

CS 367 Project #2 - Spring 2021:

Floating Point Representation

Due: Friday, March 5th 11:59pm

This is to be an individual effort. No partners.

No late work allowed after 48 hours; each day late automatically uses one token.

1. Project Overview:

In class, we talked about the IEEE standard for floating point representation and did examples using different sizes for exponent and fraction fields so that you could learn how to do the conversions.

For this assignment, you are going to write several functions in C to add a custom floating-point system to a scripting language called **MLKY**. Your functions will allow **MLKY** to convert standard C **float** floating point values to a custom bit-level floating point representation for use internally in its language. You will also write code to convert this **MLKY** floating point representation back into standard C float values. Finally, you will write code to perform addition and multiplication of these **MLKY** bit-level floating point representations.

2. Running the MLKY Scripting Language

The main input will be reading in scripts for the **MLKY** scripting language, which we have implemented and provided to you as the starting code. The language will call your functions to implement floating point support for these scripts. The **MLKY** language is very simple with only 5 different kinds of statements: **assignment**, **print**, **display**, **add**, and **multiply**. **MLKY** scripts also only support single-letter variables, as shown below.

Here is an example **MLKY** script (one statement per line):

```
zeus-1:P1$ cat sampleprogram.mlky
x = 0.26
print x
y = -15.25
print y
a = x + y
print a
z = x * y
print z
o = 1.0
print o
display o
```

3. Output from the MLKY Scripting Language

For the script in Section 2, the output would be:

Note you will only get an output to the screen for **display** or **print** commands only.

[illegible]

In the above display, we are interactively assigning values to variables **a** and **b**, then we are doing arithmetic and assigning the sum to **c**, and finally we are printing out **c**.

4. Project Code Specification

Page 2 of 13

Your functions will convert the user-input `float` values into a custom 12-bit floating point encoding, which will be of type `fp_gmu`. This custom `fp_gmu` type is stored as a 32-bit integer in memory, so you can work with it just like you would work with a signed int. (e.g. Bitwise operations and Shifting). You will be getting the S, M, and E values from the input and convert them to the S, exp, and frac fields. You will then encode these fields into the `fp_gmu` type. (Using bitwise operations and shifting).

MLKY Floating Point Bit-Level Representation

We encode the MLKY Floating Point values within a signed 32-bit `int` in this format:

Unused Bits (MUST BE 0s)																		S	exp					frac					
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0												

The int is typedef defined as a `fp_gmu` type for this project.

You are going to implement this 12-bit floating point representation:

1 bit for sign (s), 5 bits for exponent (exp) and 6 bits for fraction (frac).

The representation does allow for special values (NaN, ∞ or $-\infty$), encoded using standard conventions.

The smallest possible value (all bits = 0) is assumed to represent the value 0 as well as values very close to zero. The zero can use the sign bit to represent +0 and -0.

Rules describing the outcomes of arithmetic operations will be discussed later.

Functions to Implement

`fp_funcs.c` starting file has stubs for four functions, which you will be implementing. You are free to add any extra functions you like, but you can only modify `fp_funcs.c`. In this section, we will discuss *both* the MLKY script functions as well as the C functions which the MLKY code depends on. *You are only responsible for implementing the C functions*, since the MLKY code is already written for you.

Using bit-level operators, you will write the code for the functions (shown below):

MLKY script: `Assignment statement` (`variable = value`)

This operation calls your function:

`compute_fp` converts input from a standard C `float` to our custom 12-bit mini-float representation `fp_gmu` (which only uses the 12 lowest of the given 32-bits of an int).

The return value of the `compute_fp` function will be the `fp_gmu`, which encodes the corresponding bit representation of our `MLKY` floating-point value.

Observe how the “s”, “exp” and “frac” bits are preceded by a sequence of leading 0s to make the representation 32 bits that fit within a `fp_gmu` type (int).

