

# L<sup>A</sup>T<sub>E</sub>X Assignment-I

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## 1 Enumerate

1. Prove that there is only one identity in a Group
2. In a group G, the right and left cancellation laws hold.
3. Prove that each element in a Group has unique inverse.
4. State and prove Socks Shoes property of a Group.
5. The curve  $y = \sqrt{x}$ , where  $x \geq 0$ , is concave
6. If  $\sin \theta = 0$  and  $0 \leq \theta < 2\pi$ , then  $\theta = 0$  or  $\theta = \pi$ .

## 2 Itemize

- The identity holds for all real  $x : \sin^2 x + \cos^2 x = 1$
- Let  $x = (x_1, x_2, \dots, x_n)$  be a vector of non-negative integers. Let

$$M_r(x) = \left( \frac{x_1^r + x_2^r + \dots + x_n^r}{n} \right)^{1/r}, r \in \mathbb{R} \setminus \{0\}$$

- It is not always true that

$$\frac{a+b}{c+d} = \frac{a}{c} + \frac{b}{d}.$$

- The curve  $y_{10} = \sqrt[5]{x}$ , where  $x \geq 0$ , is concave
- A set  $A = \{x : x \text{ is an English Alphabet}\}$

## 3 Ascents

Szegö  
tilde  
Ö  
Szegő  
abD

## 4 Array

$$F(x) = \begin{cases} x, & x = 0; \\ x^2, & x > 0; \\ x + 5, & x < 0; \end{cases}$$

$$A = \begin{pmatrix} 1 & 4 & 7 & 4 & 8 \\ 2 & 5 & 8 & 5 & 9 \\ 3 & 6 & \alpha & 3 & 0 \\ \beta & 8 & 5 & 8 & 10 \\ 34 & 76 & 0 & 6 & 8 \end{pmatrix}$$

$$\det A = \begin{vmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & \alpha \end{vmatrix}$$

S.No.	Name	Marks(10)
1	ABC	7
2	DF	8

1	4	7
2	5	8
3	6	$\alpha$

$$\begin{aligned} |a+b+c| &\leq |a+b|+|c| \\ &\leq |a|+|b|+|c| \end{aligned}$$

$$\begin{aligned} |a+b+c| &\leq |a+b|+|c| \\ &\leq |a|+|b|+|c| \end{aligned} \tag{1}$$