## Price relations of food commodities in regional markets of Nepal

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## 1 Retail price of rice and wheat in major districtwise Nepalese market hubs

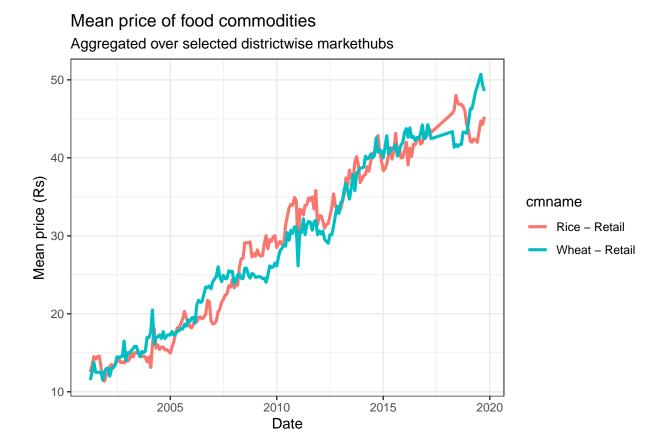
The price series of districtwise market hubs available for study is mostly imbalanced and irregular and contains data for following 21 districts.

Achham, Banke, Bhojpur, Chitwan, Dhankuta, Dhanusha, Doti, Illam, Jhapa, Jumla, Kailali, Kaski, Kathmandu, Morang, Nuwakot, Palpa, Parsa, Ramechap, Rolpa, Rupandehi, Surkhet.

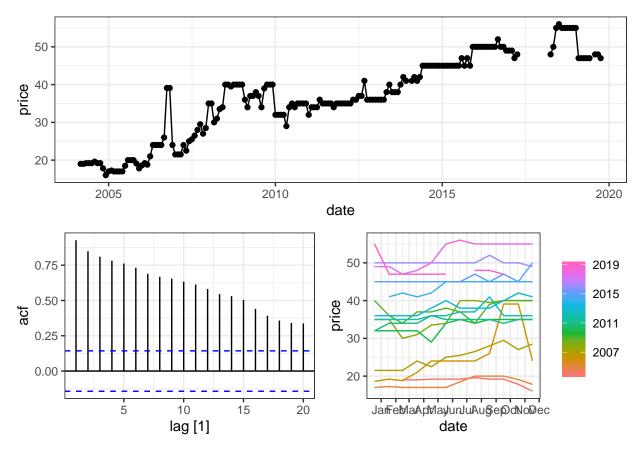
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### 1.1 Aggregate series summary

Joint time series plot of rice and wheat retail prices aggregated over selected districtwise markets.

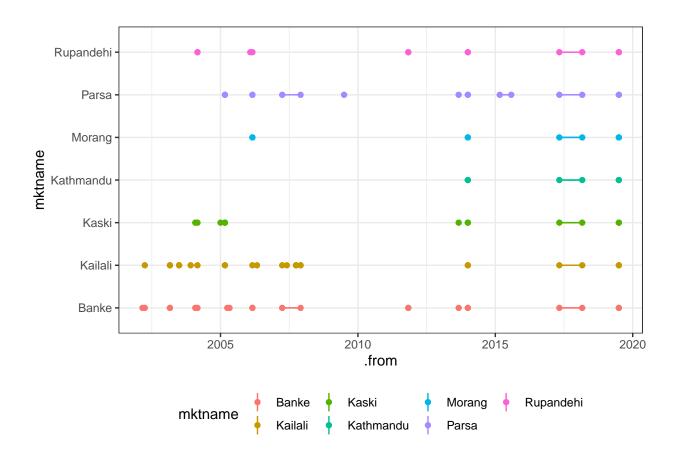


Time series plot of retail price of rice in Kathmandu market. Series has some time gaps at random periods (shown on line plot on the lower right). Similarly, autocorrelation of series for various lag, with first order difference, is presented in the lower left.



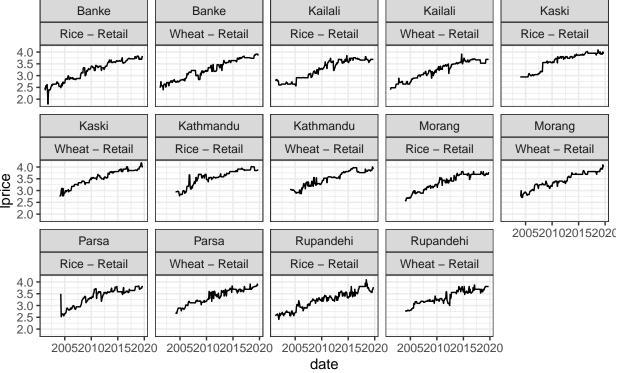
A possible measure to removing non-stationary trend in the series is by differencing (with diff). However, before progressing we confirm that justifiable lag operations can infact render the series free of trends. For this at two fundamentally different unit tests are performed – Augmented Dickey-Fueller test and KPSS test.

While the series needs detrending in order to perform regression, we also have to consider the time gaps in the available dataset.



All district market series presented after time gap filling. First order lag is used to fill the missing entries in the series. Missing values for each series are imputed independent of other series.

# Augmented log(price) of series Time gaps filled with first order lags Banke Banke



## 2 Unit root testing

## 2.1 Unit root (ADF and KPSS) test of retail price

The ADF, available in the function adf.test() (in the package tseries) implements the t-test of  $H_0: \gamma = 0$  in the regression, below.

$$\Delta Y_t = \beta_1 + \beta_2 t + \gamma Y_{t-1} + \sum_{i=1}^m \delta_i \Delta Y_{t-i} + \varepsilon_t \tag{1}$$

The null is therefore that x has a unit root. If only x has a non-unit root, then the x is stationary (rejection of null hypothesis).

The ADF test was parametrized with the alternative hypothesis of stationarity. This extends to following assumption in the model parameters;

$$-2 \leq \gamma \leq 0$$
 or  $(-1 < 1 + \phi < 1)$ 

**k** in the function refers to the number of  $\delta$  lags, i.e., 1, 2, 3, ..., m in the model equation.

Table 1: Unit root test of district market retail  $\log(\text{price})$  data of Rice

mktname	adf pvalue	adf tstatistic	adf sta- tionary	kpss pvalue	kpss tstatistic	kpss sta- tionary
Banke	0.22	-2.86	FALSE	0.01	3.70	FALSE
Kailali	0.52	-2.13	FALSE	0.01	3.72	FALSE
Kaski	0.86	-1.33	FALSE	0.01	3.20	FALSE
Kathmand	du0.45	-2.30	FALSE	0.01	3.00	FALSE
Morang	0.44	-2.32	FALSE	0.01	3.42	FALSE
Parsa Rupandeh	0.22 i 0.01	-2.86 -4.51	FALSE TRUE	0.01 0.01	2.64 3.91	FALSE FALSE

Table 2: Unit root test of district market retail log(price) data of Wheat

mktname	adf pvalue	adf tstatistic	adf sta- tionary	kpss pvalue	kpss tstatistic	kpss sta- tionary
Banke	0.01	-4.09	TRUE	0.01	3.86	FALSE
Kailali	0.47	-2.26	FALSE	0.01	3.81	FALSE
Kaski	0.05	-3.41	FALSE	0.01	3.40	FALSE
Kathman	du0.34	-2.56	FALSE	0.01	3.43	FALSE
Morang	0.03	-3.62	TRUE	0.01	3.40	FALSE
Parsa Rupandeh	0.04 ni 0.02	-3.55 -3.72	TRUE TRUE	0.01 0.01	3.05 3.16	FALSE FALSE

The number of lags k defaults to  $trunc((length(x)-1)^{(1/3)})$ , where x is the series being tested. The default value of k corresponds to the suggested upper bound on the rate at which the number of lags, k, should be made to grow with the sample size for the general ARMA(p,q) setup citation(package = "tseries").

