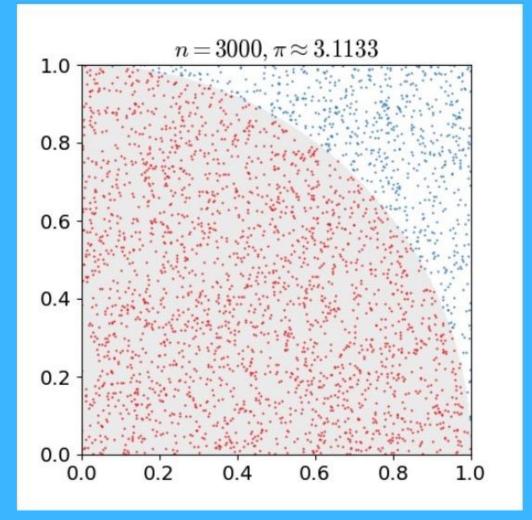
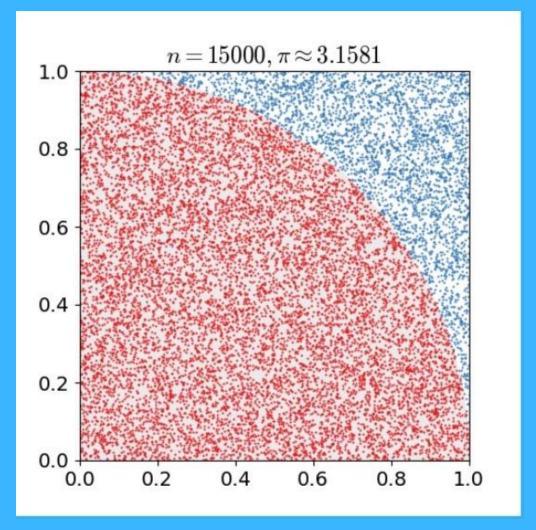
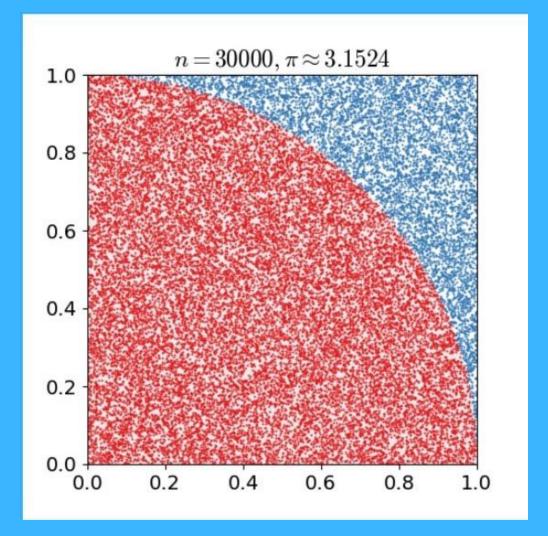


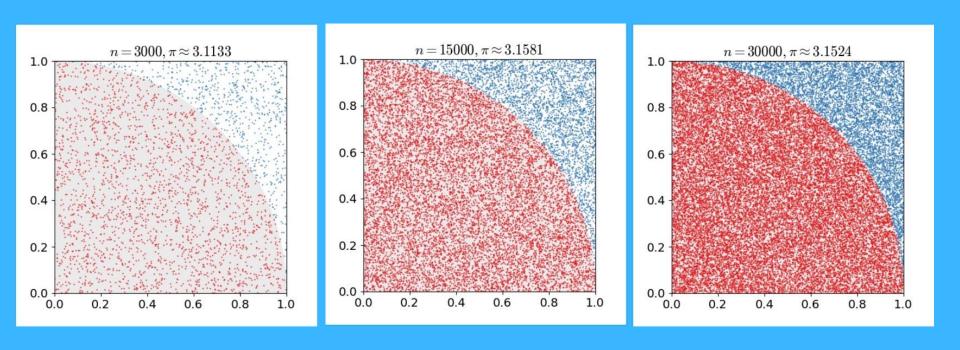
Introduction

Monte Carlo Algorithms





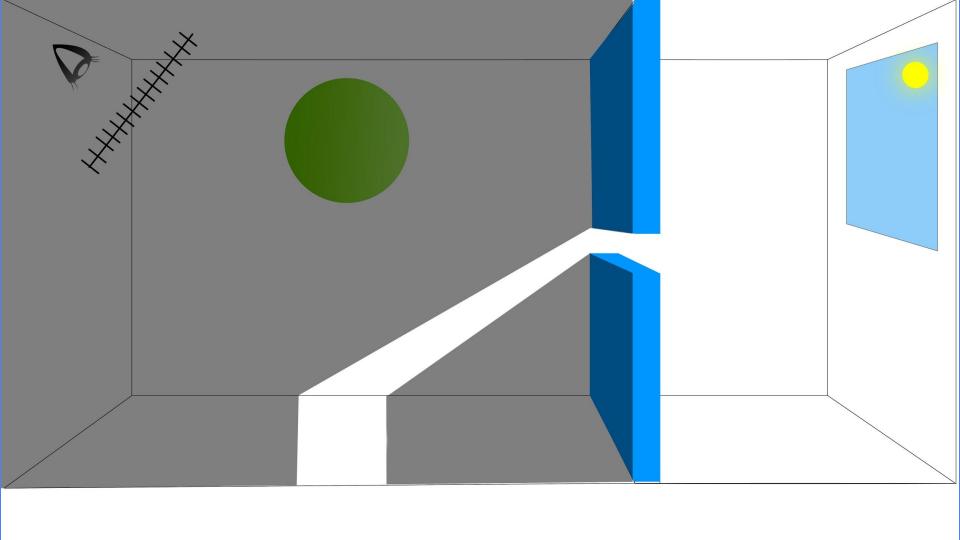


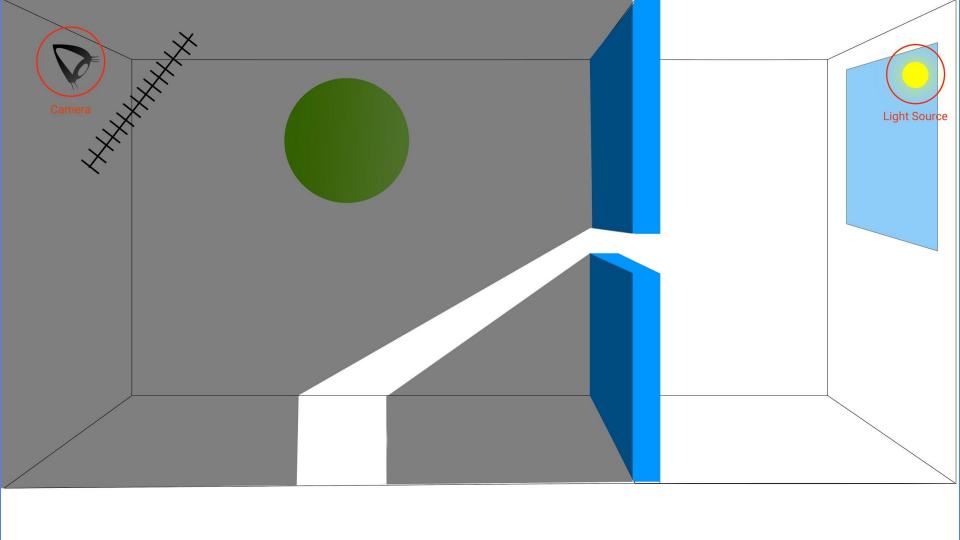


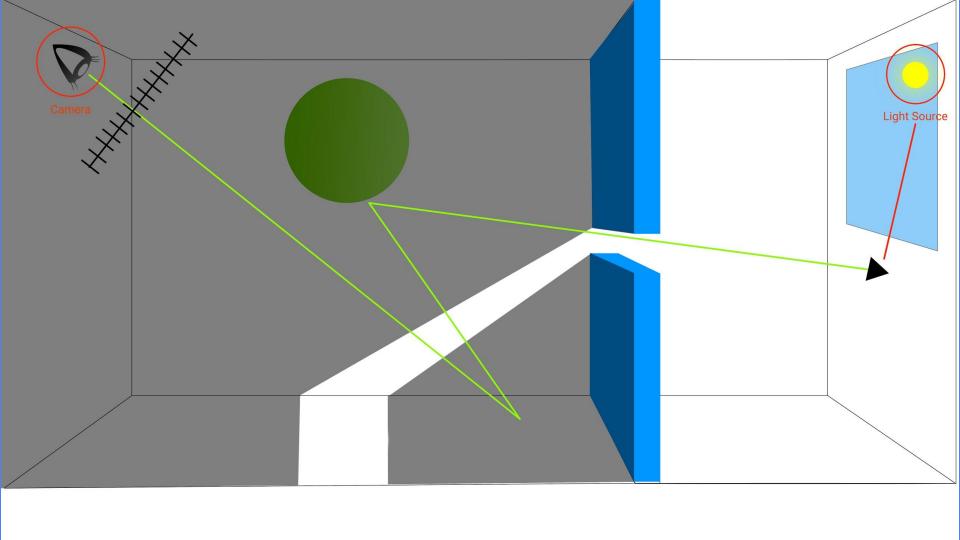
Metropolis Sampling Method

