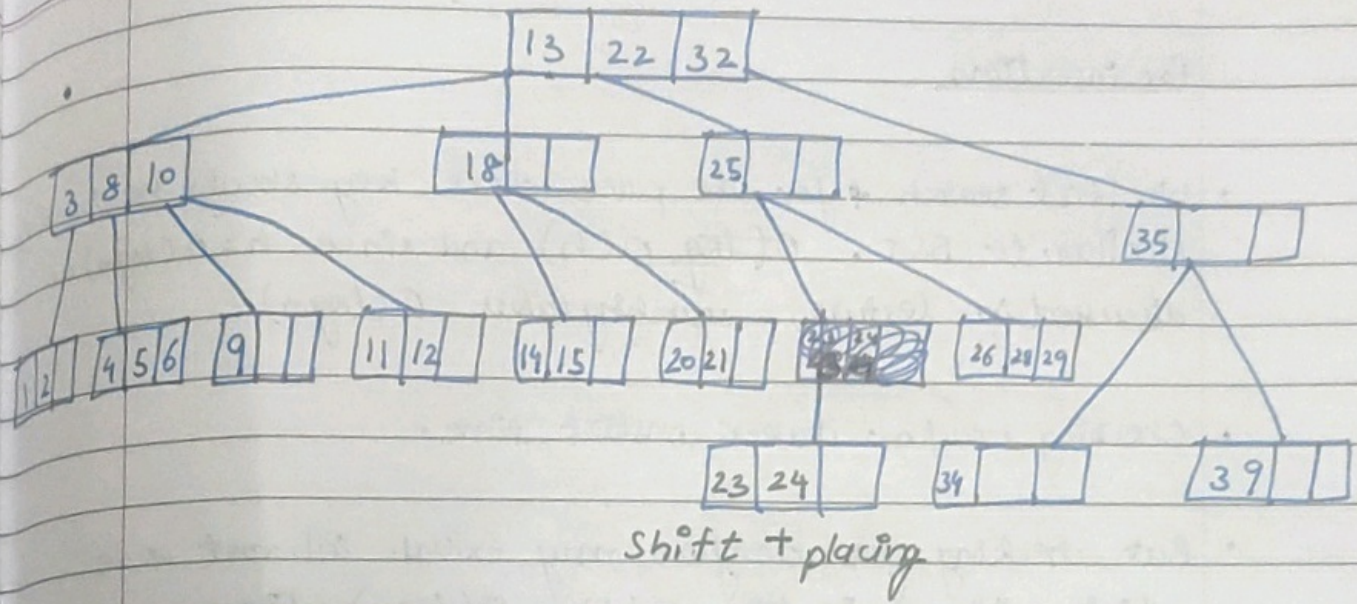
Algorithm inorder(node node)
    if (node == null)
        return
    else
        inorder(node.link[0])
        for (int i = 0; i < d; i++) // d is number of keys nodes and
            visit key[i] // consistent with Dr. Nooreen lecture
            inorder(node.link[i+1])
    
```

- Note:-
- Array link contains $d+1$ entries of respective links.
 - Array key contains the keys in a node in sorted order.
 - There are $d+1$ links for d keys.
 - First we call the inorder for child which is leftmost and plus the shortest.
 - Now since keys are in sorted and all the links are in accordance to links, traversing the array of keys from left to right AND calling function for corresponding links would yield the sorted output.

Homework 11.2

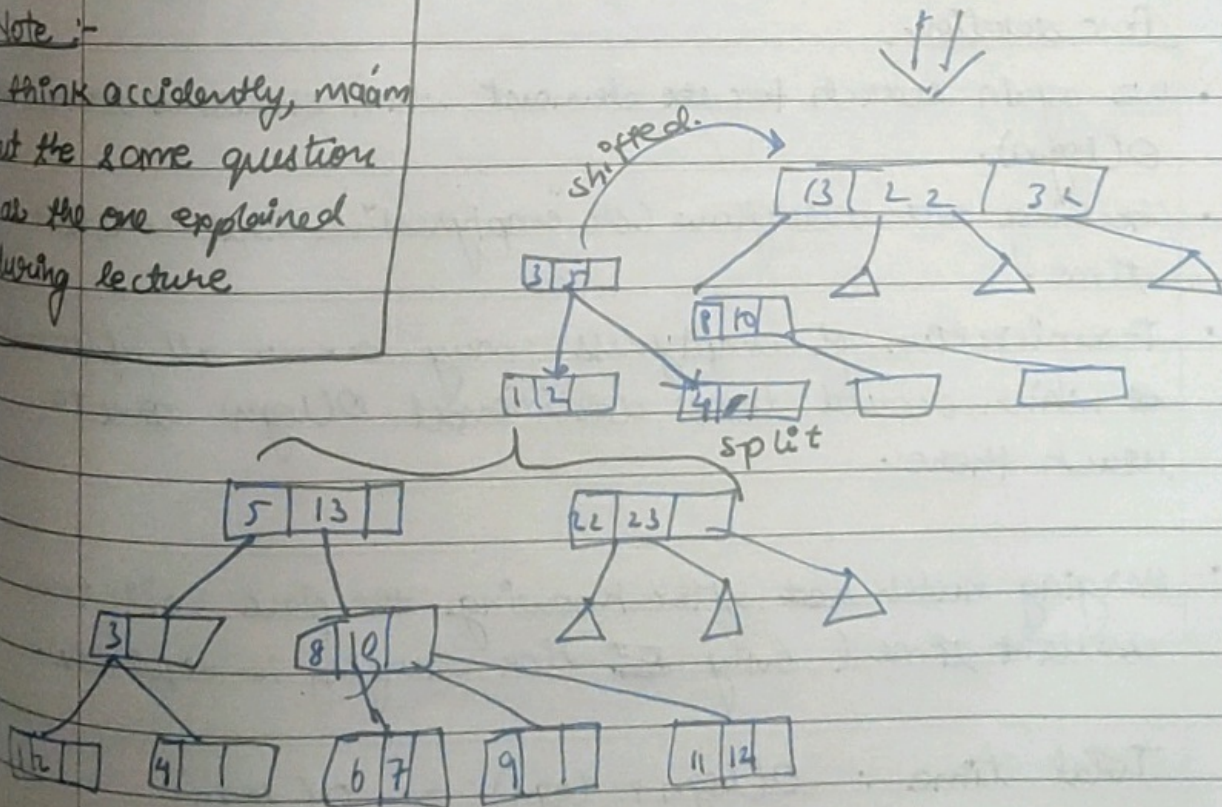
Ans →





Note :-

I think accidentally, main
 but the same question
 as the one explained
 during lecture



Homework 11:3

for insertion

- We first search for the place where key should be inserted, similar to BST. $O(\log n)$ and since $h = O(\log n)$ as discussed in lecture, searching takes $O(\log n)$.
- Checking overflow takes constant time.
- But checking for overflow may extend till root node which will again take $O(h) = O(\log n)$ time.
- Removing overflow after knowing place takes constant time (since we only require to change links).

$$\text{Total time} = O(\log n) + O(\log n) = O(\log n)$$

$$\text{Total time} = O(\log n + \log n) = O(\log n)$$

for deletion

- We again search for the element which should be removed $O(\log n)$.
- Checking ~~for~~ underflow (or "emptiness") takes constant time.
- Termination of emptiness may occur all up to root which would take additional $O(\log n)$ time to reach there.
- Merging nodes ~~and~~ after knowing the place will take constant time (only ~~the~~ link changing is required).

$$\text{Total time} : O(\log n + \log n) = O(\log n)$$