

Calculate the initial conditions for the first stage  $\text{Derivative}[1][m][x] == -u_*$

```
In[1]:= Clear[all];
      |очистить
uu = List[-u_*, +u_*, -u_*];
      |список

In[3]:= sol1 =
      Flatten[Simplify[DSolve[{θ'[x] == ω[x], ω'[x] == m[x] + θ[x], m'[x] == uu[[1]], θ[0] == 1,
      |уплостить |упростить |решить дифференциальные уравнения
      ω[0] == Ω₀, m[0] == 0}, {θ[x], ω[x], m[x]}, x], Element[x, Reals]]]
      |принадлежи... |множество действительных чисел

Out[3]= {m[x] → -x u_*, θ[x] → 1/2 e^{-x} (1 + e^{2x} + (-1 + e^{2x}) Ω₀ + (1 - e^{2x} + 2 e^x x) u_*),
      ω[x] → 1/2 e^{-x} ((1 + e^{2x}) Ω₀ - (-1 + e^x) (-1 - e^x + (-1 + e^x) u_*))}
```

```
In[4]:= initForStage2 =
      {m[x] /. sol1[[1]] /. x → τ₁, θ[x] /. sol1[[2]] /. x → τ₁, ω[x] /. sol1[[3]] /. x → τ₁}

Out[4]= {-τ₁ u_*, 1/2 e^{-τ₁} (1 + e^{2τ₁} + (-1 + e^{2τ₁}) Ω₀ + (1 - e^{2τ₁} + 2 e^{τ₁} τ₁) u_*),
      1/2 e^{-τ₁} ((1 + e^{2τ₁}) Ω₀ - (-1 + e^{τ₁}) (-1 - e^{τ₁} + (-1 + e^{τ₁}) u_*))}
```

Calculate the initial conditions for the second stage  $m'[x] == u$

```
In[5]:= sol2 =
      Flatten[Simplify[DSolve[{θ'[x] == ω[x], ω'[x] == m[x] + θ[x], m'[x] == uu[[2]], θ[τ₁] ==
      |уплостить |упростить |решить дифференциальные уравнения
      initForStage2[[2]], ω[τ₁] == initForStage2[[3]], m[τ₁] == initForStage2[[1]]},
      {θ[x], ω[x], m[x]}, x], Element[{τ₁, τ₂, τ_f, x}, Reals]]]
      |принадлежит множеству |множество действительных чисел

Out[5]= {m[x] → (x - 2 τ₁) u_*,
      θ[x] → 1/2 (e^{-x} + e^x + (-e^{-x} + e^x) Ω₀ + (e^{-x} - e^x + 2 e^{x-τ₁} - 2 e^{-x+τ₁} - 2 x + 4 τ₁) u_*),
      ω[x] → 1/2 e^{-x-τ₁} (e^{τ₁} (-1 + e^{2x}) + e^{τ₁} (1 + e^{2x}) Ω₀ - (-2 e^{2x} + e^{τ₁} - 2 e^{2τ₁} + 2 e^{x+τ₁} + e^{2x+τ₁}) u_*)}
```

