

20. (a) \Rightarrow (b): $u \in B(E, F)$, 则存在唯一的 $u^*: F^* \rightarrow E^*$, $u^* \in B(F^*, E^*)$, 且 $\|u\| = \|u^*\|$. 7-20

且满足 $\langle u^*(f^*), x \rangle = \langle f^*, u(x) \rangle$, $\forall f^* \in F^*, x \in E$.

设 $x_\alpha \xrightarrow{w} x$ (网收敛), $\alpha \in M(x)$, 则 $\forall x^* \in E^*$, $x^*(x_\alpha) \rightarrow x^*(x)$.

则 $\langle u^*(f^*), x_\alpha \rangle \rightarrow \langle u^*(f^*), x \rangle$, $\forall f^* \in F^*$.

即 $\langle f^*, u(x_\alpha) \rangle \rightarrow \langle f^*, u(x) \rangle$, $\forall f^* \in F^*$. 故 $u(x_\alpha) \xrightarrow{w} u(x)$.

(b) \Rightarrow (c): 显然.

(c) \Rightarrow (a):