

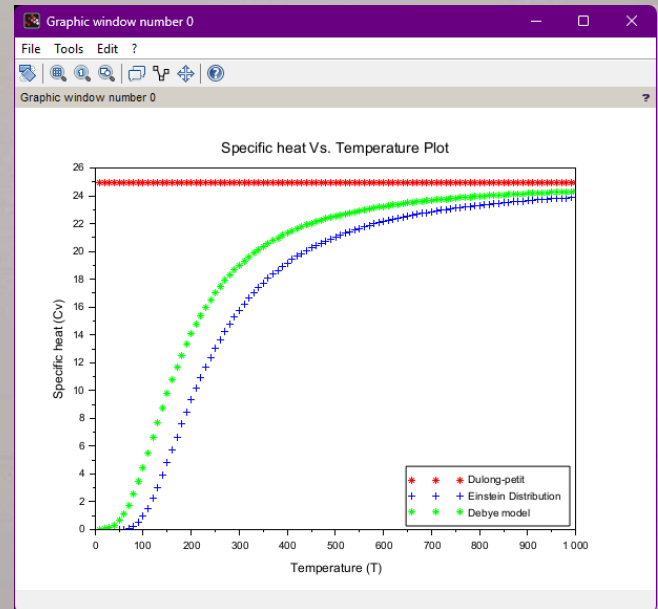
Aim: Plot specific heat of solids (a) Dulong - petit law
 (b) Einstein distribution law (c) Debye distribution for
 high & low temperature and compare them

Apparatus: Scilab with latest version

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st4.sci (P:\scilab\st4.sci) - SciNotes
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st4.sci (P:\scilab\st4.sci) - SciNotes
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1 R=8.314;
2 h=6.625*10.^-34;
3 k=1.38*10.^-23;
4 v=15*10^12;
5 for T=10:10:1000;
6     DP=3*R; //Dulong-petit-law
7     a=(h*v)/(k*T);
8     E=((3*R)*(a^2)*(exp(a))/((exp(a)-1)^2)); //Einstein-distrib
    ution-law
9     funcprot(0)
10    function c=f(x)
11    c=(x^4)*exp(x)/((exp(x)-1)^2);
12    endfunction
13    D=(9*R*((1/a)^3)*intg(0,a,f)); //Debye-Distribution-law
14    plot(T,DP,'r');
15    plot(T,E,'b+');
16    plot(T,D,'g*');
17 end
18 xlabel('Temperature (T)')
19 ylabel('Specific-heat (Cv)')
20 title('Specific-heat-Vs.-Temperature-Plot')
21 legend('Dulong-petit','Einstein-Distribution','Debye-model',4)
22 //Comparison-Results
23 printf("Comparison-Results:\n");
24 printf("At-high-temperature,-all-models-converge-to-Dulong-Petit-
    value-(3R).\n");
25 printf("At-low-temperature,-Debye-model-follows-T^3-dependence,-w
    hile-Einstein-model-deviates-from-experimental-results.\n");
26
    
```



Aim: To plot Specific heat of solids (a) Dulong - petit law, (b) Einstein distribution function, (c) Debye distribution function for high temperature & low temperature and compare them for these two cases, using Scilab

Apparatus: Scilab with latest version

Theory: Specific heat of solids is a fundamental property that describes how much heat energy is required to change the temperature of a solid material

Dulong - petit law: This law states that the molar specific heat capacity of a solid element is approximately constant at high temperature and is given by:

$$C_v = 3R \quad R - \text{Gas constant}$$

This law is derived from the classical approaches of equipartition theorem, assuming that each atom in a solid contributes equally to the total thermal energy. It holds well at high temperature but fails at low temperature, where quantum effect dominate.

Einstein model of specific heat:- He assumed that all atoms in a solid oscillate independently with the same frequency ν

$$C_v = 3R \left(\frac{x^2 e^x}{(e^x - 1)^2} \right), \quad x = \frac{h\nu}{k_B T}$$

At high temperatures ($T \gg \theta_E$), the model approaches the Dulong petit limit, $C_v \approx 3R$

At low ($T \ll \theta_E$) $C_v \propto e^{-h\nu/k_B T}$

Debye model of Specific heat: Debye extended Einstein's model by considering a continuous range of vibrational frequencies (phonons) instead of a single frequency.

$$C_v = 9R \left(\frac{T}{\theta_D} \right)^3 \int_0^{\theta_D/T} \frac{x^2 e^x}{(e^x - 1)^2} dx \quad x = \frac{h\nu}{k_B T}$$

At high temperatures $T \gg \theta_D$, The Debye model also converges to the duulong petit law

At low temperatures, the Einstein model C_v follows the Debye T^3 law

$$C_v \propto T^3$$

Code:

$$R = 8.314;$$

$$h = 6.625 \times 10^{-34};$$

$$k = 1.38 \times 10^{-23};$$

$$\nu = 15 \times 10^{12};$$

$$\text{for } T = 10 : 10 : 1000;$$

$$DP = 3R;$$

$$a = (h \times \nu) / (k \times T);$$

$$E = ((3 \times R) \times (a^2) \times \exp(a)) / (\exp(x) - 1)^2);$$

funcprof(o)

function c = f(x)

$$c = (x^4) \times \exp(x) / ((\exp(x) - 1)^2);$$

endfunction

$$\text{integral} = \text{intg}(0, a, f);$$

$$D = (9 \times R \times (1/a)^3) \times \text{integral};$$

```
plot(T, DP, 'g*');
```

```
plot(T, E, 'bt');
```

```
plot(T, D, 'g+');
```

```
end
```

```
xlabel('Temperature (T)');
```

```
ylabel('specific heat (cv)');
```

```
title('specific heat vs Temperature plot');
```

```
legend('Dulong petit', 'Einstein Distribution', 'Debye model', '4');
```

Result:

At high temperature, all models converge to Dulong petit value ($3R$)

At low temperature, Debye model follows T^3 dependence, while Einstein model deviates from experimental results