

Statement Submissions Questions



Tweedledum's Nested Brackets

Time limit: 1000 ms
Memory limit: 256 MB

The nested level of a bracket sequence S is defined as the number of unmatched left brackets that may exist in a prefix of S . For example, the nested levels of $((()))$, $(())()$, and $((()()))()$ are 3, 2, and 3 respectively.

Tweedledum has a string X consisting of a valid sequence of round brackets. In how many ways can you create a maximally nested bracket sequence by removing a continuous substring Y from X and re-inserting it into X at any location? The substring Y has to be a valid bracket sequence.

A valid bracket sequence is defined as follows:

- $()$ is a valid bracket sequence;
- If S is a valid bracket sequence, then (S) is also a valid bracket sequence;
- If Q and R are two valid bracket sequences, then the concatenation of them, $S = QR$, is also a valid bracket sequence.

Two ways are considered different if you either choose a different substring Y , or if you re-insert Y at a different position. Two equal substrings occurring at two different positions in X are considered two different choices of Y . Re-inserting Y at its original position counts if it is a maximally nested bracket sequence.

Standard input

The input has a single line consisting of the bracket sequence X .

Standard output

Output the number of ways in which you can create a maximally nested bracket sequence, by choosing and re-inserting a substring Y from X .

Constraints and notes

- $2 \leq |X| \leq 10^6$

Input	Output	Explanation
<code>((()))()</code>	2	<code>((()))</code> on the left can be moved into <code>()</code> on the right, or vice versa.

Input	Output	Explanation
<input type="text" value="((()))"/>	<input type="text" value="3"/>	<code>()</code> , <code>(())</code> , or <code>((()))</code> can all be re-inserted at their original positions.
<input type="text" value="()()()"/>	<input type="text" value="8"/>	There are 6 ways to choose one pair of brackets and insert it into either of the other two pairs and there are 2 ways to choose two consecutive pairs of brackets and insert them into the remaining pair of brackets.