

CG Tutorial - 1

1. $(10, 20)$ and $(20, 16)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{16 - 20}{20 - 10} = \frac{-4}{10} = -0.4$$

$|m| < 1$ and slope is -ve

$$\therefore x_{k+1} = x_k + 1; \quad y_{k+1} = y_k + m$$

$$(x_0, y_0) = (10, 20)$$

$$x_1 = x_0 + 1; \quad y_1 = y_0 + m$$

$$= 10 + 1; \quad = 20 - 0.4$$

$$= 11 \quad = 19.6 \approx 20$$

$$(x_1, y_1) = (11, 20)$$

$$(x_2, y_2) = (11+1, 19.6 - 0.4) \approx (12, 19)$$

$$(x_3, y_3) = (12+1, 19.2 - 0.4) \approx (13, 19)$$

$$(x_4, y_4) = (13+1, 18.8 - 0.4) \approx (14, 18.4)$$

$$(x_5, y_5) = (14+1, 18.4 - 0.4) \approx (15, 18)$$

$$(x_6, y_6) = (15+1, 18 - 0.4) \approx (16, 17.6)$$

$$(x_7, y_7) = (16+1, 17.6 - 0.4) \approx (17, 17.2)$$

$$(x_8, y_8) = (17+1, 17.2 - 0.4) \approx (18, 16.8)$$

$$(x_9, y_9) = (18+1, 16.8 - 0.4) \approx (19, 16.4)$$

$$(x_{10}, y_{10}) = (19+1, 16.4 - 0.4) \approx (20, 16)$$

\therefore The points obtained between the endpoints

$$(11, 20), (12, 19), (13, 19), (14, 18.4), (15, 18), (16, 17.6), (17, 17.2)$$

$$(18, 16.8), (19, 16.4)$$

2. $(12, 13)$ and $(16, 20)$

$$m = \frac{20 - 13}{16 - 12} = \frac{7}{4} = 1.75$$

$|m| > 1$ and slope is +ve

$$\therefore x_{k+1} = x_k + 1/m; \quad y_{k+1} = y_k + 1$$

$$(x_0, y_0) = (12, 13)$$

$$x_1 = x_0 + 1/m = 12 + 1/1.75$$

$$= 12 + 0.5714 = 12.5714 \approx 13$$

$$y_1 = y_0 + 1 = 13 + 1 = 14$$

$$\therefore (x_1, y_1) = (12, 14)$$

$$(x_2, y_2) = (12.43 + 0.43, 14+1) = (12.86, 15) = (13, 15)$$

$$(x_3, y_3) = (12.86 + 0.43, 15+1) = (13, 16)$$

$$(x_4, y_4) = (13.29 + 0.43, 16+1) = (14, 17)$$

$$(x_5, y_5) = (13.72 + 0.43, 17+1) = (14, 18)$$

$$(x_6, y_6) = (14.15 + 0.43, 18+1) = (14.58, 19) = (15, 19)$$

$$(x_7, y_7) = (14.58 + 0.43, 19+1) = (15.01, 20) = (15, 20)$$

\therefore The points obtained between the given endpoints are:
 $(12, 14), (13, 15), (14, 16), (15, 17), (16, 18)$

3. $(20, 7)$ and $(16, 11)$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{11 - 7}{16 - 20} = \frac{-4}{-4} = 1$$

Slope is one and $|m| = 1$

$$\therefore x_{k+1} = x_k - 1 \quad ; \quad y_{k+1} = y_k - m$$

$$(x_0, y_0) = (20, 7)$$

$$x_1 = x_0 - 1 = 20 - 1 = 19 \quad ; \quad y_1 = y_0 - m = 7 - (-1) = 8$$

$$(x_1, y_1) = (19, 8)$$

$$(x_2, y_2) = (19 - 1, 8 + 1) = (18, 9)$$

$$(x_3, y_3) = (17, 10)$$

$$(x_4, y_4) = (16, 11)$$

\therefore The points obtained between the given endpoints are
 $(19, 8), (18, 9), (17, 10), (16, 11)$