

Convolutional Neural Networks

A Gentle Introduction

Roberto Souza
Assistant Professor
Electrical and Software Engineering
Schulich School of Engineering

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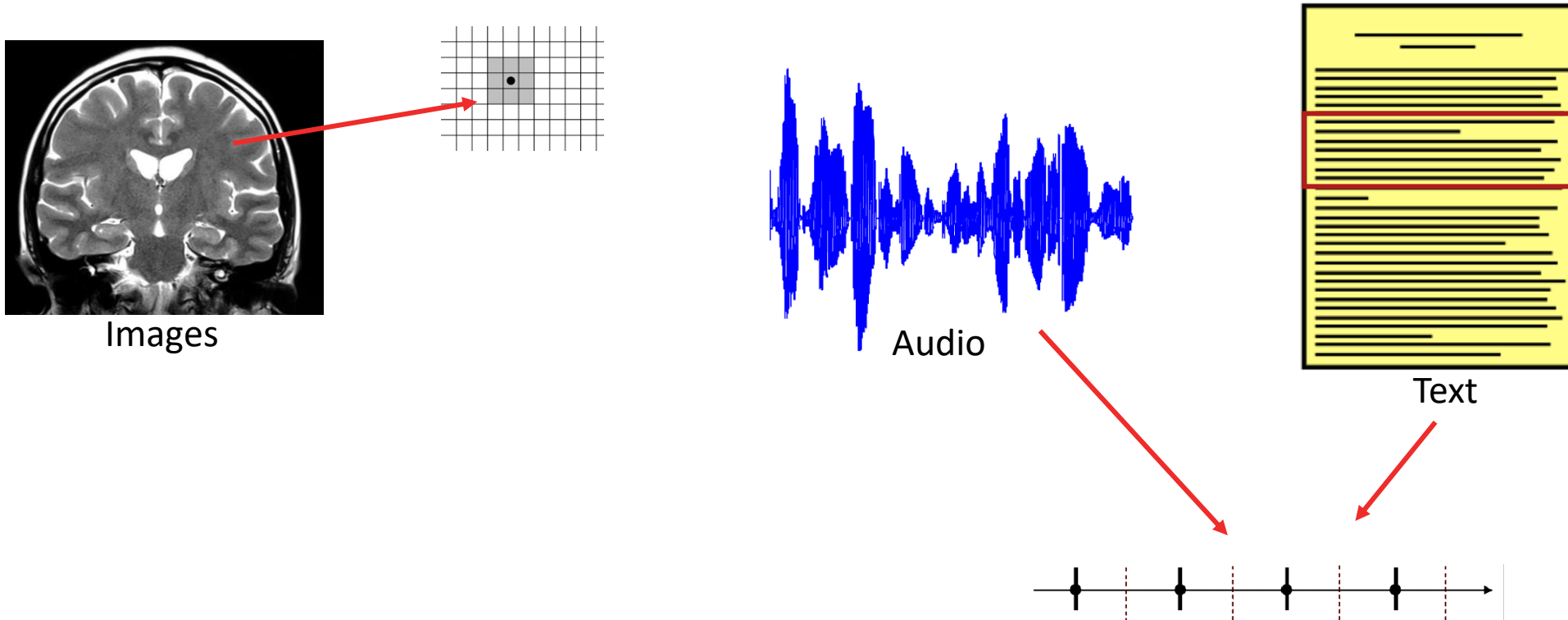
Outline

- Learning Goals
- Convolutional Neural Networks (CNNs)
 - Basic Operations
 - Properties
 - Computing number of parameters
- Summary

Learning Goals

- Understand how CNNs work and when to apply them
- Compute the number of parameters of your model

