

Scientific Computing in Python

Interpolation : scipy.interpolate

Interpolation is a term used in numerical analysis to describe the process of creating new data points from a set of known data points. Spline functions and classes, one-dimensional and multi-dimensional (univariate and multivariate) interpolation classes, and more can be found in the SciPy library's `scipy.interpolate` subpackage. Interpolation is important not only in statistics but also in science, business, and for predicting values that fall between two existent data points.

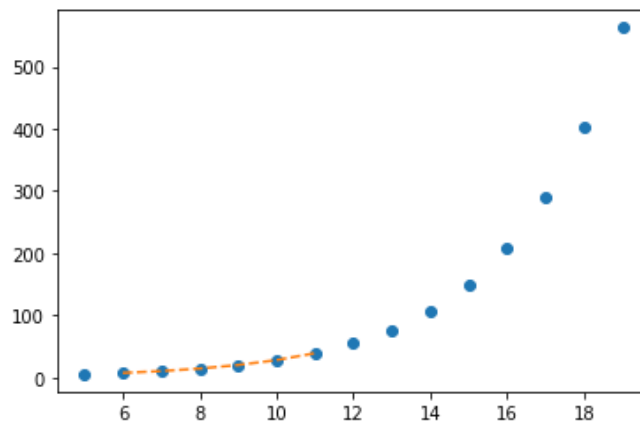
Example 1 : 1D Interpolation

The `interp1d` class in `scipy.interpolate` is a handy way to make a function out of fixed data points that may be evaluated anywhere within the domain defined by the input data using linear interpolation.

```
import matplotlib.pyplot as plt
import numpy as np
from scipy import interpolate
x = np.arange(5, 20)
y = np.exp(x/3.0)
f = interpolate.interp1d(x, y)
x1 = np.arange(6, 12)
y1 = f(x1) # use interpolation function returned by `interp1d`
plt.plot(x, y, 'o', x1, y1, '--')
plt.show()
```

Output:

Scientific Computing in Python



Example 2 : Multivariate Interpolation

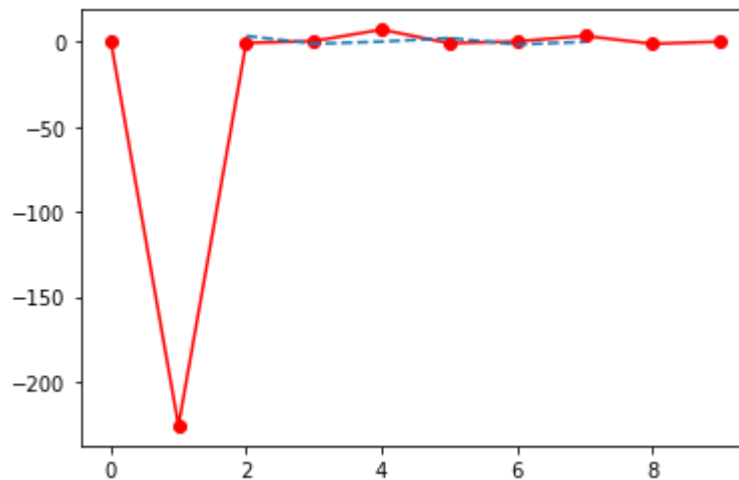
Multivariate interpolation (sometimes known as spatial interpolation) is used on functions with many variables. The `interp2d` function is demonstrated in the following example.

The `interp2d(x, y, z)` function interpolates across a 2-D grid by utilising the `x`, `y`, and `z` arrays to approximate some function $f: "z = f(x, y)"$ and returns a function whose call method employs spline interpolation to discover the value of new points.

```
from scipy import interpolate
import matplotlib.pyplot as plt
x = np.arange(0,10)
y = np.arange(10,25)
x1, y1 = np.meshgrid(x, y)
z = np.tan(x1+y1)
f = interpolate.interp2d(x, y, z, kind='cubic')
x2 = np.arange(2,8)
y2 = np.arange(15,20)
z2 = f(x2, y2)
plt.plot(x, z[0, :], 'ro-', x2, z2[0, :], '--')
plt.show()
```

Output:

Scientific Computing in Python



Example 3 : Spline Interpolation

Spline interpolation involves two steps: (1) computing a spline representation of the curve, and (2) evaluating the spline at the required points. There are two approaches to express a curve and generate (smoothing) spline coefficients in order to discover the spline representation: directly and parametrically. Using the function **splrep**, the direct technique determines the spline representation of a curve in a 2-D plane.

The function **splprep** allows you to parametrically define curves in N-D space. Only one input argument is required for this function. The curve in N-D space is represented by a list of -arrays in this input. The number of curve points equals the length of each array, and each array contains one component of the N-D data point.

```
import numpy as np
import matplotlib.pyplot as plt
from scipy import interpolate
x = np.arange(0, 2*np.pi+np.pi/4, 2*np.pi/8)
y = np.sin(x)
tck = interpolate.splrep(x, y, s=0)
xnew = np.arange(0, 2*np.pi, np.pi/50)
ynew = interpolate.splev(xnew, tck, der=0)
plt.figure()
plt.plot(x, y, 'x', xnew, ynew, xnew, np.sin(xnew), x, y, 'b')
plt.legend(['Linear', 'Cubic Spline', 'True'])
```

Scientific Computing in Python

```
plt.axis([-0.05, 6.33, -1.05, 1.05])  
plt.title('Cubic-spline interpolation')  
plt.show()
```

Output:

