

The Practice of QCF

Liquidity Cost Analysis

```
In [ ]: import wrds
import datetime
import pandas as pd
import matplotlib.pyplot as plt
```

```
In [2]: import matplotlib.pyplot as plt
import matplotlib.dates as mdates
from matplotlib.dates import DateFormatter
import seaborn as sns
import pandas as pd

# Handle date time conversions between pandas and matplotlib
from pandas.plotting import register_matplotlib_converters
register_matplotlib_converters()
import statsmodels.formula.api as smf
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/statsmodels/tools/
_testing.py:19: FutureWarning: pandas.util.testing is deprecated. Use t
he functions in the public API at pandas.testing instead.
    import pandas.util.testing as tm
```

Getting Trace data from wrds

```
In [7]: db = wrds.Connection()
```

```
Enter your WRDS username [deepsha]:madhur5
Enter your password:.....
WRDS recommends setting up a .pgpass file.
You can find more info here:
https://www.postgresql.org/docs/9.5/static/libpq-pgpass.html.
Loading library list...
Done
```

```
In [149]: sql_query = """
SELECT *
FROM trace.trace_enhanced
WHERE CUSIP_ID in ('931142EH2','931142BF9','931142AU7','931142CK7','9311
42CM3','931142CH4','931142DB6','931142CS0','931142CB7','931142CY7','9311
42CV3','931142DK6','931142DQ3','931142DD2','931142EC3','931142DG5','9311
42EB5','931142EE9','931142DW0','931142ED1','931142EK5','931142DP5','9311
42EN9','931142CZ4','931142EJ8','931142EM1','931142EP4','931142EL3','9311
42DV2','931142DH3','931142EQ2','931142DU4','931142EA7')
AND TRD_EXCTN_DT BETWEEN '2009-01-01' AND '2019-12-31';
"""

data_query = db.raw_sql(sql_query)
```

```
In [151]: len(data_query)
```

```
Out[151]: 471077
```

Dick - Nielson Filtering

```
In [ ]: data_query['trd_exctn_tm'] = data_query['trd_exctn_tm'].apply(lambda x: 
datetime.timedelta(seconds=x))
data_query['trd_rpt_tm'] = data_query['trd_rpt_tm'].apply(lambda x: date
time.timedelta(seconds=x))

### Dick-Nielsen Filtering
# Cancellations, reversals and corrections
data_query = data_query[~data_query['trc_st'].isin(['C', 'Y', 'X'])]
#After Market Hours
data_query = data_query[data_query.sale_cndtn2_cd != 'A']
# Filter below 100 percentage pts
data_query = data_query[data_query['rptd_pr'] >= 100]
# Remove agency transactions without commissions
sell_index = data_query[(data_query['rpt_side_cd'] == 'S') & (data_query
['sell_cpcty_cd'] == 'A') & (data_query['cntra_mp_id'] == 'C') & (data_q
uery['cmsn_trd'] == 'N')].index
data_query.drop(sell_index, inplace=True)
buy_index = data_query[(data_query['rpt_side_cd'] == 'B') & (data_query[
'buy_cpcty_cd'] == 'A') & (data_query['cntra_mp_id'] == 'C') & (data_que
ry['cmsn_trd'] == 'N')].index
data_query.drop(buy_index, inplace=True)
# Remove interdealer transactions
interdealer_txn = data_query[(data_query['cntra_mp_id'] == 'D') & (data_
query['rpt_side_cd'] == 'B')].index
data_query.drop(interdealer_txn, inplace=True)
```

```
In [162]: data_query_subset_rolls = data_query[['cusip_id','bond_sym_id','trd_exct
n_dt','trd_exctn_tm','rptd_pr','rpt_side_cd']]
```

```
In [164]: data_query_subset_rolls.to_csv(r'data_query_subset_rolls')
```

finding the cusip with the most transactions

```
In [8]: most_txn_bond_cusip = data_query.groupby('bond_sym_id').size().sort_values(ascending=False).index[:5].values
# most_txn_bond_cusip
bond_transactions.groupby('bond_sym_id').size().sort_values(ascending=False).index
```

```
Out[8]: Index(['AFL.GC', 'ADT4117044', 'ADT4104761', 'ADT4192152', 'AES.HU', 'AFL.GB',
               'ADT3997702', 'ADSW4074463', 'ADT3991008', 'ADT3991009', 'AEPI.GG',
               'AESO.GA', 'AEPI.GD', 'AFC.GA', 'AES.GN', 'AES.GQ', 'AES.GM', 'ADCT.GC',
               'AEPI.GB', 'THG.GA', 'AES.GR', 'AES.GO', 'ADCT.GF', 'CG3706278',
               'FNHO3862006', 'AEPI.GE', 'AES.GL', 'AES.IS', 'AEEC.AA', 'ADST.AA',
               'ADCT.GE', 'CG3706277', 'TYC.GA', 'ACLI3862006', 'TEL3672364',
               'TEL3672363', 'AEPI.GC', 'IRWL3706275', 'AFL.GD', 'AVY.IE',
               'PPL3706275', 'ADCT.GD'],
              dtype='object', name='bond_sym_id')
```

FISD data

```
In [658]: fisd_data = pd.read_csv('/users/Deepsha/Downloads/fisd.csv')
fisd_data.head()
```

Out[658]:

	Unnamed: 0	COMPLETE_CUSIP	MATURITY	COUPON_TYPE	COUPON	PROSPECTUS_ISSUER_N
0	0	000361AA3	2001-11-01	F	9.50	AAR C
1	1	000361AB1	2003-10-15	F	7.25	AAR C
2	2	00077DAB5	1996-01-12	F	4.15	ABN AMRO BK N V N Y
3	3	00077DAF6	2009-08-01	F	8.25	ABN AMRO BK N V N Y
4	4	00077TAA2	2023-05-15	F	7.75	ABN AMRO BK N V N Y

5 rows × 33 columns

```
In [23]: sql_query = """
SELECT CUSIP_ID as "CUSIP_ID", TRD_EXCTN_DT as "TRD_EXCTN_DT",
       max(TRD_EXCTN_TM) as "TRD_EXCTN_TM",
       max(RPTD_PR) as "RPTD_PR",
       sum(ENTRD_VOL_QT) as "ENTRD_VOL_QT",
       max(RPT_SIDE_CD) as "RPT_SIDE_CD",
       max(TRC_ST) as "TRC_ST",
       max(ASOF_CD) as "ASOF_CD",
       max(MSG_SEQ_NB) as "MSG_SEQ_NB",
       max(ORIG_MSG_SEQ_NB) as "ORIG_MSG_SEQ_NB"
  from trace.trace_enhanced
 WHERE TRD_EXCTN_DT>'2010-01-01'
 group by CUSIP_ID, TRD_EXCTN_DT
 order by CUSIP_ID, TRD_EXCTN_DT;
"""

q2 = db.raw_sql(sql_query)
```

```
In [24]: q2.head()
```

Out[24]:

	CUSIP_ID	TRD_EXCTN_DT	TRD_EXCTN_TM	RPTD_PR	ENTRD_VOL_QT	RPT_SIDE_CD	TRC
0	000305AB8	2010-01-22	44651.0	100.00	64000.0	S	
1	000305AB8	2010-01-29	52684.0	100.00	64000.0	B	
2	000305AB8	2010-02-09	32311.0	98.50	60000.0	B	
3	000305AB8	2010-04-16	33784.0	99.25	20000.0	B	
4	000305AB8	2010-09-22	34440.0	98.50	347900.0	B	

Walmart Bond Liquidity Analysis

```
In [312]: cleaned_wmt = pd.read_csv("Cleaned_wmt.csv")
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/IPython/core/inter
activeshell.py:3057: DtypeWarning:
```

```
Columns (8,13,16,24) have mixed types. Specify dtype option on import or
set low_memory=False.
```

In [313]: cleaned_wmt

Out[313]:

	cusip_id	bond_sym_id	company_symbol	trd_exctn_dt	trd_exctn_tm	trd_rpt_dt	trd_rp
0	931142DB6	WMT.AB	WMT	20110412	8:51:13	20110412	8:51:13
1	931142DB6	WMT.AB	WMT	20110412	10:25:08	20110412	10:25:08
2	931142DB6	WMT.AB	WMT	20110412	11:24:00	20110412	11:24:00
3	931142DB6	WMT.AB	WMT	20110412	11:24:00	20110412	11:24:00
4	931142DB6	WMT.AB	WMT	20110412	11:27:30	20110412	11:27:30
...
290276	931142EP4	WMT4887055	WMT	20200331	12:58:58	20200331	12:58:58
290277	931142EP4	WMT4887055	WMT	20200331	12:58:58	20200331	12:58:58
290278	931142EP4	WMT4887055	WMT	20200331	16:20:36	20200331	16:20:36
290279	931142EP4	WMT4887055	WMT	20200331	16:41:55	20200331	16:41:55
290280	931142EP4	WMT4887055	WMT	20200331	17:21:51	20200331	17:21:51

290281 rows × 26 columns

Calculation of Rolls Measure

In [314]: `def lagged_auto_cov(Xi,t):`

```
N = len(Xi)
Xs = np.mean(Xi)
end_padded_series = np.zeros(N+t)
end_padded_series[:N] = Xi - Xs
start_padded_series = np.zeros(N+t)
start_padded_series[t:] = Xi - Xs

auto_cov = 1. / (N-1) * np.sum( start_padded_series*end_padded_series
)
return auto_cov
```

In [315]: `cleaned_wmt["trd_exctn_dt"] = pd.to_datetime(cleaned_wmt["trd_exctn_dt"], format="%Y%m%d")`

```
In [317]: uniques_cusips = cleaned_wmt.cusip_id.unique()
df_rs_wmt = pd.DataFrame(columns = ['cusip', 'date', 'auto_cov','rolls_spread'])
for k in uniques_cusips:
    x = cleaned_wmt[cleaned_wmt.cusip_id == k]
    auto_cov = []
    rolls_spread = []
    uniques_dates = x.trd_exctn_dt.unique()
    for i in range(0,len(uniques_dates)):
        p = x[x.trd_exctn_dt == uniques_dates[i]]['rptd_pr']
        d = np.diff(p)
        if len(d) == 0 or len(d) == 1 :
            a = np.nan
            r = np.nan
            auto_cov.append(np.nan)
            rolls_spread.append(np.nan)
        else:
            a = lagged_auto_cov(d,1)
            r = 2*np.sqrt(-a)
            auto_cov.append(a)
            rolls_spread.append(r)
    data = pd.DataFrame({'cusip':k , 'date':uniques_dates[i], 'auto_cov': a, 'rolls_spread' : r },index=[0])
    df_rs_wmt = df_rs_wmt.append(data)
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:18: RuntimeWarning:

invalid value encountered in sqrt

In [659]: df_rs_wmt.head()

Out[659]:

	COMPLETE_CUSIP	trd_exctn_dt	auto_cov	rolls_spread	year	month	year_month
0	931142DB6	2011-04-12	-0.117809	0.686466	2011	4	20114
0	931142DB6	2011-04-13	-0.008013	0.179029	2011	4	20114
0	931142DB6	2011-04-14	-0.467709	1.367784	2011	4	20114
0	931142DB6	2011-04-15	-0.013290	0.230564	2011	4	20114
0	931142DB6	2011-04-18	-0.982859	1.982784	2011	4	20114

```
In [319]: df_rs_wmt['year'] = pd.DatetimeIndex(df_rs_wmt['date']).year
df_rs_wmt['month'] = pd.DatetimeIndex(df_rs_wmt['date']).month
df_rs_wmt["year_month"] = df_rs_wmt['year'].astype(str) + df_rs_wmt['month'].astype(str)
```

```
In [320]: df_rs_wmt.dtypes
```

```
Out[320]: cusip          object
date            datetime64[ns]
auto_cov        float64
rolls_spread    float64
year            int64
month           int64
year_month      object
dtype: object
```

```
In [321]: g = df_rs_wmt.groupby(["year_month"])
monthly_averages = g.aggregate({"rolls_spread":np.mean})
```

```
In [322]: monthly_averages.head()
```

```
Out[322]:
rolls_spread
```

year_month	rolls_spread
20071	2.054803
200710	1.957956
200711	2.065796
200712	2.342166
20072	2.071908

```
In [324]: monthly_averages['date'] = monthly_averages.index
monthly_averages['Date'] = pd.to_datetime(monthly_averages['date'], format='%Y%m')
monthly_averages = monthly_averages.sort_values(by="Date")
```

```
In [327]: monthly_averages.unstack(level =1).dropna()
```

```
Out[327]:
rolls_spread  year_month
20071          2.0548
20072          2.07191
20073          1.5568
20074          1.6639
20075          1.68826
...
Date          201911  2019-11-01 00:00:00
              201912  2019-12-01 00:00:00
              20201   2020-01-01 00:00:00
              20202   2020-02-01 00:00:00
              20203   2020-03-01 00:00:00
Length: 477, dtype: object
```

In [191]: df_rs

Out[191]:

month	rolls_spread									
	1	2	3	4	5	6	7	8	9	
year										
2007	2.054803	2.071908	1.556803	1.663898	1.688256	1.912134	2.608851	1.615786	1.985052	
2008	2.029783	2.244261	2.453255	2.219971	2.406434	2.092986	2.745232	2.866189	2.318209	
2009	2.514892	2.605601	2.611524	2.780327	2.650243	2.611532	2.088986	1.983868	1.776198	
2010	1.341853	1.740805	1.321628	1.802177	2.018981	1.979389	1.814921	1.645156	1.425124	
2011	1.640544	1.426926	1.497672	1.294161	1.294624	1.387083	1.552728	1.645759	1.889168	
2012	1.581219	1.527863	1.279952	1.068730	1.257127	1.274706	1.304365	1.090537	1.023637	
2013	0.901313	0.939662	0.941415	0.925082	1.020712	1.310737	0.976045	1.023553	1.020343	
2014	0.842588	1.105697	0.803572	0.881554	0.796003	0.943337	0.925418	0.891254	0.826172	
2015	0.849146	0.856662	0.913300	0.817295	0.758596	0.797849	1.192001	0.885466	0.851538	
2016	0.746235	0.913059	0.887744	0.812485	0.854331	0.849817	0.903953	0.868819	0.808108	
2017	0.682234	0.893176	0.598404	0.709409	0.645541	0.670067	0.704391	0.630452	0.575980	
2018	0.606588	1.004431	0.635912	0.910718	0.862186	0.425905	0.455956	0.504976	0.510923	
2019	0.578460	0.520910	0.551238	0.511739	0.466513	0.394595	0.462972	0.445645	0.484216	
2020	0.429784	0.390116	1.326876		NaN	NaN	NaN	NaN	NaN	

Bid - Ask Liquidity Cost

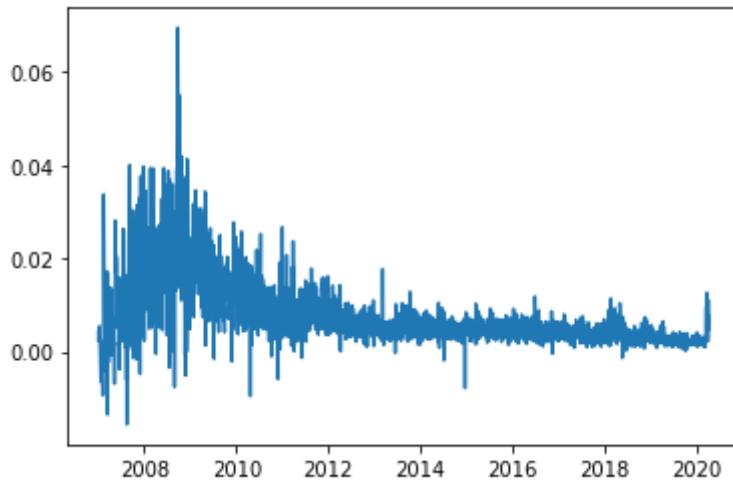
In []: data_query_subset_lc = cleaned_wmt.groupby(['cusip_id','trd_exctn_dt','rpt_side_cd'])['rptd_pr'].mean().unstack(level = 2).dropna()
 data_query_subset_lc['LC'] = (data_query_subset_lc['S']- data_query_subset_lc['B'])/(0.5*(data_query_subset_lc['S']+ data_query_subset_lc['B']))

In [508]: df_lc = data_query_subset_lc.groupby(['trd_exctn_dt']).mean()

```
In [509]: plt.plot(df_lc.LC)
```

```
Out[509]: [

```



```
In [332]: df_lc['date'] = df_lc.index
df_lc['year'] = pd.DatetimeIndex(df_lc['date']).year
df_lc['month'] = pd.DatetimeIndex(df_lc['date']).month
df_lc["year_month"] = df_lc['year'].astype(str) + df_lc['month'].astype(str)
```

```
In [333]: df_lc
```

```
Out[333]:
```

rpt_side_cd	B	S	LC	date	year	month	year_month
trd_exctn_dt							
2007-01-03	121.338000	121.838380	0.004115	2007-01-03	2007	1	20071
2007-01-04	116.006250	116.276385	0.002209	2007-01-04	2007	1	20071
2007-01-05	121.933000	122.259000	0.002670	2007-01-05	2007	1	20071
2007-01-10	121.890000	122.370600	0.003935	2007-01-10	2007	1	20071
2007-01-12	120.209999	120.864500	0.005430	2007-01-12	2007	1	20071
...
2020-03-25	109.806382	110.059774	0.002182	2020-03-25	2020	3	20203
2020-03-26	113.377161	114.695204	0.011080	2020-03-26	2020	3	20203
2020-03-27	115.707856	116.294219	0.004962	2020-03-27	2020	3	20203
2020-03-30	113.312589	114.162816	0.007273	2020-03-30	2020	3	20203
2020-03-31	114.946111	115.504779	0.004742	2020-03-31	2020	3	20203

3190 rows × 7 columns

Liquidity Cost Monthly Average

```
In [334]: df_lc = df_lc.groupby(["year_month"])
df_lc_ma = df_lc.aggregate({"LC":np.mean})
```

```
In [335]: df_lc_ma
```

Out[335]:

LC

year_month	LC
20071	0.000511
200710	0.012864
200711	0.019669
200712	0.025485
20072	0.004763
...	...
20198	0.002376
20199	0.001749
20201	0.002083
20202	0.001887
20203	0.005801

159 rows × 1 columns

Merging Rolls spread and Liquidity Cost

```
In [336]: df_lc_rs = df_lc_ma.join(monthly_averages, how='inner')
```

```
In [339]: df_lc_rs.head()
```

Out[339]:

	LC	rolls_spread	date	Date
year_month				
20071	0.000511	2.054803	20071	2007-01-01
20072	0.004763	2.071908	20072	2007-02-01
20073	0.002092	1.556803	20073	2007-03-01
20074	0.005565	1.663898	20074	2007-04-01
20075	0.009949	1.688256	20075	2007-05-01

```
In [49]: df_lc_rs['year_month'] = df_lc_rs.index
df_lc_rs['Date'] = pd.to_datetime(df_lc_rs['year_month'], format='%Y%m')
```

```
In [338]: df_lc_rs = df_lc_rs.sort_values(by="Date")
```

```
In [60]: df_lc_ma['_year_month'] = df_lc_ma.index
df_lc_ma['Date'] = pd.to_datetime(df_lc_ma['_year_month'], format='%Y%m')
df_lc_ma = df_lc_ma.sort_values(by="Date")
```

```
In [62]: df_lc_ma.head()
```

Out[62]:

	LC	_year_month	Date
year_month			
20071	0.000511	20071	2007-01-01
20072	0.004763	20072	2007-02-01
20073	0.002092	20073	2007-03-01
20074	0.005565	20074	2007-04-01
20075	0.009949	20075	2007-05-01

Average of Rolls Spread and Liquidity cost

```
In [661]: df_lc_rs["rs_and_LC_average"] = (df_lc_rs['rolls_spread'] + df_lc_rs['LC']*100)/2
df_lc_rs.head()
```

Out[661]:

	LC	rolls_spread	date	Date	rs_and_LC_average
year_month					
20071	0.000511	2.054803	20071	2007-01-01	1.052958
20072	0.004763	2.071908	20072	2007-02-01	1.274095
20073	0.002092	1.556803	20073	2007-03-01	0.883022
20074	0.005565	1.663898	20074	2007-04-01	1.110200
20075	0.009949	1.688256	20075	2007-05-01	1.341571

```
In [485]: import plotly.express as px
import plotly.graph_objects as go
fig = go.Figure(data=go.Scatter(x=df_lc_rs['Date'], y=df_lc_rs['rolls_spread'],name = 'Rolls Spread'),layout=go.Layout(
    title=go.layout.Title(text='<b>Time Series of Liquidity Measures for Walmart Bonds (as Percentage of Value)</b>')))
fig.add_scatter(x=df_lc_rs['Date'], y=df_lc_rs['LC']*100, mode='lines',name = 'Liquidity Cost(Bid-Ask Spread)')
fig.add_scatter(x=df_lc_rs['Date'], y=df_lc_rs["rs_and_LC_average"], mode='lines',name = 'Average of Rolls Spread and Liquidity Cost')
fig.update_layout(legend_title_text = "<b>Liquidity Measures</b>")
fig.update_xaxes(title_text="years -->")
fig.update_yaxes(title_text="Liquidity Measure (as Percentage of Value")
)
fig.show("notebook")
```

Time Series of Liquidity Measures for Walmart Bonds (as Percentage of Value)



Correlation of Rolls spread and Liquidity Spread

```
In [223]: df_lc_rs['rolls_spread'].corr(df_lc_rs['LC'])
```

```
Out[223]: 0.8615707694938298
```

Bond Characteristics Calculations

```
In [359]: cleaned_wmt = cleaned_wmt.rename(columns={"cusip_id": "COMPLETE_CUSIP"})
cleaned_wmt_fisd = pd.merge(cleaned_wmt,fisd_data, how = "inner", on =
"COMPLETE_CUSIP")
cleaned_wmt_fisd["trd_exctn_dt"] = pd.to_datetime(cleaned_wmt_fisd ["trd
_exctn_dt"], format="%Y%m%d")
```