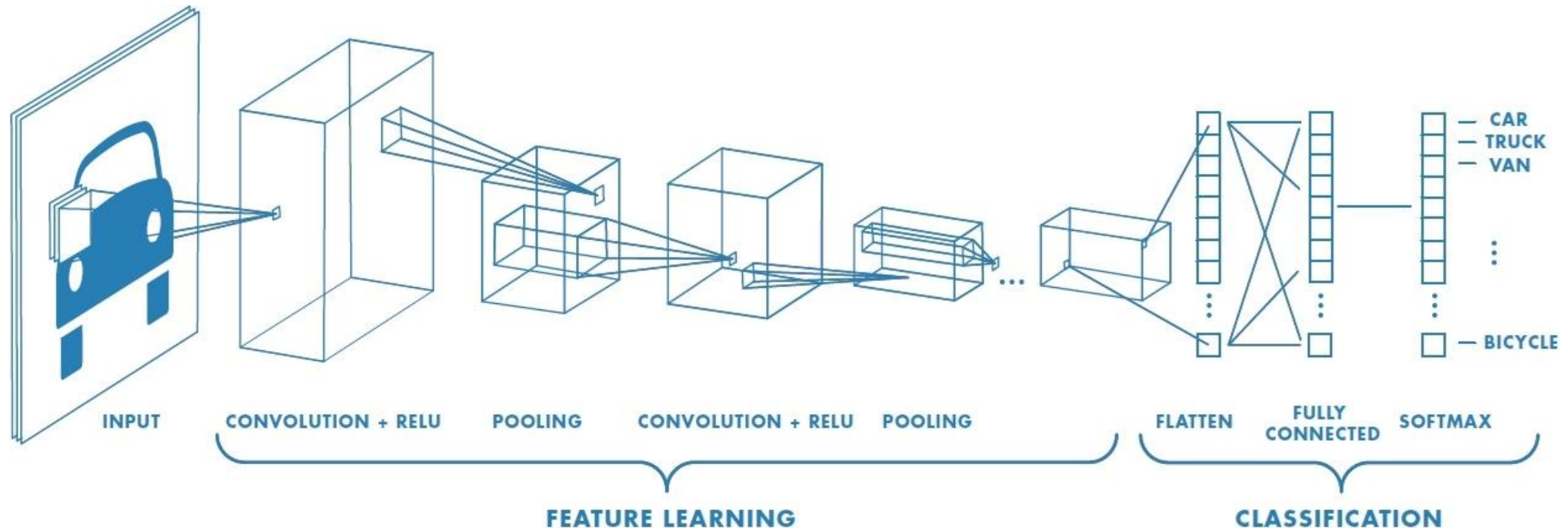
Data – Euclidean Domains



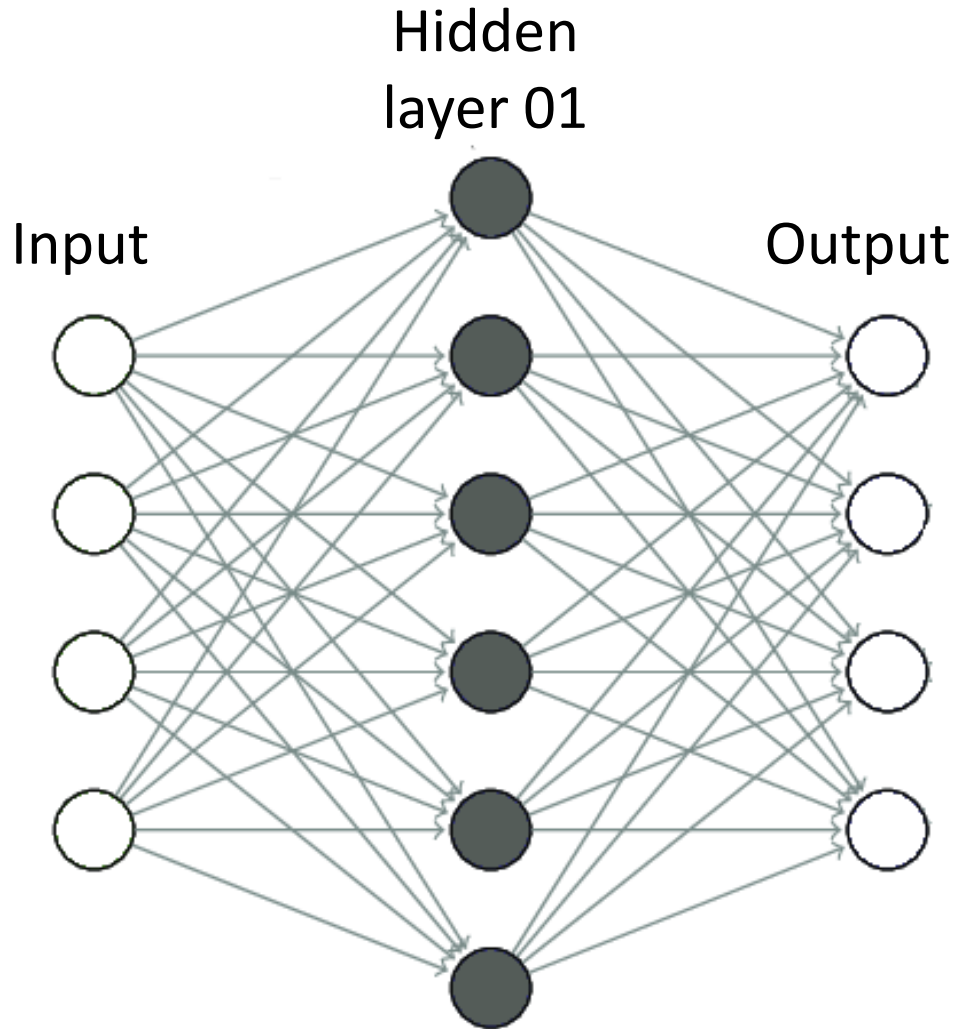
- Images, audio, text among others all have regular structures in a Euclidean space
 - Convolutions are well-defined operations that can be computed efficiently in these structures