Calculate the initial conditions for the third stage  $m'[x] == -u$

```
In[6]:= sol3 = Simplify[DSolve[
      |упростить |решить дифференциальные уравнения
      {θ'[x] == ω[x], ω'[x] == m[x] + θ[x], m'[x] == uu[[3]], θ[τ_f] == 0, ω[τ_f] == 0, m[τ_f] == 0},
      {θ[x], ω[x], m[x]}, x], Element[{τ₁, τ₂, τ_f, x}, Reals]] // Flatten
      |принадлежит множеству |множество ... |уплостить

Out[6]= {m[x] → (-x + τ_f) u_*, θ[x] → 1/2 (-e^{x-τ_f} + e^{-x+τ_f} + 2 x - 2 τ_f) u_*, ω[x] → -1/2 e^{-x-τ_f} (e^x - e^{τ_f})^2 u_*}
```

```

In[7]:= linkingStage2 = {m[x] /. sol2[[1]] /. x → τ2,
  ω[x] /. sol2[[2]] /. x → τ2 // Simplify, ω[x] /. sol2[[3]] /. x → τ2 // Simplify}
                                     упростить                                     упростить

Out[7]= { (-2 τ1 + τ2) u*,
  1/2 (e-τ2 + eτ2 + (-e-τ2 + eτ2) Ω0 + (-2 eτ1-τ2 + e-τ2 - eτ2 + 2 e-τ1+τ2 + 4 τ1 - 2 τ2) u*),
  1/2 e-τ1-τ2 (eτ1 (-1 + e2 τ2) + eτ1 (1 + e2 τ2) Ω0 - (eτ1 - 2 e2 τ1 - 2 e2 τ2 + 2 eτ1+τ2 + eτ1+2 τ2) u*) }

In[8]:= linkingStage3 = {m[x] /. sol3[[1]] /. x → τ2,
  ω[x] /. sol3[[2]] /. x → τ2 // Simplify, ω[x] /. sol3[[3]] /. x → τ2 // Simplify}
                                     упростить                                     упростить

Out[8]= { (-τ2 + τf) u*, 1/2 (-eτ2-τf + e-τ2+τf + 2 τ2 - 2 τf) u*, -1/2 e-τ2-τf (eτ2 - eτf)2 u* }

In[9]:= first = (linkingStage2[[1]] - linkingStage3[[1]] == 0 // Simplify)
                                     упростить

Out[9]= (2 τ1 - 2 τ2 + τf) u* == 0

```

Replace vars  $e^{\tau_1} == x$ ,  $e^{\tau_2} == y$ ,  $e^{\frac{\tau_f}{2}} == z$ .

```

In[10]:= first1 = z == y/x // FullSimplify
                                     упростить в полно

first1eq = first1

Out[10]= z == y/x

Out[11]= z == y/x

In[12]:= second = (linkingStage2[[2]] - linkingStage3[[2]] == 0 // Expand)
                                     раскрыть

Out[12]= e-τ2/2 + eτ2/2 - 1/2 e-τ2 Ω0 + 1/2 eτ2 Ω0 - eτ1-τ2 u* + 1/2 e-τ2 u* -
  1/2 eτ2 u* + e-τ1+τ2 u* + 1/2 eτ2-τf u* - 1/2 e-τ2+τf u* + 2 τ1 u* - 2 τ2 u* + τf u* == 0

In[13]:= Collect[second /. {e2 τ2 → y2, eτ2 → y, eτ1 → x, e-τ2 → 1/y, eτf → z2,
  τf → -2 τ1 + 2 τ2, e-τ1+τ2 → y/x, eτ1-τ2 → x/y} // Simplify, {eτ2, eτ1}, Simplify]
                                     упростить                                     упростить

Out[13]= -e2 τ1-τ2 u* + e-2 τ1+τ2 u* + (x - x y2) Ω0 + (2 x2 - 2 y2 + x (-1 + y2)) u* / (x y) == 1/y + y

```

Made handle substitutie for  $-e^{2 \tau_1 - \tau_2} u_* + e^{-2 \tau_1 + \tau_2} u_*$

In[14]:= second1 =

$$\frac{-x^2}{y} u_* + \frac{y}{x^2} u_* + \frac{(x - x y^2) \Omega_0 + (2 x^2 - 2 y^2 + x (-1 + y^2)) u_*}{x y} = \frac{1}{y} + y // \text{FullSimplify};$$

[упростить в полном](#)

Expand[second1 // FullSimplify]

[раскрыть скобки](#) [упростить в полном объеме](#)

Together[second1]

[собрать вместе](#)

$$\text{second1} = (x^2 + x^2 y^2 - x^2 \Omega_0 + x^2 y^2 \Omega_0 + x^2 u_* - 2 x^3 u_* + x^4 u_* - y^2 u_* + 2 x y^2 u_* - x^2 y^2 u_*)$$

$$\text{second1eq} = (\text{second1} == 0);$$

$$\text{Out[15]} = \frac{1}{y} + y - \frac{\Omega_0}{y} + y \Omega_0 + \frac{u_*}{y} - \frac{2 x u_*}{y} + \frac{x^2 u_*}{y} - y u_* - \frac{y u_*}{x^2} + \frac{2 y u_*}{x} == 0$$

$$\text{Out[16]} = \frac{x^2 + x^2 y^2 - x^2 \Omega_0 + x^2 y^2 \Omega_0 + x^2 u_* - 2 x^3 u_* + x^4 u_* - y^2 u_* + 2 x y^2 u_* - x^2 y^2 u_*}{x^2 y} == 0$$

$$\text{Out[17]} = x^2 + x^2 y^2 - x^2 \Omega_0 + x^2 y^2 \Omega_0 + x^2 u_* - 2 x^3 u_* + x^4 u_* - y^2 u_* + 2 x y^2 u_* - x^2 y^2 u_*$$

In[19]:= third = (linkingStage2[[3]] - linkingStage3[[3]] == 0 // Expand);

[раскрыть скобки](#)

$$\text{Collect}[third /. \{e^{\tau_2} \rightarrow y^2, e^{\tau_2} \rightarrow y, e^{\tau_1} \rightarrow x, e^{-\tau_2} \rightarrow \frac{1}{y}, e^{\tau_f} \rightarrow z^2,$$

[сгруппировать](#)

$$\tau_f \rightarrow -2 \tau_1 + 2 \tau_2, e^{-\tau_1 + \tau_2} \rightarrow \frac{y}{x}, e^{\tau_1 - \tau_2} \rightarrow \frac{x}{y} \} // \text{Simplify}, \{e^{\tau_2}, e^{\tau_1}\}, \text{Simplify}]$$

[упростить](#) [упростить](#)

$$\text{Out[20]} = e^{2 \tau_1 - \tau_2} u_* + e^{-2 \tau_1 + \tau_2} u_* + \frac{y^2 + (1 + y^2) \Omega_0 + (-1 + 2 x - 4 y - y^2 + \frac{2 y^2}{x}) u_*}{y} = \frac{1}{y}$$

handle transform  $e^{2 \tau_1 - \tau_2} u_* + e^{-2 \tau_1 + \tau_2} u_*$

$$\text{In[21]} := \text{third1} = \frac{x^2}{y} u_* + \frac{y}{x^2} u_* + \frac{y^2 + (1 + y^2) \Omega_0 + (-1 + 2 x - 4 y - y^2 + \frac{2 y^2}{x}) u_*}{y} = \frac{1}{y} // \text{FullSimplify};$$

[упростить в полном](#)

Expand[third1 // FullSimplify]

[раскрыть скобки](#) [упростить в полном объеме](#)

$$\text{Out[22]} = -\frac{x}{y} + x y + \frac{x \Omega_0}{y} + x y \Omega_0 - 4 x u_* - \frac{x u_*}{y} + \frac{2 x^2 u_*}{y} + \frac{x^3 u_*}{y} + 2 y u_* + \frac{y u_*}{x} - x y u_* == 0$$

```

In[23]:= Together[third1];
собрать вместе
third1 =
  
$$(-x^2 + x^2 y^2 + x^2 \Omega_0 + x^2 y^2 \Omega_0 - x^2 u_* + 2 x^3 u_* + x^4 u_* - 4 x^2 y u_* + y^2 u_* + 2 x y^2 u_* - x^2 y^2 u_*)$$
;
third1eq = (third1 == 0)
Expand[third1 /. {y → z * x} // FullSimplify]
раскрыть скобки упростить в полном объёме
third1 = third1 /. {y → z * x} // FullSimplify;
упростить в полном объёме
Expand[second1 /. {y → z * x} // FullSimplify]
раскрыть скобки упростить в полном объёме
second1 = second1 /. {y → z * x} // FullSimplify;
упростить в полном объёме
lasEq = second1 + third1 == 0 // FullSimplify
упростить в полном объёме
second1 - third1 == 0 // FullSimplify
упростить в полном объёме
xSol = Solve[(1 -  $\Omega_0$  + (-1 + 2 x - z) (-1 + z)  $u_*$ ) == 0, {x}] // Flatten
решить уравнения уплостить
Collect[lasEq /. {x → xSol[[1]][[2]]} // Simplify, {z}, Simplify]
сгруппировать упростить упростить
z1final = Collect[(-1 +  $\Omega_0$  + (-1 + z2)  $u_*$ ) == 0, z];
сгруппировать
z2final = Collect[(z2 - z2  $\Omega_0^2$  - (-1 + z4)  $u_*$  - (-1 + z2)2  $\Omega_0 u_*$  + (-1 + z)4  $u_*^2$ ) == 0, z];
сгруппировать

```

$$\text{Out[25]} = -x^2 + x^2 y^2 + x^2 \Omega_0 + x^2 y^2 \Omega_0 - x^2 u_* + 2 x^3 u_* + x^4 u_* - 4 x^2 y u_* + y^2 u_* + 2 x y^2 u_* - x^2 y^2 u_* == 0$$

$$\text{Out[26]} = -x^2 + x^4 z^2 + x^2 \Omega_0 + x^4 z^2 \Omega_0 - x^2 u_* + 2 x^3 u_* + x^4 u_* - 4 x^3 z u_* + x^2 z^2 u_* + 2 x^3 z^2 u_* - x^4 z^2 u_*$$

$$\text{Out[28]} = x^2 + x^4 z^2 - x^2 \Omega_0 + x^4 z^2 \Omega_0 + x^2 u_* - 2 x^3 u_* + x^4 u_* - x^2 z^2 u_* + 2 x^3 z^2 u_* - x^4 z^2 u_*$$

$$\text{Out[30]} = x (x z^2 (1 + \Omega_0) - (-1 + z) (x + (-2 + x) z) u_*) == 0$$

$$\text{Out[31]} = x (1 - \Omega_0 + (-1 + 2 x - z) (-1 + z) u_*) == 0$$


$$\text{Out[32]} = \left\{ x \rightarrow \frac{-1 + \Omega_0 - u_* + z^2 u_*}{2 (-1 + z) u_*} \right\}$$

$$\text{Out[33]} = \frac{(-1 + \Omega_0 + (-1 + z^2) u_*) (z^2 - z^2 \Omega_0^2 - (-1 + z^4) u_* - (-1 + z^2)^2 \Omega_0 u_* + (-1 + z)^4 u_*^2)}{(-1 + z) u_*} == 0$$

## Make Numeric solution

```
In[36]:= t_* = 0.174; ω_0 = 0.149;
ϕ_0 = 0.021;
u_* = -0.63;
Ω_0 =  $\frac{t_*}{\phi_0} \omega_0$ ;
Ω_0 base = Ω_0;
Print["Ω_0=", Ω_0];
[печатаТЬ]
Ω_0=1.23457
```

```
In[38]:= Ω_0 = Ω_0 base;
roots = NSolve[third1eq&&second1eq&&first1eq, {x, y, z}, Reals]
[численное решение уравнений] [множестВ]
```

 **NSolve** : NSolve was unable to solve the system with inexact coefficients. The answer was obtained by solving a corresponding exact system and numericizing the result.

```
Out[39]= { {x → 1.73191 × 10-17, y → -2.02888 × 10-17, z → -1.17147},
{ x → 2.1933 × 10-16, y → 2.56938 × 10-16, z → 1.17147},
{ x → 0.0811281, y → 0.0960679, z → 1.18415},
{ x → 0.952909, y → 0.324848, z → 0.340902} }
```

## In[40]:= Make Algebraic solution

```
Out[40]= Algebraic Make solution
```

```
In[41]:= Solve[z1final, z, Reals] ~Join~ Solve[z2final, z, Reals] // Flatten
[решить уравнения] [множес... [coe... [решить уравнения] [множеств... [уплостить]
2 * Log[1.17]
[натуральный логарифм]
```

```
Out[41]= { z → -1.17147, z → 1.17147, z → 0.340902, z → 1.18415 }
```

```
Out[42]= 0.314007
```

```
In[43]:= τ_1 = Log[roots[[1]][[2]]];
[натуральный логарифм]
τ_2 = Log[roots[[1]][[2]][[2]]];
[натуральный логарифм]
τ_f = 2 * Log[roots[[1]][[3]][[2]]];
[натуральный логарифм]
Print["τ1=", τ_1, "; τ2=", τ_2, "; τf=", τ_f]
[печатаТЬ]
τ1=-38.5947; τ2=-38.4365 + 3.14159 i; τf=0.316514 + 6.28319 i
```

```

In[45]:=  $\tau_1 = \text{Log}[\text{roots}[1][1][2]]$ ;
          [натуральный логарифм]
 $\tau_2 = \text{Log}[\text{roots}[1][2][2]]$ ;  $\tau_f = 2 * \text{Log}[\text{roots}[1][3][2]]$ ;
          [натуральный логарифм]          [натуральный логарифм]
pw1m = Piecewise[{{sol1[1][2], x > 0 && x ≤  $\tau_1$ },
                  [кусочно-заданная функция]
                  {sol2[1][2], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[1][2], x >  $\tau_2$  && x ≤  $\tau_f$ }}];
pw10 = Piecewise[{{sol1[2][2], x > 0 && x ≤  $\tau_1$ },
                  [кусочно-заданная функция]
                  {sol2[2][2], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[2][2], x >  $\tau_2$  && x ≤  $\tau_f$ }}];
pw1w = Piecewise[{{sol1[3][2], x > 0 && x ≤  $\tau_1$ },
                  [кусочно-заданная функция]
                  {sol2[3][2], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[3][2], x >  $\tau_2$  && x ≤  $\tau_f$ }}];