```
In [362]: import numpy as np
import scipy
cleaned_wmt_fisd['MATURITY'] = cleaned_wmt_fisd['MATURITY'].apply(pd.to_
datetime)
cleaned_wmt_fisd['Days_to_Maturity'] = (cleaned_wmt_fisd['MATURITY']- cl
eaned_wmt_fisd['trd_exctn_dt'])
cleaned_wmt_fisd['N_MATURITY'] = ((cleaned_wmt_fisd['Days_to_Maturity'] /
365) * 2)/np.timedelta64(1, 'D')
cleaned_wmt_fisd = cleaned_wmt_fisd[cleaned_wmt_fisd['Days_to_Maturity'] > pd.Timedelta(0, 'D')]

yld = {}
for i in range(0, len(cleaned_wmt_fisd)):
    try:
        yld.update({i:YieldCalc(cleaned_wmt_fisd['COUPON'].iloc[i]/(clea
ned_wmt_fisd['PRINCIPAL_AMT'].iloc[i]/10),cleaned_wmt_fisd['rptd_pr'].il
oc[i],
                           cleaned_wmt_fisd['PRINCIPAL_AMT'].iloc[i]/10, 2.0,
                           cleaned_wmt_fisd['N_MATURITY'].iloc[i],
                           cleaned_wmt_fisd['COUPON'].iloc[i])})
    except(RuntimeError):
        pass
    else:
        pass

l = []
for i in yld:
    l.append(yld[i])

cleaned_wmt_fisd['YTM'] = pd.Series(l, index=cleaned_wmt_fisd.index)
```

In [363]: cleaned_wmt_fisd.head()

Out[363]:

	COMPLETE_CUSIP	bond_sym_id	company_symbol	trd_exctn_dt	trd_exctn_tm	trd_rpt_dt	trd_
0	931142DB6	WMT.AB	WMT	2011-04-12	8:51:13	20110412	
1	931142DB6	WMT.AB	WMT	2011-04-12	10:25:08	20110412	1
2	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	20110412	1
3	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	20110412	1
4	931142DB6	WMT.AB	WMT	2011-04-12	11:27:30	20110412	1

5 rows × 61 columns

Merging Fisd and Walmart data

In [665]: cleaned_wmt_fisd.head()

Out[665]:

	COMPLETE_CUSIP	bond_sym_id	company_symbol	trd_exctn_dt	trd_exctn_tm	trd_rpt_dt	trd_
0	931142DB6	WMT.AB	WMT	2011-04-12	8:51:13	2011-04-12	
1	931142DB6	WMT.AB	WMT	2011-04-12	10:25:08	2011-04-12	1
2	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	2011-04-12	1
3	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	2011-04-12	1
4	931142DB6	WMT.AB	WMT	2011-04-12	11:27:30	2011-04-12	1

5 rows × 66 columns

Duration Calculation

```
In [364]: def duration(coupon,YTM,freq,years,Price,Principle):
    period=1/freq
    N=np.floor(years)/period+1
    T=years-np.floor(years)+0.5*np.arange(N)
    M=np.sum([coupon*t/pow(1+YTM,t) for t in T])+Principle*years/pow(1+YT
M,years)
    return M/(Price*10)

def days2years(d):
    return d.days/365.25

def calculate_duration(data):
    # Calculate Duration
    #data1 = pd.read_csv('trace_fisd_merged.csv') #Change directory as
necessary

    data['trd_rpt_dt']=pd.to_datetime(data['trd_rpt_dt'],format='%Y-%m-%d')
    data['MATURITY']=pd.to_datetime(data['MATURITY'])
    data['diff'] = data['MATURITY']-data['trd_rpt_dt']
    data['years_TM']=data.apply(lambda row: days2years(row['diff']),axis
=1)
    data['semicoupon']=data['COUPON']/100*data['PRINCIPAL_AMT']/data['IN
TEREST_FREQUENCY']
    data['Duration_MAC']=data.apply(lambda row:duration(row['semicoupon'
],row['YTM']),\
                                     row['INTEREST_FREQUE
NCY'],row['years_TM'],\
                                     row['rptd_pr'],row[
'PRINCIPAL_AMT']),axis=1)

    data['Duration_MOD']=data['Duration_MAC']/(1+data['YTM'])
    return data
```

```
In [365]: test = calculate_duration(cleaned_wmt_fisd)
```

```
In [666]: merged_df.head()
```

Out[666]:

	COMPLETE_CUSIP	bond_sym_id	company_symbol	trd_exctn_dt	trd_exctn_tm	trd_rpt_dt	trd_
0	931142DB6	WMT.AB	WMT	2011-04-12	8:51:13	2011-04-12	
1	931142DB6	WMT.AB	WMT	2011-04-12	10:25:08	2011-04-12	1
2	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	2011-04-12	1
3	931142DB6	WMT.AB	WMT	2011-04-12	11:24:00	2011-04-12	1
4	931142DB6	WMT.AB	WMT	2011-04-12	11:27:30	2011-04-12	1

5 rows × 71 columns

```
In [366]: df_rs_wmt = df_rs_wmt.rename(columns={"cusip": "COMPLETE_CUSIP", "date": "trd_exctn_dt"})
merged_df = test.merge(df_rs_wmt, how='inner', on=["COMPLETE_CUSIP", "trd_exctn_dt"])
```

```
In [ ]: test1 = merged_df.groupby(["trd_exctn_dt"]).mean()
test1 = test1.dropna()
test1 = test1[["rolls_spread"]]
```

30 yr Treasury Yield

```
In [90]: tr30 = pd.read_csv("DGS30.csv")
tr30 = tr30.rename(columns={"DATE": "trd_exctn_dt"})
tr30["trd_exctn_dt"] = pd.to_datetime(tr30["trd_exctn_dt"])
```

```
In [98]: tr30 = tr30[tr30['DGS30'] != ".."]
tr30
```

Out[98]:

	trd_exctn_dt	DGS30
0	2007-01-02	4.79
1	2007-01-03	4.77
2	2007-01-04	4.72
3	2007-01-05	4.74
4	2007-01-08	4.74
...
3601	2020-10-21	1.62
3602	2020-10-22	1.67
3603	2020-10-23	1.64
3604	2020-10-26	1.59
3605	2020-10-27	1.57

3460 rows × 2 columns

```
In [99]: test1_tr30= pd.merge(test1,tr30, how ="inner", on = "trd_exctn_dt")
test1_tr30[ "spread" ] = (test1_tr30[ "DGS30" ].astype(float)/100) - test1_tr30[ "YTM" ]
test1_tr30[ "spread_Duration" ] = test1_tr30[ "spread" ]*test1_tr30[ "Duration_MAC" ]
```

```
In [100]: test1_tr30_sub = test1_tr30[["rolls_spread", "spread", "spread_Duration"]]
```

Age Calculation

```
In [ ]: #import datetime
merged_df[ 'OFFERING_DATE' ] = pd.to_datetime(merged_df[ 'OFFERING_DATE' ])
merged_df[ 'Age' ] = (merged_df[ 'trd_exctn_dt' ] - merged_df[ 'OFFERING_DATE' ]).apply(lambda x: (x.days)/365)
merged_df_ = merged_df.dropna(subset=[ 'rolls_spread' ])
merged_df_age = merged_df_.groupby([ "COMPLETE_CUSIP" ])['rolls_spread', 'Age'].mean()

In [113]: merged_df[ 'trd_exctn_dt' ] = pd.to_datetime(merged_df[ 'trd_exctn_dt' ])
```

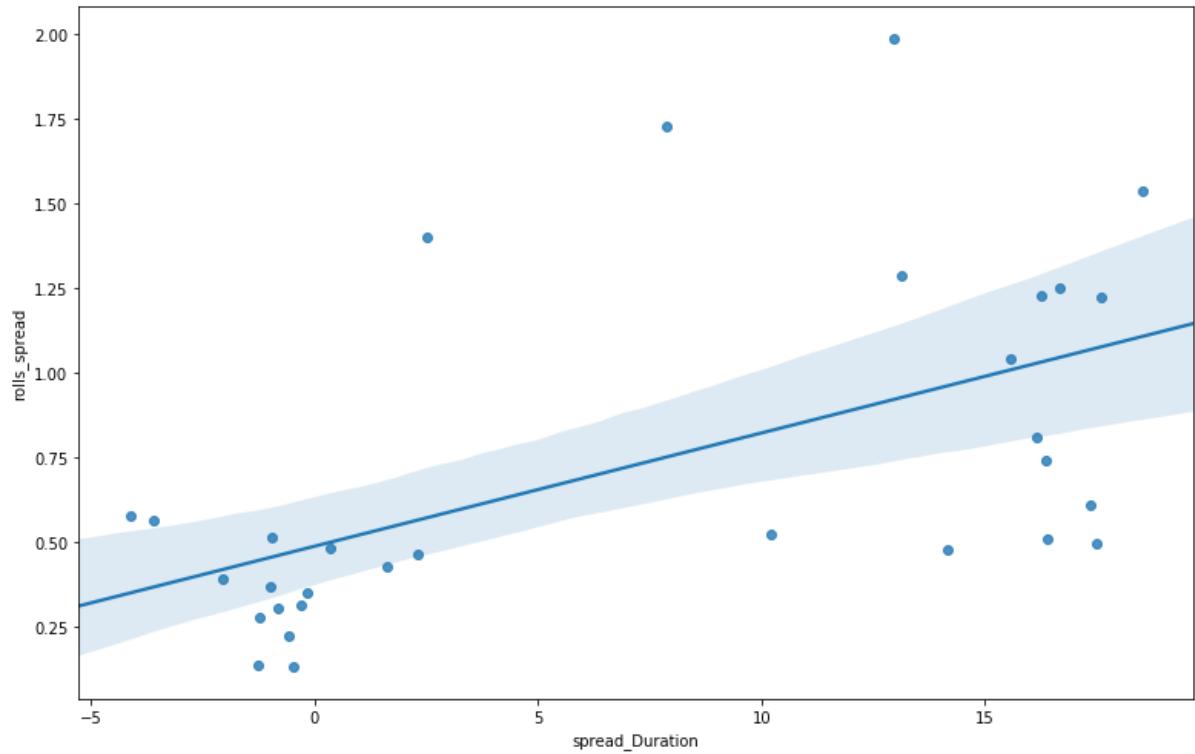
Spread Duration and Issue size Calculation

```
In [123]: merged_df_tr30= pd.merge(merged_df_,tr30, how ="inner", on = "trd_exctn_dt")
merged_df_tr30[ "spread" ] = merged_df_tr30[ "YTM" ] - (merged_df_tr30[ "DGS30" ].astype(float)/100)
merged_df_tr30[ "spread_Duration" ] = merged_df_tr30[ "spread" ]*merged_df_tr30[ "Duration_MAC" ]*100
merged_df_tr30[ "issue_size" ] = merged_df_tr30[ "OFFERING_AMT" ]*merged_df_tr30[ "PRINCIPAL_AMT" ]
merged_df_spreadD = merged_df_tr30.groupby([ "COMPLETE_CUSIP" ])['rolls_spread', 'spread_Duration'].mean()

In [ ]: merged_df_issue_size = merged_df_tr30.groupby([ "COMPLETE_CUSIP" ])['rolls_spread', 'issue_size'].mean()
merged_df_issue_size[ "issue_size" ] = merged_df_issue_size[ "issue_size" ]/1000000000
sns.jointplot(x=merged_df_issue_size[ "issue_size" ], height = 8, y=merged_df_issue_size[ "rolls_spread" ],color= "black", kind="reg", stat_func=r2)
```

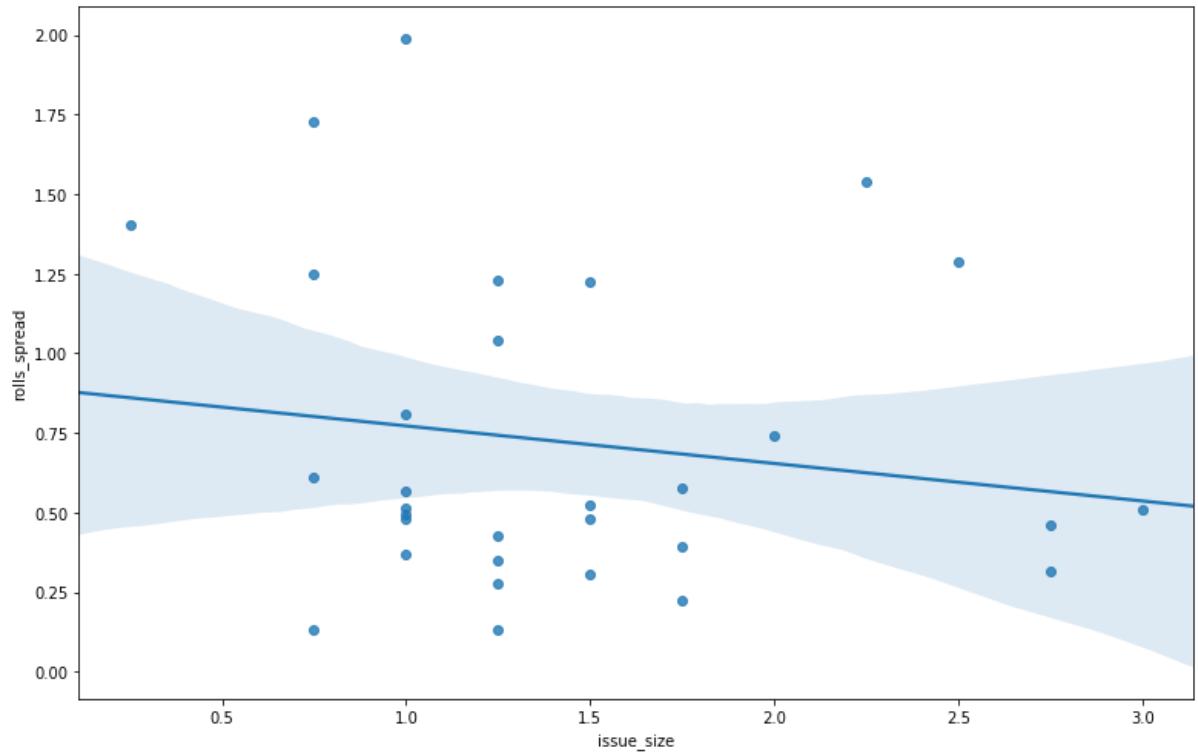
```
In [195]: a4_dims = (13, 8.27)
fig, ax = pyplot.subplots(figsize=a4_dims)
sns.regplot(x=merged_df_spreadD["spread_Duration"], y=merged_df_spreadD[
    "rolls_spread"])
```

Out[195]: <matplotlib.axes._subplots.AxesSubplot at 0x173dc74a8>



```
In [216]: a4_dims = (13, 8.27)
fig, ax = pyplot.subplots(figsize=a4_dims)
sns.regplot(x=merged_df_issue_size["issue_size"], y=merged_df_issue_size
[ "rolls_spread" ])
```

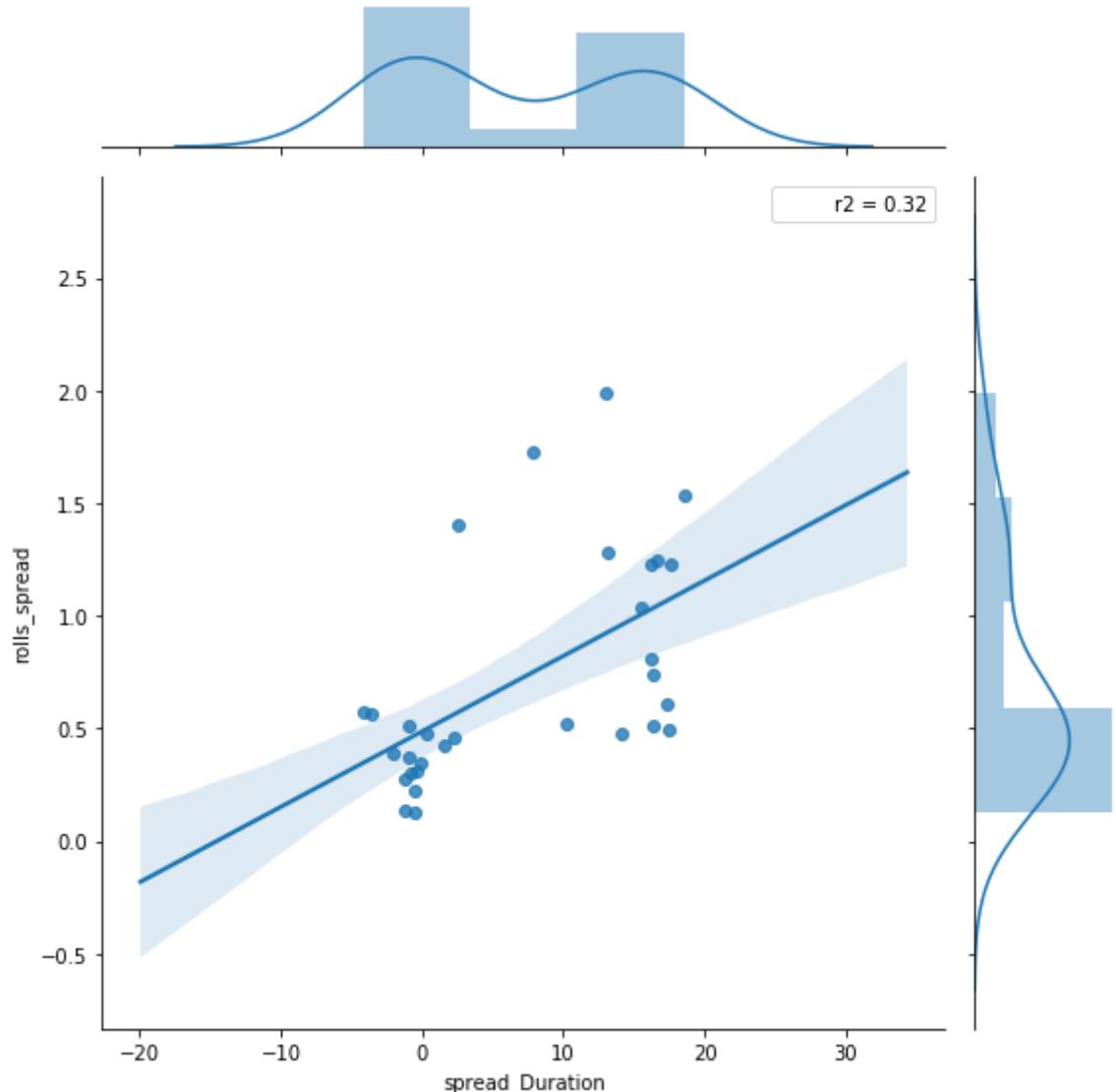
Out[216]: <matplotlib.axes._subplots.AxesSubplot at 0x177786f60>



Joinplots with R square

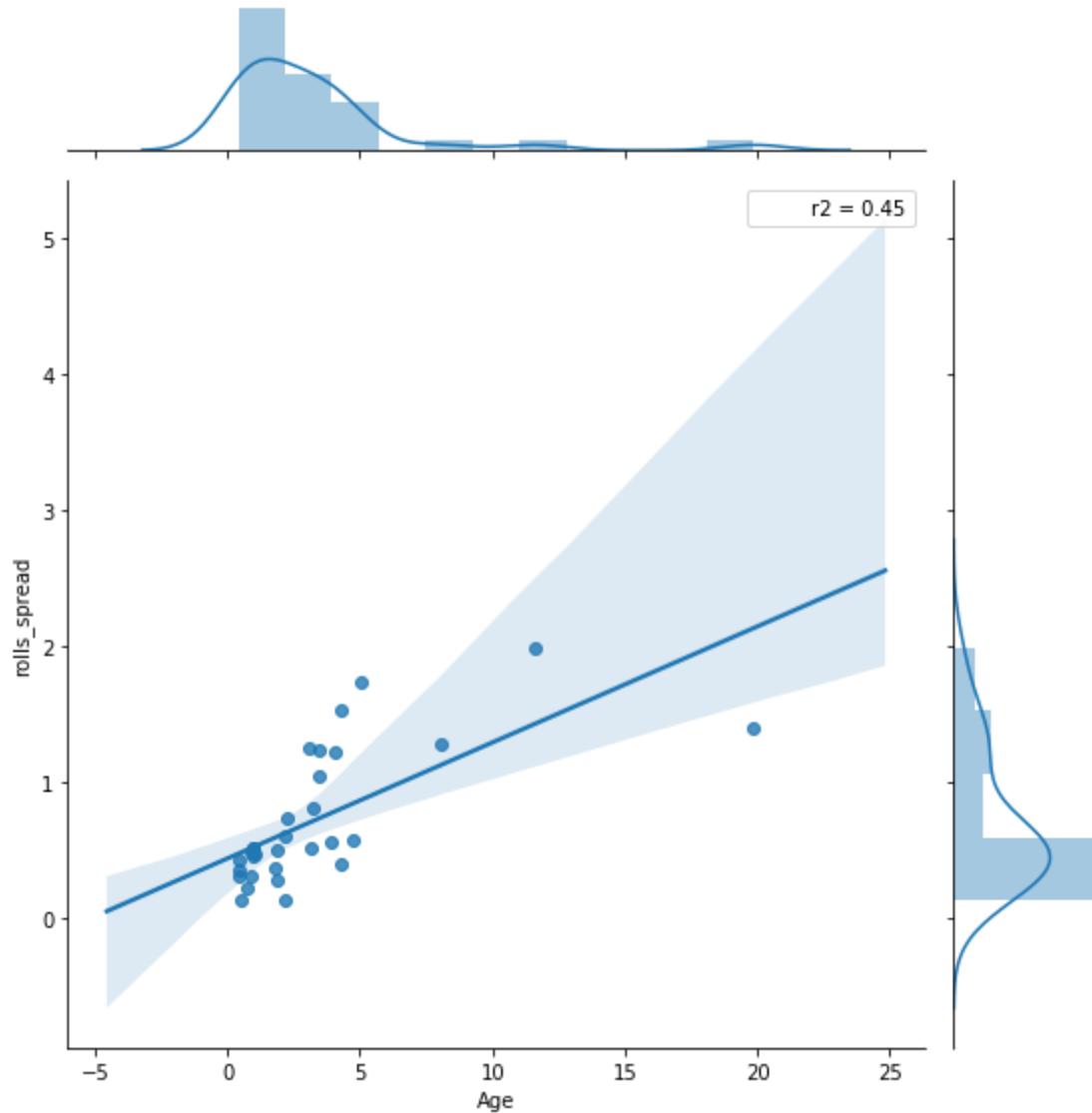
```
In [330]: from scipy import stats
def r2(x, y):
    return stats.pearsonr(x, y)[0] ** 2
sns.jointplot(x=merged_df_spreadD["spread_Duration"], y=merged_df_spreadD["rolls_spread"], height = 8,kind="reg", stat_func=r2)
```

Out[330]: <seaborn.axisgrid.JointGrid at 0x1633a7c18>



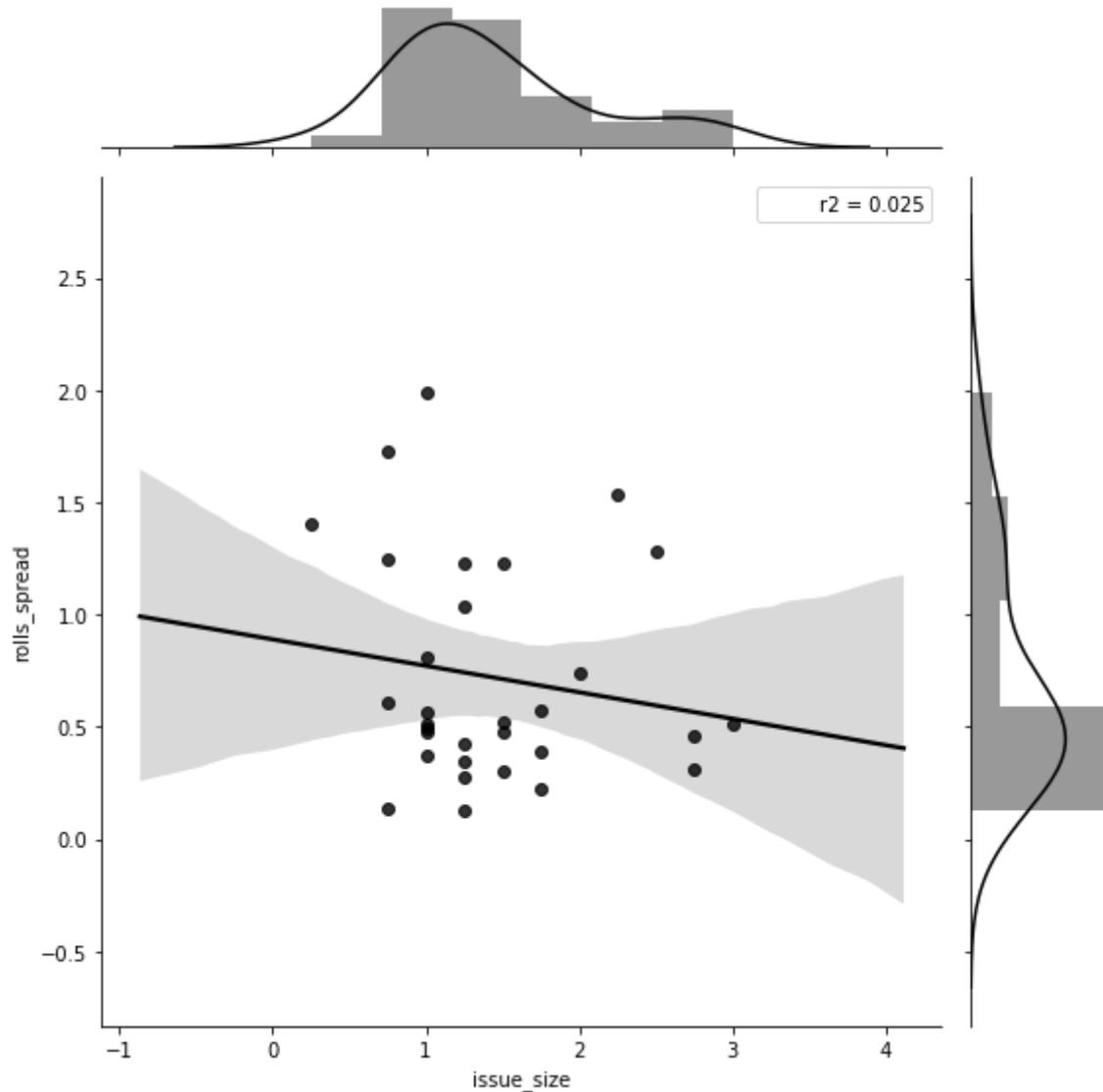
```
In [329]: sns.jointplot(x=merged_df_age[ "Age" ], y=merged_df_age[ "rolls_spread" ], height = 8, kind="reg", stat_func=r2)
```

```
Out[329]: <seaborn.axisgrid.JointGrid at 0x16e44f320>
```



```
In [333]: sns.jointplot(x=merged_df_issue_size["issue_size"], height = 8, y=merged_df_issue_size["rolls_spread"],color= "black", kind="reg", stat_func=r2)
```

```
Out[333]: <seaborn.axisgrid.JointGrid at 0x16fa74898>
```



Regression Summary for Issue size, Age and Spread Duration

```
In [222]: import statsmodels.formula.api as smf
import statsmodels.api as sm

results = smf.ols('rolls_spread ~ issue_size', data=merged_df_issue_size
).fit()
print(results.summary())
```

OLS Regression Results

=====
Dep. Variable: rolls_spread R-squared: 0.025
Model: OLS Adj. R-squared: -0.009
Method: Least Squares F-statistic: 0.7413
Date: Thu, 29 Oct 2020 Prob (F-statistic): 0.396
Time: 18:01:34 Log-Likelihood: -21.240
No. Observations: 31 AIC: 46.48
Df Residuals: 29 BIC: 49.35
Df Model: 1
Covariance Type: nonrobust
=====

=====
coef std err t P>|t| [0.025
0.975]

	coef	std err	t	P> t	[0.025 0.975]
Intercept	0.8898	0.215	4.143	0.000	0.451 1.329
issue_size	-0.1179	0.137	-0.861	0.396	-0.398 0.162

=====
Omnibus: 4.909 Durbin-Watson: 0.354
Prob(Omnibus): 0.086 Jarque-Bera (JB): 4.304
Skew: 0.909 Prob(JB): 0.116
Kurtosis: 2.834 Cond. No. 5.12
=====

=====
Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [224]: results = smf.ols('rolls_spread ~ Age', data= merged_df_age).fit()
print(results.summary())
```

OLS Regression Results

=====
Dep. Variable: rolls_spread R-squared: 0.452
Model: OLS Adj. R-squared: 0.433
Method: Least Squares F-statistic: 23.89
Date: Thu, 29 Oct 2020 Prob (F-statistic): 3.47e-05
Time: 18:03:15 Log-Likelihood: -12.316
No. Observations: 31 AIC: 28.63
Df Residuals: 29 BIC: 31.50
Df Model: 1
Covariance Type: nonrobust
=====

=====
0.975] coef std err t P>|t| [0.025

	coef	std err	t	P> t	[0.025
Intercept	0.4395	0.088	4.976	0.000	0.259
Age	0.0852	0.017	4.888	0.000	0.050

=====
Omnibus: 2.511 Durbin-Watson: 1.113
Prob(Omnibus): 0.285 Jarque-Bera (JB): 1.859
Skew: 0.599 Prob(JB): 0.395
Kurtosis: 2.955 Cond. No. 6.81
=====

=====
Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [225]: results = smf.ols('rolls_spread ~ spread_Duration', data=merged_df_spreadD).fit()
print(results.summary())
```

OLS Regression Results

=====

Dep. Variable: rolls_spread R-squared:

0.319

Model: OLS Adj. R-squared:

0.296

Method: Least Squares F-statistic:

13.61

Date: Thu, 29 Oct 2020 Prob (F-statistic):

0.000924

Time: 18:04:10 Log-Likelihood:

-15.666

No. Observations: 31 AIC:

35.33

Df Residuals: 29 BIC:

38.20

Df Model: 1

Covariance Type: nonrobust

=====

	coef	std err	t	P> t	[0.025
0.975]					

Intercept	0.4873	0.098	4.979	0.000	0.287
0.687					
spread_Duration	0.0335	0.009	3.689	0.001	0.015
0.052					
=====					
Omnibus:	8.540	Durbin-Watson:			
0.739					
Prob(Omnibus):	0.014	Jarque-Bera (JB):			
7.015					
Skew:	1.086	Prob(JB):			
0.0300					
Kurtosis:	3.845	Cond. No.			
14.2					
=====					
=====					
Warnings:					
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.					

Trailing One month Volume Calculation

```
In [134]: uniques_cusips = merged_df_.COMPLETE_CUSIP.unique()
merged_df_TV = pd.DataFrame(columns = ['entrnd_vol_qt','rolls_spread','COMPLETE_CUSIP','_year_month','date_monthly','trailing_vol'])
for k in uniques_cusips:
    x = merged_df_[merged_df_.COMPLETE_CUSIP == k]
    x['year'] = pd.DatetimeIndex(x['trd_exctn_dt']).year
    x['month'] = pd.DatetimeIndex(x['trd_exctn_dt']).month
    x["year_month"] = x['year'].astype(str) + x['month'].astype(str)
    x = x.groupby(["year_month"])
    x_s = x.aggregate({"entrnd_vol_qt":np.sum,"rolls_spread": np.mean})
    x_s['COMPLETE_CUSIP'] = k
    x_s['_year_month'] = x_s.index
    x_s['date_monthly'] = pd.to_datetime(x_s['_year_month'], format='%Y%m')
    x_s = x_s.sort_values(by="date_monthly")
    x_s['trailing_vol'] = x_s['entrnd_vol_qt'].shift(1)
    merged_df_TV = merged_df_TV.append(x_s)
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:5: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:6: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:7: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

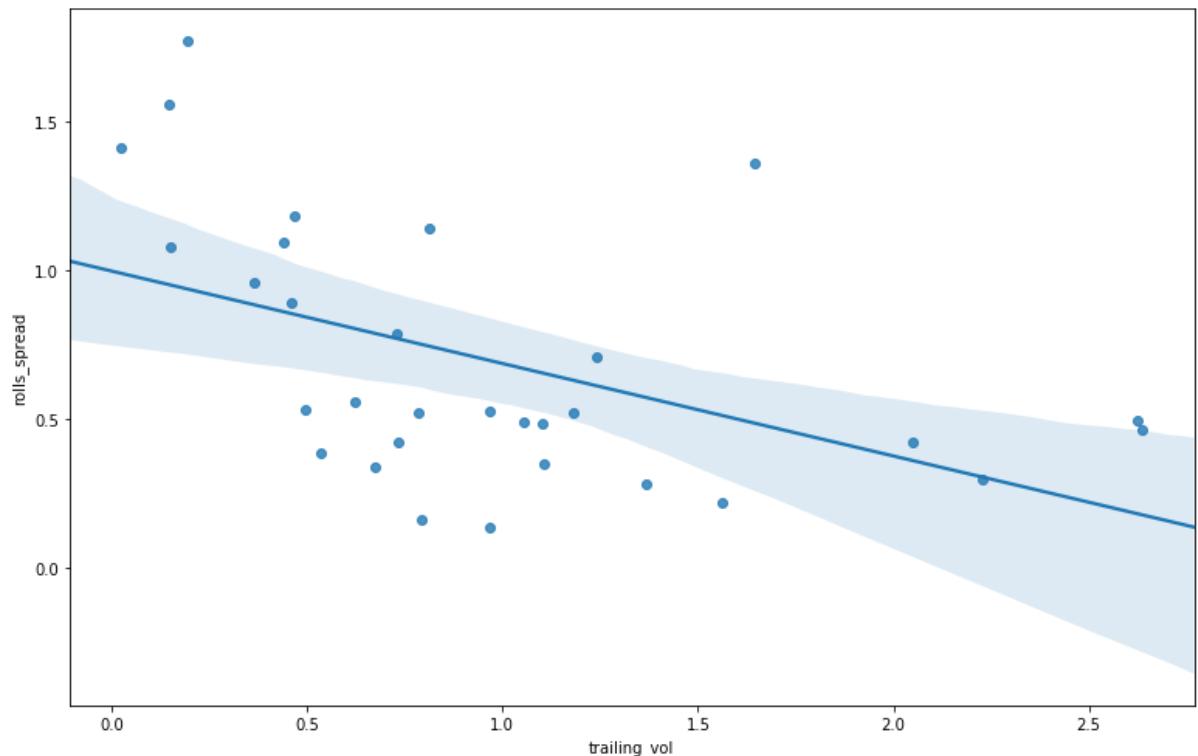
See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
In [138]: merged_df_TV_main = merged_df_TV.groupby(["COMPLETE_CUSIP"])['rolls_spread','trailing_vol'].mean()
merged_df_TV_main['trailing_vol'] = merged_df_TV_main['trailing_vol']/1000000
```

Regplot of Trailing One Month Volume

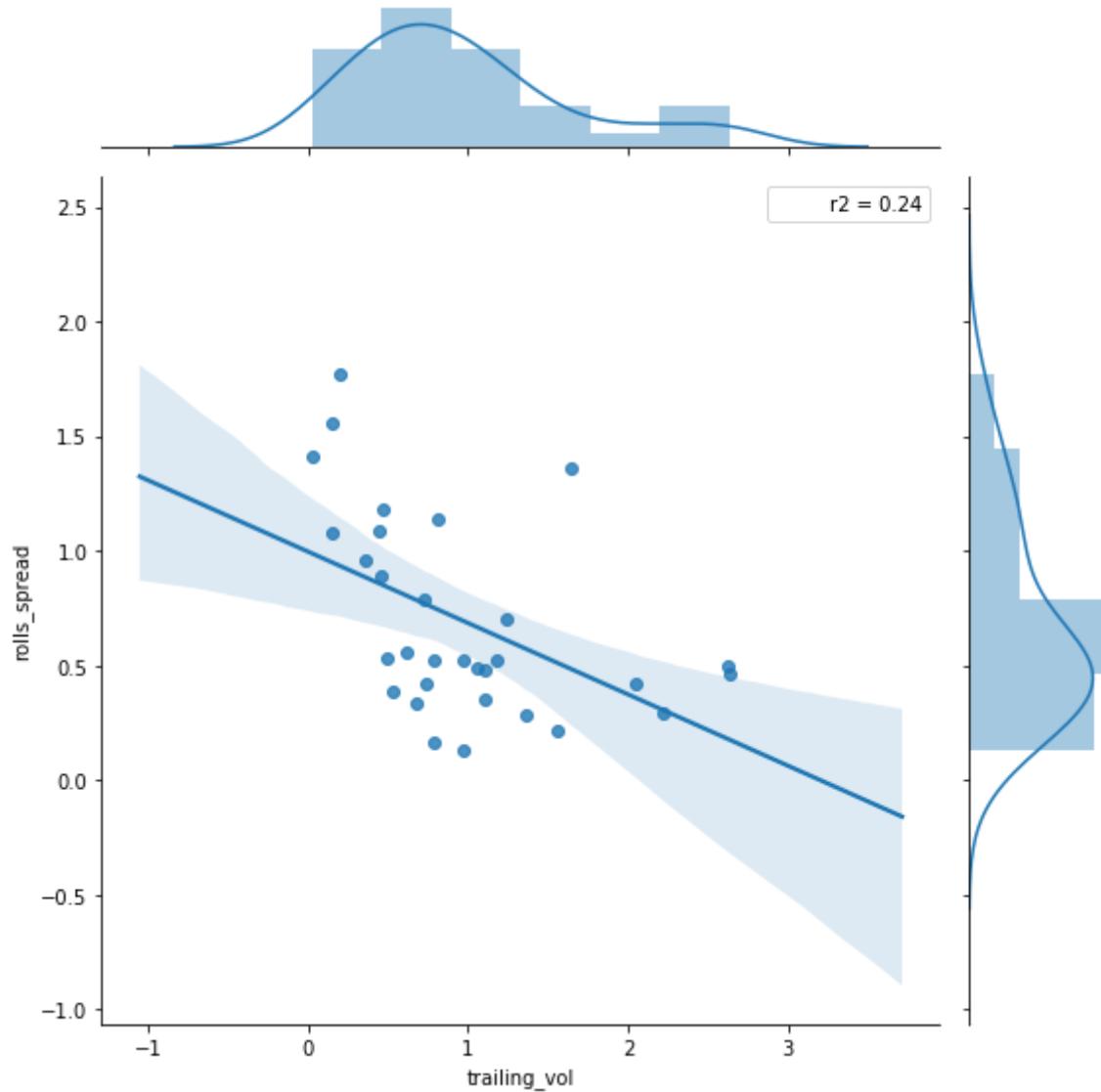
```
In [283]: a4_dims = (13, 8.27)
fig, ax = pyplot.subplots(figsize=a4_dims)
sns.regplot(x=merged_df_TV_main["trailing_vol"], y=merged_df_TV_main["rolls_spread"])
```

```
Out[283]: <matplotlib.axes._subplots.AxesSubplot at 0x171168160>
```



```
In [327]: sns.jointplot(x=merged_df_TV_main["trailing_vol"], y = merged_df_TV_main["rolls_spread"], height = 8 ,kind="reg", stat_func=r2)
```

```
Out[327]: <seaborn.axisgrid.JointGrid at 0x170177b38>
```



regression Summary for One month trailing Volume

```
In [287]: results = smf.ols('rolls_spread ~ trailing_vol', data=merged_df_TV_main)
    .fit()
print(results.summary())
```

OLS Regression Results

=====
Dep. Variable: rolls_spread R-squared: 0.242
Model: OLS Adj. R-squared: 0.216
Method: Least Squares F-statistic: 9.275
Date: Thu, 29 Oct 2020 Prob (F-statistic): 0.00491
Time: 20:22:54 Log-Likelihood: -13.344
No. Observations: 31 AIC: 30.69
Df Residuals: 29 BIC: 33.56
Df Model: 1
Covariance Type: nonrobust
=====

coef std err t P>|t| [0.025
0.975]

	coef	std err	t	P> t	[0.025 0.975]
Intercept	0.9965	0.121	8.239	0.000	0.749 1.244
trailing_vol	-0.3107	0.102	-3.045	0.005	-0.519 -0.102

=====
Omnibus: 2.332 Durbin-Watson: 1.007
Prob(Omnibus): 0.312 Jarque-Bera (JB): 1.928
Skew: 0.599 Prob(JB): 0.381
Kurtosis: 2.760 Cond. No. 3.24
=====

=====
Warnings:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
In [141]: merged_df_spreadD = merged_df_tr30.groupby(["COMPLETE_CUSIP"])['rolls_spread', "spread_Duration"].mean()  
merged_df_issue_size = merged_df_tr30.groupby(["COMPLETE_CUSIP"])['rolls_spread', "issue_size"].mean()
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:1: FutureWarning:
```

```
Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: FutureWarning:
```

```
Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.
```

```
In [148]: merged_1 = pd.merge(merged_df_issue_size,merged_df_spreadD,how ="inner",  
on = "COMPLETE_CUSIP")  
merged_2 = pd.merge(merged_1,merged_df_TV_main,how ="inner", on = "COMPLETE_CUSIP")  
merged_3 = pd.merge(merged_2,merged_df_age,how ="inner", on = "COMPLETE_CUSIP")
```

```
In [151]: merged_3 = merged_3[['rolls_spread_x','issue_size','spread_Duration','trailing_vol','Age']]
```

Generic Model

```
In [169]: merged_3 = merged_3.loc[:,~merged_3.columns.duplicated()]
merged_3['log_issue_size'] = merged_3['issue_size'].apply(lambda x: np.log(x))
results_m = smf.ols('rolls_spread_x ~ spread_Duration + trailing_vol + Age', data=merged_3).fit()
print(results_m.summary())
```

OLS Regression Results

Dep. Variable: rolls_spread_x R-squared: 0.714

Model: OLS Adj. R-squared: 0.683

Method: Least Squares F-statistic: 22.51

Date: Tue, 10 Nov 2020 Prob (F-statistic): 1.64e-07

Time: 15:55:07 Log-Likelihood: -2.2091

No. Observations: 31 AIC: 12.42

Df Residuals: 27 BIC: 18.15

Df Model: 3

Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025
0.975]					
-----	-----	-----	-----	-----	-----
Intercept	0.3539	0.138	2.572	0.016	0.072
0.636					
spread_Duration	0.0296	0.006	4.821	0.000	0.017
0.042					
trailing_vol	-0.0079	0.009	-0.911	0.370	-0.026
0.010					
Age	0.0718	0.015	4.678	0.000	0.040
0.103					
-----	-----	-----	-----	-----	-----
Omnibus:	6.152	Durbin-Watson:			
1.421					
Prob(Omnibus):	0.046	Jarque-Bera (JB):			
4.517					
Skew:	0.721	Prob(JB):			
0.105					
Kurtosis:	4.191	Cond. No.			
38.9					
-----	-----	-----	-----	-----	-----
=====	=====	=====	=====	=====	=====
Warnings:					
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.					

```
In [174]: merged_3.to_csv("merged_3.csv")
```

```
In [176]: merged_df_tr30.to_csv("wmt_data4Regression.csv")
```

