

Conventional ML

- Prepare the data
- Train model from training data to estimate models
- Parameters
- Stores Models in Suitable forms
- Predict unseen Query instance

Instance Based Learning

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- Do not train model
- Pattern discovery postponed until scoring query

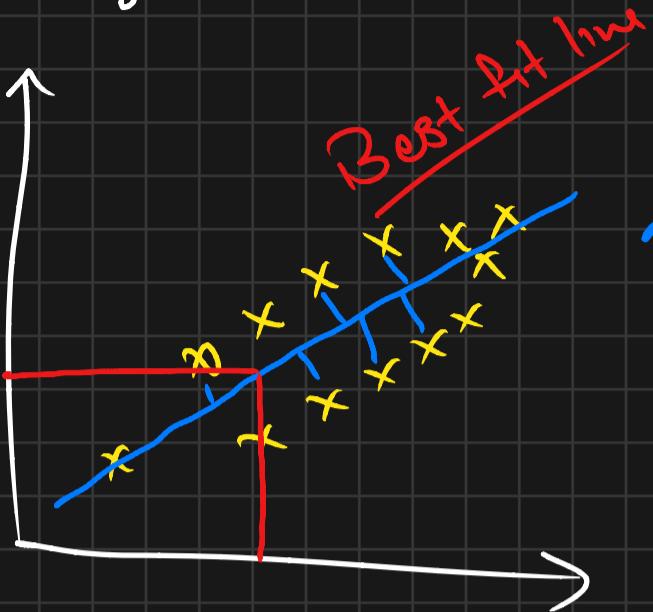
- There is no model to store

Simple Linear Regression

Supervised ML:

weight	height
74	170
80	180
75	175.5cm

new weight \rightarrow Model \rightarrow height

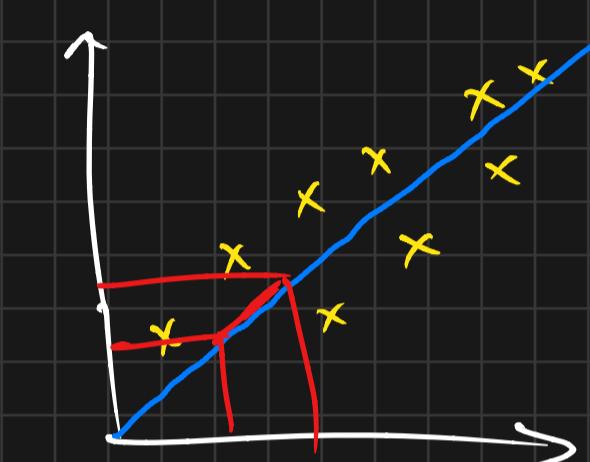


{ error sum should be
minimum}

$$y = mx + c$$

$$y = \beta_0 + \beta_1 x$$

$$h_{\theta}(x) = \theta_0 + \theta_1 x$$



$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

θ_0 = Intercept

θ_1 = Slope or coefficient

$h_{\theta}(x)$ = Predicted Point

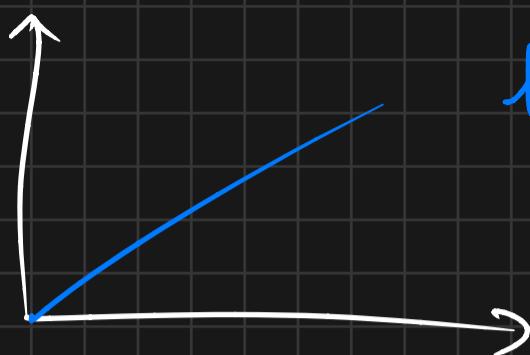
Cost function

$$J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

- mean squared error

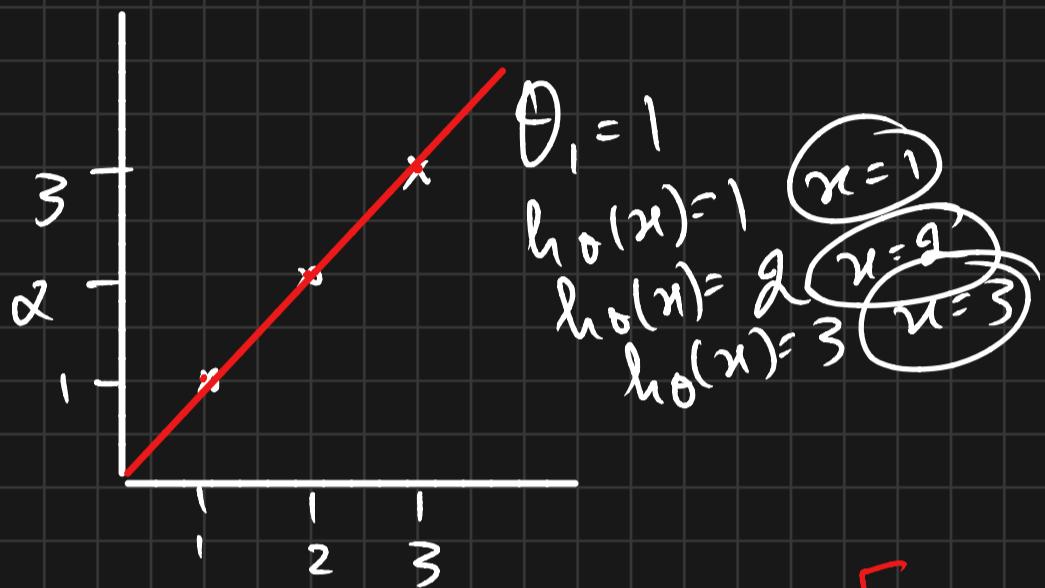
$$\text{minimize } J(\theta_0, \theta_1) = \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

