



UNIVERSITÀ DEGLI STUDI DI TRENTO

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THESIS

Phase-matching method by temperature control
of partially degenerate Four-Wave Mixing phenomena

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Abstract: studying degenerate Four-Wave Mixing phenomena in a rectangular silicon-based waveguide. Analyze its behaviour at different temperatures to maximize phase-match. Developing a project to build an actual prototype.

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1 Introduction

1.1 Motivation

In my scholastic career I approached the study of optics in an elective course of my third year of undergraduate academic degree. I became very interested in the subject, in particular because of the potential development of photonics for communication and computing. I discussed different topics with the professors and some researchers. One of them suggested me a few interesting topics in guided-wave optics which could be studied as a undergraduate thesis.

I chose to study the the temperature behaviour of silicon waveguides. The reason of the choice is that there are always discrepancies between the design of silicon objects and their actual production by the factory. The aim of the study is to exploit this behaviour to correct possible production defects of the materials.

The study is focused on a silicon-based waveguide with rectangular section with a silicon (Si) core and a silica (SiO₂) cladding. Its purpose is to generate light through a partial degenerate Four-Wave Mixing phenomenon

1.2 Partially degenerate Four-Wave Mixing

Four-Wave Mixing (FWM) is a nonlinear optical effect due to the susceptibility of silicon. Silicon is an isotropic material and therefore second order susceptibility $\chi^{(2)}$ (almost) vanishes. Third order susceptibility $\chi^{(3)}$, on the other hand, is not zero and is responsible among the other effects for FWM, which is indeed a third order phenomenon.

In general FWM implies the mix of four waves of different frequency. Partial degenerate FWM, instead, is a specific case in which two waves have the same frequency. Therefore it is about two waves (pump and signal) which generate a third wave (idler).

2 Linear optics

A linear dielectric medium is characterized by a linear relation between the polarization density and the electric field, $\mathbf{P} = \varepsilon_0\chi\mathbf{E}$, where ε_0 is the permittivity of free space and χ is the susceptibility of the medium.

In linear optics the technology for transmitting a light wave by confining it in a finite space is the guided-wave optics. The instruments employed for achieving such purpose are called waveguides.

2.1 Silicon waveguides

Silicon waveguides are dielectric waveguides and make use of the interface between two media with different refractive index. Precisely they exploit the phenomenon of total internal reflection: if a propagating wave reaches a boundary between two mediums, one with higher refractive index (n_H) and another with lower refractive index (n_L), with an angle of incidence greater than the *critical angle*, then the wave is completely reflected in the first medium. Angles are defined relative to the normal vector of the interface and the critical angle can be obtained by the Snell law:

$$\theta_C = \arcsin\left(\frac{n_L}{n_H}\right)$$

Silicon waveguides are composed by core and cladding (?). The former is the higher refractive index medium in which the wave is confined, the latter is the lower refractive index medium which surrounds the core, thus creating the interface. Theoretically the cladding could also be vacuum.

Considering an ideal dielectric waveguide (no absorption) and the total field distribution as sum of transverse electromagnetic (TEM) plane waves is possible to study the propagation of the wave along the waveguide with an electromagnetic analysis. Furthermore it can be shown that not all field distribution are transmitted through the waveguide without energy loss (?).

Those field distributions, which maintain the same transverse distribution and polarization at all locations along the waveguide axis, are called modes. These modes can be categorized in two main groups, depending on the polarization of the wave: transverse electric (TE) modes and transverse magnetic (TM) modes, which have respectively the electric and magnetic field transverse to the waveguide axis. Both TE and TM modes can be again classified by their order, that is proportional to the number of maxima of the modulus of the electric and magnetic fields in the core section.

**** *effective index*

2.2 Rectangular dielectric waveguides

In general, in a rectangular dielectric waveguide the classification of modes need two indexes because we have two degrees of freedom. For our purpose, due to the thin geometry of the core, modes with the higher effective index are fundamental modes in the height axis. Only one significant index is then left to describe the order of modes.

photos?

3 Non-linear optics

A nonlinear dielectric medium is characterized by a nonlinear relation between \mathbf{P} and \mathbf{E} , such as

$$\mathbf{P} = \varepsilon_0 \left(\chi^{(1)} \cdot \mathbf{E} + \chi^{(2)} : \mathbf{E}^2 + \chi^{(3)} : \mathbf{E}^3 + \dots \right)$$

In everyday condition linear effects are much larger than nonlinear ones. The relation between \mathbf{P} and \mathbf{E} becomes nonlinear when \mathbf{E} has a value comparable to interatomic electric fields, which are typically $\sim 10^5 - 10^8 \text{ V m}^{-1}$.

For an isotropic medium the second order term is zero (in the dipole approximation) and this is our scenario. Thus the dominant non-linearity is the third order and the material is called a Kerr medium.

3.1 Third order effect: Four-Wave Mixing

Many processes are result of third order nonlinearities: Third-Harmonic Generation (THG), Optical Kerr Effect, Cross-phase modulation (XPM), Self-phase modulation (SPM) and Four-Wave Mixing (FWM).

Four-Wave Mixing originates from the third order nonlinear response of a material to an electromagnetic field, precisely from the behaviour of bound electrons. This parametric process involve nonlinear interaction among four optical waves.

4 Simulating and coding

To understand the behaviour of the waveguide, it is necessary to first know how waves of different frequency are transmitted through the waveguide. We chose to simulate the modes with temperature and frequency as a parameters.

Our aim was to develop a model to work with an infrared laser pump with $\lambda_p = 1.55 \mu\text{m}$. We narrowed our simulations to a frequency gap centered in $\omega_p = 2\pi\nu_p = 2\pi c/\lambda_p$. The gap chosen was precisely $[1.45 \mu\text{m}, 1.65 \mu\text{m}]$ or the equivalent $[182 \text{ THz}, 207 \text{ THz}]$.

Our data output was therefore the field distribution and effective index for a number of modes for each parametric configuration.

The next step was to classify these data depending on the order and type (TE or TM) of the modes. We achieved this by analyzing the maxima of the field distributions. We obtained then a well organized data matrix filled with the value of effective index for each combination of parameters.

4.1 Data processing

Then we fit effective index data for each parametric configuration with a polinomial function of frequency $\omega = 2\pi\nu$ and temperature T :

$$n_{eff} = f_{mt,mo}(\omega, T)$$

where *mt* and *mo* means respectively *mode type* (TE or TM) and *mode order* (0, 1, 2, ...)

$$\omega_1 + \omega_2 = \omega_3 + \omega_4$$

$$\omega_1 = \omega_2 = \omega_P$$

$$\omega_I = 2\omega_P - \omega_S$$

$$\Omega_S = \omega_1 + \omega_3 = \omega_4 - \omega_1$$

where we assume $\omega_3 < \omega_4$.

$$\Omega_S = |\omega_P - \omega_I| = |\omega_S - \omega_P|$$

$$\Delta k = \beta_3 + \beta_4 - \beta_1 - \beta_2$$

$$\Delta k = \beta_3 + \beta_4 - 2\beta_1$$

$$L_{coh} = \frac{2\pi}{|\Delta k|}$$

5 Prototyping

5.1 Heater configurations

In order to achieve a greater effect from the different temperature, we tried to move the heater from the center of the core to the side. This operation was intended to increase the difference of behaviour between low and high orders.

5.2 Different geometries

6 Conclusion

References

- [1] G. Agrawal. Nonlinear Fiber Optics, 5th edition. 2013
- [2] B. E. A. Saleh, M. C. Teich. Fundamentals of photonics, 2nd edition. 2007