NEW CUSIP(Investment grade Bonds) Liquidity ANALYSIS

```
In [8]: sql_query = """
SELECT *
FROM trace.trace_enhanced
WHERE CUSIP_ID in ('92343VFT6','92343VBR4','110122DQ8','110122DR6','4664
7PBB1','46625HHA1','6174468U6','6174468T9','J57160DZ3','404280CL1','2003
0NBX8','035240ANO','097023CZ6','63254AAE8','92976GAG6','012725AD9','1127
1LAB8','097023BX2','26969PAA6','343498AA9','88732JBB3','37045VAT7','7847
10AB1','418056AS6','059438AG6','251526BR9','04621XAF5','38376AAB9','0970
23CM5','25470DBF5','25272KAK9','071813BW8','05526DBP9','281020AM9','292
480AM2','674599CW3','614810AB5')
AND TRD_EXCTN_DT BETWEEN '2007-01-01' AND '2019-12-31';
"""
new_data_query1 = db.raw_sql(sql_query)
```

```
In [9]: new_data_query2 = pd.read_csv("extra_wmt.csv")
new_data_query2.dtypes

/Users/deepsha/anaconda3/lib/python3.7/site-packages/IPython/core/inter
activeshell.py:3057: DtypeWarning: Columns (8,13,16,23) have mixed type
s.Specify dtype option on import or set low_memory=False.
    interactivity=interactivity, compiler=compiler, result=result)
```

```
Out[9]: cusip_id          object
bond_sym_id        object
company_symbol      object
trd_exctn_dt       int64
trd_exctn_tm       object
trd_rpt_dt         int64
trd_rpt_tm         object
trc_st              object
scrty_type_cd      object
wis_fl              object
cmsn_trd           object
entrд_vol_qt       float64
rptd_pr             float64
yld_sign_cd         object
yld_pt              float64
asof_cd             object
sale_cndtn_cd      object
rpt_side_cd         object
buy_cmsn_rt         float64
buy_cpcty_cd        object
sell_cmsn_rt        float64
sell_cpcty_cd       object
cntra_mp_id         object
agu_qsr_id          object
trdg_mkt_cd         object
stlmnt_dt           float64
trd_mod_3            object
rptg_party_type     object
pr_trd_dt            float64
first_trade_ctrl_date float64
dtype: object
```

```
In [11]: new_data_query2["trd_exctn_dt"] = pd.to_datetime(new_data_query2['trd_ex
ctn_dt'], format='%Y%m%d').dt.date
new_data_query2["trd_rpt_dt"] = pd.to_datetime(new_data_query2['trd_rpt_
dt'], format='%Y%m%d').dt.date
```

```
In [12]: new_data_query2["trd_rpt_tm"] = pd.to_datetime(new_data_query2["trd_rpt_
tm"], format='%H:%M:%S').dt.time
```

```
In [13]: new_data_query1['trd_exctn_tm'] = new_data_query1['trd_exctn_tm'].apply(
lambda x: datetime.timedelta(seconds=x))
new_data_query1['trd_rpt_tm'] = new_data_query1['trd_rpt_tm'].apply(lambda
x: datetime.timedelta(seconds=x))
```

```
In [14]: frames = [new_data_query1, new_data_query2]
new_data_query = pd.concat(frames)
```

```
In [15]: ### Dick-Nielsen Filtering
# Cancellations, reversals and corrections
new_data_query = new_data_query[~new_data_query['trc_st'].isin(['C', 'Y',
'X'])]
#After Market Hours
new_data_query = new_data_query[new_data_query.sale_cndtn2_cd != 'A']
# Filter below 100 percentage pts
new_data_query = new_data_query[new_data_query['rptd_pr'] >= 100]
# Remove agency transactions without commissions
sell_index = new_data_query[(new_data_query['rpt_side_cd'] == 'S') & (new_data_query['sell_cpcty_cd'] == 'A') & (new_data_query['cntra_mp_id'] == 'C') & (new_data_query['cmsn_trd'] == 'N')].index
new_data_query.drop(sell_index, inplace=True)
buy_index = new_data_query[(new_data_query['rpt_side_cd'] == 'B') & (new_data_query['buy_cpcty_cd'] == 'A') & (new_data_query['cntra_mp_id'] == 'C') & (new_data_query['cmsn_trd'] == 'N')].index
new_data_query.drop(buy_index, inplace=True)
# Remove interdealer transactions
interdealer_txn = new_data_query[(new_data_query['cntra_mp_id'] == 'D') & (new_data_query['rpt_side_cd'] == 'B')].index
new_data_query.drop(interdealer_txn, inplace=True)
```

```
In [18]: new_data_query = new_data_query.rename(columns={"cusip_id": "COMPLETE_CUSIP"})
new_data_query_fisd = pd.merge(new_data_query, fisd_data, how = "inner",
on = "COMPLETE_CUSIP")
new_data_query_fisd["trd_exctn_dt"] = pd.to_datetime(new_data_query_fisd
["trd_exctn_dt"], format="%Y-%m-%d")
```

```
In [20]: new_data_query_fisd[ 'MATURITY' ] = new_data_query_fisd[ 'MATURITY' ].apply( pd.to_datetime)
new_data_query_fisd[ 'Days_to_Maturity' ] = (new_data_query_fisd[ 'MATURITY' ] - new_data_query_fisd[ 'trd_exctn_dt' ])
new_data_query_fisd[ 'N_MATURITY' ] = ((new_data_query_fisd[ 'Days_to_Maturity' ] / 365) * 2)/np.timedelta64(1, 'D')
new_data_query_fisd = new_data_query_fisd[new_data_query_fisd[ 'Days_to_Maturity' ] > pd.Timedelta(0, 'D')]

yld = {}
for i in range(0, len(new_data_query_fisd)):
    try:
        yld.update({i:YieldCalc(new_data_query_fisd[ 'COUPON' ].iloc[i]/(new_data_query_fisd[ 'PRINCIPAL_AMT' ].iloc[i]/10),new_data_query_fisd[ 'rpt_d_pr' ].iloc[i],
                               new_data_query_fisd[ 'PRINCIPAL_AMT' ].iloc[i]/10, 2.0,
                               new_data_query_fisd[ 'N_MATURITY' ].iloc[i], new_data_query_fisd[ 'COUPON' ].iloc[i])})
    except(RuntimeError):
        pass
    else:
        pass

l = []
for i in yld:
    l.append(yld[i])

new_data_query_fisd[ 'YTM' ] = pd.Series(l, index=new_data_query_fisd.index)
```

```
In [23]: new_data_query_fisd = calculate_duration(new_data_query_fisd)
```

```
In [27]: uniques_cusips = new_data_query.COMPLETE_CUSIP.unique()
Ncs_rs_all = pd.DataFrame(columns = ['COMPLETE_CUSIP', 'date', 'auto_cov',
'rolls_spread'])
for k in uniques_cusips:
    x = new_data_query[new_data_query.COMPLETE_CUSIP == k]
    auto_cov = []
    rolls_spread = []
    uniques_dates = x.trd_exctn_dt.unique()
    for i in range(0,len(uniques_dates)):
        p = x[x.trd_exctn_dt == uniques_dates[i]]['rptd_pr']
        d = np.diff(p)
        if len(d) == 0 or len(d) == 1 :
            a = np.nan
            r = np.nan
            auto_cov.append(np.nan)
            rolls_spread.append(np.nan)
        else:
            a = lagged_auto_cov(d,1)
            r = 2*np.sqrt(-a)
            auto_cov.append(a)
            rolls_spread.append(r)
    data = pd.DataFrame({'COMPLETE_CUSIP':k , 'date':uniques_dates[i],
'auto_cov': a,'rolls_spread' : r },index=[0])
    Ncs_rs_all = Ncs_rs_all.append(data)
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:18: RuntimeWarning: invalid value encountered in sqrt

```
In [28]: len(uniques_cusips)
```

```
Out[28]: 35
```

In [29]: Ncs_rs_all

Out[29]:

	COMPLETE_CUSIP	date	auto_cov	rolls_spread
0	012725AD9	2014-11-17	-0.002260	0.095077
0	012725AD9	2014-11-19	NaN	NaN
0	012725AD9	2014-11-20	-0.326059	1.142031
0	012725AD9	2014-11-21	NaN	NaN
0	012725AD9	2014-11-24	-0.311787	1.116757
...
0	00206RAS1	2020-03-24	-1.810418	2.691036
0	00206RAS1	2020-03-25	0.444078	NaN
0	00206RAS1	2020-03-26	0.004771	NaN
0	00206RAS1	2020-03-30	NaN	NaN
0	00206RAS1	2020-03-31	NaN	NaN

19222 rows × 4 columns

In [30]:

```
Ncs_rs_all['year'] = pd.DatetimeIndex(Ncs_rs_all['date']).year
Ncs_rs_all['month'] = pd.DatetimeIndex(Ncs_rs_all['date']).month
Ncs_rs_all["year_month"] = Ncs_rs_all['year'].astype(str) + Ncs_rs_all['month'].astype(str)
```

In [31]:

```
Ncs_rs_all_ma = Ncs_rs_all.groupby(["year_month"])
Ncs_rs_all_ma = Ncs_rs_all_ma.aggregate({"rolls_spread":np.mean}).dropna()
```

In [34]: Ncs_rs_all_ma

Out[34]:

	rolls_spread	_year_month	Date
year_month			
20073	0.245000	20073	2007-03-01
20074	0.798000	20074	2007-04-01
20076	0.055540	20076	2007-06-01
20083	5.271000	20083	2008-03-01
20084	2.368246	20084	2008-04-01
...
201911	0.540249	201911	2019-11-01
201912	0.514775	201912	2019-12-01
20201	0.626234	20201	2020-01-01
20202	0.567962	20202	2020-02-01
20203	1.280718	20203	2020-03-01

139 rows × 3 columns

In [33]:

```
Ncs_rs_all_ma['_year_month'] = Ncs_rs_all_ma.index
Ncs_rs_all_ma['Date'] = pd.to_datetime(Ncs_rs_all_ma['_year_month'], format='%Y%m')
Ncs_rs_all_ma = Ncs_rs_all_ma.sort_values(by="Date")
```

```
In [35]: import plotly.express as px
import plotly.graph_objects as go
fig = go.Figure(data=go.Scatter(x=Ncs_rs_all_ma['Date'], y=Ncs_rs_all_ma['rolls_spread'], name = 'rolls_spread'))
fig.show("notebook")
```



```
In [36]: Ncs_rs_all = Ncs_rs_all.rename(columns={"date": "trd_exctn_dt"})
Ncs_rs_all['trd_exctn_dt'] = pd.to_datetime(Ncs_rs_all['trd_exctn_dt'],
format='%Y-%m-%d')
merged_df_cusips_all = new_data_query_fisid.merge(Ncs_rs_all, how='inner',
on=[ "COMPLETE_CUSIP", "trd_exctn_dt"])
```

```
In [333]: merged_df_cusips_all.to_csv("merged_df_cusips_all.csv")
```

Bond Characteristic Analysis for Investment Grade Bonds

```
In [38]: merged_df_cusips_all['OFFERING_DATE'] = pd.to_datetime(merged_df_cusips_all['OFFERING_DATE'])
merged_df_cusips_all['Age'] = (merged_df_cusips_all['trd_exctn_dt'] - merged_df_cusips_all['OFFERING_DATE']).apply(lambda x: (x.days)/365)
merged_df_cusips_all_= merged_df_cusips_all.dropna(subset=['rolls_spread'])
merged_df_cusips_all_age = merged_df_cusips_all_.groupby(['COMPLETE_CUSIP'])['rolls_spread', "Age"].mean()
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:4: FutureWarning:
```

```
Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.
```

```
In [40]: sns.jointplot(x=merged_df_cusips_all_age[ 'Age' ], y=merged_df_cusips_all_age[ "rolls_spread" ], height = 8,kind="reg", stat_func=r2)
```

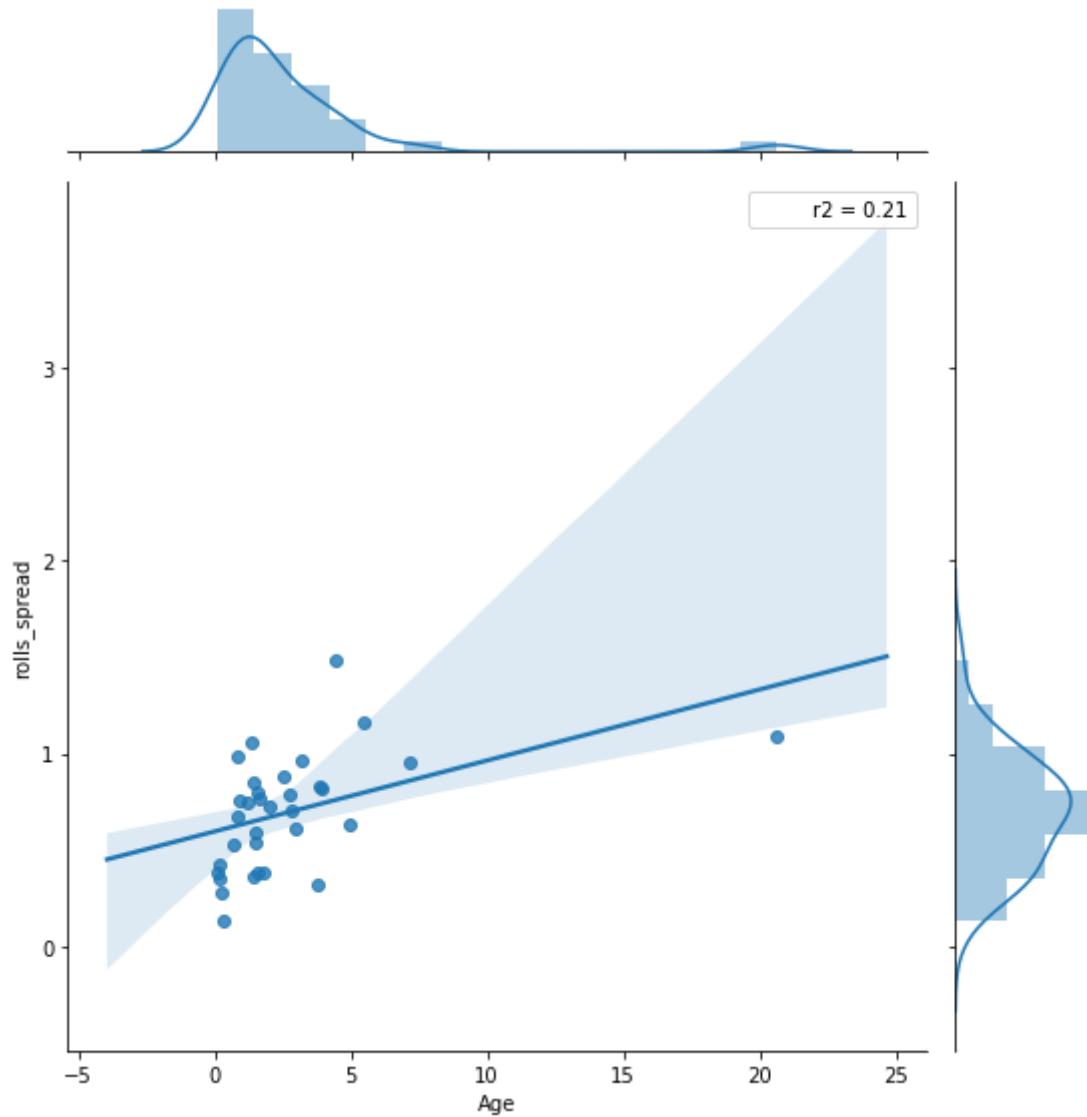
```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/scipy/stats/stats.py:1713: FutureWarning:
```

Using a non-tuple sequence for multidimensional indexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the future this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/seaborn/axisgrid.py:1847: UserWarning:
```

JointGrid annotation is deprecated and will be removed in a future release.

```
Out[40]: <seaborn.axisgrid.JointGrid at 0x139d18860>
```



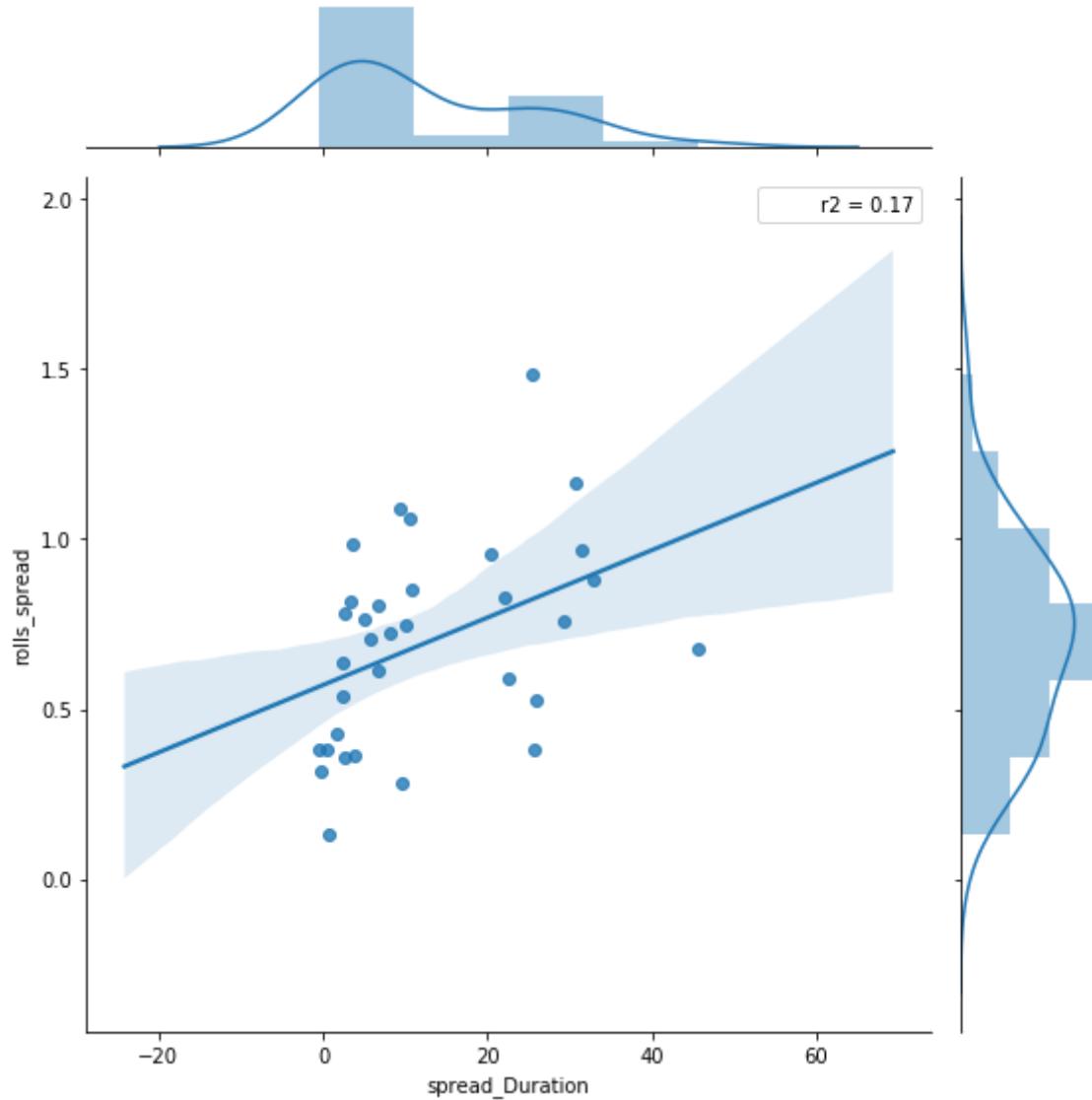
```
In [42]: merged_df_cusips_all_tr30= pd.merge(merged_df_cusips_all_,tr30, how ="inner", on = "trd_exctn_dt")
merged_df_cusips_all_tr30[ "spread" ] = merged_df_cusips_all_tr30[ "YTM" ]
- (merged_df_cusips_all_tr30[ "DGS30" ].astype(float)/100)
merged_df_cusips_all_tr30[ "spread_Duration" ] = merged_df_cusips_all_tr30
[ "spread" ]*merged_df_cusips_all_tr30[ "Duration_MAC" ]*100
merged_df_cusips_all_tr30[ "issue_size" ] = merged_df_cusips_all_tr30[ "OFF
ERING_AMT" ]*merged_df_cusips_all_tr30[ "PRINCIPAL_AMT" ]
merged_df_cusips_all_spreadD = merged_df_cusips_all_tr30.groupby([ "COMPL
ETE_CUSIP" ])['rolls_spread', "spread_Duration"].mean()
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launche
r.py:5: FutureWarning:

Indexing with multiple keys (implicitly converted to a tuple of keys) w
ill be deprecated, use a list instead.

```
In [43]: sns.jointplot(x=merged_df_cusips_all_spreadD['spread_Duration'], y=merge  
d_df_cusips_all_spreadD["rolls_spread"], height = 8, kind="reg", stat_fun  
c=r2)
```

```
Out[43]: <seaborn.axisgrid.JointGrid at 0x1278387b8>
```

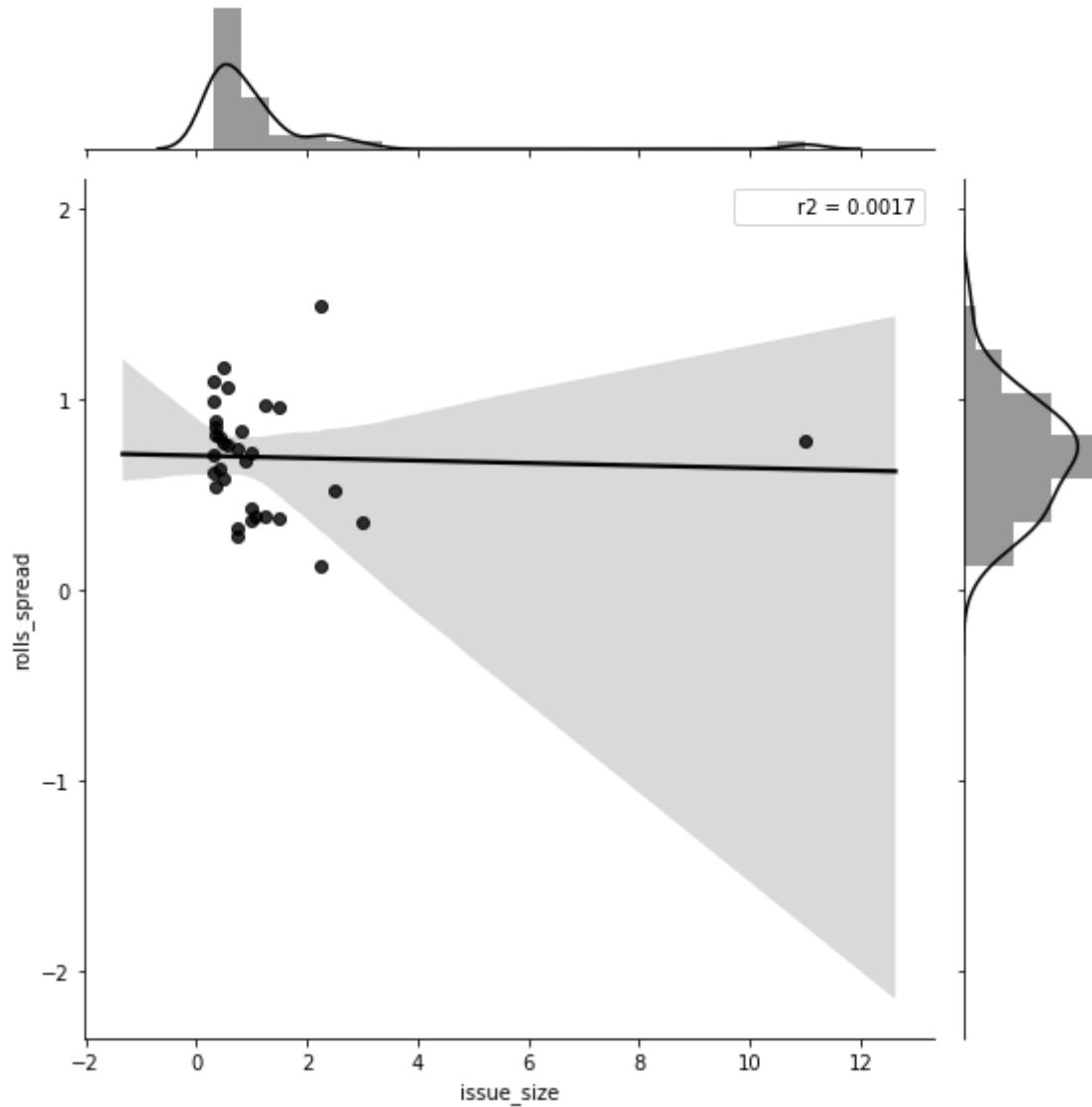


```
In [44]: merged_df_cusips_all_issue_size = merged_df_cusips_all_tr30.groupby(["COMPLETE_CUSIP"])[["rolls_spread", "issue_size"]].mean()
merged_df_cusips_all_issue_size["issue_size"] = merged_df_cusips_all_issue_size["issue_size"]/10000000000
sns.jointplot(x=merged_df_cusips_all_issue_size["issue_size"], height = 8, y=merged_df_cusips_all_issue_size["rolls_spread"],color= "black", kind="reg", stat_func=r2)
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:1: FutureWarning:

Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.

Out[44]: <seaborn.axisgrid.JointGrid at 0x12853c550>



```
In [45]: uniques_cusips = merged_df_cusips_all_.COMPLETE_CUSIP.unique()
merged_df_cusips_all_TV = pd.DataFrame(columns = ['entrdf_vol_qt','rolls_spread','COMPLETE_CUSIP','_year_month', 'date_monthly','trailing_vol'])
for k in uniques_cusips:
    x = merged_df_cusips_all_[merged_df_cusips_all_.COMPLETE_CUSIP == k]
    x['year'] = pd.DatetimeIndex(x['trd_exctn_dt']).year
    x['month'] = pd.DatetimeIndex(x['trd_exctn_dt']).month
    x["year_month"] = x['year'].astype(str) + x['month'].astype(str)
    x = x.groupby(["year_month"])
    x_s = x.aggregate({"entrdf_vol_qt":np.sum,"rolls_spread": np.mean})
    x_s['COMPLETE_CUSIP'] = k
    x_s['_year_month'] = x_s.index
    x_s['date_monthly'] = pd.to_datetime(x_s['_year_month'], format='%Y%m')
    x_s = x_s.sort_values(by="date_monthly")
    x_s['trailing_vol'] = x_s['entrdf_vol_qt'].shift(1)
    merged_df_cusips_all_TV = merged_df_cusips_all_TV.append(x_s)
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:5: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:6: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:7: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
In [47]: merged_df_cusips_all_TV_main = merged_df_cusips_all_TV.groupby(["COMPLETE_CUSIP"])[["rolls_spread", "trailing_vol"]].mean()
merged_df_cusips_all_TV_main["trailing_vol"] = merged_df_cusips_all_TV_main["trailing_vol"]/10000000

sns.jointplot(x=merged_df_cusips_all_TV_main["trailing_vol"], y = merged_df_cusips_all_TV_main["rolls_spread"], height = 8 ,kind="reg", stat_func=r2)
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:1: FutureWarning:
```

Indexing with multiple keys (implicitly converted to a tuple of keys) will be deprecated, use a list instead.