```

... LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... LessEqual : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

... LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... LessEqual : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

$$\text{Out[47]} = \begin{cases} \frac{1}{2} e^{-x} (1 + e^{2x} + 1.23457 (-1 + e^{2x}) - 0.63 (1 - e^{2x} + 2 e^x x)) & x > 0 \text{ \& \& } x \leq -38.5947 \\ \frac{1}{2} (e^{-x} + e^x + 1.23457 (-e^{-x} + e^x) - 0.63 (-154.379 - 2 e^{-38.5947-x} + e^{-x} - e^x + 2 e^{38.5947+x} - 2 x)) & x > -38.5947 \text{ \& \& } x \leq -38.4365 + 3.14159 i \\ -0.315 ((-0.633028 - 12.5664 i) + e^{(0.316514+6.28319 i)-x} - e^{(-0.316514-6.28319 i)+x} + 2 x)) & x > -38.4365 + 3.14159 i \text{ \& \& } x \leq 0.316514 + 6.28319 i \\ 0 & \text{True} \end{cases}$$

... LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... LessEqual : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

$$\text{Out[48]} = \begin{cases} \frac{1}{2} e^{-x} (1.23457 (1 + e^{2x}) - (-1 + e^x) (-1 - e^x - 0.63 (-1 + e^x))) & x > 0 \text{ \& \& } x \leq -38.5947 \\ \frac{1}{2} e^{38.5947-x} (1.73191 \times 10^{-17} (-1 + e^{2x}) + 2.13817 \times 10^{-17} (1 + e^{2x}) + 0.63 (1.73191 \times 10^{-17} + 2 e^{-38.5947+x} - 2 e^{2x} + e^{-38.5947+2x})) & x > -38.5947 \text{ \& \& } x \leq -38.4365 + 3.14159 i \\ 0.315 e^{(-0.316514-6.28319 i)-x} ((-1.37234 + 3.36125 \times 10^{-16} i) + e^x)^2 & x > -38.4365 + 3.14159 i \text{ \& \& } x \leq 0.316514 + 6.28319 i \\ 0 & \text{True} \end{cases}$$

In[49]:=  $\Omega_0 = 1.3 \Omega_0 \text{ base}$ ; roots = NSolve[third1 && second1 && first1, {x, y, z}, Reals]  
[численное решение уравнений] [множеств]

$\tau_1 = \text{Log}[\text{roots}[[1]][[2]]];$   
[натуральный логарифм]

$\tau_2 = \text{Log}[\text{roots}[[1]][[2]]]; \tau_f = 2 * \text{Log}[\text{roots}[[1]][[3]][[2]]];$   
[натуральный логарифм] [натуральный логарифм]

pw13m = Piecewise[{{sol1[[1]][[2]], x > 0 && x ≤  $\tau_1$ },  
[кусочно-заданная функция]

{sol2[[1]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[1]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}];

pw13θ = Piecewise[{{sol1[[2]][[2]], x > 0 && x ≤  $\tau_1$ },  
[кусочно-заданная функция]

{sol2[[2]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[2]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}]

pw13ω = Piecewise[{{sol1[[3]][[2]], x > 0 && x ≤  $\tau_1$ },  
[кусочно-заданная функция]

{sol2[[3]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[3]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}]

... NSolve :

$$x^2 (-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + \text{Times}[\llbracket 2 \rrbracket]))) \&\& x^2 (1 + x^2 z^2 + 0.63 (-1 + z) x)^2 (-1 + z^2) + 1.60494 (-1 + x^2 z^2) \&\& z = \frac{y}{x} \text{ is not a}$$

quantified system of equations and inequalities.