Convolutional Neural Networks

- Convolutional layers learn features
- Connected layers perform classification
- Fewer trainable parameters than fully connected networks

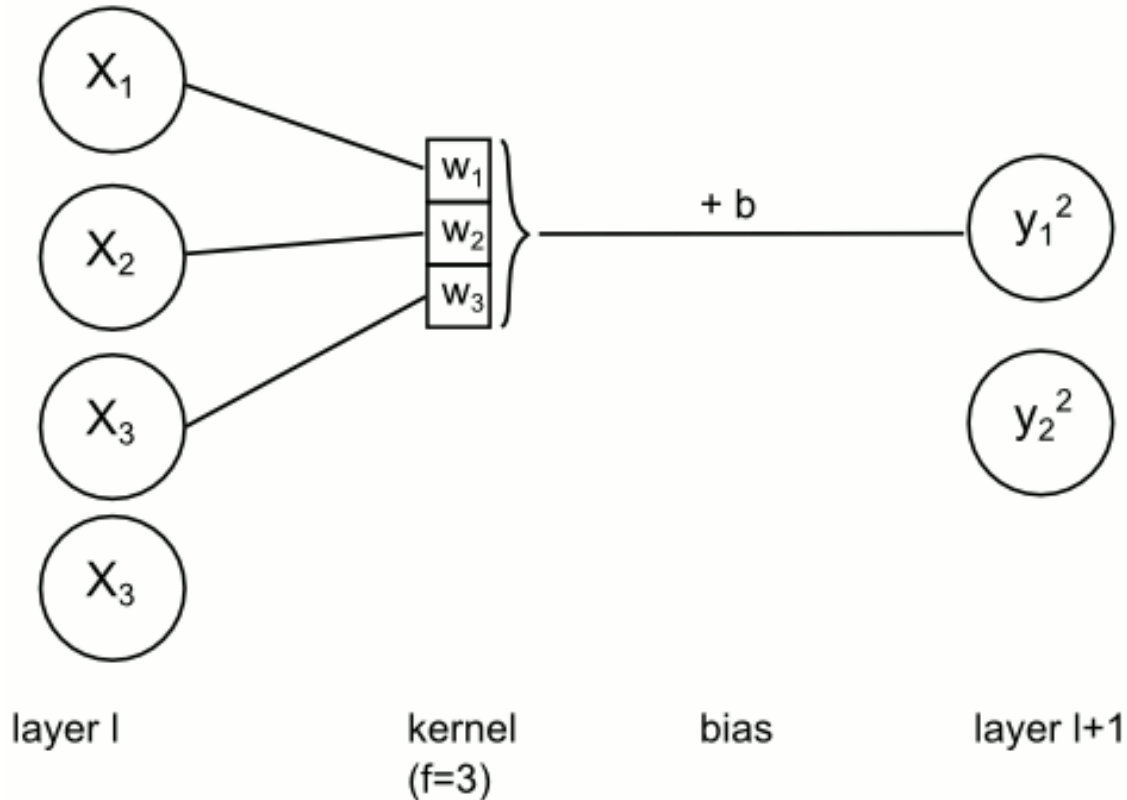


Fully Connected Neural Network – Global Property



- The fully connected layer can lead to an explosion in the number of parameters
- Imagine your input is a 256 x 256 image and your layer has 10 outputs, how many parameters would the model have?
 - $256 \times 256 \times 10 + 10 = 655,370$

Convolutional Neural Network – Weight Sharing



- Convolutional neural networks share weights across inputs (*i.e.*, connection **sparsity**)
- Convolutions leverage local correlations (*i.e.*, **locality**)
- Imagine your input is a 1D signal of size L , your convolution size is 3 and your layer has 10 filters, how many parameters would the model have?
 - $3 \times 10 + 10 = 40$