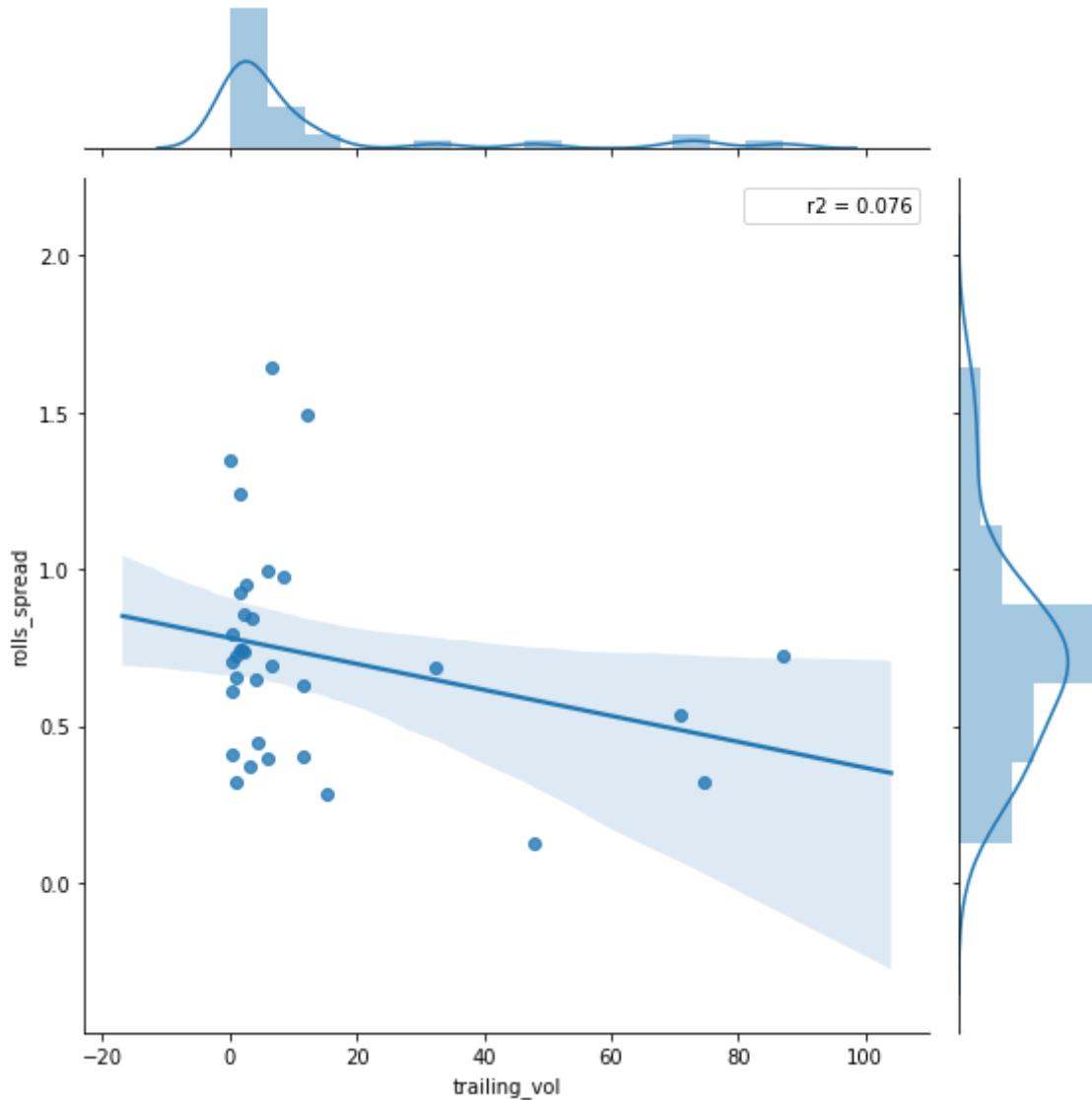
```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/scipy/stats/stats.py:1713: FutureWarning:
```

Using a non-tuple sequence for multidimensional indexing is deprecated; use `arr[tuple(seq)]` instead of `arr[seq]`. In the future this will be interpreted as an array index, `arr[np.array(seq)]`, which will result either in an error or a different result.

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/seaborn/axisgrid.py:1847: UserWarning:
```

JointGrid annotation is deprecated and will be removed in a future release.

Out[47]: <seaborn.axisgrid.JointGrid at 0x12b2f98d0>



```
In [48]: merged_1 = pd.merge(merged_df_cusips_all_issue_size,merged_df_cusips_all_spreadD,how = "inner", on = "COMPLETE_CUSIP")
merged_2 = pd.merge(merged_1,merged_df_cusips_all_TV_main,how ="inner",
on = "COMPLETE_CUSIP")
merged_3_all = pd.merge(merged_2,merged_df_cusips_all_age,how ="inner",
on = "COMPLETE_CUSIP")
```

Final Investment grade Bonds

```
In [49]: merged_3_all
```

Out[49]:

COMPLETE_CUSIP	rolls_spread_x	issue_size	rolls_spread_y	spread_Duration	rolls_spread_x	tra
00206RAS1	1.485341	2.250000	1.485341	25.371667	1.495307	12
012725AD9	0.880805	0.350000	0.880805	32.956884	0.742098	1
02406PAU4	0.588226	0.499760	0.588226	22.647077	0.649296	2
035240AN0	0.525740	2.500000	0.525740	25.796990	0.532878	70
04621XAF5	0.817231	0.350000	0.817231	3.402616	0.791784	0
059438AG6	1.090580	0.300000	1.090580	9.403359	1.348438	0
097023BX2	0.538606	0.350000	0.538606	2.450760	0.611648	0
097023CM5	0.426020	1.000000	0.426020	1.539362	0.402830	11
11271LAB8	0.760152	0.550000	0.760152	29.159131	1.641362	6
126307AY3	0.383804	1.045882	0.383804	25.589729	0.409313	0
177376AE0	0.744194	0.750000	0.744194	10.153748	0.695913	6
20030NAY7	0.828751	0.800000	0.828751	22.110255	0.953500	2
20030NBX8	0.381215	1.250000	0.381215	-0.453488	0.396264	6
251526BR9	0.361262	1.000000	0.361262	3.785005	0.446092	2
25470DBF5	0.283568	0.750000	0.283568	9.622756	0.286386	15
269246BQ6	0.803162	0.400000	0.803162	6.665016	0.845828	3
26969PAA6	0.851833	0.350000	0.851833	10.780075	0.858604	2
281020AM9	1.061425	0.550000	1.061425	10.428552	0.992845	5
30212PAP0	0.723679	1.000000	0.723679	8.238717	0.630828	11
31428XBP0	0.766469	0.500000	0.766469	4.973166	0.733916	2
343498AA9	0.636902	0.400000	0.636902	2.255282	0.653576	0
37045VAT7	0.677915	0.900000	0.677915	45.606817	0.685273	32
38376AAB9	0.987394	0.300000	0.987394	3.521339	0.744221	2
418056AS6	1.162382	0.500000	1.162382	30.806409	1.237482	1
46647PBB1	0.131441	2.250000	0.131441	0.694481	0.129313	47
52107QAH8	0.705176	0.300000	0.705176	5.791111	0.708517	0
614810AB5	0.615543	0.300000	0.615543	6.742356	0.722599	1
63254AAE8	0.318886	0.750000	0.318886	-0.201531	0.321282	1
674599CW3	0.356788	3.000000	0.356788	2.621921	0.321816	74
713448DY1	0.379390	1.500000	0.379390	0.359984	0.370328	3
88732JBB3	0.965914	1.250000	0.965914	31.478948	0.978918	8
92343VBR4	0.783273	11.000000	0.783273	2.563271	0.723661	87
92976GAG6	0.953884	1.500000	0.953884	20.411201	0.928018	1

Generic Model for Investment grade Bonds

```
In [50]: merged_3_all = merged_3_all.loc[:,~merged_3_all.columns.duplicated()]
merged_3_all['log_issue_size'] = merged_3_all['issue_size'].apply(lambda
x: np.log(x))
results_m = smf.ols('rolls_spread_x ~ spread_Duration + trailing_vol + A
ge ', data = merged_3_all).fit()
print(results_m.summary())
```

OLS Regression Results

=====					
=====					
Dep. Variable:	rolls_spread_x	R-squared:			
0.390					
Model:	OLS	Adj. R-squared:			
0.327					
Method:	Least Squares	F-statistic:			
6.187					
Date:	Sun, 29 Nov 2020	Prob (F-statistic):			
0.00221					
Time:	14:39:04	Log-Likelihood:			
2.1619					
No. Observations:	33	AIC:			
3.676					
Df Residuals:	29	BIC:			
9.662					
Df Model:	3				
Covariance Type:	nonrobust				
=====					
=====					
	coef	std err	t	P> t	[0.025
0.975]					

Intercept	0.5094	0.076	6.722	0.000	0.354
0.664					
spread_Duration	0.0096	0.003	2.775	0.010	0.003
0.017					
trailing_vol	-0.0019	0.002	-1.016	0.318	-0.006
0.002					
Age	0.0332	0.012	2.754	0.010	0.009
0.058					
=====					
=====					
Omnibus:	3.189	Durbin-Watson:			
1.623					
Prob(Omnibus):	0.203	Jarque-Bera (JB):			
2.307					
Skew:	0.645	Prob(JB):			
0.316					
Kurtosis:	3.110	Cond. No.			
49.3					
=====					
=====					

Warnings:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:2: SettingWithCopyWarning:
```

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/statsmodels/computations/pandas.py:23: FutureWarning:
```

The Panel class is removed from pandas. Accessing it from the top-level namespace will also be removed in the next version

New Liquidity Indicators Calculation on Walmart Bonds and Investment grade Bonds

```
In [54]: # Investment grade
Daily_range = merged_df_cusips_all.groupby(['trd_exctn_dt'])[['rptd_pr']].max() - merged_df_cusips_all.groupby(['trd_exctn_dt'])[['rptd_pr']].min()

In [486]: # Walmart Bonds
Daily_range_wmt = merged_df.groupby(['trd_exctn_dt'])[['rptd_pr']].max() - merged_df.groupby(['trd_exctn_dt'])[['rptd_pr']].min()
```

```
In [488]: Daily_range_wmt['date'] = Daily_range_wmt.index
Daily_range_wmt
```

Out[488]:

rptd_pr	date
trd_exctn_dt	

rptd_pr	date
2007-01-02	10.68700 2007-01-02
2007-01-03	2.17800 2007-01-03
2007-01-04	16.15100 2007-01-04
2007-01-05	13.70800 2007-01-05
2007-01-08	1.71900 2007-01-08
...	...
2020-03-25	46.50100 2020-03-25
2020-03-26	47.56801 2020-03-26
2020-03-27	47.63700 2020-03-27
2020-03-30	52.28100 2020-03-30
2020-03-31	54.87600 2020-03-31

3340 rows × 2 columns

```
In [371]: Daily_range_wmt['date'] = Daily_range_wmt.index
Daily_range_wmt['year'] = pd.DatetimeIndex(Daily_range_wmt['date']).year
Daily_range_wmt['month'] = pd.DatetimeIndex(Daily_range_wmt['date']).month
Daily_range_wmt["year_month"] = Daily_range_wmt['year'].astype(str) + Daily_range_wmt['month'].astype(str)
```

```
In [372]: Daily_range_wmt = Daily_range_wmt.groupby(['year_month']).mean()
Daily_range_wmt['_year_month'] = Daily_range_wmt.index
Daily_range_wmt['Date'] = pd.to_datetime(Daily_range_wmt['_year_month'],
                                         format='%Y%m')
Daily_range_wmt = Daily_range_wmt.sort_values(by="Date")
```

Daily RANGE OF Prices of Walmart Bonds

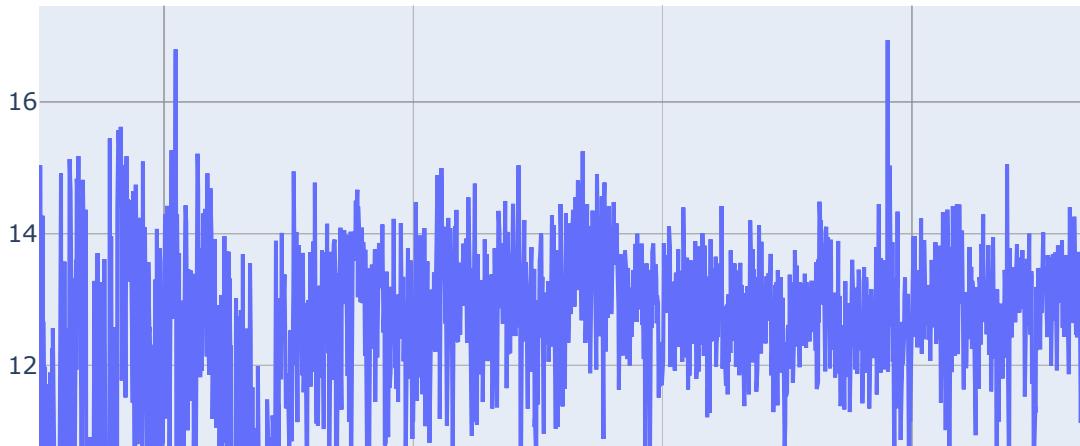
```
In [489]: fig = go.Figure(data=go.Scatter(x=Daily_range_wmt['date'], y=Daily_range_wmt['rptd_pr'], name = 'Daily range'))
fig.show("notebook")
```



Trading Volume of Walmart Bonds

```
In [526]: trading_vol_WMT = merged_df[["COMPLETE_CUSIP", "trd_exctn_dt", "entrnd_vol_qt"]]
trading_vol_WMT = trading_vol_WMT.groupby(['trd_exctn_dt']).mean()
trading_vol_WMT['date'] = trading_vol_WMT.index
trading_vol_WMT["inverse_vol"] = -np.log(1/trading_vol_WMT["entrnd_vol_qt"])
trading_vol_WMT["Date"] = trading_vol_WMT["date"]
```

```
In [502]: fig = go.Figure(data=go.Scatter(x=trading_vol_WMT['date'], y=trading_vol_WMT[ "inverse_vol"],name = 'trading_vol_WMT'))
fig.show("notebook")
```



trading_volume for Investment grade Bonds

```
In [374]: trading_vol = merged_df_cusips_all[["COMPLETE_CUSIP","trd_exctn_dt","entrnd_vol_qt"]]
trading_vol_m = trading_vol.groupby(['trd_exctn_dt']).mean()
trading_vol_m[ '_year_month' ] = trading_vol_m.index
trading_vol_m[ 'Date' ] = pd.to_datetime(trading_vol_m[ '_year_month' ], format='%Y-%m')
trading_vol_m = trading_vol_m.sort_values(by="Date")
trading_vol_m[ 'year' ] = pd.DatetimeIndex(trading_vol_m[ 'Date' ]).year
trading_vol_m[ 'month' ] = pd.DatetimeIndex(trading_vol_m[ 'Date' ]).month
trading_vol_m[ "year_month" ] = trading_vol_m[ 'year' ].astype(str) + trading_vol_m[ 'month' ].astype(str)
trading_vol_m = trading_vol_m.groupby([ 'year_month' ]).mean()
trading_vol_m[ "inverse_vol" ] = 1/trading_vol_m[ "entrnd_vol_qt" ]
```

```
In [386]: trading_vol_mWMT[ '_year_month' ] = trading_vol_mWMT.index  
trading_vol_mWMT[ 'Date' ] = pd.to_datetime(trading_vol_mWMT[ '_year_mont  
h' ], format='%Y%m')  
trading_vol_mWMT = trading_vol_mWMT.sort_values(by="Date")
```

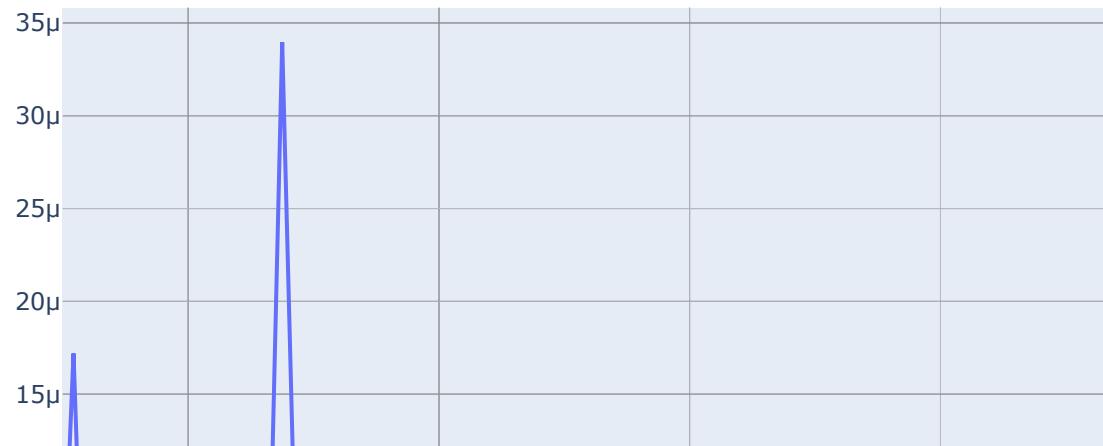
```
In [388]: trading_vol_mWMT[ "inverse_vol" ] = 1/trading_vol_mWMT[ "entrnd_vol_qt" ]
```

Plots of Monthly trading Volume and Inverse Volume for Walmart Bonds

```
In [390]: fig = go.Figure(data=go.Scatter(x=trading_vol_mWMT[ 'Date' ], y=trading_vo  
l_mWMT[ 'entrnd_vol_qt' ],name = 'Trading Vol'))  
fig.show("notebook")
```



```
In [392]: fig = go.Figure(data=go.Scatter(x=trading_vol_mWMT[ 'Date' ], y=trading_vo  
l_mWMT[ "inverse_vol" ] ,name = 'Trading Vol'))  
fig.show("notebook")
```

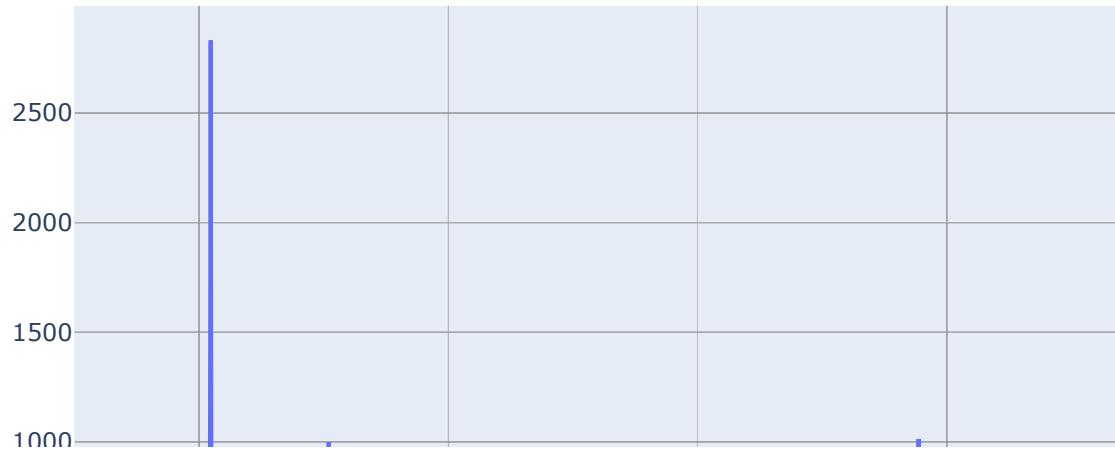


Amihud Ratio Calculation for Walmart Bonds

```
In [ ]: uniques_cusips_WMT = merged_df.COMPLETE_CUSIP.unique()
amihud_all_WMT = pd.DataFrame(columns = ['COMPLETE_CUSIP', 'date', 'amihud'])
for k in uniques_cusips_WMT:
    x = merged_df[merged_df.COMPLETE_CUSIP == k]
    un = [str(i)[:10] for i in x.trd_exctn_dt.unique()]
    for i in range(0,len(un)):
        p = x[x.trd_exctn_dt == un[i]]['rptd_pr'].values.tolist()
        v = x[x.trd_exctn_dt == un[i]]['entrnd_vol_qt'].values.tolist()
        d = np.diff(p)
        if len(d) == 0:
            s = np.nan
        else:
            s = sum([(abs(d[i])/p[i+1]*v[i+1]) for i in range(0,len(d))]) / len(d)
        data = pd.DataFrame({'COMPLETE_CUSIP':k , 'date':un[i], 'amihud':s},index=[0])
        amihud_all_WMT = amihud_all_WMT.append(data)
```

Plot for Daily Amihud ratio

```
In [516]: amihud_all_WMT_DAILY = amihud_all_WMT.groupby(['date']).mean()
amihud_all_WMT_DAILY[ "Date" ] = amihud_all_WMT_DAILY.index
fig = go.Figure(data=go.Scatter(x=amihud_all_WMT_DAILY[ 'Date' ], y=amihud_all_WMT_DAILY[ 'amihud' ]/100, name = 'amihud_all'))
fig.show("notebook")
```



Monthly Amihud Ratio Calculation