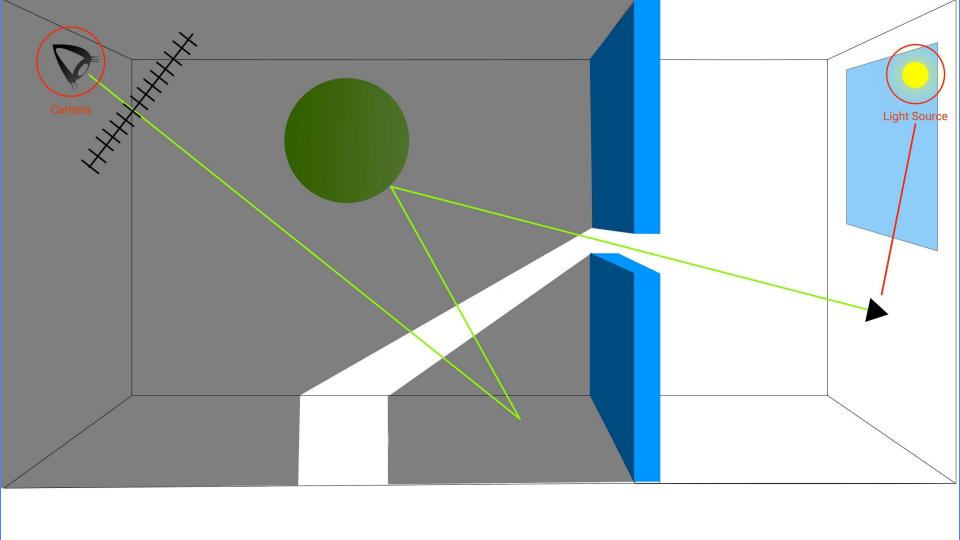
Metropolis Light Transport

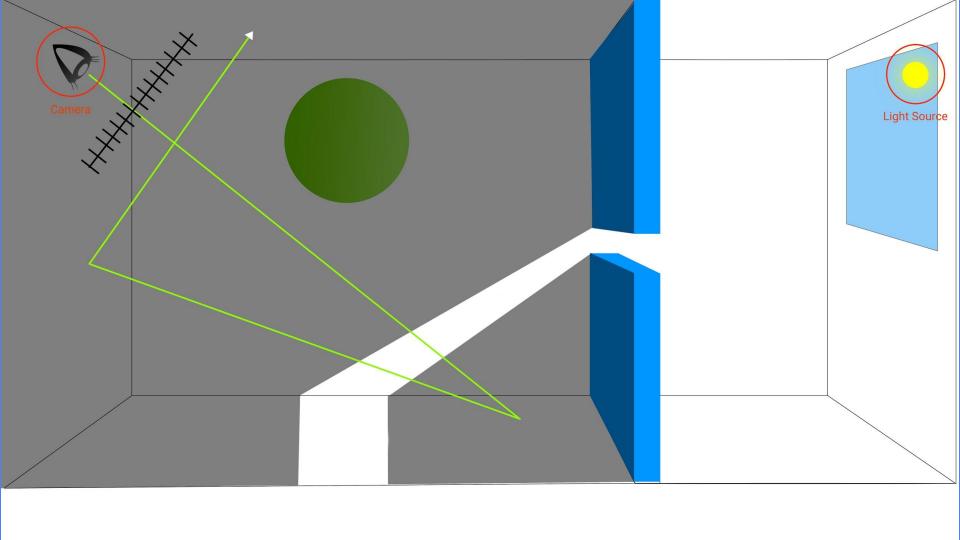
Method Overview

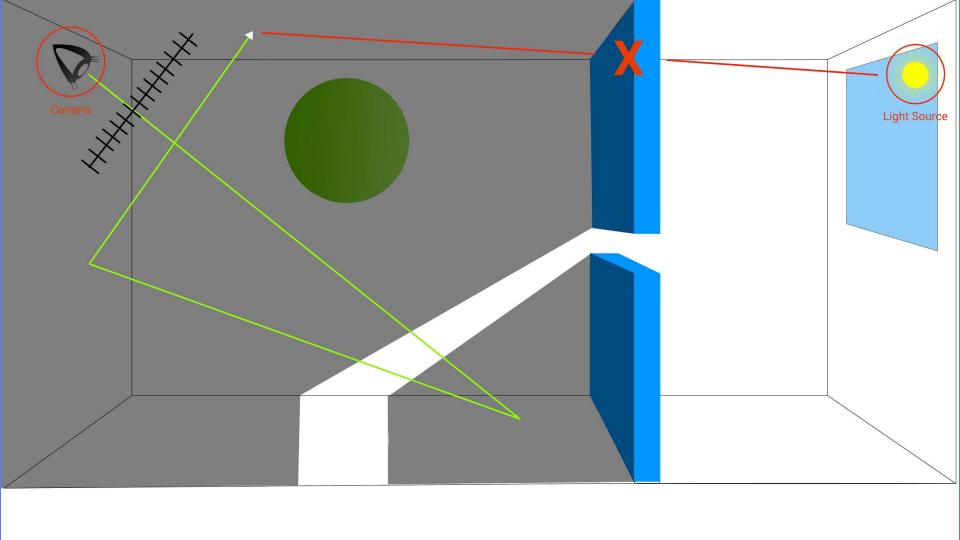












Algorithm

```
\bar{x} \leftarrow \text{InitialPath}()
image ← { array of zeros }
for i \leftarrow 1 to N
      \bar{y} \leftarrow \text{Mutate}(\bar{x})
       a \leftarrow AcceptProb(\bar{y} | \bar{x})
       if Random() < a
              then \bar{x} \leftarrow \bar{y}
       RecordSample(image, \bar{x})
return image
```