For a Dickey-Fueller test, so only up to AR(1) time dependency in our stationary process, we set k = 0. Hence we have no  $\delta s$  (lags) in our test.

The DF model can be written as:

$$Y_t = \beta_1 + \beta_2 t + \phi Y_{t-1} + \varepsilon_t$$

It can be re-written so we can do a linear regression of  $\Delta Y_t$  against t and  $Y_{t-1}$  and test if  $\phi$  is different from 0. If only,  $\phi$  is not zero and assumption above  $(-1 < 1 + \phi < 1)$  holds, the process is stationary. If  $\phi$  is straight up 0, then we have a random walk process – all white noise.

$$\Delta Y_t = \beta_1 + \beta_2 t + \gamma Y_{t-1} + \varepsilon_t$$

Alternative to above discussed tests, the Phillips-Perron test with its nonparametric correction for autocorrelation (essentially employing a HAC estimate of the long-run variance in a Dickey-Fuller-type test instead of parametric decorrelation) may be used. It is available in the function pp.test().

#### 2.2 Unit root test based lag order differencing determination

An alternative to decomposition for removing trends is differencing (Woodward, Gray, and Elliott 2017). We define the difference operator as,

$$\nabla x_t = x_t - x_{t-1},\tag{2}$$

and, more generally, for order d

$$\nabla^d x_t = (1 - \mathbf{B})^d x_t, \tag{3}$$

Where **B** is the backshift operator (i.e.,  $\mathbf{B}^k x_t = x_{t-k}$  for  $k \ge 1$ ).

Applying the difference to a random walk, the most simple and widely used time series model, will yield a time series of Gaussian white noise errors  $\{w_t\}$ :

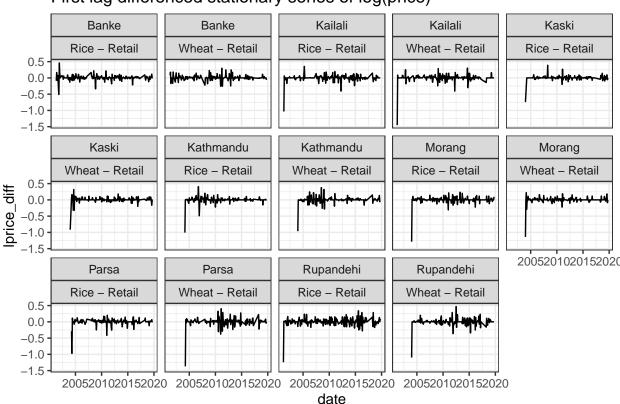
$$\nabla(x_t = x_{t-1} + w_t) x_t - x_{t-1} = x_{t-1} - x_{t-1} + w_t x_t - x_{t-1} = w_t$$
(4)

Differencing is required for *all* series to make them stationary, as inferred by the ndiffs function which employed popular unit root tests. A detailed presentation of the test routines is given below. We describe in detail the ADF test, while only tabluation of summary statistics of kpss test is made herein.

#### 2.3 Unit root tests of first order differenced series

All major districtwise market series series are non-stationary, meaning that they have a trend associated with time.

We test the logged prices of the series after first order differencing. Here we perform a more conservative Dickey-Fueller, instead of Augmented DF, test.



First lag differenced stationary series of log(price)

The first order differencing renders all series stationary.

### 3 ARIMA model

#### 3.1 AR model

A simple way to model dependence between consecutive observations is by specification of model such as one in Equation 5.

$$y_t = \mu_0 + \phi_1 y_{t-1} + \varepsilon_t \tag{5}$$

Where,  $\varepsilon_t$  is the white noise having constant mean and variance and is independently distributed, i.e., has no autocorrelation.

Model representation of equation 5 is called a first-order autoregressive process (AR(1)), as it has one lag of  $y_t$ .

A  $p^{th}$  order autoregressive model – AR(p) can be defined as in Equation 6.

$$y_t = \mu_0 + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_n y_{t-n} + \varepsilon_t \tag{6}$$

Autoregressive process of order (p) can also be represented using lag operator as in Equation 7.

$$y_t = \mu_0 + \sum_{i=1}^p \phi_i L^i y_t + \varepsilon_t \tag{7}$$

Where,

$$Ly_t = y_{t-1}, \ L^2y_t = y_{t-2}, \ L^iy_t = y_{t-i}$$

For an AR(1) model (Equation 5), following states may exist:

- When  $\phi_1 = 0$ ,  $y_t$  is equivalent to white noise;
- When  $\phi_1 = 1$  and  $\mu_0 = 0$ ,  $y_t$  is equivalent to random walk;
- When  $\phi_1 = 1$  and  $c \neq 0$ ,  $y_t$  is equivalent to a random walk with drift;
- When  $\phi_1 < 0$ ,  $y_t$  tends to oscillate between positive and negative value.

#### 3.2 MA model

An MA(q) process is

$$y_t = c + \varepsilon_t + \theta_1 \varepsilon_{t-1} + \theta_2 \varepsilon_{t-2} + \dots + \theta_q \varepsilon_{t-q}$$
 (8)

Following assumptions may hold for a MA(q) model

- For an MA(1) model:  $-1 < \theta_1 < 1$
- For an MA(2) model:  $-1 < \theta_2 < 1, \, \theta_2 + \theta_1 > -1, \, \theta_1 \theta_2 < 1$

A process  $x_t$  is said to be ARIMA(p, d, q) if

$$\nabla^d x_t = (1 - B)^d x_t \tag{9}$$

Table 3: ARIMA model summary for multiple  $\log(\text{price})$  series of major districtwise market hubs of Rice - Retail

mktname	sigma2	log_lik	AIC	AICc	BIC
Kathmandu	0.004	243.522	-479.045	-478.825	-466.120
Parsa	0.010	167.945	-331.890	-331.824	-325.438
Morang	0.004	257.864	-509.728	-509.598	-500.003
Kailali	0.004	290.087	-568.173	-567.781	-547.784
Banke	0.005	265.152	-520.305	-520.027	-503.291
Kaski Rupandehi	$0.002 \\ 0.007$	304.876 234.554	-603.752 -463.107	-603.622 -462.997	-594.027 -452.899

