

CISC5352: Financial Data Analytics Homework (2)

High-frequency trading data

Basics (100 points)

The `TAQ_JNJ_1004_1015_2010_trading.csv` has all transactions of JNJ stock from Oct 4, 2010 to Oct 15, 2010 (Note: this csv is not a very standard csv because not all data are separated in different columns)

1. Trim all transactions not in the normal trading window: 9:30 am -4:00 pm EST and write the transactions in the normal trading window in to a csv file: `TAQ_JNJ_1004_1015_2010_trading_normal_hours.csv`. We assume we only consider the transactions during normal trading windows for the following problems.
2. Visualize the first and last 5000 transactions from file:
 - (a) `TAQ_JNJ_1004_1015_2010_trading_normal_hours.csv`
3. Let t_i be the trading time in which i^{th} transaction took place and P_{t_i} be the transaction price at t_i , The price change in the time interval $\Delta t_i = t_i - t_{i-1}$ is $y_i = \Delta P_{t_i} = P_{t_i} - P_{t_{i-1}}$
 - (a) Count the number of transitions with price change, i.e., the cardinality of the set $\Theta = \{i | y_i \neq 0\}$.
 - (b) Visualize the price change y_i , $i = 1, 2, \dots$ such that the y-axis is the range of price changes (e.g. $-\$0.5$ to $\$0.5$). (Note: your x-axis is the index of i)
 - (c) Draw a histogram of the frequency of all transactions with a price change
4. Partition the trading time sequence into 5/10/30/60-minute intervals by picking the *mean* transaction price and volumes in each interval and compute the log-return (aka 'U sequence') and write it into a corresponding csv file, in addition to visualizing them.
 - (a) `TAQ_JNJ_1004_1015_2010_5_min_trading_unit.csv`
 - (b) `TAQ_JNJ_1004_1015_2010_10_min_trading_unit.csv`
 - (c) `TAQ_JNJ_1004_1015_2010_30_min_trading_unit.csv`

(d) [TAQ_JNJ_1004_1015_2010_60_min_trading_unit.csv](#)

5. Compute “section volatility”: $s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n u_i^2 - \frac{1}{n(n-1)} (\sum_{i=1}^n u_i)^2}$ for each case, where n is the number of transaction units in each case and u_i is the i^{th} item in the log return sequence
6. Compute “volume section standard deviation”:

$$s_v = \sqrt{\frac{1}{n-1} \sum_{i=1}^n v_i^2 - \frac{1}{n(n-1)} (\sum_{i=1}^n v_i)^2}$$

for each case, where n is the number of transaction units in each case and v_i is the i^{th} item in the volume sequence.

7. Compute section *skewness* and *kurtosis* values for each case and draw your conclusions based on the definitions of skewness and kurtosis.

$$skewness(X) = \frac{n}{(n-1)(n-2)} \frac{\sum_{i=1}^n (u_i - \bar{u})^3}{s^3}$$

$$Kurtosis(X) = \frac{1}{n} \frac{\sum_{i=1}^n (u_i - \bar{u})^4}{s^4} - 3$$

Repeat 1-7 for TAQ_CAT_Feb_2010_trading_.csv, which includes all transactions for caterpillar (CAT) stock in Feb 2010

Bid-ask spread

1. TAQ_CAT_QUOTE_0104_2010.csv includes all quote information for caterpillar (CAT) stock transaction on Jan 04, 2010.
2. Compute and visualize its bid-ask spread: $\delta_p = P_{offer} - P_{bid}$, which is an important information for market liquidity, for each transaction.
3. Partition the trading time sequence into 5/10/30-minute intervals by picking the *mean* bid and offer prices and their corresponding in each interval and write it into a corresponding csv file, in addition to visualizing them.
 - (a) [TAQ_CAT_QUOTE_0104_2010_5_min_trading_unit.csv](#)
 - (b) [TAQ_CAT_QUOTE_0104_2010_10_min_trading_unit.csv](#)
 - (c) [TAQ_CAT_QUOTE_0104_2010_30_min_trading_unit.csv](#)
4. Compute the following entropy values for offer and bid volume as follows
 - (a) $H_{offer} = - \sum_{i=1}^N p_i \log_2 p_i$,

- (b) $p_i = \frac{V_i^{(offer)}}{\sum_{k=1}^N V_i^{(offer)}}$, where $V_i^{(offer)}$ is the mean offer volume in the i^{th} interval.
- (c) $H_{bid} = -\sum_{i=1}^N q_i \log_2 q_i$,
- (d) $q_i = \frac{V_i^{(bid)}}{\sum_{k=1}^N V_i^{(bid)}}$, where $V_i^{(bid)}$ is the mean bid volume in the i^{th} interval.
- (e) Relative entropy for offer and bid volume $H(P||Q) = \sum_{i=1}^N p_i \log_2 \frac{p_i}{q_i}$
- (f) Note: $\log_2 t$ should be automatically set as zero if $t = 0$. Similarly $\log_2 \frac{2}{0} = \log_2 \frac{0}{0} = 0$

What should you turn in?

- 1. A folder contains your source files and related output.
- 2. Please name your folder as first-name_last-name_CISC5352_homework_2.
For example, John_Smith_CISC5352_homework_2 if your name is John Smith.
- 3. Send the zipped file (.zip instead of ,rar) of your folder to Blackboard before 11:59 pm Dec 16, 2016