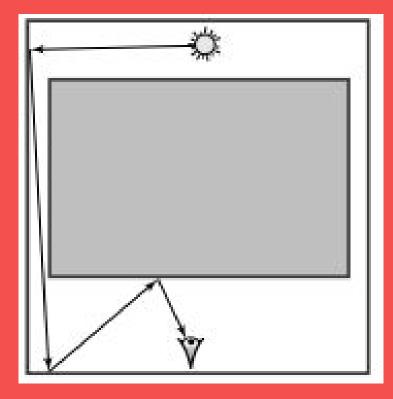
Initialization Phase

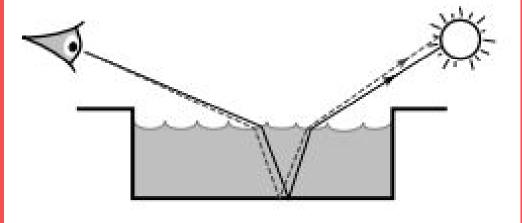
Spectral Sampling

Algorithm: With Color

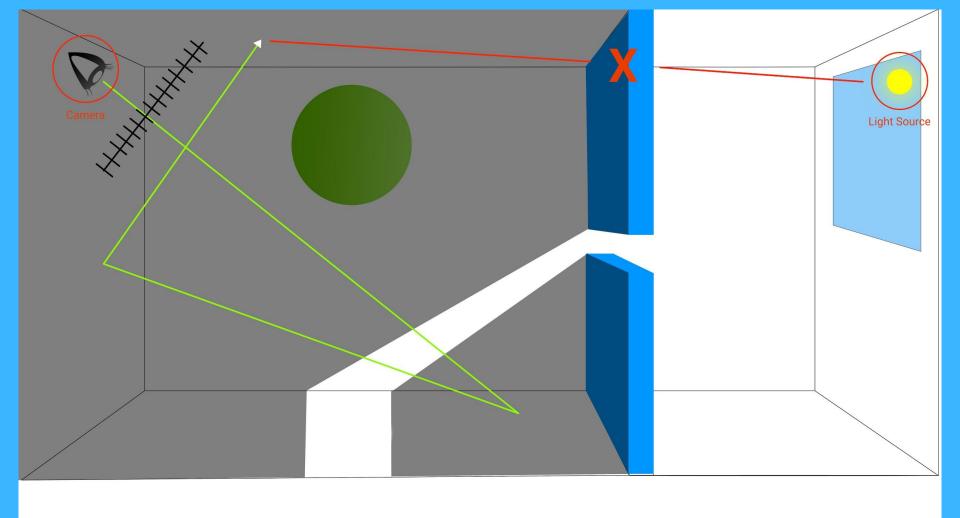
```
\bar{x} \leftarrow \text{InitialPath}()
image ← { array of zeros }
for i \leftarrow 1 to N
     \bar{y} \leftarrow \text{Mutate}(\bar{x})
     xColor = color(\bar{x})
      yColor = color(\bar{y})
      xLum = luminance(xColor)
      yLum = luminance( yColor )
      a \leftarrow AcceptProb(yLum \mid xLum)
     if Random() < a
            \bar{x} \leftarrow \bar{v}
           xColor = yColor
     RecordSample( image , \bar{x}, xColor)
return image
```