For example, the closest representable value for **56.24** can be determined by looking at the all values program output (detailed later in this document).

[illegible]

This means that when 56.24 is converted to the binary floating-point representation in our format, some precision is lost, and the resulting bit pattern

corresponds to 56.0, which is the closer value. If we had picked a number in the middle (56.25), then it still would have gone to 56.0, because 56.0 has an M of 1.110000 and 56.5 has an M of 1.110001, so rounding to even would mean you would round down to 56. If you enter 56.75, however, it would round up to 57 (1.110010) as the even value.

Handling cases in `compute_fp()`

- **For Underflows** (eg. Denormalized or $\text{exp} \leq 0$):
 - There are no Denormalized values. If your number is smaller than the smallest representable Normalized value, then it will round-to-nearest-even. If it rounds down, encode it as either 0 or -0 as appropriate.
 - In particular, an $\text{exp} < 0$ will always result in a value of 0 or -0.
- **For Overflows** (eg. exp is too large for Normalized), return the `fp_gmu` floating-point representation of the special value ∞ or $-\infty$ as needed.

MLKY script: Print statement (`print variable`)

This uses your `float get_fp()` function to convert from our `fp_gmu` floating-point representation to a regular C `float` value and returns it as a C `float`.

```
float get_fp(fp_gmu val) {}
```

- **If val represents ∞ or $-\infty$** , return a pre-defined C `float` constant `INFINITY`
 - In C, this is simply one of these two following lines exactly:
`return INFINITY;`
`return -INFINITY;`
 - Note: the `INFINITY` constant will **not** work with your `fp_gmu` floating-point representation. It is how C `floats` store infinity.
- **For NaN**, return the pre-defined C `float` constant `NAN`
 - In C, this is simply this line exactly:
`return NAN;`
 - There is no such thing as negative Not a Number. So, it doesn't matter what the sign bit is, you will return `NAN` with `sign = 0`.

MLKY script: Add statement (`variable = variable + variable`)

This uses your C function:

```
fp_gmu add_vals(fp_gmu source1, fp_gmu source2) {}
```

For this statement, you are going to take two values in our **fp_gmu** floating-point representation and use the same technique as described in class to add these values and return the result converted back into our representation.

Align M2 by making E2 equal to E1 (or vice versa), then $M = M1 + M2$, $E = E1$, then encode your S, M, and E back into a **fp_gmu** value.

- **Rounding** will be through round-to-nearest-even (as with **compute_fp**)
- **For Overflows** (eg. exp is too large for Normalized), return the **fp_gmu** floating-point representation of the special value ∞ or $-\infty$
- **For Underflows**: These will round down to 0 or -0 as appropriate.
- **Sign**: Adding positive and negative values may require subtraction instead of addition.
- **Special Cases**: See the next section on **Arithmetic Rules**

When implementing this statement, DO NOT convert the numbers back to C floats, add them directly as C floats, and then convert to the new representation (doing so will not bring any credit).

You must work with the S, M, and E components of the representations as described above. You may, however, work with M as a C **float**.

MLKY script: **Multiply statement** (**variable** = **variable** * **variable**)

This uses your C function:

```
fp_gmu mult_vals(fp_gmu source1, fp_gmu source2) {}
```

For this statement, you are going to take two values in our **fp_gmu** representation and use the same technique as described in class to multiply these values and return the result in our representation.

$M = M1 * M2$, $E = E1 + E2$, $S = S1 \wedge S2$, then encode S, M, E back to a **fp_gmu** value.

- **Rounding** will be through round-to-nearest-even. (as with **compute_fp**)
- **For Overflows** (eg. exp is too large for Normalized), return the **fp_gmu** floating-point representation of the special value ∞ or $-\infty$
- **For Underflows**: These will round down to 0 or -0 as appropriate.

- **Special Cases:** See the next section on **Arithmetic Rules**

When implementing this statement, DO NOT convert the numbers back to C floats, add them directly as C floats, and then convert to the new representation (doing so will not bring any credit).

