

## Phase 7.3 – Statistical Anomaly Detection (Hybrid Approach)

### 7.3.1 Purpose of this Phase

Up to now the system on the **Arduino UNO Q** can:

- Listen to the CAN bus
- Decode ECU voltages via the `harness_demo.dbc`
- Apply **rule-based harness fault detection** in real time
- Raise clear alerts for:
  - Harness A (ECU A only low)
  - Harness B (ECU B only low)
  - Harness C (both ECUs low vs DCDC)

Phase 7.3 adds a **statistical layer on top** of those rules to:

1. Detect **early, subtle drift** before rule thresholds are hit
2. Characterise **trends over time** (which direction and how fast)
3. Lay the groundwork for simple **Remaining Useful Life (RUL-style) reasoning**, without needing heavy ML or cloud compute

This is **not** a full prognostics stack. It's a **hybrid design**: lightweight analytics on the UNO Q, with a clear path to more advanced methods later.

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## 7.3.2 Signals and Derived Quantities

The statistical layer works on the **same decoded signals** as the rules:

- **V\_DCDC** (DCDC\_Output\_Voltage)
- **V\_A** (ECUA\_Supply\_Voltage)
- **V\_B** (ECUB\_Supply\_Voltage)

We reuse the deltas:

- $\Delta A = V\_DCDC - V\_A$
- $\Delta B = V\_DCDC - V\_B$

From these we derive:

- **Level metrics** – current  $\Delta A$ ,  $\Delta B$
- **Smoothed metrics** – filtered versions of  $\Delta A$ ,  $\Delta B$
- **Trend metrics** – rate-of-change of  $\Delta A$ ,  $\Delta B$

These are all cheap to compute and suitable for the UNO Q's Linux environment.

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### 7.3.3 Lightweight Features on the UNO Q

We implement three simple statistical tools:

#### (1) Sliding window mean

Over the last **N samples** (e.g.  $N = 50$  at  $100 \text{ ms} \approx 5 \text{ seconds}$ ):

- $\text{mean\_}\Delta A$  = average of  $\Delta A$  over the window
- $\text{mean\_}\Delta B$  = average of  $\Delta B$  over the window

Purpose:

- Filters out short spikes
- Gives a “local baseline” around which we can measure drift

#### (2) Exponential smoothing (EWMA)

We also maintain an **exponential moving average**:

- $\text{ewma\_}\Delta A \leftarrow \alpha * \Delta A_{\text{now}} + (1 - \alpha) * \text{ewma\_}\Delta A_{\text{prev}}$
- $\text{ewma\_}\Delta B \leftarrow \alpha * \Delta B_{\text{now}} + (1 - \alpha) * \text{ewma\_}\Delta B_{\text{prev}}$

Where  $\alpha$  is a smoothing factor, e.g.:

- $\alpha \approx 0.05 \rightarrow$  strong smoothing, slow response
- $\alpha \approx 0.2 \rightarrow$  faster response, less smoothing

Purpose:

- Stable, low-memory estimate of “underlying” delta
- Robust against noise, still responsive to gradual drift

### (3) Approximate slope (trend)

We estimate a **trend** (rate-of-change) over the window:

$$\begin{aligned}\text{trend\_}\Delta A &\approx (\Delta A_{\text{latest}} - \Delta A_{\text{oldest\_in\_window}}) / \text{window\_duration} \\ \text{trend\_}\Delta B &\approx (\Delta B_{\text{latest}} - \Delta B_{\text{oldest\_in\_window}}) / \text{window\_duration}\end{aligned}$$

For example, if  $\Delta A$  grows from 0.2 V to 0.8 V over 60 seconds:

- $\text{trend\_}\Delta A \approx (0.8 - 0.2) / 60 \approx 0.01 \text{ V/s}$

Purpose:

- Distinguishes:
    - **Sudden jumps** (bad connection, intermittent contact)
    - **Slow monotonic drift** (classic corrosion / resistance growth)
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## 7.3.4 Statistical Anomaly Rules

The **statistical layer does not replace the hard rules**; it augments them.

We define **early warning conditions** such as:

### 1. Drift warning (Harness A example)

“ $\Delta A$  is still below the hard alarm threshold but is **steadily trending up**.”

