

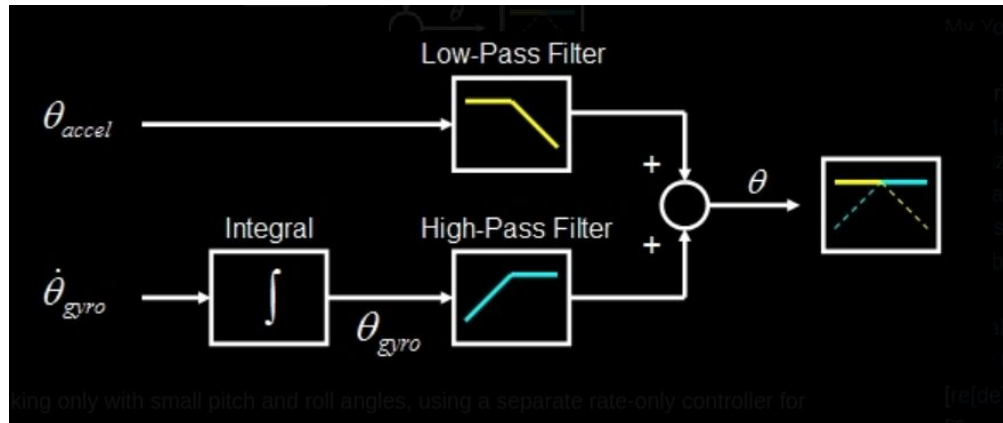
Complementary Filter

-Sensor fusion algorithm .

(This slides demonstrates fusion of 6dof IMU)

Complementary Filter:

- A complementary filter is a simple and effective technique used to **fuse the data from different sensors** to provide a **more accurate and stable output**.
- Combine many sensors that **complement each other's weaknesses** (hence complementary) with their **strengths**.



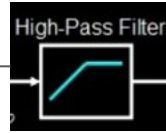
- This is achieved by blending the complementary characteristics of the sensors using a
 - HIGH PASS FILTER on one sensor's output and a
 - LOW PASS FILTER on another sensor's output.
- High Pass Filter:
 - Allows or let pass through only the High frequency signals (Quick changes)
 - Attenuates or reduces the amplitude of the Low frequency signals (Drifts)
- Low Pass Filter:
 - Allows or let pass through only the Low frequency signals (stable readings)
 - Attenuates or reduces the amplitude of the High frequency signals .

Complementary data ,

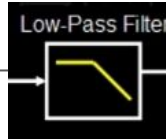
==> $\text{Accelerometer_data} * (\text{low pass filter}) + \text{Gyroscope_data} * (\text{High pass filter})$

(Fast and noiseless reading)

GYROSCOPE
DATA

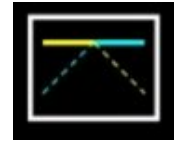


ACCELEROMETER
DATA



(Reliable and noisy reading)

CALIBRATED DATA



(Filtered, Reliable, Noiseless reading)

Mathematical Equation of complementary filter

$$\Theta_n = \alpha \cdot (\Theta_{n-1} + g \cdot \Delta t) + (1 - \alpha) \cdot a$$

ACCELEROMETER
PART

$$\text{Filtered_angle} = \{ \alpha \times (\text{previous_filtered_angle} + \text{gyro_rate} \times \Delta t) \} + \{ (1 - \alpha) \times \text{accel_angle} \}$$

GYRO PART

- α is the filter coefficient ($0 < \alpha < 1$), typically close to 1. $(1 - \alpha)$ is complement of α

Applying High Pass Filter

- For gyroscope data, this helps in removing the **slow drift** and **focusing on the rapid changes**.
- The high-pass filter is typically applied by integrating the gyroscope rate of change over time and combining it with the previous filtered angle.

Gyro:

$$(\text{previous_filtered_angle} + \text{gyro_rate} \times \Delta t) \text{ ----- } 1$$

Applying Low pass Filter

- For accelerometer data, this helps in **smoothing out the noisy data** and **focusing on the stable, long-term orientation**.
- The low-pass filter is applied by using the accelerometer data to directly calculate the angle.

Accel: (accelerometer_angle) ----- 2

$$\text{Complementary Filter} = [\text{Low Pass (Accele)}] + [\text{High Pass (Gyro)}] = 1 + 2$$

$$\Rightarrow [(1-\alpha) \times \text{accel_angle}] + \alpha \times (\text{previous_filtered_angle} + \text{gyro_rate} \times \Delta t)$$