Out[49]= NSolve[ $x^2 (-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))) \&\&$

$$x^2 (1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.60494 (-1 + x^2 z^2)) \&\& z = \frac{y}{x}, \{x, y, z\}, \mathbb{R}]$$

$$\frac{1}{2} e^{-x} (1 + e^{2x} + 1.60494 (-1 + e^{2x}) - 0.63 (1 - e^{2x} + 2 e^x x)) \quad x > 0 \&\& x \leq \text{Log}[-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))] ]$$

$$\frac{1}{2} (e^{-x} + e^x + 1.60494 (-e^{-x} + e^x) - 0.63 (e^{-x} - e^x - 2x + (2e^x) / (-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))) - \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.60494 (-1 + x^2 z^2)]) \&\& x \leq \text{Log}[-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))] ] \&\& x \leq \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.60494 (-1 + x^2 z^2)] ]$$

$$\text{Out[52]=} \left\{ \begin{array}{l} 2 e^{-x} (-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))) + 4 \text{Log}[-1 + x^2 z^2 + 1.60494 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))] ] \end{array} \right.$$

$$-0.315 \left( 2x - \frac{e^x x^2}{y^2} + \frac{e^{-x} y^2}{x^2} - 4 \text{Log}\left[\frac{y}{x}\right] \right) \quad x > \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.60494 (-1 + x^2 z^2)] \&\& x \leq 2 \text{Log}\left[\frac{y}{x}\right]$$

0

True

$$\frac{1}{2} e^{-x} \left( 1.60494 \left( 1 + e^{2x} \right) - \left( -1 + e^x \right) \left( -1 - e^x - 0.63 \left( -1 + e^x \right) \right) \right)$$

$$\left( e^{-x} \left( \left( -1 + e^{2x} \right) \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + 1.60494 \left( 1 + e^{2x} \right) \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + 0.63 \left( -1 - 2 e^{2x} + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) + 2 e^x \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + e^{2x} \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) \right) - 2 \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right)^2 \right) \right) /$$

$$\left( 2 \left( -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) \right)$$

$$\frac{0.315 e^{-x} x^2 \left( e^x - \frac{y^2}{x^2} \right)^2}{y^2}$$

0

$$x > 0 \&\& x \leq \text{Log} \left[ -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right]$$

$$x > \text{Log} \left[ -1 + x^2 z^2 + 1.60494 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right] \&\& x \leq \text{Log} \left[ 1 + x^2 z^2 + 0.63 \left( -1 + x \right)^2 \left( -1 + z^2 \right) + 1.60494 \left( -1 + x^2 z^2 \right) \right]$$

$$x > \text{Log} \left[ 1 + x^2 z^2 + 0.63 \left( -1 + x \right)^2 \left( -1 + z^2 \right) + 1.60494 \left( -1 + x^2 z^2 \right) \right] \&\& x \leq 2 \text{Log} \left[ \frac{y}{x} \right]$$

True



In[54]:=  $\Omega_0 = 0.7 \Omega_0 \text{ base};$  roots = NSolve[third1 && second1 && first1, {x, y, z}, Reals]  
численное решение уравнений множества

$\tau_1 = \text{Log}[\text{roots}[[1]][[2]]];$   
натуральный логарифм

$\tau_2 = \text{Log}[\text{roots}[[1]][[2]][[2]]];$   $\tau_f = 2 * \text{Log}[\text{roots}[[1]][[3]][[2]]];$   
натуральный логарифм натуральный логарифм

pw07m = Piecewise[{{sol1[[1]][[2]], x > 0 && x ≤  $\tau_1$ },  
кусочно-заданная функция

{sol2[[1]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[1]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}];

pw07θ = Piecewise[{{sol1[[2]][[2]], x > 0 && x ≤  $\tau_1$ },  
кусочно-заданная функция

{sol2[[2]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[2]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}]

pw07ω = Piecewise[{{sol1[[3]][[2]], x > 0 && x ≤  $\tau_1$ },  
кусочно-заданная функция

{sol2[[3]][[2]], x >  $\tau_1$  && x ≤  $\tau_2$ }, {sol3[[3]][[2]], x >  $\tau_2$  && x ≤  $\tau_f$ }}]

NSolve :  $x^2 (-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + \text{Times}[\llbracket 2 \rrbracket \rrbracket])) \&\& x^2 (1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.12346 (-1 + x^2 z^2)) \&\& z = \frac{y}{x}, \{x, y, z\}, \mathbb{R}$   
 equations and inequalities.