Table 4: ARIMA model summary for multiple log(price) series of major districtwise market hubs of Wheat - Retail

mktname	sigma2	log_lik	AIC	AICc	BIC
Kathmandu	0.005	239.962	-473.923	-473.793	-464.198
Parsa	0.006	212.092	-418.184	-418.052	-408.507
Morang	0.003	282.470	-554.939	-554.611	-538.730
Kailali	0.004	293.371	-578.742	-578.558	-565.131
Banke	0.004	291.350	-568.700	-568.176	-544.881
Kaski Rupandehi	0.003	274.450 212.393	-540.900 -414.786	-540.682 -414.458	-527.933 -398.578
Rupandehi	0.006	212.393	-414.786	-414.458	-398.578

if ARMA(p, q). In general, we write the total model as:

$$\phi(B)(1-B)^d x_t = \theta(B)w_t \tag{10}$$

If  $E(\nabla^d x_t) = \mu$ , we write the model as:

$$\phi(B)(1-B)^d x_t = \delta + \theta(B)w_t \tag{11}$$

Where  $\delta = \mu(1 - \phi_1 - \dots - \phi_p)$ .

Table 5: Model coefficients of ARIMA model for multiple  $\log(\text{price})$  series of major district-wise market hubs of Rice - Retail

mktname	term	estimate	std.error	statistic	p.value
Kathmandu	ma1	0.025	0.072	0.350	0.727
Kathmandu	ma2	-0.353	0.074	-4.789	0.000
Kathmandu	constant	0.005	0.003	1.512	0.132
Parsa	ar1	-0.198	0.104	-1.912	0.057
Morang	ma1	-0.403	0.079	-5.096	0.000
Morang	constant	0.006	0.003	2.311	0.022
Kailali	ar1	1.387	NaN	NaN	NaN
Kailali	ar2	-0.485	NaN	NaN	NaN
Kailali	ma1	-1.579	NaN	NaN	NaN
Kailali	ma2	0.617	NaN	NaN	NaN
Kailali	constant	0.000	0.000	2.511	0.013
Banke	ar1	0.702	0.065	10.752	0.000
Banke	ma1	-0.947	0.030	-32.040	0.000
Banke	sar1	-0.013	0.093	-0.141	0.888
Banke	constant	0.002	0.000	6.728	0.000
Kaski	ma1	-0.316	0.070	-4.542	0.000
Kaski	constant	0.005	0.002	2.233	0.027
Rupandehi	ma1	-0.359	0.063	-5.701	0.000
Rupandehi	sma1	0.100	0.064	1.557	0.121

Table 6: Model coefficients of ARIMA model for multiple  $\log(\text{price})$  series of major districtwise market hubs of Wheat - Retail

mktname	term	estimate	std.error	statistic	p.value
Kathmandu	ma1	-0.499	0.066	-7.600	0.000
Kathmandu	constant	0.005	0.002	1.901	0.059
Parsa	ma1	-0.618	0.061	-10.188	0.000
Parsa	constant	0.006	0.002	2.906	0.004
Morang	ma1	-0.235	0.072	-3.249	0.001
Morang	ma2	-0.107	0.077	-1.384	0.168
Morang	sar1	0.118	0.083	1.418	0.158
Morang	constant	0.006	0.003	2.249	0.026
Kailali	ar1	0.276	0.148	1.865	0.063
Kailali	ma1	-0.700	0.116	-6.017	0.000
Kailali	constant	0.004	0.001	3.111	0.002
Banke	ma1	-0.310	0.066	-4.678	0.000
Banke	ma2	-0.213	0.074	-2.872	0.004
Banke	sar1	-0.746	0.315	-2.366	0.019
Banke	sar2	-0.183	0.074	-2.481	0.014
Banke	sma1	0.647	0.323	2.002	0.047
Banke	constant	0.012	0.003	3.299	0.001
Kaski	ar1	-0.412	0.066	-6.196	0.000
Kaski	sar1	0.093	0.097	0.954	0.341
Kaski	constant	0.008	0.004	2.066	0.040
Rupandehi	ar1	-0.715	0.163	-4.393	0.000
Rupandehi	ma1	0.403	0.158	2.554	0.011
Rupandehi	ma2	-0.381	0.070	-5.480	0.000
Rupandehi	sma1	0.215	0.075	2.854	0.005

### 4 VAR model

#### 4.1 VAR

VAR is a system regression model, i.e., there are more than one dependent variable. The regression is defined by a set of linear dynamic equations where each variable is specified as a function of an equal number of lags of itself and all other variables in the system. Any additional variable, adds to the modeling complexity by increasing an extra equation to be estimated.

The vector autoregression (VAR) model extends the idea of univariate autoregression to k time series regressions, where the lagged values of all k series appear as regressors. Put differently, in a VAR model we regress a vector of time series variables on lagged vectors of these variables. As for AR(p) models, the lag order is denoted by p so the VAR(p) model of two variables  $X_t$  and  $Y_t$  (k = 2) is given by a vector of equations (Equation 12).

$$\begin{split} Y_t &= \beta_{10} + \beta_{11} Y_{t-1} + \dots + \beta_{1p} Y_{t-p} + \gamma_{11} X_{t-1} + \dots + \gamma_{1p} X_{t-p} + u_{1t}, \\ X_t &= \beta_{20} + \beta_{21} Y_{t-1} + \dots + \beta_{2p} Y_{t-p} + \gamma_{21} X_{t-1} + \dots + \gamma_{2p} X_{t-p} + u_{2t}. \end{split} \tag{12}$$

The  $\beta$ s and  $\gamma$ s can be estimated using OLS on each equation.

Simplifying this to a bivariate VAR(1), we can write the model in matrix form as:

$$Y_t = \beta_0 + \beta_1 Y_{t-1} + \mu_t \tag{13}$$

Where,

- $Y_t, Y_{t-1}$  and  $\mu_t$  are (2 x 1) column vectors
- $\beta_0$  is a  $(2 \times 1)$  column vector
- $\beta_1$  is a  $(2 \times 2)$  matrix

also,

$$Y_{t} = \begin{pmatrix} y_{1t} \\ y_{2t} \end{pmatrix}, \ Y_{t-1} = \begin{pmatrix} y_{1t-1} \\ y_{2t-1} \end{pmatrix}$$

$$\mu_{t} = \begin{pmatrix} \mu_{1t} \\ \mu_{2t} \end{pmatrix}, \beta_{0} = \begin{pmatrix} \beta_{10} \\ \beta_{20} \end{pmatrix}, \beta_{1} = \begin{pmatrix} \beta_{11} & \alpha_{11} \\ \alpha_{21} & \beta_{21} \end{pmatrix}$$

It is straightforward to estimate VAR models in R. A feasible approach is to simply use lm() for estimation of the individual equations. Furthermore, the vars package provides standard tools for estimation, diagnostic testing and prediction using this type of models.