```
In [ ]: amihud_all_WMT[ 'year' ] = pd.DatetimeIndex(amihud_all_WMT[ 'date' ]).year
amihud_all_WMT[ 'month' ] = pd.DatetimeIndex(amihud_all_WMT[ 'date' ]).month
amihud_all_WMT[ "year_month" ] = amihud_all_WMT[ 'year' ].astype(str) + amihud_all_WMT[ 'month' ].astype(str)
amihud_all_WMT = amihud_all_WMT.groupby([ 'year_month' ]).mean()
amihud_all_WMT[ '_year_month' ] = amihud_all_WMT.index
amihud_all_WMT[ 'Date' ] = pd.to_datetime(amihud_all_WMT[ '_year_month' ],
format='%Y%m')
amihud_all_WMT = amihud_all_WMT.sort_values(by="Date")
```

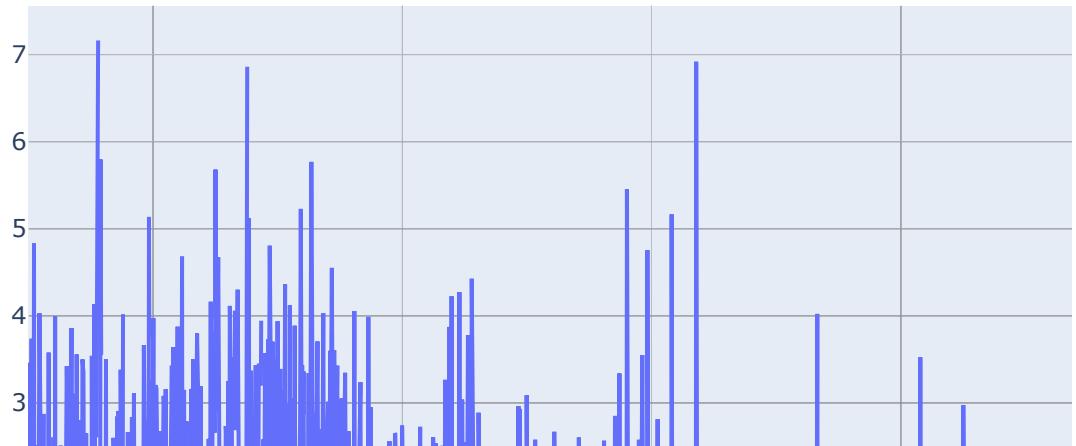
Rolls spread Plot for Walmart Bonds

```
In [523]: test1["Date"] = test1.index
fig = go.Figure(data=go.Scatter(x=test1['Date'], y=test1['rolls_spread'],
],name = 'rolls_spread'))
fig.show("notebook")
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:1: SettingWithCopyWarning:
```

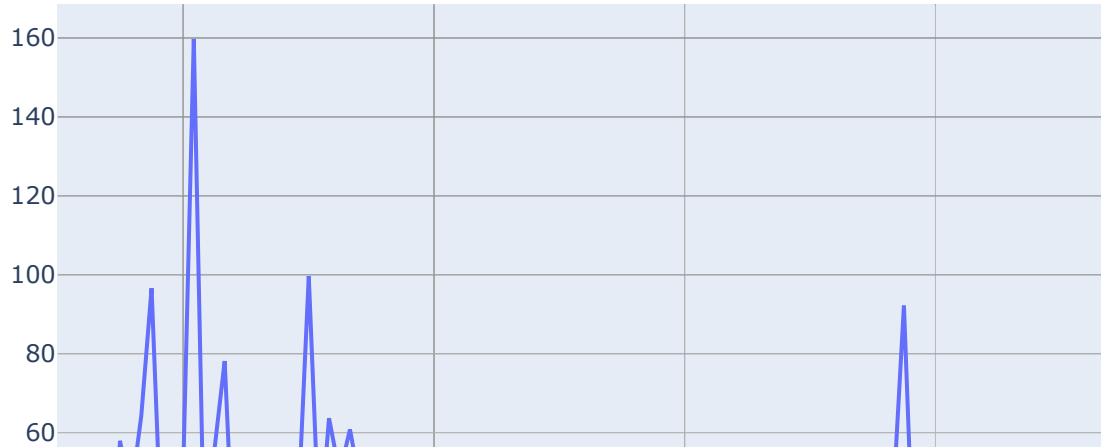
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy



Monthly Amihud plot for Walmart Bonds

```
In [397]: fig = go.Figure(data=go.Scatter(x=amihud_all_WMT['Date'], y=amihud_all_WMT['amihud']/100, name = 'amihud_all'))
fig.show("notebook")
```



```
In [400]: amihud_all_s_wmt = amihud_all_WMT[["amihud", "Date"]]
trading_vol_m_s_wmt = trading_vol_mWMT[["entrdd_vol_qt", "Date", "inverse
_vol"]]
Daily_range_s_wmt = Daily_range_wmt[["rptd_pr", "Date"]]
```

In [474]: amihud_all_WMT

Out[474]:

	amihud	year	month	_year_month	Date
year_month					
20071	1739.829906	2007	1	20071	2007-01-01
20072	252.663188	2007	2	20072	2007-02-01
20073	1309.790088	2007	3	20073	2007-03-01
20074	2218.378820	2007	4	20074	2007-04-01
20075	1353.411753	2007	5	20075	2007-05-01
...
201911	630.805226	2019	11	201911	2019-11-01
201912	506.733101	2019	12	201912	2019-12-01
20201	742.501362	2020	1	20201	2020-01-01
20202	715.183241	2020	2	20202	2020-02-01
20203	4156.077972	2020	3	20203	2020-03-01

159 rows × 5 columns

In [404]:

```
merged_pca_wmt = pd.merge(amihud_all_s_wmt,df_lc_rs,how ="inner", on = "Date")
#merged_pca2 = pd.merge(merged_pca_wmt,bonds_d_s,how ="inner", on = "Date")
merged_pca2_wmt = pd.merge(merged_pca_wmt,trading_vol_m_s_wmt,how ="inner", on = "Date")
merged_pca43_wmt = pd.merge(merged_pca2_wmt,Daily_range_s_wmt,how ="inner", on = "Date")
```

In [559]:

```
#Daily data merge
```

```
merged_pca_wmt_d = pd.merge(amihud_all_WMT_DAILY,test1,how ="inner", on = "Date")
merged_pca2 = pd.merge(merged_pca_wmt,bonds_d_s,how ="inner", on = "Date")
merged_pca2_wmt_d = pd.merge(merged_pca_wmt_d ,trading_vol_WMT,how ="inner", on = "Date")
merged_pca43_wmt_d= pd.merge(merged_pca2_wmt,df_lc,how ="inner", on = "Date")
merged_pca5 = pd.merge(merged_pca43_wmt_d,Daily_range_wmt,how ="inner", on = "Date")
```

In [558]:

```
Daily_range_wmt["Date"] = pd.to_datetime(Daily_range_wmt["date"]).dt.date
```

In [560]: `## daily data for PCA`

`merged_pca5`

Out[560]:

	amihud	Date	LC_x	rolls_spread	date_x	rs_and_LC_average	entrnd_vol_qt	inver
0	252.663188	2007-02-01	0.004763	2.071908	20072	1.274095	5.815561e+04	1.71%
1	1309.790088	2007-03-01	0.002092	1.556803	20073	0.883022	4.631617e+05	2.15%
2	4370.334760	2007-08-01	0.003869	1.615786	20078	1.001340	1.409888e+06	7.09%
3	2825.686234	2007-11-01	0.019669	2.065796	200711	2.016327	2.709361e+05	3.69%
4	15974.072014	2008-02-01	0.017720	2.244261	20082	2.008130	1.497256e+06	6.67%
...
89	986.526755	2019-05-01	0.002442	0.466513	20195	0.355375	4.745336e+05	2.10%
90	934.742874	2019-07-01	0.002462	0.462972	20197	0.354570	4.397811e+05	2.27%
91	575.729444	2019-08-01	0.002376	0.445645	20198	0.341646	4.112111e+05	2.43%
92	515.030591	2019-10-01	0.001932	0.422847	201910	0.308048	3.941469e+05	2.53%
93	630.805226	2019-11-01	0.002191	0.419778	201911	0.319454	3.062157e+05	3.26%

94 rows × 11 columns

VIX index

In [177]: `vix = pd.read_csv("vixcurrent.csv", header=1)`

```
In [82]: fig = go.Figure(data=go.Scatter(x=vix[ 'Date' ], y=vix[ 'VIX Close' ],name = 'amihud_all '))
fig.show( "notebook" )
```



Liquidity Indicator Calculation for Investment grade Bonds

```
In [87]: amihud_all_s = amihud_all[["amihud", "Date"]]
trading_vol_m_s = trading_vol_m[["entrdrd_vol_qty", "Date", "inverse_vol"]]
Daily_range_s = Daily_range[["rptd_pr", "Date"]]
```

```
In [102]: ns_lc = merged_df_cusips_all.groupby(['trd_exctn_dt', 'rpt_side_cd'])['rp
td_pr'].mean().unstack(level = 1).dropna()
ns_lc['LC'] = (ns_lc['S'] - ns_lc['B'])/(0.5*(ns_lc['S'] + ns_lc['B']))
```

```
In [91]: bonds_d[ "Date" ] = bonds_d.index
bonds_d_s = bonds_d[["rolls_spread", "Date"]]
```

```
In [106]: ns_lc_s = ns_lc[["LC", "Date"]]
```

```
In [104]: ns_lc[ 'Date' ] = ns_lc.index
ns_lc[ 'year' ] = pd.DatetimeIndex(ns_lc[ 'Date' ]).year
ns_lc[ 'month' ] = pd.DatetimeIndex(ns_lc[ 'Date' ]).month
ns_lc[ "year_month" ] = ns_lc[ 'year' ].astype(str) + ns_lc[ 'month' ].astype(str)
```

```
In [108]: ns_lc = ns_lc.groupby(["year_month"])
ns_lc_ma = ns_lc.aggregate({ "LC":np.mean})
ns_lc_ma[ '_year_month' ] = ns_lc_ma.index
ns_lc_ma[ 'Date' ] = pd.to_datetime(ns_lc_ma[ '_year_month' ], format='%Y %m')
ns_lc_ma = ns_lc_ma.sort_values(by="Date")
```

Data Preparation for PCA of Investment grade Bonds

```
In [118]: merged_pca = pd.merge(amihud_all_s,ns_lc_s,how ="inner", on = "Date")
merged_pca2 = pd.merge(merged_pca ,bonds_d_s,how ="inner", on = "Date")
merged_pca3 = pd.merge(merged_pca2,trading_vol_m_s,how ="inner", on =
"Date")
merged_pca4 = pd.merge(merged_pca3,Daily_range_s,how ="inner", on = "D
ate")
```

```
In [561]: merged_pca5[ "amihud" ] = merged_pca5[ "amihud" ]/100
pca4 = merged_pca4[["amihud","LC","rolls_spread","inverse_vol","rptd_p
r"]]
pca5 = merged_pca5[["amihud","LC_x","rolls_spread","inverse_vol","rptd_
pr"]]
```

```
In [407]: pca4_wmt = merged_pca43_wmt[["amihud","LC","rolls_spread","inverse_vol"
,"rptd_pr"]]
```

PCA on Walmart Bonds

```
In [128]: from sklearn.preprocessing import StandardScaler
pca4_wmt = StandardScaler().fit_transform(pca4_wmt)
pca_ = PCA(n_components=2)
principalComponents_ = pca_.fit_transform(pca4_wmt)
```

```
In [ ]: feat_cols = ['feature'+str(i) for i in range(pca4_wmt.shape[1])]
normalised_feat = pd.DataFrame(pca4_wmt,columns=feat_cols)
principal_Df = pd.DataFrame(data = principalComponents_
, columns = [ 'principal component 1', 'principal component
2'])
```

```
In [ ]: feature_weights = pca_.components_
squared_factor_weights = np.array([[i*i for i in k] for k in feature_weights]).T
max_el = [{list(i).index(max(i)): max(i)} for i in squared_factor_weights]
```

PCA on Investment grade Bonds

```
In [567]: from sklearn.decomposition import PCA
pca5 = StandardScaler().fit_transform(pca5)
pca_ = PCA(n_components=2)
principalComponents_ = pca_.fit_transform(pca5)
```

```
In [568]: np.mean(pca5),np.std(pca5)
```

```
Out[568]: (-1.209434443846979e-16, 1.0)
```

```
In [569]: feat_cols = ['feature'+str(i) for i in range(pca5.shape[1])]
normalised_feat = pd.DataFrame(pca5,columns=feat_cols)
```

```
In [571]: normalised_feat.head()
```

```
Out[571]:
```

	feature0	feature1	feature2	feature3	feature4
0	-1.046565	-0.495242	1.349736	8.018346	-3.019824
1	-0.532159	-1.070150	0.542736	-0.091347	-1.613716
2	0.957127	-0.687684	0.635143	-0.873288	-2.964957
3	0.205489	2.713797	1.340160	0.734841	-1.559897
4	6.603598	2.294287	1.619756	-0.895610	-1.513260

```
In [573]: principal_Df = pd.DataFrame(data = principalComponents_
, columns = ['principal component 1', 'principal component
2'])
```

In [574]: `principal_Df.head()`

Out[574]:

	principal component 1	principal component 2
0	1.996762	8.063796
1	0.287687	0.669545
2	1.754688	-0.368914
3	3.088195	0.918712
4	5.480346	-3.528773

In [575]: `print('Explained variation per principal component: {}'.format(pca_.explained_variance_ratio_))`

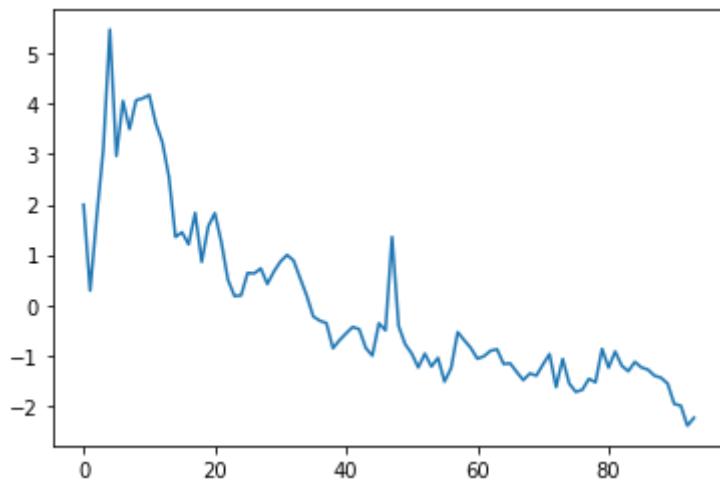
Explained variation per principal component: [0.58483393 0.25791861]

In [576]: `pca_.explained_variance_ratio_[0]`

Out[576]: 0.5848339336975913

In [577]: `#x_std = pca.transform(transformed)plt.figure()
plt.plot(principal_Df.iloc[:,0])`

Out[577]: [`<matplotlib.lines.Line2D at 0x16bdda390>`]



Partial and Final Weight Calculation

In [578]: `feature_weights = pca_.components_`

In [579]: `feature_weights`

Out[579]: `array([[0.40340911, 0.53835853, 0.55592833, 0.0588107 , -0.4846815
3],
 [-0.48686855, -0.03335338, 0.07653984, 0.83167913, -0.2535705
9]])`

```
In [582]: squared_factor_weights
```

```
Out[582]: array([[0.16273891, 0.23704098],
       [0.2898299 , 0.00111245],
       [0.3090563 , 0.00585835],
       [0.0034587 , 0.69169018],
       [0.23491619, 0.06429805]])
```

```
In [581]: squared_factor_weights = np.array([[i*i for i in k] for k in feature_weights ]).T
max_el = [{list(i).index(max(i)): max(i)} for i in squared_factor_weights]
```

```
In [585]: import collections
counter = collections.Counter()
for d in max_el:
    counter.update(d)
m = dict(counter)
```

```
In [586]: p_final = [[v/m[k] for k, v in max_el[i].items()]for i in range(0, len(max_el))]
flat_p_final = [item for sublist in p_final for item in sublist]
flat_w_final = [i*pca_.explained_variance_ratio_[0] for i in flat_p_final]
flat_w_final[0] = (flat_w_final[0]/pca_.explained_variance_ratio_[0])*pca_.explained_variance_ratio_[1]
flat_w_final[3] = (flat_w_final[3]/pca_.explained_variance_ratio_[0])*pca_.explained_variance_ratio_[1]
```

```
In [590]: sum(flat_w_final)
```

```
Out[590]: 0.842752545977197
```

```
In [591]: normalised_feat.loc[:, ["feature0", "feature1", "feature2", "feature3",
"feature4"]] *= np.array(flat_w_final)
normalised_feat["new_index"] = normalised_feat["feature0"]+normalised_feat["feature1"]+normalised_feat["feature2"]+normalised_feat["feature3"]+normalised_feat["feature4"]
```

```
In [592]: merged__pca5["new_index"] = normalised_feat["new_index"]
```

In [593]: merged_pca5

Out[593]:

	amihud	Date	LC_x	rolls_spread	date_x	rs_and_LC_average	entrд_vol_qt	inverse
0	2.526632	2007-02-01	0.004763	2.071908	20072	1.274095	5.815561e+04	1.7195
1	13.097901	2007-03-01	0.002092	1.556803	20073	0.883022	4.631617e+05	2.1590
2	43.703348	2007-08-01	0.003869	1.615786	20078	1.001340	1.409888e+06	7.0927
3	28.256862	2007-11-01	0.019669	2.065796	200711	2.016327	2.709361e+05	3.6909
4	159.740720	2008-02-01	0.017720	2.244261	20082	2.008130	1.497256e+06	6.6788
...
89	9.865268	2019-05-01	0.002442	0.466513	20195	0.355375	4.745336e+05	2.1073
90	9.347429	2019-07-01	0.002462	0.462972	20197	0.354570	4.397811e+05	2.2738
91	5.757294	2019-08-01	0.002376	0.445645	20198	0.341646	4.112111e+05	2.4318
92	5.150306	2019-10-01	0.001932	0.422847	201910	0.308048	3.941469e+05	2.5371
93	6.308052	2019-11-01	0.002191	0.419778	201911	0.319454	3.062157e+05	3.2656

94 rows × 12 columns

Comparison of Monthly Liquidity Indicators with VIX for Investment grade Bonds

```
In [275]: fig = go.Figure(data=go.Scatter(x=merged_pca4['Date'], y=merged_pca4['new_index'],name = 'syn'))
#fig.add_scatter(x=merged_pca4['Date'], y=merged_pca4['LC'],name = 'LC')
fig.add_scatter(x=merged_pca4['Date'], y=merged_pca4['rolls_spread'],name = 'rolls_spread')
#Fig.add_scatter(x=merged_pca4['Date'], y=merged_pca4['inverse_vol'],name = 'inverse_vol')
fig.add_scatter(x=mwm['Date'], y=mwm['VIX Close']/10,name = 'VIX Close')
fig.show("notebook")
```



FINAL Walmart Data with Liquidity Measures

```
In [600]: mmm_wmt = pd.merge(merged_pca43_wmt,vix_ma, on = "Date")
mmm_wmt
```

Out[600]:

	amihud	Date	LC	rolls_spread	date	rs_and_LC_average	entrд_vol_qt	inver
0	1739.829906	2007-01-01	0.000511	2.054803	20071	1.052958	2.891318e+05	3.45
1	252.663188	2007-02-01	0.004763	2.071908	20072	1.274095	5.815561e+04	1.71
2	1309.790088	2007-03-01	0.002092	1.556803	20073	0.883022	4.631617e+05	2.15
3	2218.378820	2007-04-01	0.005565	1.663898	20074	1.110200	1.146345e+06	8.72
4	1353.411753	2007-05-01	0.009949	1.688256	20075	1.341571	5.863556e+05	1.70
...
154	630.805226	2019-11-01	0.002191	0.419778	201911	0.319454	3.062157e+05	3.26
155	506.733101	2019-12-01	0.002401	0.389722	201912	0.314898	3.307363e+05	3.02
156	742.501362	2020-01-01	0.002083	0.429784	20201	0.319032	4.090183e+05	2.44
157	715.183241	2020-02-01	0.001887	0.390116	20202	0.289405	4.179085e+05	2.39
158	4156.077972	2020-03-01	0.005801	1.326876	20203	0.953508	5.548511e+05	1.80

159 rows × 12 columns

Factor Loading Plots for Walmart Daily Data

```
In [399]: columns = ('amihud', 'LC', 'rolls_spread', 'inverse_vol', 'Daily price range')
rows = ['Principal Component %d' % x for x in (1,2)]
plt.figure(figsize=(8,5))

values = np.arange(-1.0, 1, 0.1)
value_increment = 1

# Get some pastel shades for the colors
colors = plt.cm.Wistia(np.linspace(0, 0.5, len(rows)))
n_rows = len(feature_weights)
index = np.arange(len(columns)) + 0.3
bar_width = 0.4

y_offset = np.zeros(len(columns))

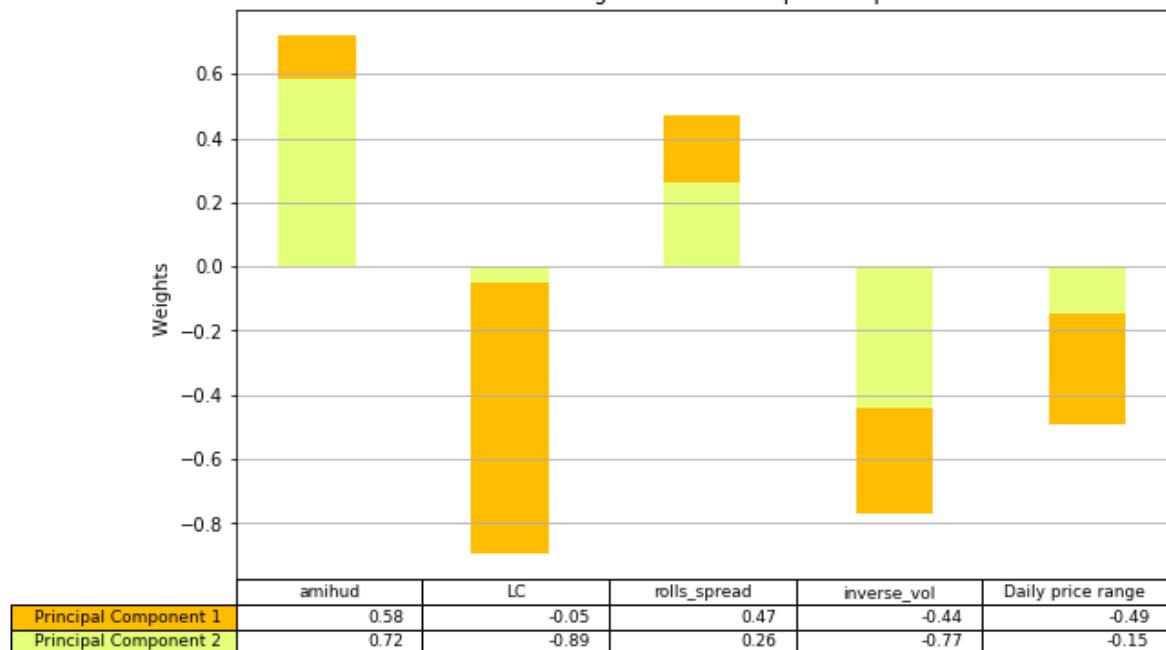
cell_text = []
for row in range(n_rows):
    plt.bar(index, feature_weights[row], bar_width, bottom=y_offset, color=colors[row])
    y_offset = y_offset + feature_weights[row]
    cell_text.append(['%1.2f' % (x) for x in y_offset])
# Reverse colors and text labels to display the last value at the top.
colors = colors[::-1]
#cell_text.reverse()

# Add a table at the bottom of the axes
the_table = plt.table(cellText=cell_text,
                      rowLabels=rows,
                      rowColours=colors,
                      colLabels=columns,
                      loc='bottom')