Convolution (single-channel input)

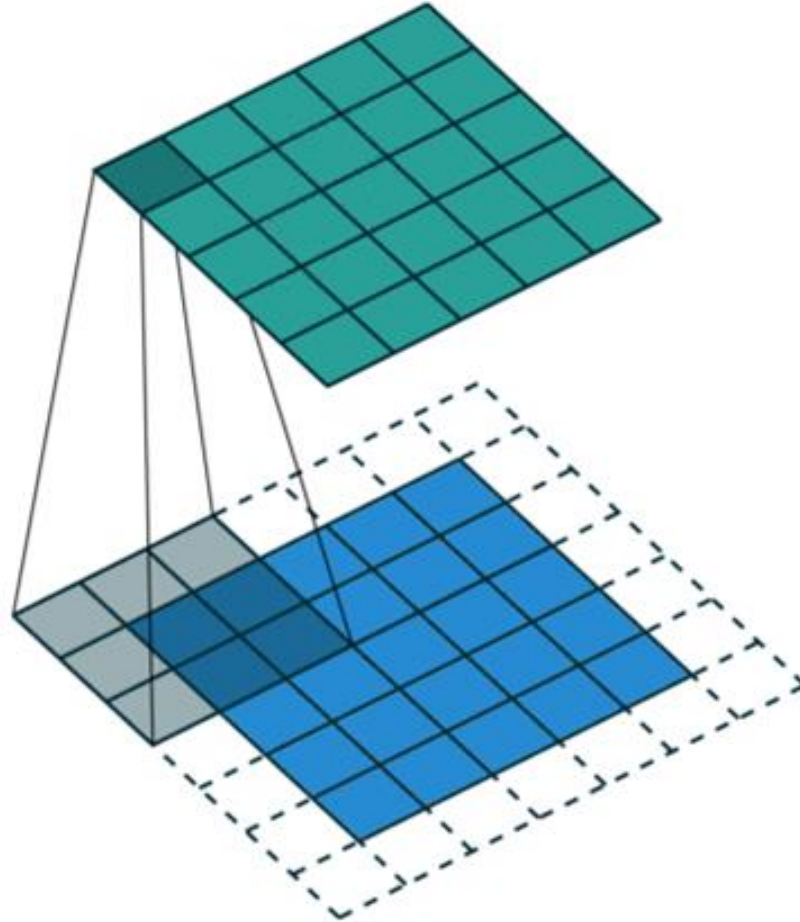
1x1	1x0	1x1	0	0
0x0	1x1	1x0	1	0
0x1	0x0	1x1	1	1
0	0	1	1	0
0	1	1	0	0