Only when the assumptions presented below hold, the OLS estimators of the VAR coefficients are consistent and jointly normal in large samples so that the usual inferential methods such as confidence intervals and t-statistics can be used (Metcalfe and Cowpertwait 2009).

Two series  $w_{x,t}$  and  $w_{y,t}$  are bivariate white noise if they are stationary and their cross-covariances  $\gamma_{xy}(k) = Cov(w_{x,t},w_{y,t+k})$  satisfies

$$\gamma_{xx}(k) = \gamma_{yy}(k) = \gamma_{xy}(k) = 0$$
 for all  $k \neq 0$ 

The parameters of a var(p) model can be estimated using the **ar** function in R, which selects a best-fitting order p based on the smallest information criterion values.

The structure of VARs also allows to jointly test restrictions across multiple equations. For instance, it may be of interest to test whether the coefficients on all regressors of the lag p are zero. This corresponds to testing the null that the lag order p-1 is correct. Large sample joint normality of the coefficient estimates is convenient because it implies that we may simply use an F-test for this testing problem. The explicit formula for such a test statistic is rather complicated but fortunately such computations are easily done using the ttcode("R") functions we work with in this chapter. Just as in the case of a single equation, for a multiple equation model we choose the specification which has the smallest BIC(p), where

$$BIC(p) = \log\left[\det(\widehat{\Sigma}_u)\right] + k(kp+1)\frac{\log(T)}{T}.$$

with  $\widehat{\Sigma}_u$  denoting the estimate of the  $k \times k$  covariance matrix of the VAR errors and  $\det(\cdot)$  denotes the determinant.

As for univariate distributed lag models, one should think carefully about variables to include in a VAR, as adding unrelated variables reduces the forecast accuracy by increasing the estimation error. This is particularly important because the number of parameters to be estimated grows quaratically to the number of variables modeled by the VAR.

Table 7: Model performance indicators of VAR(AR(1)) model for selected districtwise market hub series in Rice and Wheat.

cmname-mktname	sigma2	log_lik	AIC	AICc	BIC
Rice - Retail / Banke	0.005987452	254.108	-502.216	-502.106	-492.008
Rice - Retail / Kailali	0.004562652	282.494	-560.989	-560.934	-554.192
Rice - Retail / Kaski	0.002558304	296.841	-587.682	-587.552	-577.956
Rice - Retail / Kathmandu	0.004799157	234.890	-463.780	-463.649	-454.086
Rice - Retail / Morang	0.004287195	248.052	-490.103	-489.973	-480.378
Rice - Retail / Parsa	0.009750488	167.714	-329.427	-329.295	-319.750
Rice - Retail / Rupandehi	0.007998555	221.963	-437.926	-437.816	-427.718
Wheat - Retail / Banke	0.004799646	278.653	-551.306	-551.196	-541.098

Wheat - Retail / Kailali Wheat - Retail / Kaski	$\begin{array}{c} 0.004939438 \\ 0.003879621 \end{array}$				
Wheat - Retail / Kathmandu Wheat - Retail / Morang Wheat - Retail / Parsa Wheat - Retail / Rupandehi	0.005504843 0.003155432 0.007953767 0.007253182	277.016 186.655	-548.033 -367.310	-547.903 -367.178	-538.308 -357.633

Table 8: Model coefficients of VAR model for multiple log(price) series of major districtwise market hubs of Rice - Retail

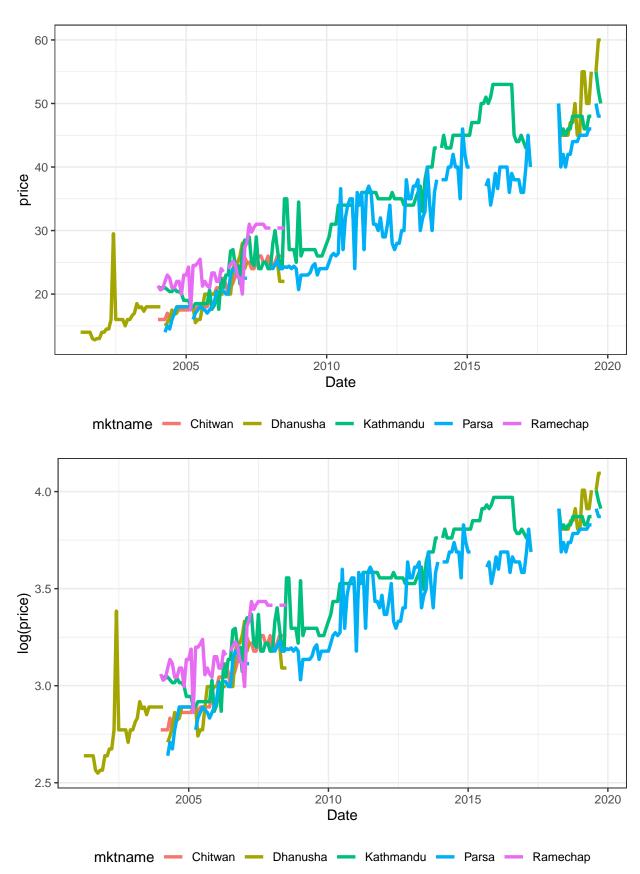
mktname	term	estimate	std.error	statistic	p.value
Banke	lag(lprice,1)	0.982	0.012	82.933	0.000
Banke	constant	0.062	0.038	1.626	0.105
Kailali	lag(lprice,1)	1.001	0.001	723.506	0.000
Kaski	lag(lprice,1)	0.985	0.010	99.189	0.000
Kaski	constant	0.059	0.036	1.654	0.100
Kathmandu	lag(lprice,1)	0.971	0.015	63.567	0.000
Kathmandu	constant	0.109	0.055	1.999	0.047
Morang	lag(lprice,1)	0.973	0.014	71.100	0.000
Morang	constant	0.098	0.046	2.121	0.035
Parsa	lag(lprice,1)	0.963	0.021	46.349	0.000
Parsa	constant	0.125	0.070	1.774	0.078
Rupandehi	lag(lprice,1)	0.972	0.016	62.573	0.000
Rupandehi	constant	0.097	0.050	1.927	0.055

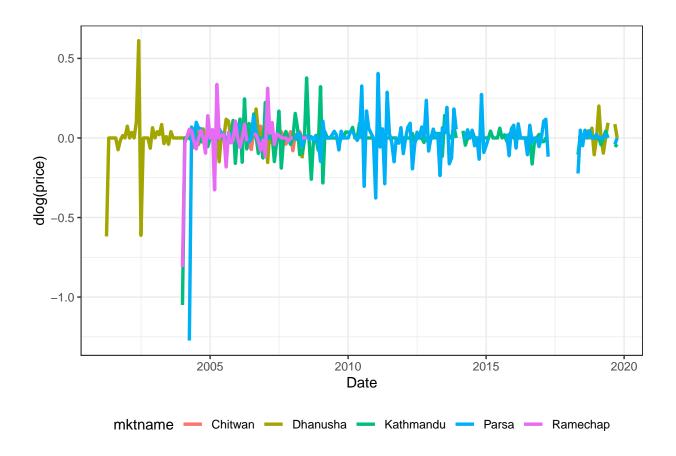
Table 9: Model coefficients of VAR model for multiple log(price) series of major districtwise market hubs of Wheat - Retail

