

9.2 perform encryption and decryption using the RSA algorithm, as in figure 9.5, for the following:

a)  $P=3$  ;  $q=11$  ,  $e=7$  ;  $M=5$

① select primes :  $P=3$  &  $q=11$

② lakukan Komputasi :  $N = P \cdot q = 3 \cdot 11 = 33$

③ lakukan Komputasi :  $\phi(n) = (p-1)(q-1) = (3-1)(11-1) = 2 \cdot 10 = 20$

④ select  $e$  ;  $\gcd(e, 20) = 1$  ; choose  $e = 7$

⑤ Tentukan  $d$  ;  $d \cdot e = 1 \pmod{20}$  dan  $d < 20$  ,

maka  $d = 3$  , karena :  $3 \times 7 = 21 = 2 \times 10 + 1$

⑥ publish public key  $KU = \{7, 33\}$

⑦ keep secret private key  $KR = \{3, 3, 11\}$

Proses enkripsi dan deskripsi :

① Message  $M = 5$  ( $5 < 33$ )

② Encryption

$$C = M^e \pmod{N} = 5^7 \pmod{33} = 78125 \pmod{33} = 14$$

③ Decryption

$$M = C^d \pmod{N} = 14^3 \pmod{33} = 2744 \pmod{33} = 5 \text{ (terbukti)}$$

b)  $P=5$  ;  $q=11$  ;  $e=3$  ;  $M=9$

① select primes :  $P=5$  &  $q=11$

② lakukan Komputasi :  $N = P \cdot q = 5 \cdot 11 = 55$

③ lakukan Komputasi :  $\phi(n) = (p-1)(q-1) = (5-1)(11-1) = 4 \cdot 10 = 40$

④ select  $e$  ;  $\gcd(e, 40) = 1$  ; choose  $e = 3$

⑤ Tentukan  $d$  ;  $d \cdot e = 1 \pmod{40}$  dan  $d < 40$  ,

maka  $d = 27$  , karena  $3 \times 27 = 81 = 2 \times 40 + 1$

⑥ publish public key  $KU = \{3, 55\}$

⑦ keep secret private key  $KR = \{13, 5, 11\}$

Proses enkripsi dan dekripsi :

① Message  $M = 9$  ( $9 < 55$ )

② Encryption

$$C = M^e \pmod{N} = 9^3 \pmod{55} = 729 \pmod{55} = 14$$

③ Decryption

$$M = C^d \pmod{N} = 14^{27} \pmod{55} = 9 \text{ (terbukti)}$$

$$d = (\phi(n) \cdot i + 1) / e$$

$$(i=1) \quad d = (40 \cdot 1 + 1) / 3 = 41/3$$

$$= 13.67 \rightarrow \text{bukan integer}$$

$$(i=2) \quad d = (40 \cdot 2 + 1) / 3 = 81/3$$

$$= 27 \rightarrow \text{integer}$$



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9.3 In a public key system using RSA, you intercept the cipher-text  $C=10$  sent to a user whose public key is  $e=5$ ,  $n=35$ , what is the plaintext  $M$ ?

Pembahasan:

Dik:  $C = 10$

$e = 5$

$N = 35$

Dit:  $M = \dots ?$

Jwb:

$$\begin{aligned} C &= M^e \bmod N \\ 10 &= M^5 \bmod 35 \end{aligned}$$

- ① select primes :  $p=5$  &  $q=7$
- ② lakukan komputasi :  $N = p \cdot q = 5 \cdot 7 = 35$
- ③ lakukan komputasi :  $\phi(n) = (p-1)(q-1) = (5-1)(7-1) = 4 \cdot 6 = 24$
- ④ select  $e$  :  $\gcd(e, 24) = 1$ , choose  $e=5$
- ⑤ Tentukan  $d$  :  $d \cdot e = 1 \bmod 24$  dan  $d < 24$   
 $d = (\phi(n) \cdot i + 1) / e$

$$(i=1) \rightarrow d = (24 \cdot 1 + 1) / 5 = 25 / 5 = 5 \text{ (integer)}$$

maka  $d=5 \rightarrow$  karena  $5 \times 5 = 25 = 4 \times 6 + 1$

- ⑥ publish public key  $KU = \{5, 35\}$
- ⑥ secret private key  $KR = \{5, 5, 7\}$

do encryp & decryp :

①  $M = ?$

②  $C = 10$

③  $M = C^d \bmod N$

$$M = 10^5 \bmod 35$$

$$M = 100.000 \bmod 35$$

$$\boxed{M = 5} \text{ (maka plaintextnya adalah 5)}$$

Pembuktian bahwa cipher-text  $C=10$   $\Downarrow$

①  $C = M^e \bmod N$

$$C = 5^5 \bmod 35$$

$$C = 3125 \bmod 35$$

$$C = 10 \text{ (terbukti cipher-text / } C=10)$$

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9.4. In RSA system, the public key of a given user is  $e = 31$ ,  $n = 3599$ . What is the private key of this user? Hint: First use trial-and-error to determine  $p$  and  $q$ ; then use the extended Euclidean algorithm to find the multiplicative inverse of 31 modulo  $\phi(n)$ .

### Pembahasan

$$\odot KU = \{e, N\}$$

$$KU = \{31, 3599\}$$

$$\odot p = 59 \text{ \& } q = 61$$

$$\begin{aligned}\odot \phi(n) &= (p-1) \cdot (q-1) \\ &= (59-1) \cdot (61-1) \\ &= 58 \cdot 60 \\ &= 3480\end{aligned}$$

$$\begin{aligned}\odot e \cdot d &= 1 \pmod{\phi(n)} \\ 31 \cdot d &= 1 \pmod{3480}\end{aligned}$$

$$d = \frac{1 + k\phi(n)}{e}$$

$$d = \frac{1 + 3480k}{31}$$

$$(k=0) \rightarrow d = \frac{1 + 3480(0)}{31} = \frac{1}{31}$$

$$(k=1) \rightarrow d = \frac{1 + 3480(1)}{31} = \frac{3481}{31}$$

$$(k=2) \rightarrow d = \frac{1 + 3480(2)}{31} = \frac{6961}{31}$$

$\vdots$

$$(k=27) \rightarrow d = \frac{1 + 3480(27)}{31} = 3031 \left( \frac{93961}{31} \right)$$

Jadi private key  $KR = [d, p, q]$

$$KR = [3031, 59, 61]$$