Concretely:

- $\text{ewma\_}\Delta A > 0.3 \text{ V}$
- $\text{trend\_}\Delta A > 0.002 \text{ V/s}$
- Duration condition: above for  $\geq 30$  seconds

This is logged as:

```
[EARLY][HARNESS_A_DRIFT] ΔA increasing steadily (ewma=...,  
trend=...)
```

## 2. Volatility anomaly

If the short-term standard deviation of  $\Delta A$  or  $\Delta B$  grows:

- `std( $\Delta A_{\text{window}}$ ) >  $\sigma_{\text{threshold}}$`

Interpretation:

- Contact is becoming intermittent
- Loose terminal / vibration / micro-arcing

This can be flagged:

```
[EARLY][HARNESS_A_NOISY] ΔA variance high (std=...)
```

## 3. Multi-node statistical confirmation

We ensure that:

- For Harness A drift:
  - $\Delta A$  trending up
  - $\Delta B$  stable
  - DCDC reasonably stable

So we require, for example:

- `trend_ΔA > drift_min`
- `|trend_ΔB| < drift_tolerance`

- `|trend_V_DCDC| < small_tolerance`

This **reinforces localization**: we only call it a harness issue if the pattern is consistent with the physical model.

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### 7.3.5 Simple RUL-Style Estimation (Conceptual)

While not a full RUL engine, we can derive a **rough Remaining Useful Life style metric** from:

- Current delta:  $\Delta$
- Trend: `trend_Δ`

If we know:

- Soft limit: `Δ_warn` (e.g. 0.5 V)
- Hard limit: `Δ_fail` (e.g. 1.5 V)

When `trend_Δ > 0` (degradation worsening), we can approximate:

```
time_to_warn ≈ max(0, (Δ_warn - current_Δ) / trend_Δ)
time_to_fail ≈ max(0, (Δ_fail - current_Δ) / trend_Δ)
```

We then present it to the logs as **qualitative RUL**:

- `> 60 min` → “Low risk”
- `10–60 min` → “Plan maintenance”
- `< 10 min` → “High risk – intervention soon”

This is intentionally **coarse**, but it gives a taste of:

“Not only do we know you have a problem, we have an idea of how fast it is getting worse.”

We **do not** hard-wire this into safety decisions; it is an **advisory metric**.

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## 7.3.6 Integration with the Existing Rule Engine

The runtime now has **three layers**:

1. **Raw decode layer**

- From CAN frames → ECU voltages via DBC
- Already implemented and validated

2. **Rule-based fault layer**

- Hard logical conditions
- Distinguishes Harness A/B/C
- emits `[ALERT][HARNESS_X] ...`

3. **Statistical layer (this phase)**

- Monitors drift, volatility, trend
- Issues early warnings and RUL-style estimates
- emits `[EARLY][HARNESS_X_DRIFT] ...` and optionally RUL text

The **key design decision**:

Rules always remain the **primary functional diagnostic**,  
statistics act as an **early warning and context provider**.

This keeps the system explainable and robust.

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## 7.3.7 Resource Constraints and UNO Q Considerations

Our design is conscious of the UNO Q environment:

- **CPU:** simple arithmetic, no heavy matrix operations
- **RAM:** only small sliding windows (e.g. 50–100 samples) per signal
- **Storage:** all statistics computed in real-time; nothing stored long-term unless we choose to log them

We avoid:

- Large numpy/scipy stacks
- Heavy ML frameworks
- Compiled C extensions for this phase

This keeps deployment and debugging on the UNO Q straightforward.

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## 7.3.8 Limitations and Future Extension Path

**Limitations of the current approach:**

- Thresholds and windows are **hand-tuned**, not data-driven
- RUL estimates are **linear extrapolations**, not physically derived models
- Environmental effects (temperature, load) are not yet modeled

**Future extensions (if project extends beyond current scope):**

- Use real fleet data to:
  - learn baseline distributions of  $\Delta A$ ,  $\Delta B$
  - calibrate trend thresholds automatically



- Introduce simple **Bayesian** or **Kalman** filters for better noise handling
  - Add **temperature and load** as contextual features
  - Move heavy training to the cloud, keep only lightweight inference on the UNO Q
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## 7.3.9 Summary and Link to Next Phases

By the end of **Phase 7.3**, the system can:

- Detect harness issues through **deterministic rules** (Phase 7.2)
- Monitor **drift and volatility** statistically in real time
- Provide **early warnings** and **rough RUL-style** indications
- Still run entirely on the **UNO Q** with modest resource usage

### Next Step: Phase 7.4 – Edge vs Off-Board Trade-Offs

In Phase 7.4 we will document:

- Which logic must run **on the UNO Q** (safety, latency)
- Which analytics can be **offloaded** (detailed RUL, model refinement)
- What data to log and send off-board (CAN snippets, deltas, trends, alerts)
- How this balances:
  - bandwidth
  - cost
  - updatability
  - cybersecurity