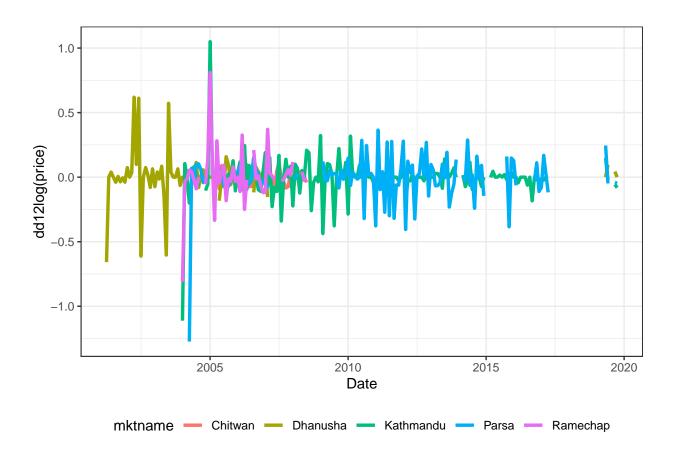
mktname	term	estimate	std.error	statistic	p.value
Banke	lag(lprice,1)	0.982	0.011	86.538	0.000
Banke	constant	0.063	0.037	1.698	0.091
Kailali	lag(lprice,1)	0.977	0.012	80.478	0.000
Kailali	constant	0.080	0.039	2.033	0.043
Kaski	lag(lprice,1)	0.974	0.013	72.988	0.000
Kaski	constant	0.097	0.047	2.046	0.042
Kathmandu	lag(lprice,1)	0.972	0.017	57.967	0.000
Kathmandu	constant	0.103	0.059	1.741	0.083
Morang	lag(lprice,1)	0.983	0.012	79.565	0.000
Morang	constant	0.063	0.043	1.492	0.137

Parsa	lag(lprice,1)	0.949	0.021	45.575	0.000
Parsa	constant	0.178	0.071	2.514	0.013
Rupandehi	lag(lprice,1)	0.955	0.021	46.210	0.000
Rupandehi	constant	0.157	0.070	2.259	0.025

## 4.2 Differenced series







#### 4.3 Causality test

Causality test is VAR based approach to explain cause-effect relationship among endogenous variables. However, the Granger-causality (Granger 1988) inference does not, of course, establish the real causation phenomena. If one of the variables is sufficiently correlated to the other so that forecast of former depends on the later to a considerable extent, then the first variable is *granger-caused* by the second one.

The Granger causality has been briefed to be useable test in certain cases of two series violating the stationarity assumption<sup>1</sup>. Papana et al. (2014) state that GC test can only to applied if both the series are stationary<sup>2</sup>. Same paper also cautioned that VAR(1) models of cointegrated endogenous series will fail to capture long-run relationships. Therefore, the authors suggest surplus lag Granger-causality test be used if the series are a nonstationary data.

Below are the results of GC test showing consequences of using both stationarity and non stationary data, with bootstrapped confidence intervals.

<sup>&</sup>lt;sup>1</sup>https://davegiles.blogspot.com/2011/04/testing-for-granger-causality.html

<sup>&</sup>lt;sup>2</sup>Mindy Mallory's blog article also suggests that series be stationary

#### 4.3.1 Case I: GC test on undifferenced log(price) series

Table 10: Granger causality test of multivariate (7 market series) var models of Rice  $\log(\text{price})$  series

statistic	p.value	parameter	method
1.053	0.200	5000	Granger causality H0: kathmandu do not
			Granger-cause parsa morang kailali banke
			kaski rupandehi
0.641	0.527	5000	Granger causality H0: parsa do not
			Granger-cause kathmandu morang kailali
			banke kaski rupandehi
1.098	0.381	5000	Granger causality H0: morang do not
			Granger-cause kathmandu parsa kailali banke
			kaski rupandehi
0.614	0.740	5000	Granger causality H0: kailali do not
			Granger-cause kathmandu parsa morang
			banke kaski rupandehi
2.744	0.065	5000	Granger causality H0: banke do not
			Granger-cause kathmandu parsa morang
			kailali kaski rupandehi
2.637	0.062	5000	Granger causality H0: kaski do not
			Granger-cause kathmandu parsa morang
			kailali banke rupandehi
1.262	0.171	5000	Granger causality H0: rupandehi do not
			Granger-cause kathmandu parsa morang
			kailali banke kaski

Table 11: Granger causality test of multivariate (7 market series) var models of Wheat  $\log(\text{price})$  series

statistic	p.value	parameter	method
2.555	0.029	5000	Granger causality H0: kathmandu do not
			Granger-cause parsa morang kailali banke
0.646	0.738	5000	kaski rupandehi Granger causality H0: parsa do not
0.040	0.130	5000	Granger cause kathmandu morang kailali
			banke kaski rupandehi
2.865	0.037	5000	Granger causality H0: morang do not
			Granger-cause kathmandu parsa kailali banke
1.684	0.204	5000	kaski rupandehi Granger causality H0: kailali do not
1.004	0.204	5000	Granger-cause kathmandu parsa morang
			banke kaski rupandehi
1.086	0.452	5000	Granger causality H0: banke do not
			Granger-cause kathmandu parsa morang
			kailali kaski rupandehi
3.554	0.007	5000	Granger causality H0: kaski do not
			Granger-cause kathmandu parsa morang
3.172	0.021	5000	kailali banke rupandehi Granger causality H0: rupandehi do not
3,1,2	0.021	3000	Granger-cause kathmandu parsa morang
			kailali banke kaski

#### 4.3.2 Case II: GC test on differenced log(price) series

Table 12: Granger causality test of multivariate (7 market series) var models of Rice first order differenced log(price) series

statistic	p.value	parameter	method
0.388	0.641	5000	Granger causality H0: kathmandu do not
			Granger-cause parsa morang kailali banke
			kaski rupandehi
1.610	0.147	5000	Granger causality H0: parsa do not
			Granger-cause kathmandu morang kailali
2 0 2 0	0.040	<b>~</b> 000	banke kaski rupandehi
2.020	0.218	5000	Granger causality H0: morang do not
			Granger-cause kathmandu parsa kailali banke
1 710	0.005	<b>5</b> 000	kaski rupandehi
1.713	0.085	5000	Granger causality H0: kailali do not
			Granger-cause kathmandu parsa morang
0.699	0.511	F000	banke kaski rupandehi
0.622	0.511	5000	Granger causality H0: banke do not
			Granger-cause kathmandu parsa morang
			kailali kaski rupandehi
0.778	0.393	5000	Granger causality H0: kaski do not
			Granger-cause kathmandu parsa morang
			kailali banke rupandehi
0.423	0.739	5000	Granger causality H0: rupandehi do not
			Granger-cause kathmandu parsa morang
			kailali banke kaski