4		

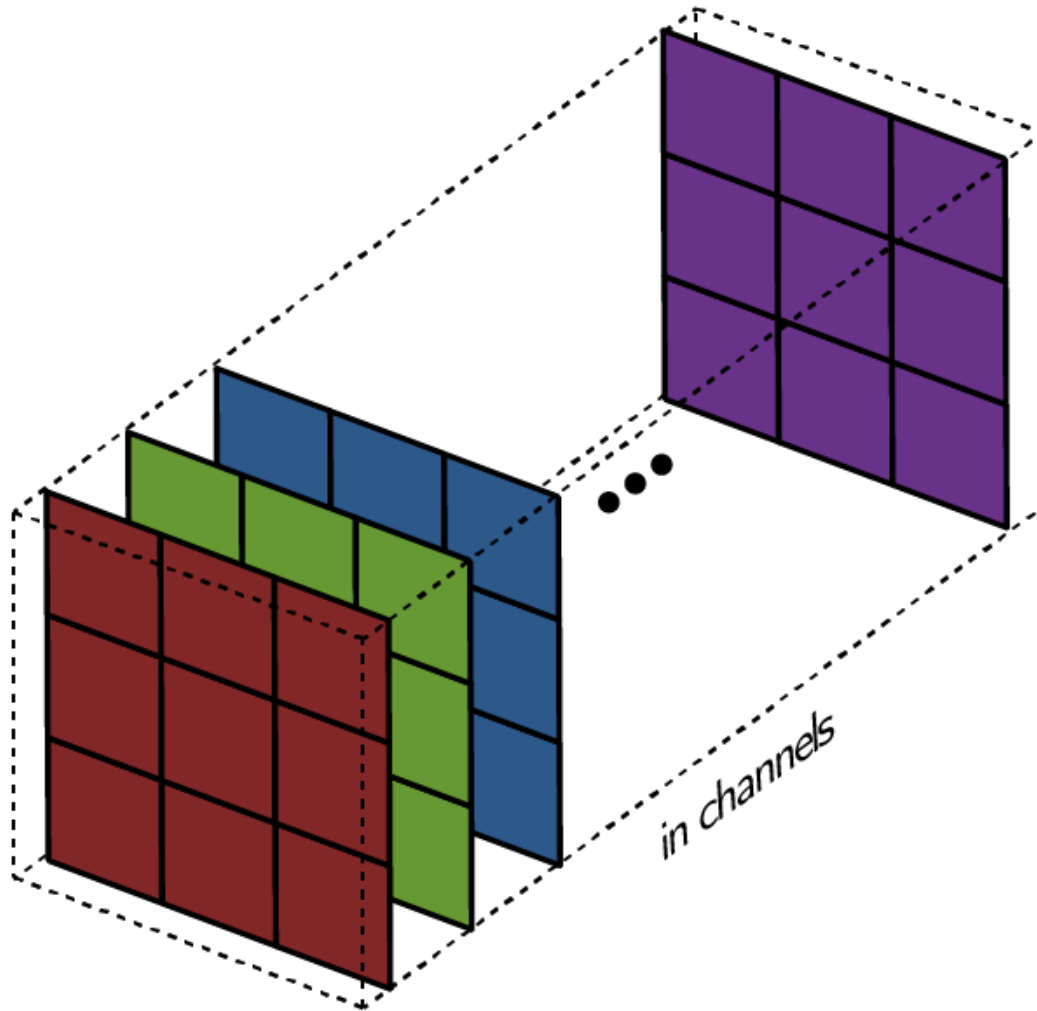
The bias term is added after the convolution

Convolution (padding)