$$① h_0(x) = \theta_0 + \theta_1 x \quad [\underline{\theta_0 = 0}]$$



$$h_0(x) = \theta_1 x$$

x	y
1	1
2	2
3	3



$$\theta_1 = 1$$

$$h_0(x) = 1$$

$$h_0(x) = 2$$

$$h_0(x) = 3$$

$$J(\theta_0, \theta_1) = \frac{1}{\alpha \times 3} \sum_{i=1}^3 [(1-1)^2 + (2-2)^2 + (3-3)^2]$$

$$J(\theta_0, \theta_1) = \frac{1}{\alpha \times 3}$$

$$[\underline{J = 0}]$$

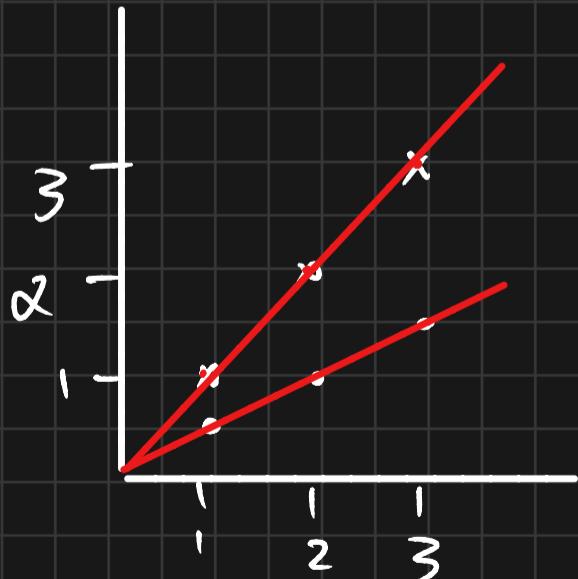
$$\text{Let } h_0(x) = \theta_1 x$$

$$h_0(x) = 0.5 \quad x = 1$$

$$\theta_1 = 0.5$$

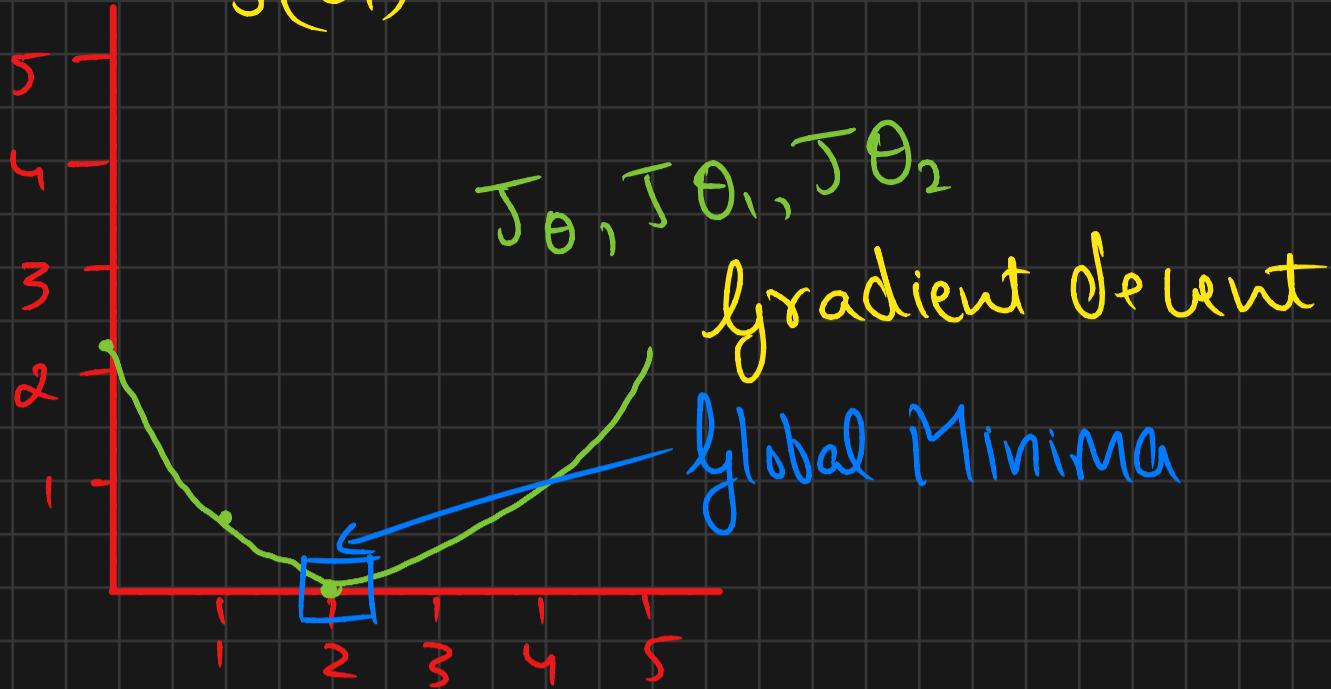
$$\theta_2 = 1$$

$$\theta_3 = 1.5$$



$$\frac{1}{\alpha \times 3} \sum_{i=1}^3 [(0.5-1)^2 + (1-1)^2 + (1.5-3)^2] = 0.58$$