The Metropolis **Phase: Mutation** Strategies

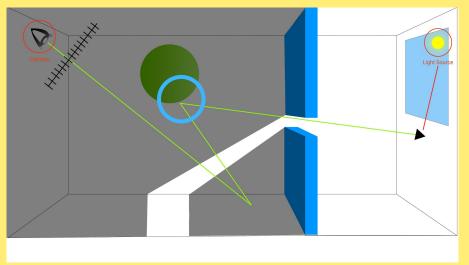


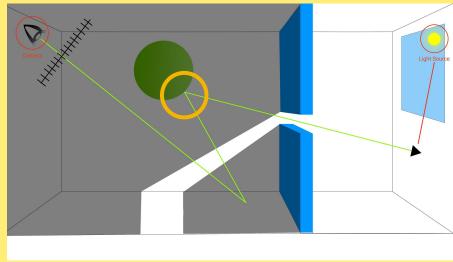


Acceptance Probability

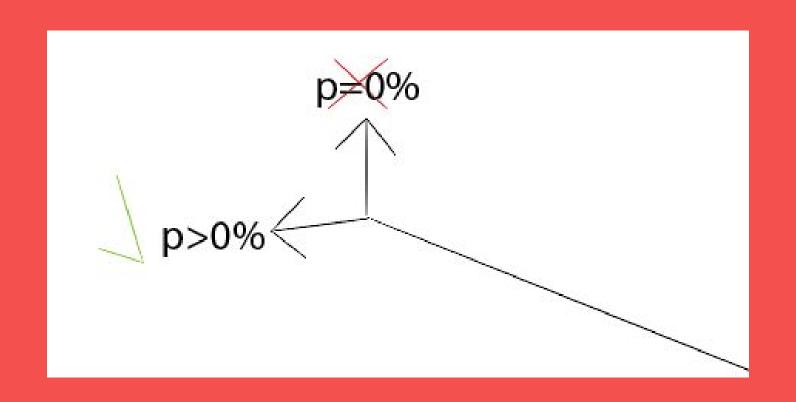


Path Change

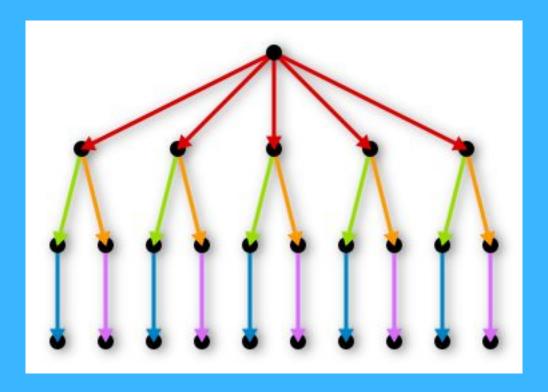




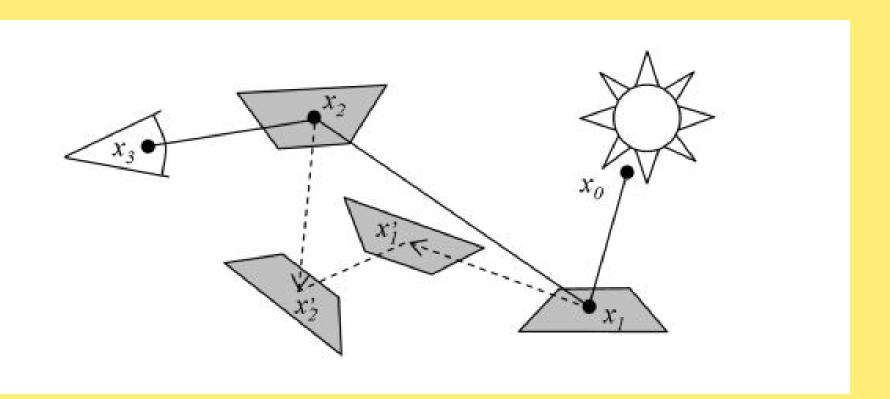
Ergodicity



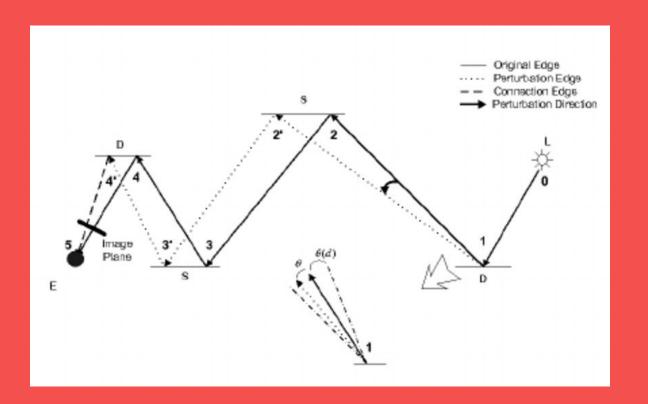
Stratification

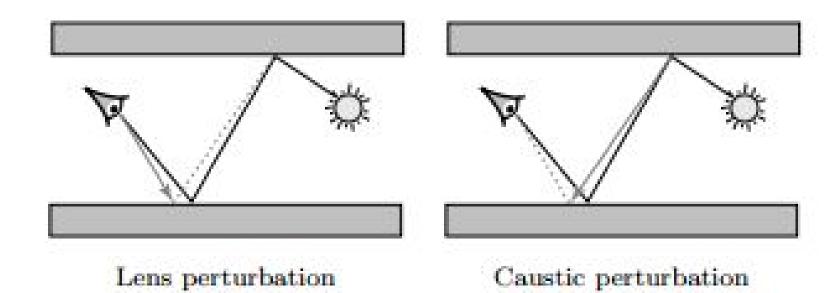


Bidirectional Mutations

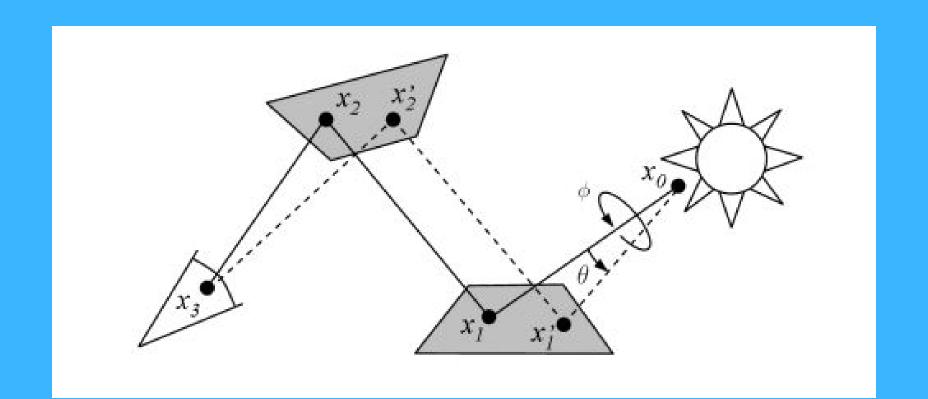


Perturbations





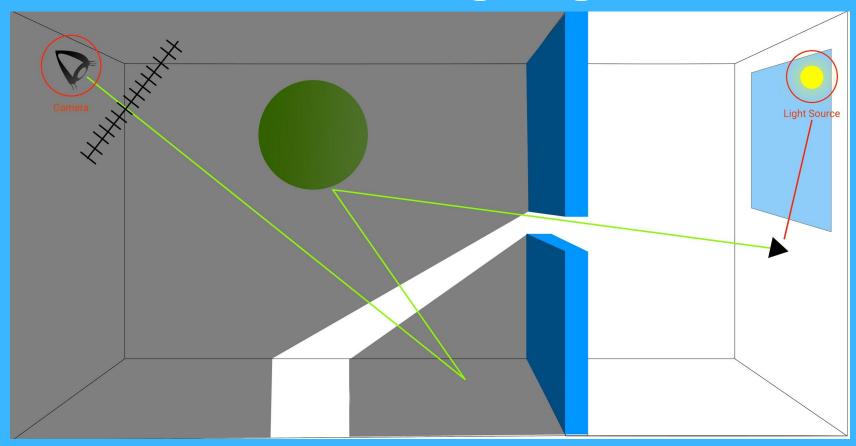