- Image can be padded prior to convolution to preserve its dimensions

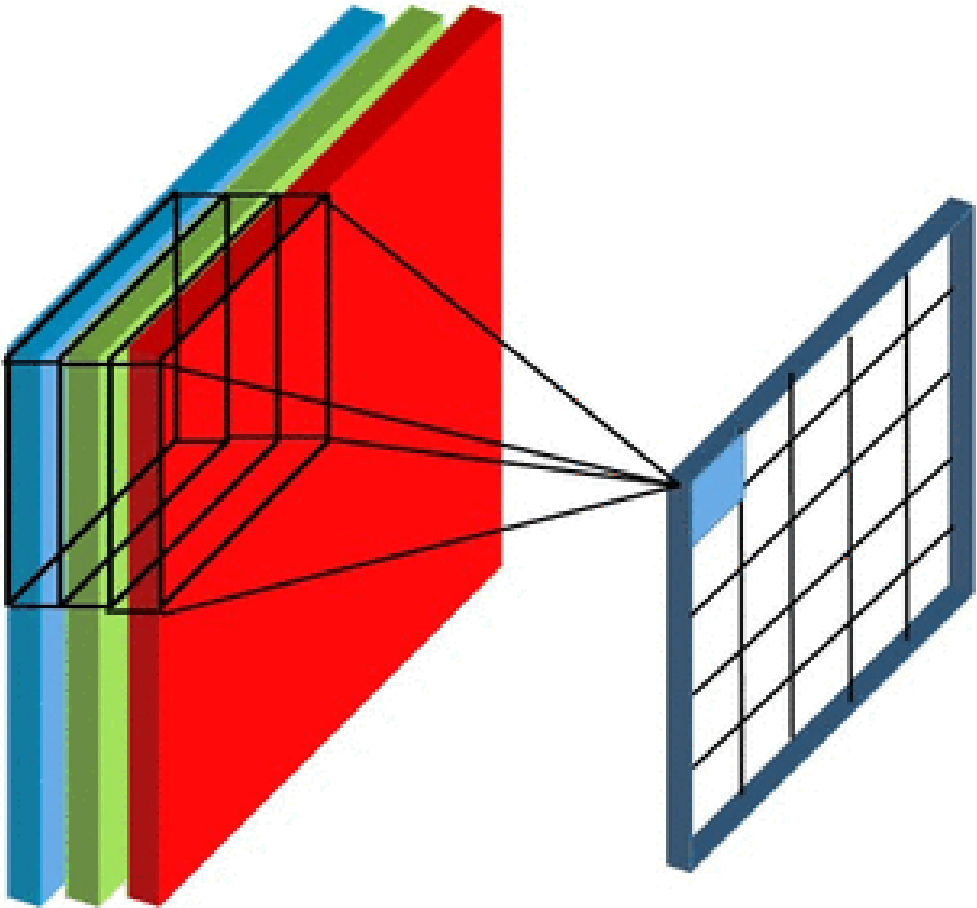


N-channel Images/Signals



- Results of convolutions are stacked resulting in n-channel images/signals

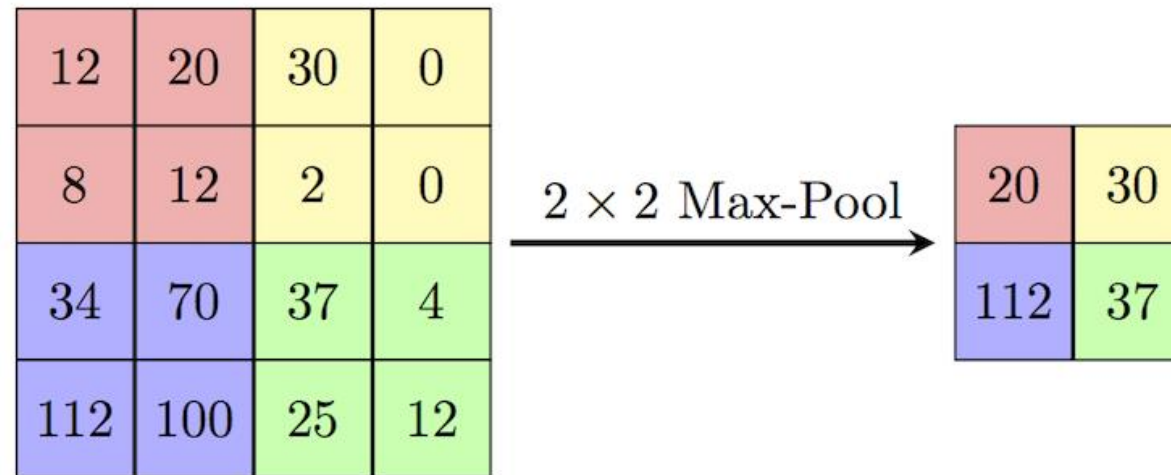
Convolution – multi-channel input



- The convolutions encompass the channels of the input
- A $W1 \times W2$ convolution is actually a $W1 \times W2 \times n_{\text{channels}}$ convolution