Table 13: Granger causality test of multivariate (7 market series) var models of Wheat first order differenced log(price) series

statistic p.value	paramete	r method
0.787 0.504	5000	Granger causality H0: kathmandu do not
		Granger-cause parsa morang kailali banke
		kaski rupandehi
1.165  0.235	5000	Granger causality H0: parsa do not
		Granger-cause kathmandu morang kailali
		banke kaski rupandehi
1.788  0.097	5000	Granger causality H0: morang do not
		Granger-cause kathmandu parsa kailali banke
		kaski rupandehi
$0.961 \qquad 0.422$	5000	Granger causality H0: kailali do not
		Granger-cause kathmandu parsa morang
		banke kaski rupandehi
1.942  0.139	5000	Granger causality H0: banke do not
		Granger-cause kathmandu parsa morang
		kailali kaski rupandehi
0.274 0.777	5000	Granger causality H0: kaski do not
		Granger-cause kathmandu parsa morang
		kailali banke rupandehi
1.642  0.104	5000	Granger causality H0: rupandehi do not
		Granger-cause kathmandu parsa morang
		kailali banke kaski

### 5 Cointegration

#### 5.1 Residual based

Since the food commodities are spatially linked, more of so because they occupy the same domestic market, it is obvious that factor affecting price of one inevitably affects other, especially that of same crop in a nearby market. Having evidence for nonstationarity, it is of interest to test for a common nonstationary component by means of a cointegration test (Non-stationarity is more valid for development regionwise price series).

A two step method proposed by Hylleberg et al. (1990) can be used to test for cointegration.

The procedure simply regressess one series on the other and performs a unit root test on the residuals. This test is often named after Phillips, Ouliaris, and others (1990). Specifically, po.test() performs a Phillips-Perron test using an auxiliary regression without a constant and linear trend and the Newey-West estimator for the required long-run variance.

The test computes the Phillips-Ouliaris test for the null hypothesis that series is not cointegrated (Trapletti and Hornik 2019).

We check the rice retail price series for all combination major districtwise markets.

Table 14: Phillips-Ouliaris cointegration test for Rice log(price) series of selected district markethubs

combination	p_value	statistic
Morang-Parsa	0.010	-96.515
Morang-Kathmandu	0.010	-34.869
Morang-Kaski	0.010	-37.126
Morang-Rupandehi	0.010	-42.435
Morang-Banke	0.010	-65.794
Morang-Kailali	0.010	-66.540
Parsa-Kathmandu	0.010	-59.925
Parsa-Kaski	0.010	-94.521
Parsa-Rupandehi	0.010	-63.256
Parsa-Banke	0.010	-91.480
Parsa-Kailali	0.010	-89.453
Kathmandu-Kaski	0.010	-35.060
Kathmandu-Rupandehi	0.010	-37.100
Kathmandu-Banke	0.010	-34.602
Kathmandu-Kailali	0.010	-34.579
Kaski-Rupandehi	0.013	-27.453
Kaski-Banke	0.010	-41.121
Kaski-Kailali	0.010	-52.289
Rupandehi-Banke	0.010	-89.619
Rupandehi-Kailali	0.010	-41.667
Banke-Kailali	0.010	-58.835

Table 15: Phillips-Ouliaris cointegration test for Wheat log(price) series of selected district markethubs

combination	p_value	statistic
Morang-Parsa	0.01	-79.626
Morang-Kathmandu	0.01	-53.276
Morang-Kaski	0.01	-71.222
Morang-Rupandehi	0.01	-79.788
Morang-Banke	0.01	-56.448
Morang-Kailali	0.01	-55.875
Parsa-Kathmandu	0.01	-80.952

Parsa-Kaski	0.01	-90.071
Parsa-Rupandehi	0.01	-78.571
Parsa-Banke	0.01	-57.703
Parsa-Kailali	0.01	-92.198
Kathmandu-Kaski	0.01	-82.232
Kathmandu-Rupandehi	0.01	-48.619
Kathmandu-Banke	0.01	-50.344
Kathmandu-Kailali	0.01	-73.156
Kaski-Rupandehi	0.01	-58.758
Kaski-Banke	0.01	-49.955
Kaski-Kailali	0.01	-87.482
Rupandehi-Banke	0.01	-57.133
Rupandehi-Kailali	0.01	-64.151
Banke-Kailali	0.01	-53.604

Note po.test does not handle missing values, so we fix them through imputation. It is implemented through tidyr::fill(..., .direction = "down").

The test suggests that all series (Both that of wheat and rice) are cointegrated for selected pairwise combination of district markets.

The problem with this approach is that it treats both series in an asymmetric fashion, while the concept of cointegration demands that the treatment be symmetric.

The po.test() function is testing the cointegration with Phillip's Z\_alpha test, which is the second residual-based test described by Phillips, Ouliaris, and others (1990). Because the po.test() will use the series at the first position to derive the residual used in the test, results would be determined by the series on the most left-hand side<sup>3</sup>.

The Phillips-Ouliaris test implemented in the ca.po() function from the urca package is different. In the ca.po() function, there are two cointegration tests implemented, namely "Pu" and "Pz" tests. Although both the ca.po() function and the po.test() function are supposed to do the Phillips-Ouliaris test outcomes from both functions are completely different.

Similar to Phillip's Z\_alpha test, the Pu test also is not invariant to the position of each series and therefore would give different outcomes based upon the series on the most left-hand side. On the contrary, the multivariate trace statistic of Pz test has its appeal in that the outcome won't change by the position of each series.

#### 5.2 VAR based

The standard tests proceeding in a symmetric manner stem from Johansen's full-information maximum likelihood approach (Johansen 1991).

 $<sup>^3 \</sup>rm https://www.r-craft.org/r-news/phillips-ouliaris-test-for-cointegration/$ 

A general vector autoregressive model is similar to the AR(p) model except that each quantity is vector valued and matrices are used as the coefficients. The general form of the VAR(p) model, without drift, is given by:

$$\mathbf{y_t} = +A_1 \mathbf{y_{t-1}} + \dots + A_i \mathbf{y_{t-i}} + \mathbf{t}$$
 (14)

Where is the vector-valued mean of the series,  $A_i$  are the coefficient matrices for each lag and t is a multivariate Gaussian noise term with mean zero.

At this stage we can form a Vector Error Correction Model (VECM) by differencing the series (Equation 15).

$$\Delta \mathbf{y_t} = +A\mathbf{y_{t-1}} + \Gamma_1 \Delta \mathbf{y_{t-1}} + \dots + \Gamma_j \Delta \mathbf{y_{t-j}} + \mathbf{t}$$
(15)

Where  $\Delta \mathbf{y_t} = \mathbf{y_t} - \mathbf{y_{t-1}}$  is the differencing operator, A is the coefficient matrix for the first lag and  $\Gamma_i$  are the matrices for each differenced lag.