$$J(\theta_1) = 0 \leftarrow$$



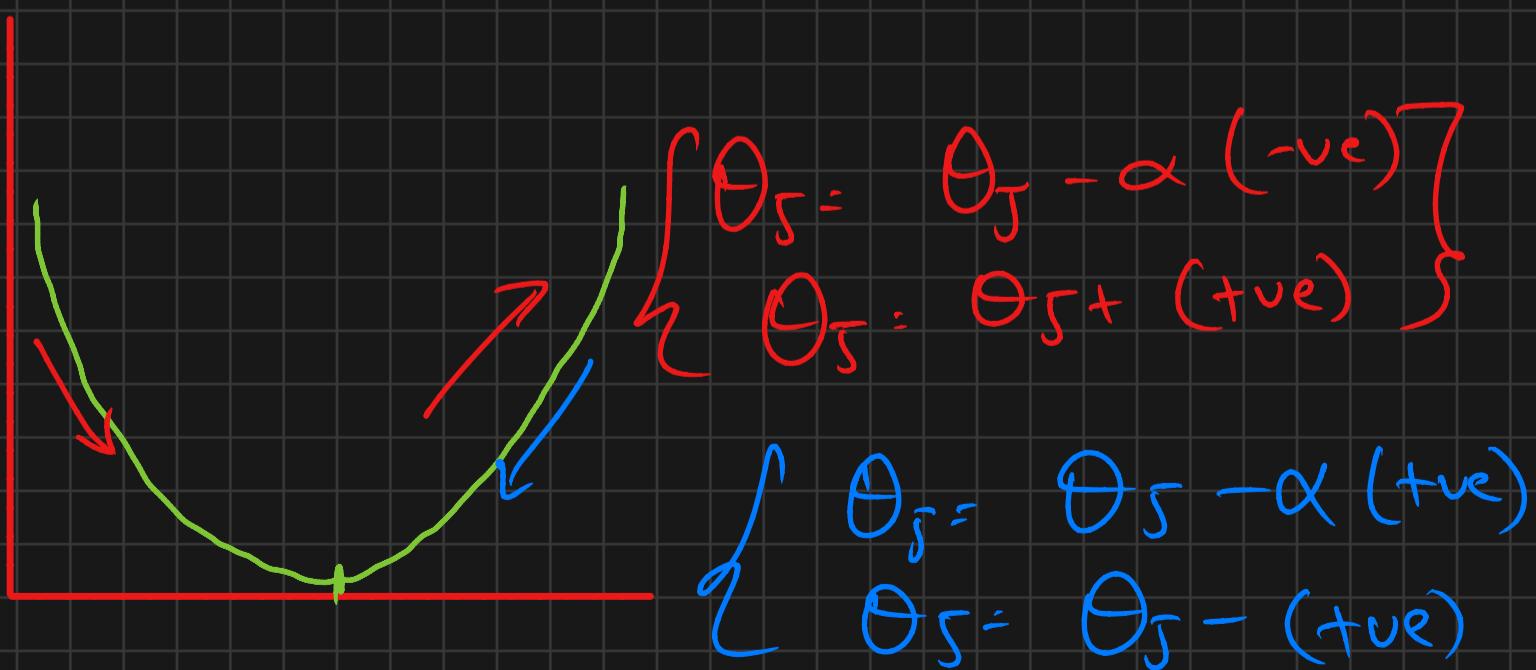
Convergence Algorithm

Optimize the changes of θ_j value

Repeat until convergence

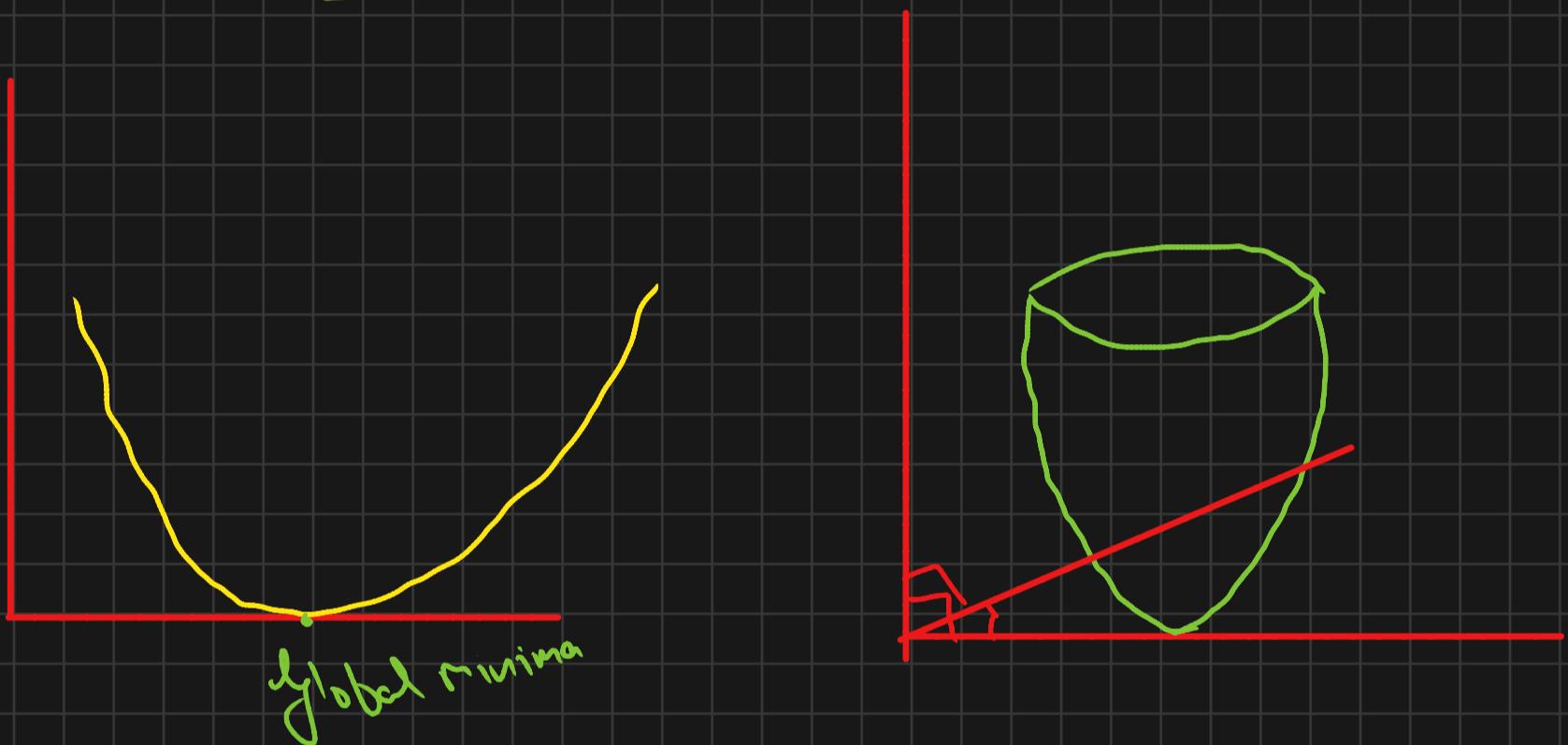
θ_j value change efficiently

$$\left\{ \theta_j = \theta_j - \alpha \frac{\partial J(\theta_j)}{\partial \theta_j} \right\}$$



α (alpha): learning Rate if it is very small
 it will keep on iterating if α is too big
 then H will vary too much

Gradient Descent



$$\frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1) = \frac{\partial}{\partial \theta_j} \frac{1}{m} \sum_{i=1}^m (h_\theta(x)^T - y^{(i)})^2$$

$$J = 0 \Rightarrow \frac{\partial}{\partial \theta_0} J(\theta_0, \theta) =$$

$$\frac{\partial}{\partial \theta_0} \frac{1}{m} \left[\sum_{i=1}^m (h_\theta(x)^T - y^i)^2 \right]$$