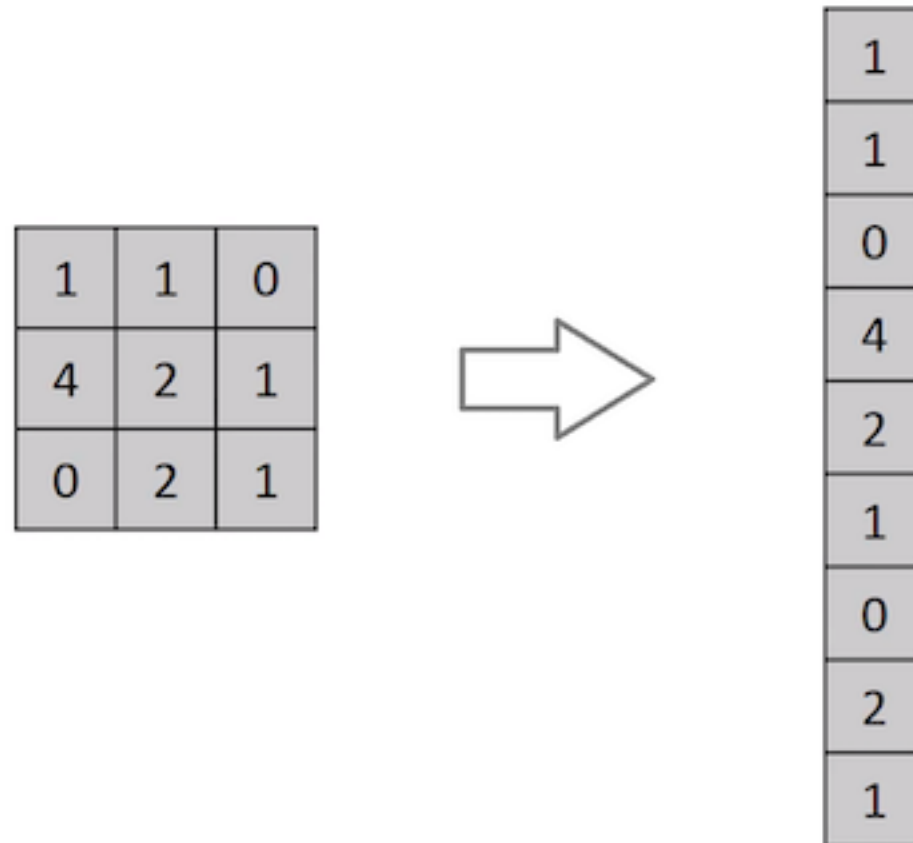
Max-Pooling

- Non-linear operation
- Reduce dimensionality and computational cost
- After a max-pooling, the number of filters in the subsequent layer is increased