For a  $p^{th}$  -order cointegrated vector autoregressive (VAR) model, the error correction form is (omitting deterministic components; both no intercept or trend in either cointegrating equation or test var), we may rewrite the VAR in the form of Equation 16 (Johansen 1991).

$$\Delta y_t = \Pi y_{t-1} + \sum_{j=1}^{p-1} \Gamma_j \Delta y_{t-j} + \varepsilon_t \tag{16}$$

Where,

$$\Pi = \sum_{i=1}^p A_i - I; \Gamma = -\sum_{j=i+1}^p j$$

(Although, for simplicity sake, we assume absence of deterministic trends, there are five popular scenarios of including such trends in a cointegration test. All of these are described in (Johansen 1995).)

Granger's representation theorem asserts that if the coefficient matrix  $\Pi$  has reduced rank r < k, then there exist kxr matrices  $\alpha$  and  $\beta$  each with rank k such that  $\Pi = \alpha\beta'$  and  $\beta'y_t$  is I(0).

To achieve this an eigenvalue decomposition of A is carried out. The rank of the matrix A is given by r and the Johansen test sequentially tests whether this rank r is equal to zero, equal to one, through to r = n - 1, where n is the number of time series under test.

The null hypothesis of r = 0 means that there is no cointegration at all. A rank r > 0 implies a cointegrating relationship between two or possibly more time series.

The eigenvalue decomposition results in a set of eigenvectors. The components of the largest eigenvector admits the important property of forming the coefficients of a linear combination of time series to produce a stationary portfolio. Notice how this differs from the CADF test

(often known as the Engle-Granger procedure) where it is necessary to ascertain the linear combination a priori via linear regression and ordinary least squares (OLS).

In summary, the test checks for the situation of no cointegration, which occurs when the matrix A=0. So, starting with the base value of r (i.e., r=0), if the test statistic is greater than critical values of at the 10%, 5% and 1% levels, this would imply that we are **able** to reject the null of no cointegration. For the case r <=1, we if the calculated test statistic is below the critical values of, we are **unable** to reject the null, and the number of cointegrating vectors is between 0 and 1. The relevant tests are available in the function urca::ca.jo(). The basic version considers the eigenvalues of the matrix  $\Pi$  in the preceding equation.

Here, we employ the trace statistic – the maximum eigenvalue, or "lambdamax" test is available as well – in an equation amended by a constant term (specified by ecdet = "const"), yielding:

Johansen cointegration test summary and time series plots for rice (district marketwise)

Table 16: Johansen cointegration test summary for Morang-Parsa

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array} $	8.047588 29.352546		9.24 19.96	12.01

Table 17: Johansen cointegration test summary for Morang-Kathmandu

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \\ r = 0 \\ \end{array} $	7.080797 26.213687			12.97 24.60

Table 18: Johansen cointegration test summary for Morang-Kaski

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array} $	10.47841 26.58143			

Table 19: Johansen cointegration test summary for Morang-Rupandehi

gamma test_stat 10pct 5pct 1pct
---------------------------------

r <= 1	9.529231	7.52	9.24	12.97
r = 0	28.702528	17.85	19.96	24.60

Table 20: Johansen cointegration test summary for Morang-Banke

gamma	test_stat	10pct	5pct	1pct
$\begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array}$	11.07168	7.52	9.24	12.97
	43.79799	17.85	19.96	24.60

Table 21: Johansen cointegration test summary for Morang-Kailali

gamma	test_stat	10pct	5pct	1pct
	8.627746 37.159947			

Table 22: Johansen cointegration test summary for Parsa-Kathmandu

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	7.117339 28.121237	7.52 17.85	J 1	12.97 24.60

Table 23: Johansen cointegration test summary for Parsa-Kaski

gamma	test_stat	10pct	5pct	1pct
r <= 1   r = 0	8.739686 33.345326			12.97 24.60

Table 24: Johansen cointegration test summary for Parsa-Rupandehi

gamma	test_stat	10pct	5pct	1pct
$\begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array}$	5.241234 21.237513			

Table 25: Johansen cointegration test summary for Parsa-Banke

gamma	test_stat	10pct	5pct	1pct
$\begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array}$	8.905272 35.297439	7.52 17.85		

Table 26: Johansen cointegration test summary for Parsa-Kailali

gamma	test_stat	10pct	5pct	1pct
	6.477453			
r = 0	30.475019	17.85	19.96	24.60

Table 27: Johansen cointegration test summary for Kathmandu-Kaski

gamma	test_stat	10pct	5pct	1pct
	6.896813 30.474234			,

Table 28: Johansen cointegration test summary for Kathmandu-Rupandehi

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	5.706426 24.640127	7.52 17.85	-	12.97 24.60

Table 29: Johansen cointegration test summary for Kathmandu-Banke

gamma	test_stat	10pct	5pct	1pct
r <= 1	9.024811	7.52	9.24	12.97
r = 0	30.343046	17.85	19.96	24.60

Table 30: Johansen cointegration test summary for Kathmandu-Kailali

gamma	$test\_stat$	10pct	5pct	1pct
r <= 1	6.166887	7.52	9.24	12.97
r = 0	27.654849	17.85	19.96	24.60

Table 31: Johansen cointegration test summary for Kaski-Rupandehi

gamma	test_stat	10pct	5pct	1pct
	7.905289 22.551933	7.52 17.85	U.= 1	12.97 24.60

Table 32: Johansen cointegration test summary for Kaski-Banke

gamma	test_stat	10pct	5pct	1pct
	8.927975 29.193633			

Table 33: Johansen cointegration test summary for Kaski-Kailali

gamma	test_stat	10pct	5pct	1pct
	7.744047 31.015706	7.52 17.85	-	

Table 34: Johansen cointegration test summary for Rupandehi-Banke

gamma	test_stat	10pct	5pct	1pct
	4.441382 46.391884			

Table 35: Johansen cointegration test summary for Rupandehi-Kailali

gamma	test_stat	10pct	5pct	1pct
r <= 1	2.995481	7.52	9.24	12.97

 $r = 0 \mid 20.488277 \quad 17.85 \quad 19.96 \quad 24.60$ 

Table 36: Johansen cointegration test summary for Banke-Kailali

gamma	test_stat	10pct	5pct	1pct
r <= 1	2.788889	7.52	9.24	12.97
r = 0	40.728755	17.85	19.96	24.60

Johansen cointegration test summary and time series plots for wheat (district marketwise)

Table 37: Johansen cointegration test summary for Morang-Parsa

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array} $	8.67185 38.90466			12.97 24.60

Table 38: Johansen cointegration test summary for Morang-Kathmandu

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \\ r = 0 \\ \end{array} $	$6.03380 \\ 32.39395$		-	12.97 24.60

Table 39: Johansen cointegration test summary for Morang-Kaski

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	14.80835 47.39019	7.52 17.85	9.24 19.96	12.0.