You must work with the S, M, and E components of the representations as described above. You may, however, work with M as a C **float**.

MLKY script: **Display statement** (**display variable**)

Nothing to do here, it's all done for you!

Arithmetic Rules

Here are a list of rules for when you are multiplying or adding values.

Your result will be:

1. NaN (*Use 0 for the Sign Bit.*)

- If you add $\infty + -\infty$ (either order), return your **fp_gmu** NaN.
- If you multiply ∞ (or $-\infty$) by 0 return your **fp_gmu** NaN.
- If either argument is NaN, return your **fp_gmu** NaN

2. Infinity

- If you add any value (non NaN, $-\infty$) to ∞ , return ∞ .
- If you add any value (non NaN, ∞) to $-\infty$, return $-\infty$.
- If you multiply any non-Zero, non NaN value to ∞ *or* $-\infty$, return ∞ *or* $-\infty$ as appropriate based on the sign rules for multiplication

3. Zero

- If you multiply 0 or -0 by non NaN, non Infinity, return either 0 or -0 (*based on the normal sign rules for multiplication*)
- If you add -0 + -0, you will return -0.
- If you add -0 + 0, or vice versa, you will return 0.
- If you add 0 or -0 to any value that is non NaN, non Infinity, you will return that other value.
- If you multiply 0 * -0, or vice versa, you will return either 0 or -0
(*based on the normal sign rules for multiplication*)
- For any other arithmetic operation which would result in a zero, return 0.

Project Constraints

There are Two Special Number Types: Infinity and NaN.

- These will be implemented using a proper special number pattern in your **fp_gmu** floating-point representation. (Remember ∞ *and* $-\infty$)
- There is only one NaN, regardless of sign, it's not a number.
 - Any pattern which matches a NaN is considered equivalent.
 - Your **fp_gmu** function inputs should be able to recognize any bit representation of NaN.
 - Your **fp_gmu** outputs may use any valid NaN bit representation.

- For your `get_fp()` function only, you will be converting your `fp_gmu` floating-point representation value back into a standard C `float` type.
 - If your `fp_gmu` representation is storing ∞ or $-\infty$, then your `get_fp()` will return using a pre-defined C float constant, `INFINITY`. (or `-INFINITY`)
 - `return INFINITY;` // or `return -INFINITY;`
 - This `INFINITY` only works with C `floats`, not with our representation, so it's only used to return from `get_fp()` when the input is ∞ .
 - If your `fp_gmu` is storing NaN, then you can return NaN;
 - `return NAN;`
 - There is no negative NaN. If the sign is a 1, still `return NAN;`

Denormalized Numbers are not part of this assignment.

- When working with arithmetic, it is possible to start with a Normalized number and end with a value that should round down to 0.
- Always check and encode accordingly.

You may Not use any `math.h` functions, including `pow()`

You may Not use any unions in your code.

You may Not work directly with the bits of a C float.

Negative Numbers must be handled.

- All values (including ∞) will be handled properly with negatives.
- `compute_fp`, `mult_vals`, and `add_vals`, will need to support -0 encoding.
- -0 in your integer-based floating point representation is the expected return value for underflows that occur with a negative value.

(eg. if exp is too small when encoding a negative number, underflow to -0)

When working in your functions, you may work with M as a C float.

- You can use C `floats` in your code to do your work generally.
- The only restriction is that in `add_vals` and `mult_vals`, you can't convert the entire inputs to C `floats`, then just add/multiply them together and convert them back.
- You have to do the operations on the S, M, and E components.
- You can still use normal C `floats` in those functions for your work on M.

5. Input Checking

In our `fp_gmu` representation, we have to do rounding on a lot of our values because they aren't directly representable. In float types in C, the same thing has to happen.