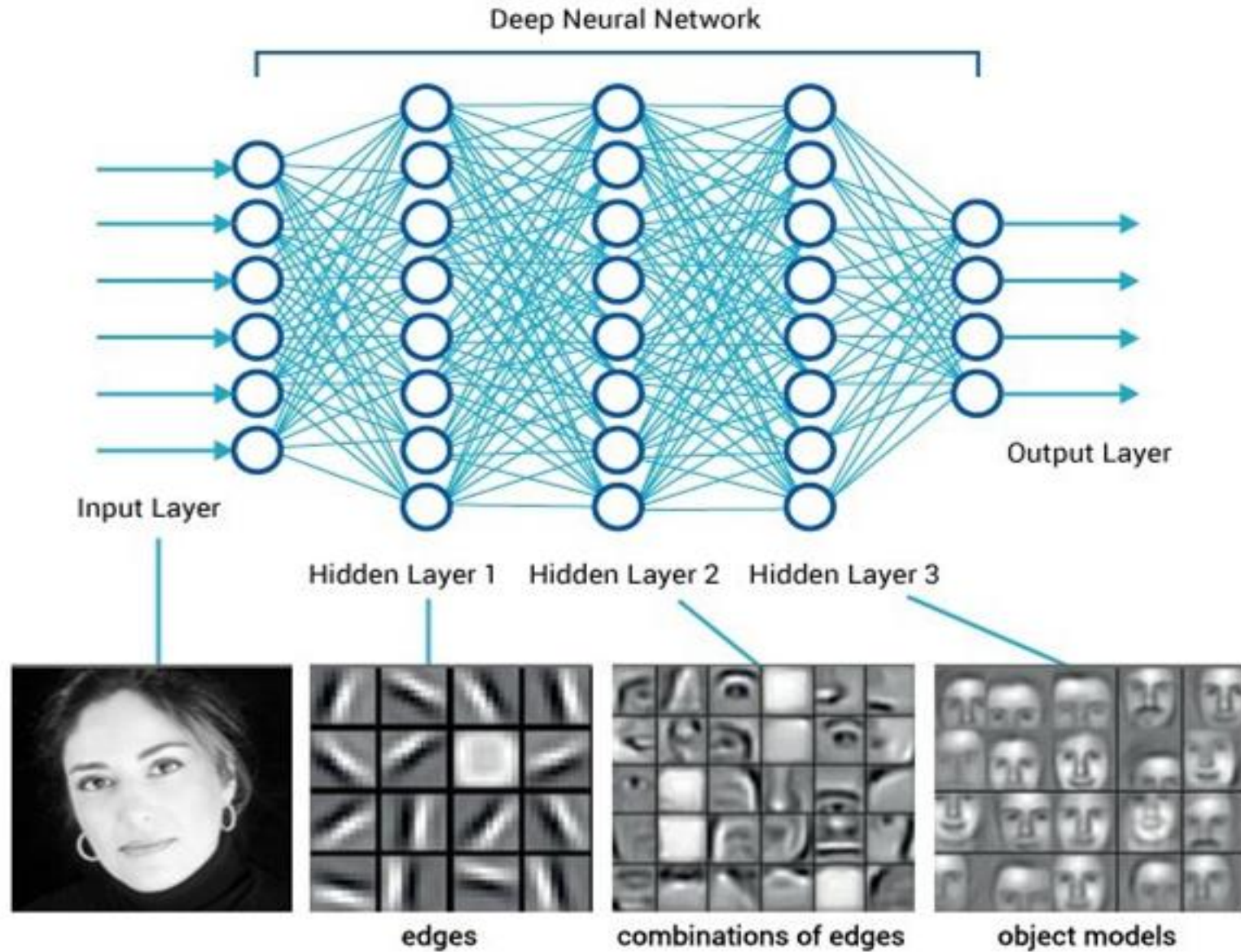


Flatten

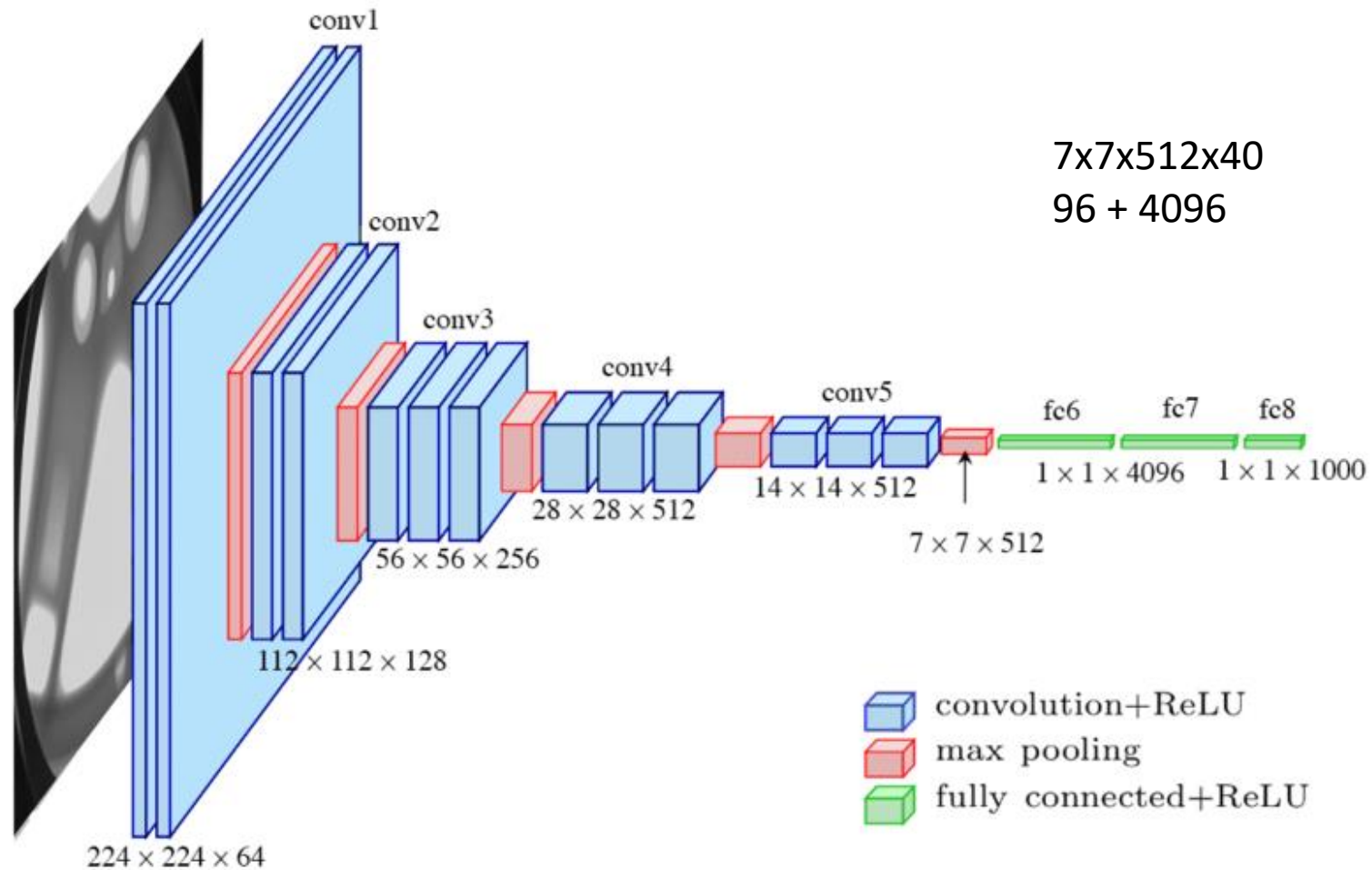
- The flatten operation is applied before the fully connected layer



CNN Hierarchy of Concepts



VGG- 16 Architecture



Summary

- CNNs share weights and have sparse connections
- They depend on local correlations to operate
- The basic operations are convolutions and max-pooling layers
- Implicit hierarchy of concepts

Thank you!