# Adjust layout to make room for the table:
plt.subplots_adjust(left=0.01, bottom=0.01)

plt.ylabel("Weights ")
#plt.yticks(values * value_increment, ['%d' % val for val in values])
plt.xticks([])
plt.title('Factor Loadings for each Principal Component ')
plt.grid(True)
plt.show()
```

Factor Loadings for each Principal Component



New Liquidity Indec vs VIX index

```
In [484]: import plotly.graph_objects as go
from plotly.subplots import make_subplots
fig = make_subplots(specs=[[{"secondary_y": True}]])

fig.add_trace(
    go.Scatter(x=merged_pca43_wmt['Date'], y=merged_pca43_wmt['new_index'],
               name='synthetic Index'),
    secondary_y=False,
)

fig.add_trace(
    go.Scatter(x=mmm_wmt['Date'], y=mmm_wmt['VIX Close'], name = 'VIX'),
    secondary_y=True,
)

fig.update_layout(
    title_text=" Market liquidity synthetic indicator (monthly averages) and VIX index "
)
# Set x-axis title
fig.update_xaxes(title_text="years -->")

# Set y-axes titles
fig.update_yaxes(title_text="Synthetic Index ", secondary_y=False)
fig.update_yaxes(title_text="VIX ", secondary_y=True)

fig.show("notebook")
```

Market liquidity synthetic indicator (monthly averages) a



New Liquidity Index Created

```
In [598]: fig = go.Figure(data=go.Scatter(x=merged_pca5['Date'], y=(merged_pca5['new_index']), name = 'rolls_spread'))
fig.show("notebook")
```



```
In [606]: plot_d = mmm_wmt[["Date", "amihud", "rolls_spread", "inverse_vol", "rptd_pr", "LC"]]
plot_d.head()
```

Out[606]:

	Date	amihud	rolls_spread	inverse_vol	rptd_pr	LC
0	2007-01-01	1739.829906	2.054803	3.458630e-06	7.480328	0.000511
1	2007-02-01	252.663188	2.071908	1.719525e-05	7.343895	0.004763
2	2007-03-01	1309.790088	1.556803	2.159073e-06	9.173682	0.002092
3	2007-04-01	2218.378820	1.663898	8.723377e-07	18.696334	0.005565
4	2007-05-01	1353.411753	1.688256	1.705450e-06	19.519186	0.009949

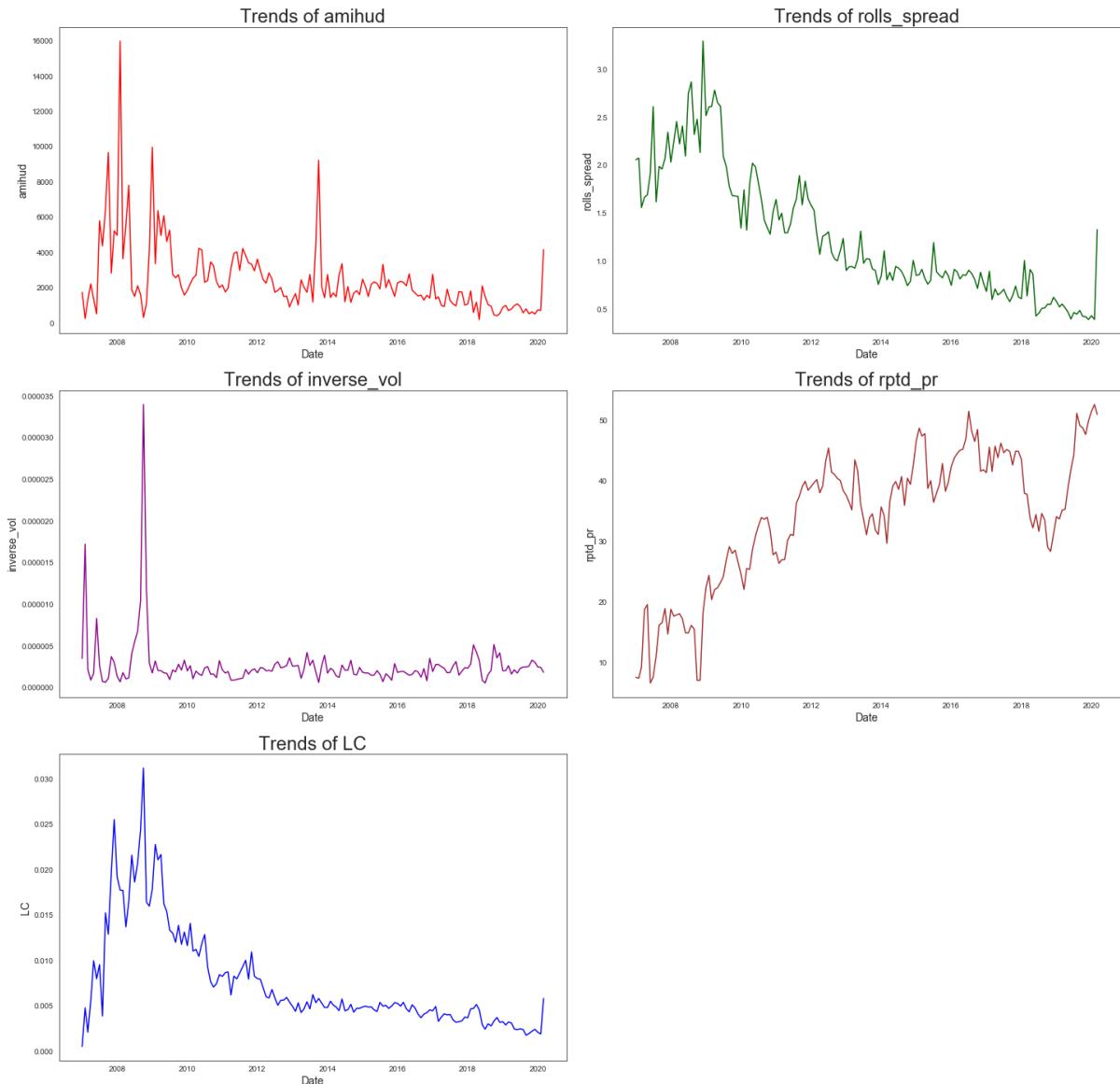
Plot trends for Liquidity Indicators

```
In [621]: keylist = list(plot_d.columns[1:])
colors = ['Red', 'darkgreen', 'darkmagenta', 'brown', 'blue'][len(keylist):]
colors_val = dict(zip(keylist, colors))
```

```
In [622]: req_rows = int(len(keylist)/2) if len(keylist)%2==0 else int(len(keylist)/2) + 1
fig, axs = plt.subplots(nrows=req_rows, ncols=2, figsize = (20,20), constrained_layout = True)
i = 0
index = 0
while i < len(keylist):
    j=0
    while j < 2:
        sns.set_style('white')
        axs[index,j].plot(plot_d['Date'], plot_d[keylist[i]], color = colors_val[keylist[i]], label = keylist[i][:])
        axs[index,j].set_xlabel('Date', size = 14)
        axs[index,j].set_ylabel(keylist[i][:], size = 14)
        axs[index,j].set_title('Trends of ' + keylist[i], size = 24)
        # For Legend
        ln_1, lab_1 = axs[index,j].get_legend_handles_labels()
        ax.legend(ln_1, lab_1, loc=0)

        j = j + 1
        i = i + 1
    if (i == len(keylist)) & (j != 2):
        axs[index,j].axis("off")
        break
    index = index + 1
plt.suptitle('Trends of the liquidity Indicators', size = 35)
fig.savefig('Trends of the liquidity Indicators.png')
plt.show()
```

Trends of the liquidity Indicators



```
In [627]: merged_3.head()
```

```
Out[627]:
```

	COMPLETE_CUSIP	rolls_spread_x	issue_size	spread_Duration	trailing_vol	Age	log_
0	931142AU7	1.403100	2.500000e+08	2.508518	0.247132	19.865254	
1	931142BF9	1.988638	1.000000e+09	12.974996	1.959841	11.598015	
2	931142CB7	1.285224	2.500000e+09	13.131005	4.685502	8.029763	
3	931142CH4	1.728408	7.500000e+08	7.866904	1.452575	5.045386	
4	931142CK7	1.536798	2.250000e+09	18.528089	16.459191	4.314677	

```
In [656]: keylist = list(merged_3.columns[2:])
colors = ['darkorchid', 'seagreen', 'darkmagenta', 'orangered', 'navy']
colors_val = dict(zip(keylist, colors))
```

Grid Plot for Bond Characteristics

```
In [ ]: req_rows = int(len(keylist)/2) if len(keylist)%2==0 else int(len(keylist)/2) + 1
fig, axs = plt.subplots(nrows=req_rows, ncols=2, figsize = (20,20), constrained_layout = True)
i = 0
index = 0
while i < len(keylist):
    j=0
    while j < 2:
        sns.set_style('white')
        sns.jointplot(x = merged_3[keylist[i][:]], y =merged_3["rolls_spread_x"], color = colors_val[keylist[i]], ax = axs[index,j], label=keylist[i][:], kind="reg")
        axs[index,j].set_xlabel(keylist[i][:], size = 14)
        axs[index,j].set_ylabel('rolls_spread', size = 14)
        axs[index,j].set_title('rolls_spread vs ' + keylist[i][:], size = 24)

    # For Legend
    ln_1, lab_1 = axs[index,j].get_legend_handles_labels()

    ax.legend(ln_1, lab_1, loc=0)

    j = j + 1
    i = i + 1
    if (i == len(keylist)) & (j != 2):
        axs[index,j].axis("off")
        break
    index = index + 1
plt.suptitle('Regression plot wrt Bond Characteristics', size = 35)
fig.savefig('Regression plot wrt Bond Characteristics.png')
```

Dealer's run

```
In [675]: import numpy as np
import scipy
import scipy.optimize as optimize
import datetime
import pandas as pd
import pandas_datareader.data as web
import matplotlib.pyplot as plt
```

```
In [686]: Data_RUN = pd.read_csv('Temp_Data_Runs.csv')
Data_RUN.head()
```

Out[686]:

	Time	ISIN	Price	Size	Axe	Dealer	Side	PriceType	Vendor	t
0	2020-06-15T08:11:37Z	US92343VBR42	113.614	0.0	I	BANCO BILBAO VIZCAYA	Offer	Percentage	Dealer Runs	2
1	2020-06-03T07:01:38Z	US92343VBR42	114.750	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
2	2020-06-17T11:10:33Z	US92343VBR42	113.922	0.0	I	BANCO BILBAO VIZCAYA	Offer	Percentage	Dealer Runs	2
3	2020-06-08T15:16:47Z	US92343VBR42	114.300	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
4	2020-06-02T09:00:18Z	US92343VBR42	114.430	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2

```
In [685]: Data_RUN['trd_exctn_dt'] = pd.to_datetime(Data_RUN['Time'], format='%Y-%m-%dT%H:%M:%S.%f')
Data_RUN['trd_exctn_dt'] = Data_RUN['trd_exctn_dt'].dt.date
```

```
In [687]: start = datetime.datetime(2007, 1, 30)
end = datetime.datetime(2020, 3, 31)
oas_percent = web.DataReader("BAMLC0A4CBBA", "fred", start, end)
yield_10y = web.DataReader("DGS10", "fred", start, end)
```

```
In [707]: # filtering data to actionable prices:
```

```
Data_RUN_A = Data_RUN[Data_RUN.Axe == "A"]
Data_RUN_A = Data_RUN_A[Data_RUN_A.PriceType != "Spread"]
Data_RUN_A.head()
```

Out[707]:

	Time	ISIN	Price	Size	Axe	Dealer	Side	PriceType	Vendor	tr
1	2020-06-03T07:01:38Z	US92343VBR42	114.75	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
3	2020-06-08T15:16:47Z	US92343VBR42	114.30	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
4	2020-06-02T09:00:18Z	US92343VBR42	114.43	1000000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
5	2020-06-10T10:19:12Z	US92343VBR42	113.91	660000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2
7	2020-06-10T09:34:08Z	US92343VBR42	113.91	660000.0	A	JP MORGAN	Offer	Percentage	Dealer Runs	2

```
In [719]: def Px(Rate,Mkt_Price,Face,Freq,N,C):
    return Mkt_Price - (Face * ( 1 + Rate / Freq ) ** ( - N ) + ( C / Rate ) * ( 1 - (1 + ( Rate / Freq )) ** -N ) )

def YieldCalc(guess,Mkt_Price,Face,Freq,N,C):
    x = scipy.optimize.newton(Px, guess,args = (Mkt_Price,Face,Freq,N,C),
    tol=.0000001, maxiter=100)
    return x
Data_RUN_A['price_diff'] = Data_RUN_A.groupby(['trd_exctn_dt','ISIN'])['Price'].diff().fillna(0)
```

```
In [709]: Data_RUN_A['cusip_id'] = Data_RUN_A["ISIN"].apply(lambda x: x[2:-1])
```

```
In [711]: fisd = pd.read_csv('fisd.csv')
fisd.drop(fisd.columns[0], axis=1, inplace=True)
fisd_offer = fisd.loc[fisd['COMPLETE_CUSIP'].isin(Data_RUN_A['cusip_id'].unique())][['COMPLETE_CUSIP','OFFERING_DATE', 'COUPON', 'MATURITY']]
fisd_offer
```

Out[711]:

	COMPLETE_CUSIP	OFFERING_DATE	COUPON	MATURITY
309710	92343VBR4	2013-09-11	5.15	2023-09-15

```
In [717]: Data_RUN_A_merge = pd.merge(Data_RUN_A, fisd_offer, left_on='cusip_id', right_on='COMPLETE_CUSIP')
Data_RUN_A_merge['MATURITY'] = pd.to_datetime(Data_RUN_A_merge['MATURITY'], format='%Y-%m-%d')
Data_RUN_A_merge['OFFERING_DATE'] = pd.to_datetime(Data_RUN_A_merge['OFFERING_DATE'], format='%Y-%m-%d')
Data_RUN_A_merge['trd_exctn_dt'] = pd.to_datetime(Data_RUN_A_merge['trd_exctn_dt'], format='%Y-%m-%d')

Data_RUN_A_merge['N_PERIODS'] = (((Data_RUN_A_merge['MATURITY'] - Data_RUN_A_merge['trd_exctn_dt'])/ np.timedelta64(1, 'Y'))*2).astype(int)

Data_RUN_A_merge['YTM'] = Data_RUN_A_merge.apply(lambda x: YieldCalc(x['COUPON']/100.0, x['Price'], 100, 2, x['N_PERIODS'], x['COUPON']), axis=1)
Data_RUN_A_merge['Age'] = (Data_RUN_A_merge['trd_exctn_dt'] - Data_RUN_A_merge['OFFERING_DATE'])/ np.timedelta64(1, 'D')
```

In [722]: Data_RUN_A_merge

Out[722]:

	Time	ISIN	Price	Size	Axe	Dealer	Side	PriceType	Vend
0	2020-06-03T07:01:38Z	US92343VBR42	114.750	1000000.0	A	JP MORGAN	Offer	Percentage	Deal Rur
1	2020-06-08T15:16:47Z	US92343VBR42	114.300	1000000.0	A	JP MORGAN	Offer	Percentage	Deal Rur
2	2020-06-02T09:00:18Z	US92343VBR42	114.430	1000000.0	A	JP MORGAN	Offer	Percentage	Deal Rur
3	2020-06-10T10:19:12Z	US92343VBR42	113.910	660000.0	A	JP MORGAN	Offer	Percentage	Deal Rur
4	2020-06-10T09:34:08Z	US92343VBR42	113.910	660000.0	A	JP MORGAN	Offer	Percentage	Deal Rur
...
38312	2020-03-12T13:32:59Z	US92343VBR42	110.206	1001000.0	A	JP MORGAN	Bid	Percentage	JPM F
38313	2020-03-12T13:33:36Z	US92343VBR42	110.188	1001000.0	A	JP MORGAN	Bid	Percentage	JPM F
38314	2020-03-12T13:33:54Z	US92343VBR42	110.201	1001000.0	A	JP MORGAN	Bid	Percentage	JPM F
38315	2020-03-12T13:33:58Z	US92343VBR42	110.210	1001000.0	A	JP MORGAN	Bid	Percentage	JPM F
38316	2020-03-12T13:37:44Z	US92343VBR42	110.221	1001000.0	A	JP MORGAN	Bid	Percentage	JPM F

38317 rows × 19 columns

In [723]:

```
def duration(c, y, m, n):
    macaulay_duration = ((1+y) / (m*y)) - ( (1 + y + n*(c-y)) / ((m*c*((1+y)**n - 1)) + m*y) )
    modified_duration = macaulay_duration / (1 + y)
    return macaulay_duration, modified_duration
```

In [724]:

```
duration_ = duration(Data_RUN_A_merge['COUPON'].astype('float')/100.0, Data_RUN_A_merge['YTM']/2.0, 2.0, Data_RUN_A_merge['N_PERIODS'])
```

In [725]:

```
Data_RUN_A_merge['mac_duration'] = duration_[0]
Data_RUN_A_merge['mod_duration'] = duration_[1]
Data_RUN_A_merge = pd.merge(Data_RUN_A_merge, yield_10y, left_on='trd_ex_ctn_dt', right_on='DATE')
Data_RUN_A_merge = pd.merge(Data_RUN_A_merge, oas_percent, left_on='trd_exctn_dt', right_on='DATE')
```

```
In [726]: Data_RUN_A_merge = Data_RUN_A_merge.rename(columns={'BAMLC0A4CBBB': 'BAML_OAS', 'DGS10': 'Yield_10YT'})
Data_RUN_A_merge['spread'] = Data_RUN_A_merge['YTM']*100 - Data_RUN_A_merge['Yield_10YT']

t_diff = Data_RUN_A_merge.groupby(['trd_exctn_dt', 'cusip_id'])['Yield_10YT'].mean().diff().fillna(0).reset_index()#['Yield_10YT'].diff()
t_diff = t_diff.rename(columns={'Yield_10YT':'T_diff'})
Data_RUN_A_merge_1 = Data_RUN_A_merge.merge(t_diff, left_on=['trd_exctn_dt', 'cusip_id'], right_on = ['trd_exctn_dt', 'cusip_id'], how='left')
```

```
In [728]: Data_RUN_A_merge_1['yield_change'] = Data_RUN_A_merge_1['mod_duration']*Data_RUN_A_merge_1['T_diff']

Data_RUN_A_merge_1['spread_duration'] = Data_RUN_A_merge_1['spread']*Data_RUN_A_merge_1['mod_duration']
Data_RUN_A_merge_1['spread_change'] = Data_RUN_A_merge_1.groupby(['trd_exctn_dt', 'cusip_id'])['spread_duration'].diff()

Data_RUN_A_merge_2 = Data_RUN_A_merge_1[Data_RUN_A_merge_1['spread_change'].notna()]

Data_RUN_A_merge_2['p_ret'] = Data_RUN_A_merge_2.groupby(['trd_exctn_dt', 'cusip_id'])['Price'].pct_change()*100
Data_RUN_A_merge_2 = Data_RUN_A_merge_2[Data_RUN_A_merge_2['p_ret'].notna()]

Data_RUN_A_merge_2.to_csv('Data_RUN_A_merge_2.csv')
```

/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:9: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

In [729]: Data_RUN_A_merge_2

Out[729]:

	Time	ISIN	Price	Size	Axe	Dealer	Side	PriceType	Ven
2	2020-02-07T06:15:13Z	US92343VBR42	111.450	10000000.0	A	JP MORGAN	Offer	Percentage	Dea R
3	2020-02-07T08:34:24Z	US92343VBR42	111.510	10000000.0	A	JP MORGAN	Offer	Percentage	Dea R
4	2020-02-07T07:32:48Z	US92343VBR42	111.370	10000000.0	A	JP MORGAN	Offer	Percentage	Dea R
5	2020-02-07T08:15:16Z	US92343VBR42	111.470	10000000.0	A	JP MORGAN	Offer	Percentage	Dea R
6	2020-02-07T06:14:39Z	US92343VBR42	111.450	10000000.0	A	JP MORGAN	Offer	Percentage	Dea R
...
26291	2020-03-27T21:05:12Z	US92343VBR42	108.735	1001000.0	A	JP MORGAN	Bid	Percentage	JPI
26292	2020-03-27T21:08:39Z	US92343VBR42	108.739	1001000.0	A	JP MORGAN	Bid	Percentage	JPI
26293	2020-03-27T21:10:40Z	US92343VBR42	108.753	1001000.0	A	JP MORGAN	Bid	Percentage	JPI
26294	2020-03-27T21:12:54Z	US92343VBR42	108.748	1001000.0	A	JP MORGAN	Bid	Percentage	JPI
26295	2020-03-27T21:13:15Z	US92343VBR42	108.721	1001000.0	A	JP MORGAN	Bid	Percentage	JPI

26078 rows × 29 columns

```
In [745]: results_m = smf.ols('p_ret ~ yield_change + spread_change ', data = Data
_RUN_A_merge_2).fit()
print(results_m.summary())
```

OLS Regression Results

Dep. Variable: p_ret R-squared:

1.000

Model: OLS Adj. R-squared:

1.000

Method: Least Squares F-statistic: 3.

586e+07

Date: Thu, 10 Dec 2020 Prob (F-statistic):

0.00

Time: 02:55:58 Log-Likelihood: 1.1

936e+05

No. Observations: 26078 AIC: -2.

387e+05

Df Residuals: 26075 BIC: -2.

387e+05

Df Model: 2

Covariance Type: nonrobust

	coef	std err	t	P> t	[0.025
0.975]					

Intercept	9.632e-05	1.57e-05	6.143	0.000	6.56e-05
0.000					
yield_change	0.0001	5.22e-05	2.235	0.025	1.43e-05
0.000					
spread_change	-1.0722	0.000	-8469.196	0.000	-1.072
-1.072					

Omnibus:	75129.280	Durbin-Watson:			
2.006					
Prob(Omnibus):	0.000	Jarque-Bera (JB):			
284.029					
Skew:	39.509	Prob(JB):			
0.00					
Kurtosis:	1891.898	Cond. No.			
8.23					

=====					
Warnings:					
[1] Standard Errors assume that the covariance matrix of the errors is					
correctly specified.					

Liquidity cost for the data Run

```
In [733]: sql_query = """
SELECT *
FROM trace.trace_enhanced
WHERE CUSIP_ID in ('92343VBR4','110122DQ8','110122DR6','92343VFT6')
AND TRD_EXCTN_DT BETWEEN '2007-01-01' AND '2019-12-31';
"""
new_data_query1 = db.raw_sql(sql_query)
```

```
In [732]: db = wrds.Connection()
```

```
Enter your WRDS username [deepsha]:madhur5
Enter your password:*****
WRDS recommends setting up a .pgpass file.
You can find more info here:
https://www.postgresql.org/docs/9.5/static/libpq-pgpass.html.
Loading library list...
Done
```

```
In [734]: new_data_query1.to_csv('new_data_query1.csv')
```

```
In [736]: def lagged_auto_cov(Xi,t):
```

```

    N = len(Xi)
    Xs = np.mean(Xi)
    end_padded_series = np.zeros(N+t)
    end_padded_series[:N] = Xi - Xs
    start_padded_series = np.zeros(N+t)
    start_padded_series[t:] = Xi - Xs

    auto_cov = 1./(N-1) * np.sum( start_padded_series*end_padded_series
)
    return auto_cov