Out[54]= NSolve[ $x^2 (-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z)) \&\&$   
 $x^2 (1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.12346 (-1 + x^2 z^2)) \&\& z = \frac{y}{x}, \{x, y, z\}, \mathbb{R}]$

$\frac{1}{2} e^{-x} (1 + e^{2x} + 1.12346 (-1 + e^{2x}) - 0.63 (1 - e^{2x} + 2 e^x x))$   $x > 0 \&\& x \leq \text{Log}[-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))]$

$\frac{1}{2} (e^{-x} + e^x + 1.12346 (-e^{-x} + e^x) - 0.63 (e^{-x} - e^x - 2 x + (2 e^x) / (-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z)) \&\& x \leq \text{Log}[-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))]) \&\& x \leq \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.12346 (-1 + x^2 z^2)])$

Out[57]= {  
 $2 e^{-x} (-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z)) \&\& x \leq \text{Log}[-1 + x^2 z^2 + 1.12346 (1 + x^2 z^2) + 0.63 (-1 + z) (-1 - z + x (2 + x + (-2 + x) z))]) \&\& x \leq \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.12346 (-1 + x^2 z^2)])$   
 $-0.315 (2 x - \frac{e^x x^2}{y^2} + \frac{e^{-x} y^2}{x^2} - 4 \text{Log}[\frac{y}{x}])$   $x > \text{Log}[1 + x^2 z^2 + 0.63 (-1 + x)^2 (-1 + z^2) + 1.12346 (-1 + x^2 z^2)] \&\& x \leq 2 \text{Log}[\frac{y}{x}]$   
 0 True

$$\frac{1}{2} e^{-x} \left( 1.12346 \left( 1 + e^{2x} \right) - \left( -1 + e^x \right) \left( -1 - e^x - 0.63 \left( -1 + e^x \right) \right) \right)$$

$$\left( e^{-x} \left( \left( -1 + e^{2x} \right) \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + 1.12346 \left( 1 + e^{2x} \right) \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + 0.63 \left( -1 - 2 e^{2x} + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) + 2 e^x \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) + e^{2x} \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) \right) - 2 \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) \right) \right) /$$

$$\left( 2 \left( -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right) \right)$$

$$\frac{0.315 e^{-x} x^2 \left( e^x - \frac{y^2}{x^2} \right)^2}{y^2}$$

0

$$x > 0 \&\& x \leq \text{Log} \left[ -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right]$$

$$x > \text{Log} \left[ -1 + x^2 z^2 + 1.12346 \left( 1 + x^2 z^2 \right) + 0.63 \left( -1 + z \right) \left( -1 - z + x \left( 2 + x + \left( -2 + x \right) z \right) \right) \right] \&\& x \leq \text{Log} \left[ 1 + x^2 z^2 + 0.63 \left( -1 + x \right)^2 \left( -1 + z^2 \right) + 1.12346 \left( -1 + x^2 z^2 \right) \right]$$

$$x > \text{Log} \left[ 1 + x^2 z^2 + 0.63 \left( -1 + x \right)^2 \left( -1 + z^2 \right) + 1.12346 \left( -1 + x^2 z^2 \right) \right] \&\& x \leq 2 \text{Log} \left[ \frac{y}{x} \right]$$