When you enter a value when `fp`, you're actually entering it as a C float, which means that some of the values you type in won't be exactly the same when they get passed into your `compute_fp` function. Most of the time the rounding is so close that it won't matter, but there may be occasions where you enter a value and get an unexpected result.

The first thing to do when debugging is to run a provided program, called `input_checker`. This program will be created when you use `make` and will let you enter a value just like you would on `fp`, but this will show you exactly which value will be passed into your `compute_fp` function for that input.

This shows that if you do the following:

[illegible]

You can see exactly what value will be passed into your `compute_fp` function.

[illegible]

So, we can see here that your `compute_fp` function will get `123.45677947998046875000000000000000000000000000000` passed into it. Usually, this is fine, but for some values it may account for any discrepancies you may see.

First, get the starting code (`project1_handout.tar`) from the same place you got this document. Once you un-tar the handout on zeus (using `tar xvf project1_handout.tar`), you will have the following files:

- For each E (the E is given and the exp equivalent is given in binary), **all_values** lists all possible values that can be represented (vals). For each val, you get the M in decimal and in binary for convenience.

For example, in the sample program we assign `0.26` to `x`. This number is not a valid **val** in the output for this program, as shown in the snippet from the `all values` output below.

The closest values to **0.26** are **0.2578125** and **0.26171875**. Since we're using round-to-nearest-even (truncation), we round up to **0.26171875** as seen in the sample output.

Of course, doing this in decimal is very hard. It's a lot easier once you're working in the code to do the rounding from the binary directly. You'll have your *M* (which you can work with as a **float** in C) and you'll have to find a way to get the first 6 bits of the fraction part of *M* as an integer for encoding in *frac*.

Sample Test with easier test values for rounding:

x = -127.74	This will round down to -128
y = -1.0	This is directly representable.
z = x + y	The true answer is -129, which is not representable.
print z	This will print -128 (after rounding)

- **samplescript.mlky** – The sample script used in this document.
- **fpParse.h**, **fp.h**, and **fp.1** – You can ignore these files - They are the Lex specification which tokenizes input and sends it to the recursive descent parser in the main program.

7. Implementation Notes

- **MLKY** Script Files – The accepted syntax is very simplistic and it should be easy to write your own scripts to test your code (which we strongly encourage).
 - **MLKY** only uses single-letter, lowercase variable names.
 - **MLKY's** only commands are:
 - **print x** where *x* is a variable to print the value.
 - **display x** where *x* is a variable to display the bit representation
 - **x = value** for some floating point value. Performs assignment.
 - **x = y + z** for any legal variable names to add variables.
 - **x = y * z** for any legal variable names to multiply variables.
- If you run **fp** from the command line without inputting a script file, you can end the session by pressing enter with no input.
- To run **fp** with a script file, use redirects. `./fp < samplescript.mlky`

8. Submitting & Grading

Submit this assignment electronically on Blackboard. Note that the only file that gets submitted is **fp_funcs.c**. Make sure to put your name and G# as a commented line in the beginning of your program **fp_funcs.c**

You can make multiple submissions; but we will test and grade **ONLY** the latest version that you submit (with the corresponding late penalty, if applicable).

Important: Make sure to submit the correct version of your file on Blackboard! Submitting the correct version late will incur a late penalty; and submitting the correct version 48 hours after the due date will not bring any credit.

Questions about the specification should be directed to the CS 367 Piazza forum.

Your grade will be determined as follows:

- **20 points** - code & comments. Be sure to document your design clearly in your code comments. This score will be based on reading your source code.
- **80 points** – correctness. We will be building your code using the `fp_funcs.c` code you submit along with our code.
 - If your program does not compile, **we cannot grade it.**
 - If your program compiles but does not run, **we cannot grade it.**
 - We will give partial credit for incomplete programs that build and run.
 - You will not get credit for a particular part of the assignment (multiplication for example), if you do not use the required techniques, even if your program performs correctly on the test cases for this part.