Table 40: Johansen cointegration test summary for Morang-Rupandehi

gamma	$test\_stat$	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	6.698168 41.851350			

Table 41: Johansen cointegration test summary for Morang-Banke

gamma	test_stat	10pct	5pct	1pct
r <= 1	6.791701	7.52	J 1	12.97
r = 0	29.981567	17.85		24.60

Table 42: Johansen cointegration test summary for Morang-Kailali

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	10.09031	7.52	9.24	12.97
	34.84797	17.85	19.96	24.60

Table 43: Johansen cointegration test summary for Parsa-Kathmandu

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	5.572257 39.875312		U 1	12.97 24.60

Table 44: Johansen cointegration test summary for Parsa-Kaski

gamma	test_stat	10pct	5pct	1pct
r <= 1   r = 0	9.047446 $43.549450$	7.52 17.85	-	12.97 24.60

Table 45: Johansen cointegration test summary for Parsa-Rupandehi

gamma	test_stat	10pct	5pct	1pct
	7.098776 35.167352			12.97 24.60

Table 46: Johansen cointegration test summary for Parsa-Banke

gamma	$test\_stat$	10pct	5pct	1pct
!	7.52789		9.24	
r = 0	36.13913	17.85	19.96	24.60

Table 47: Johansen cointegration test summary for Parsa-Kailali

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	8.944134 48.858929			

Table 48: Johansen cointegration test summary for Kathmandu-Kaski

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	9.856107 48.980703			

Table 49: Johansen cointegration test summary for Kathmandu-Rupandehi

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	4.913668 27.111863			12.97 24.60

Table 50: Johansen cointegration test summary for Kathmandu-Banke

gamma	test_stat	10pct	5pct	1pct
r <= 1   r = 0	5.079637 27.171088			12.97 24.60

Table 51: Johansen cointegration test summary for Kathmandu-Kailali

gamma	test_stat	10pct	5pct	1pct
$\begin{array}{c c} r <= 1 \mid \\ r = 0 \mid \end{array}$	6.417786 35.001568	7.52 17.85	-	

Table 52: Johansen cointegration test summary for Kaski-Rupandehi

gamma	test_stat	10pct	5pct	1pct
$r <= 1 \mid r = 0 \mid$	10.27943 33.21418	7.52 17.85	•	12.97 24.60

Table 53: Johansen cointegration test summary for Kaski-Banke

gamma	test_stat	10pct	5pct	1pct
r <= 1   r = 0	8.023414 32.713727			

Table 54: Johansen cointegration test summary for Kaski-Kailali

gamma	test_stat	10pct	5pct	1pct
$ \begin{array}{c c} r <= 1 \\ r = 0 \\ \end{array} $	11.36236 40.97431		9.24 19.96	

Table 55: Johansen cointegration test summary for Rupandehi-Banke

gamma	test_stat	10pct	5pct	1pct
	6.253642 34.339634			

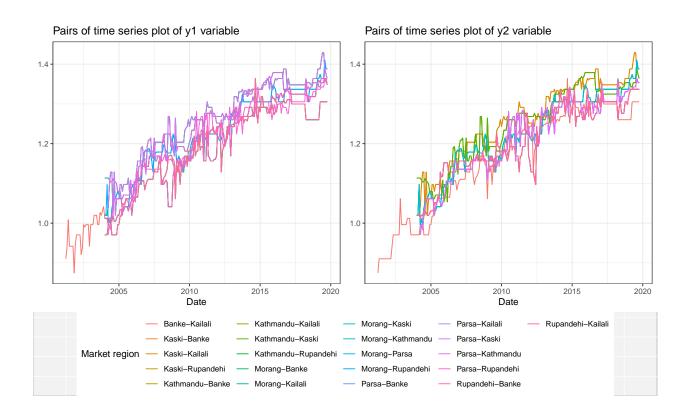
Table 56: Johansen cointegration test summary for Rupandehi-Kailali

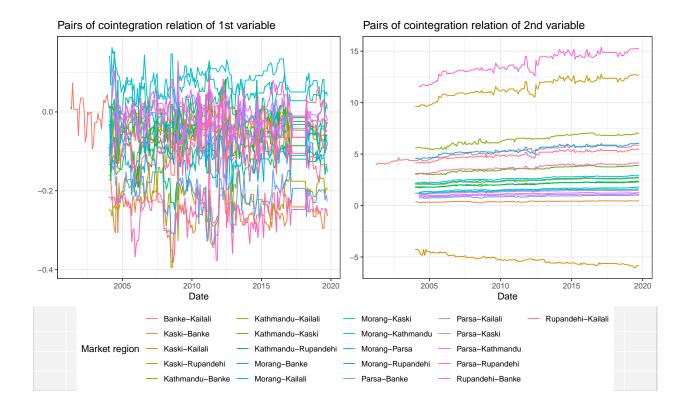
gamma	test_stat	10pct	5pct	1pct
	7.004144 31.782559			

Table 57: Johansen cointegration test summary for Banke-Kailali

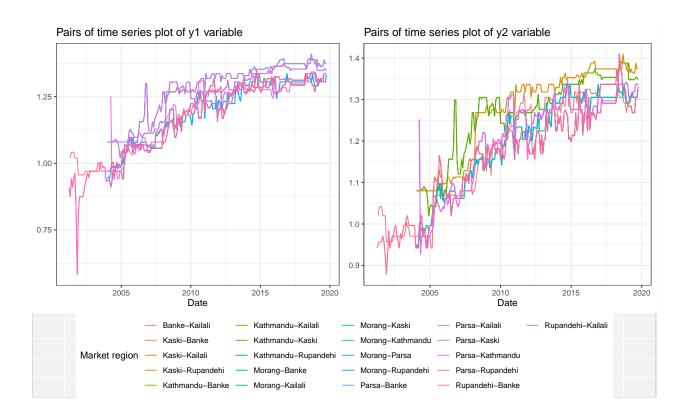
gamma	$test\_stat$	10pct	5pct	1pct
	7.875127 32.936232		-	

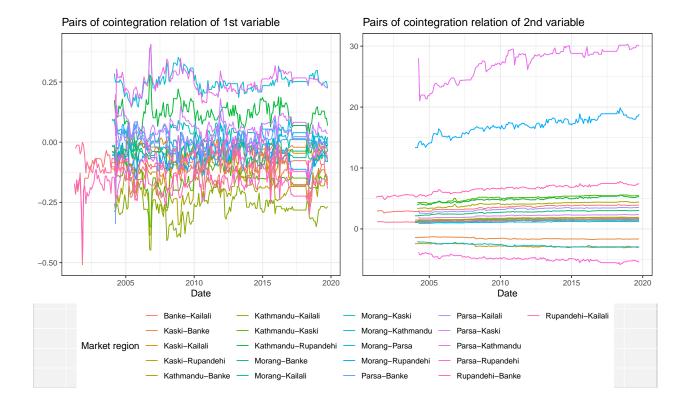
Wheat series and cointegration plots





Rice series and cointegration plots





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