Lens Subpath Mutations



Advantages and Disadvantages of MLT

MLT Use Cases

Indirect Lighting



Caustics





https://en.wikipedia.org/wiki/Caustic_(optics)

Non-Diffuse Surfaces



http://www.neilblevins.com/cg_education/reflection_highlight/reflection_highlight.htm

Method Comparisons







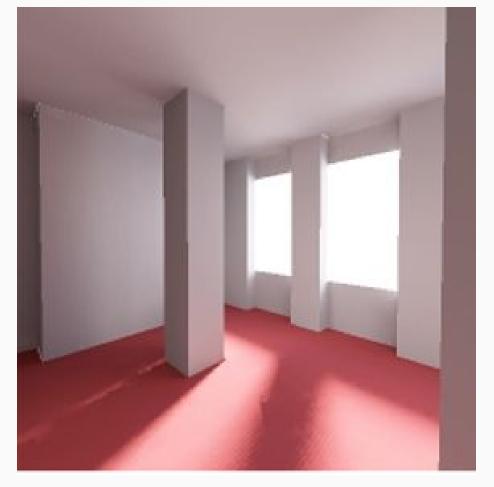


Compared to Ray Tracing



https://courses.cs.washington.edu/courses/cse557/08wi/projects/trace/

Compared to Radiosity



http://csis.pace.edu/~marchese/CG/Lect1/Lecture_1.html

Conclusion

Questions?