True

In[59]:= `Plot[{pw1m, pw13m, pw07m}, {x, 0, 7},`

`GraphicsFunction`

`AxesLabel -> {Style[" $\tau$ ", 17, Black], Style["m[ $\tau$ ]", 17, Black]},`

`Obозначения н...`

`Стиль`

`Чёрный`

`Стиль`

`Чёрный`

`PlotLegends -> {" $\Omega_0$ ", "1.3 $\Omega_0$ ", "0.7 $\Omega_0$ "}`

`Легенды графика`

`LessEqual` : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

`Greater` : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

`LessEqual` : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

`LessEqual` : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

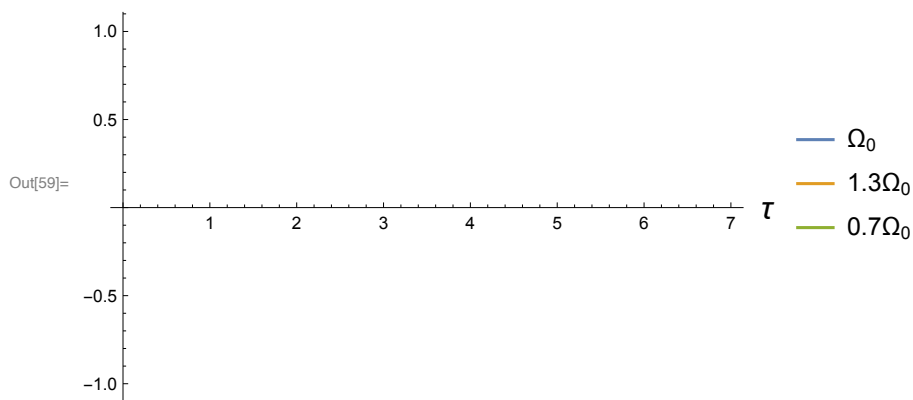
`General` : Further output of `LessEqual::nord` will be suppressed during this calculation.

`Greater` : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

`Greater` : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

`General` : Further output of `Greater::nord` will be suppressed during this calculation.

`m[ $\tau$ ]`



```
In[60]:= Plot[{pw10, pw130, pw070}, {x, 0, 7},
  AxesLabel → {Style["τ", 17, Black], Style["Θ[τ]", 17, Black]},
  PlotLegends → {"Ω0", "1.3Ω0", "0.7Ω0"}]
```

LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

LessEqual : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

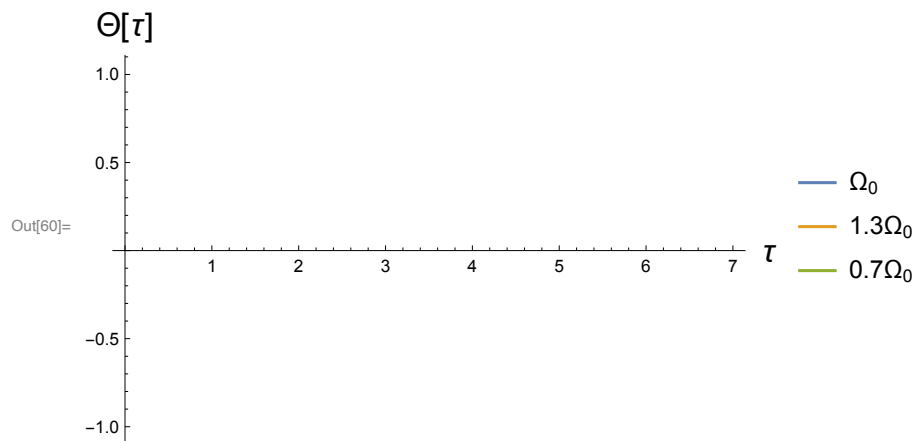
LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

General : Further output of LessEqual::nord will be suppressed during this calculation.

Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

General : Further output of Greater::nord will be suppressed during this calculation.



In[61]:= Plot[{pw1 $\omega$ , pw13 $\omega$ , pw07 $\omega$ }, {x, 0, 7},

[\[график функции\]](#)

AxesLabel  $\rightarrow$  {Style[" $\tau$ ", 17, Black], Style[" $\omega[\tau]$ ", 17, Black]},

[\[обозначения н...\]](#) [\[стиль\]](#)

[\[чёрный\]](#)

[\[стиль\]](#)

[\[чёрный\]](#)

PlotLegends  $\rightarrow$  {" $\Omega_0$ ", "1.3 $\Omega_0$ ", "0.7 $\Omega_0$ "}]

[\[легенды графика\]](#)

... LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... LessEqual : Invalid comparison with  $0.316514 + 6.28319 i$  attempted.

... LessEqual : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... General : Further output of LessEqual::nord will be suppressed during this calculation.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... Greater : Invalid comparison with  $-38.4365 + 3.14159 i$  attempted.

... General : Further output of Greater::nord will be suppressed during this calculation.

$\omega[\tau]$