# Data Run
new_data_query = pd.read_csv('new_data_query1.csv')
new_data_query = new_data_query.rename(columns={"cusip_id": "COMPLETE_CUSIP"})
new_data_query[ "trd_exctn_dt"] = pd.to_datetime(new_data_query[ "trd_exctn_dt"], format="%Y-%m-%d")

# rolls spread calculation

uniques_cusips = new_data_query.COMPLETE_CUSIP.unique()
Ncs_rs_all = pd.DataFrame(columns = ['COMPLETE_CUSIP', 'date', 'auto_cov', 'rolls_spread'])
for k in uniques_cusips:
    x = new_data_query[new_data_query.COMPLETE_CUSIP == k]
    auto_cov = []
    rolls_spread = []
    uniques_dates = x.trd_exctn_dt.unique()
    for i in range(0,len(uniques_dates)):
        p = x[x.trd_exctn_dt == uniques_dates[i]]['rptd_pr']
        d = np.diff(p)
        if len(d) == 0 or len(d) == 1 :
            a = np.nan
            r = np.nan
            auto_cov.append(np.nan)
            rolls_spread.append(np.nan)
        else:
            a = lagged_auto_cov(d,1)
            r = 2*np.sqrt(-a)
            auto_cov.append(a)
            rolls_spread.append(r)
    data = pd.DataFrame({'COMPLETE_CUSIP':k , 'date':uniques_dates[i], 'auto_cov': a, 'rolls_spread' : r },index=[0])
    Ncs_rs_all = Ncs_rs_all.append(data)

#rename date
Ncs_rs_all = Ncs_rs_all.rename(columns={"date":"trd_exctn_dt"})


## Ncs_rs_all contains rolls spread for all cusips for all dates. You can merge this with your predicted price data.

Ncs_rs_all.to_csv('new_data_query14regression.csv')
```

```
/Users/deepsha/anaconda3/lib/python3.7/site-packages/ipykernel_launcher.py:37: RuntimeWarning:
      invalid value encountered in sqrt
```

In [737]: Ncs_rs_all

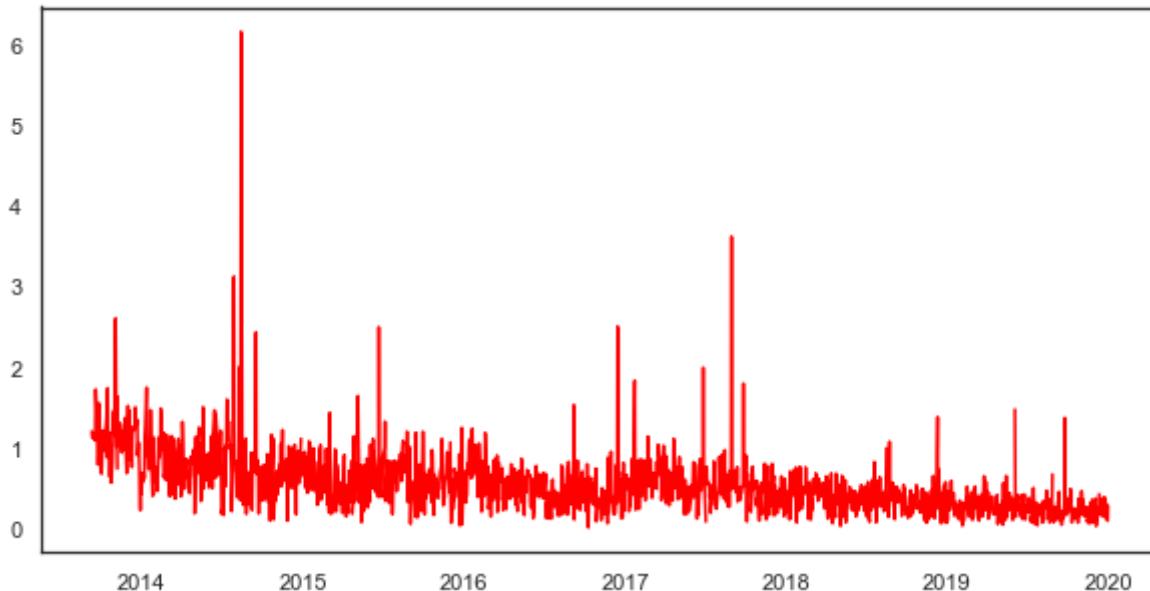
Out[737]:

	COMPLETE_CUSIP	trd_exctn_dt	auto_cov	rolls_spread
0	92343VBR4	2013-09-11	-0.359518	1.199196
0	92343VBR4	2013-09-12	-0.317982	1.127799
0	92343VBR4	2013-09-13	-0.309822	1.113234
0	92343VBR4	2013-09-16	-0.330675	1.150087
0	92343VBR4	2013-09-17	-0.339058	1.164573
...
0	92343VBR4	2019-12-24	-0.004041	0.127141
0	92343VBR4	2019-12-26	-0.023100	0.303974
0	92343VBR4	2019-12-27	-0.012442	0.223092
0	92343VBR4	2019-12-30	-0.001810	0.085078
0	92343VBR4	2019-12-31	-0.018010	0.268402

1587 rows × 4 columns

In [744]: fig, ax = plt.subplots(figsize = (10,5))
sns.set_style('white')
ax.plot(Ncs_rs_all['trd_exctn_dt'], Ncs_rs_all['rolls_spread'], color = "red", label = 'rolls_spread')

Out[744]: [`<matplotlib.lines.Line2D at 0x14a167c88>`]



```
In [747]: Data_RUN_price = pd.read_csv('Data_RUN_A_merge_2.csv')
Data_RUN_price = Data_RUN_price.iloc[:, 1:]

Data_RUN_price['deltaP'] = (9.632e-05 + 0.0001*Data_RUN_price['yield_change']-1.0722*Data_RUN_price['spread_change'])
Data_RUN_price['prevP'] = Data_RUN_price.groupby(['trd_exctn_dt','cusip_id'])['Price'].shift(1)
Data_RUN_price['predictedP'] = Data_RUN_price['prevP'] * (1 + (0.01 * Data_RUN_price['deltaP']))

Data_RUN_pred_Price = Data_RUN_price[['cusip_id', 'trd_exctn_dt', 'Price', 'predictedP']]

new_data_query14regression = pd.read_csv('new_data_query14regression.csv')
new_data_query14regression = new_data_query14regression.iloc[:, 1:]

new_data_rollSpread = new_data_query14regression[['COMPLETE_CUSIP', 'trd_exctn_dt', 'rolls_spread']]
#wmt_rollSpread["trd_exctn_dt"] = pd.to_datetime(wmt_rollSpread["trd_exctn_dt"], format="%Y%m%d")
new_data_rollSpread.trd_exctn_dt = new_data_rollSpread.trd_exctn_dt.astype(str)
#print(wmt_rollSpread.head())
Data_RUN_band = Data_RUN_pred_Price.merge(new_data_rollSpread, left_on=['cusip_id', 'trd_exctn_dt'], right_on=['COMPLETE_CUSIP', 'trd_exctn_dt'])

Data_RUN_band['price_lower_bound'] = Data_RUN_band['predictedP'] - 0.5*(Data_RUN_band['rolls_spread']*Data_RUN_band['predictedP'] /100)
Data_RUN_band['price_upper_bound'] = Data_RUN_band['predictedP'] + 0.5*(Data_RUN_band['rolls_spread']*Data_RUN_band['predictedP'] /100)

good_trade = Data_RUN_band.apply(lambda x: 0 if (x['Price'] >= x['price_lower_bound'] and x['Price'] <= x['price_upper_bound']) else 1, axis=1)

print(sum(good_trade)/len(good_trade))
```

0.010431484115694643

/Users/deepsha/anaconda3/lib/python3.7/site-packages/pandas/core/generics.py:5165: SettingWithCopyWarning:

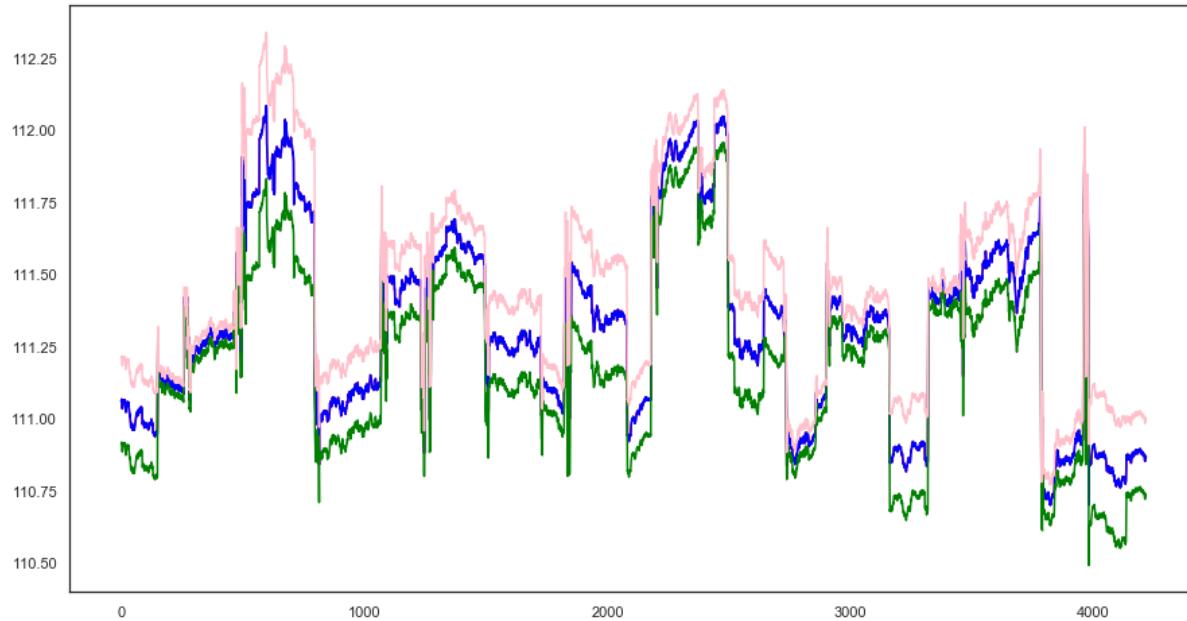
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```
In [755]: Data_RUN_band_ana = Data_RUN_band.dropna()
```

```
In [756]: fig, ax = plt.subplots(figsize = (15,8))
sns.set_style('white')
ax.plot( Data_RUN_band_ana['predictedP'], color = "red", label = 'rolls_spread')
ax.plot( Data_RUN_band_ana['Price'], color = "blue", label = 'rolls_spread')
ax.plot( Data_RUN_band_ana['price_lower_bound'], color = "green", label = 'rolls_spread')
ax.plot( Data_RUN_band_ana['price_upper_bound'], color = "pink", label = 'rolls_spread')
```

Out[756]: [`<matplotlib.lines.Line2D at 0x16de40748>`]



ADF testing for Mean Reversion

```
In [757]: import statsmodels.tsa.stattools as ts
```

```
In [759]: ts.adfuller(Data_RUN_band_ana['predictedP'])
```

```
Out[759]: (-3.269212196423111,
 0.0163120474923516,
25,
4148,
{'1%': -3.431927471404566,
 '5%': -2.862237040274829,
 '10%': -2.5671410407892545},
-12958.644444157177)
```

Since the Test statistic value is smaller than the 5 and 10 levels, it is likely to reject the null hypothesis and the series is mean reverting

```
In [766]: adf_statistic = ts.adfuller(Data_RUN_band_ana[ 'predictedP' ], 1)
adf_statistic
```

```
Out[766]: (-4.357451443554643,
 0.00035275248743890143,
 1,
 4172,
 {'1%': -3.431918391192134,
 '5%': -2.8622330290415605,
 '10%': -2.5671389053926603},
 -13000.908382996844)
```

```
In [771]: import os
import sys
import warnings
from datetime import date
import pandas as pd
import pandas_datareader.data as web
import numpy as np
from numpy.linalg import LinAlgError

import statsmodels.tsa.api as tsa
from statsmodels.graphics.tsaplots import plot_acf, acf, plot_pacf, pacf
from statsmodels.tsa.stattools import acf, q_stat, adfuller
import statsmodels.api as sm
from scipy.stats import probplot, moment
from sklearn.metrics import mean_squared_error

import quandl
import matplotlib.pyplot as plt
import matplotlib as mpl
```

```
In [772]: %matplotlib inline
warnings.filterwarnings('ignore')
plt.style.use('ggplot')
```

```
In [773]: def plot_correlogram(x, lags=None, title=None):
    lags = min(10, int(len(x)/5)) if lags is None else lags
    fig, axes = plt.subplots(nrows=2, ncols=2, figsize=(14, 8))
    x.plot(ax=axes[0][0])
    q_p = np.max(q_stat(acf(x, nlags=lags), len(x))[1])
    stats = f'Q-Stat: {np.max(q_p):>8.2f}\nADF: {adfuller(x)[1]:>11.2f}'
    axes[0][0].text(x=.02, y=.85, s=stats, transform=axes[0][0].transAxes)
    probplot(x, plot=axes[0][1])
    mean, var, skew, kurtosis = moment(x, moment=[1, 2, 3, 4])
    s = f'Mean: {mean:>12.2f}\nSD: {np.sqrt(var):>16.2f}\nSkew: {skew:1.2f}\nKurtosis:{kurtosis:9.2f}'
    axes[0][1].text(x=.02, y=.75, s=s, transform=axes[0][1].transAxes)
    plot_acf(x=x, lags=lags, zero=False, ax=axes[1][0])
    plot_pacf(x, lags=lags, zero=False, ax=axes[1][1])
    axes[1][0].set_xlabel('Lag')
    axes[1][1].set_xlabel('Lag')
    fig.suptitle(title, fontsize=20)
    fig.tight_layout()
    fig.subplots_adjust(top=.9)
```

```
In [774]: ts_p = Data_RUN_band_ana['predictedP']
```

```
In [776]: (ts_p == 0).any()
```

Out[776]: False

```
In [783]: ts_p_diff = ts_p.diff().dropna()
```

```
In [777]: ts_p_log = np.log(ts_p)
```

```
In [778]: ts_p_log_diff = ts_p_log.diff().dropna()
```

```
In [784]: fig, axes = plt.subplots(nrows=4, ncols=1, figsize=(14,6))

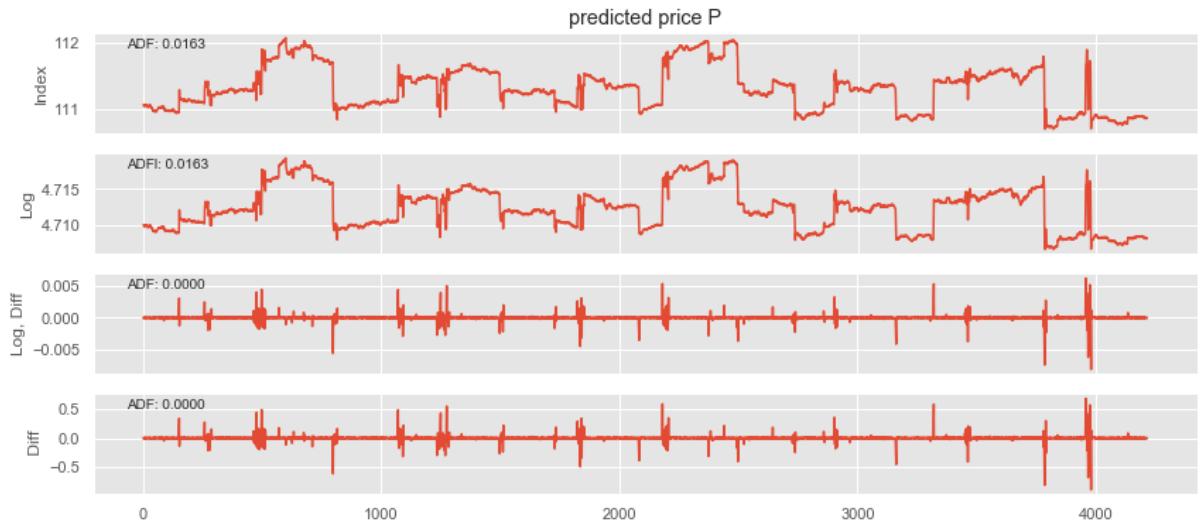
ts_p.plot(ax=axes[0], title='predicted price P')
axes[0].text(x=.03, y=.85, s=f'ADF: {tsa.adfuller(ts_p.dropna())[1]:.4f}', transform=axes[0].transAxes)
axes[0].set_ylabel('Index')

ts_p_log.plot(ax=axes[1], sharex=axes[0])
axes[1].text(x=.03, y=.85, s=f'ADFl: {tsa.adfuller(ts_p_log.dropna())[1]:.4f}', transform=axes[1].transAxes)
axes[1].set_ylabel('Log')

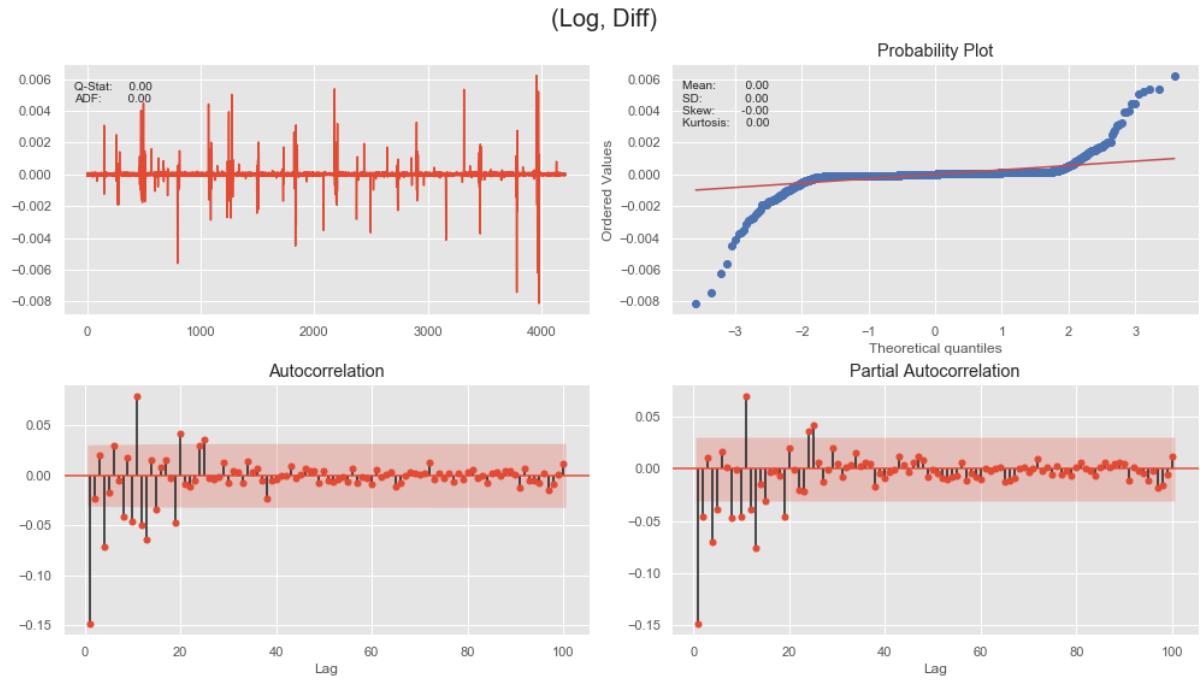
ts_p_log_diff.plot(ax=axes[2], sharex=axes[0])
axes[2].text(x=.03, y=.85, s=f'ADF: {tsa.adfuller(ts_p_log_diff.dropna())[1]:.4f}', transform=axes[2].transAxes)
axes[2].set_ylabel('Log, Diff')

ts_p_diff.plot(ax=axes[3], sharex=axes[0])
axes[3].text(x=.03, y=.85, s=f'ADF: {tsa.adfuller(ts_p_diff.dropna())[1]:.4f}', transform=axes[3].transAxes)
axes[3].set_ylabel('Diff')
```

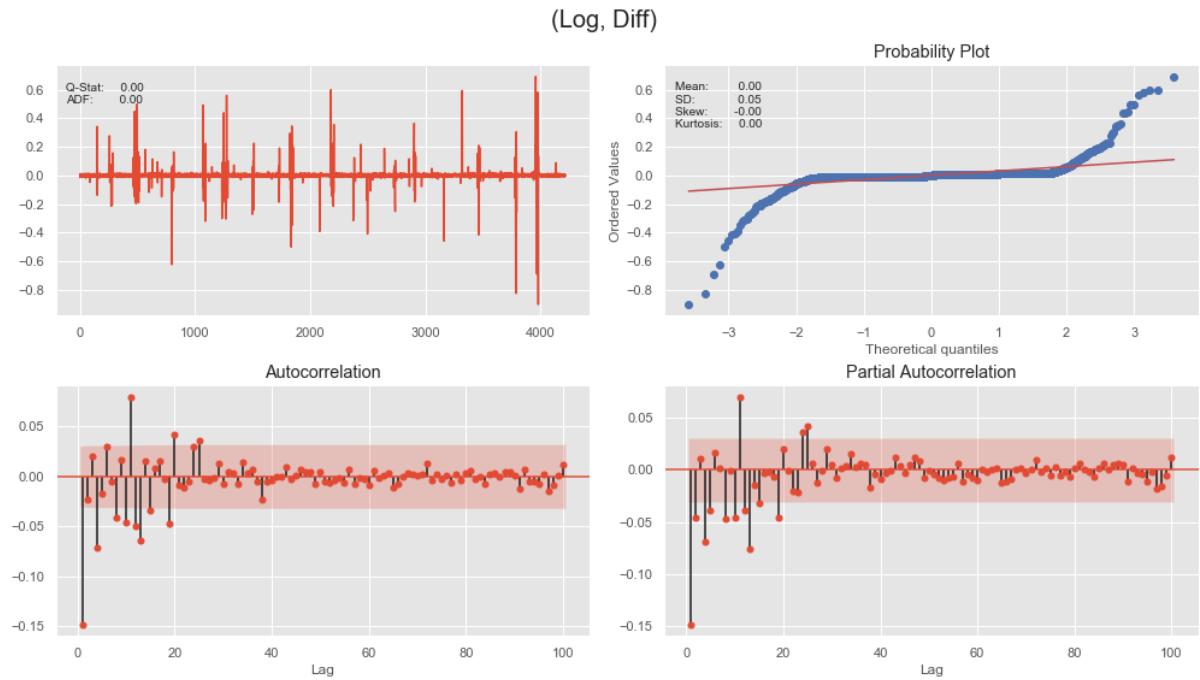
Out[784]: Text(0, 0.5, ' Diff')



In [782]: `plot_correlogram(ts_p_log_diff, lags=100, title='(Log, Diff)')`



In [785]: `plot_correlogram(ts_p_diff, lags=100, title='(Log, Diff)')`



In []: