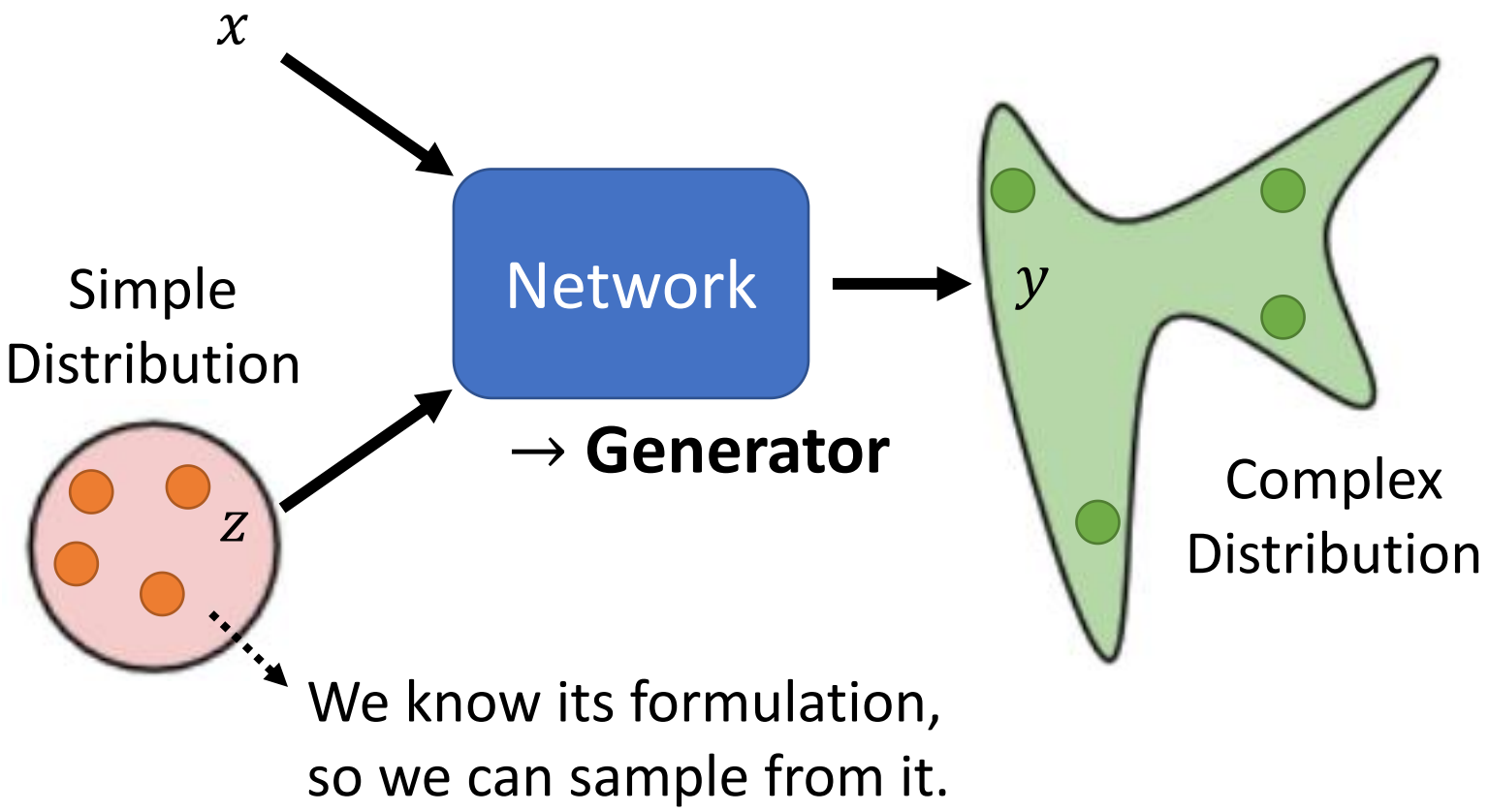
Generation

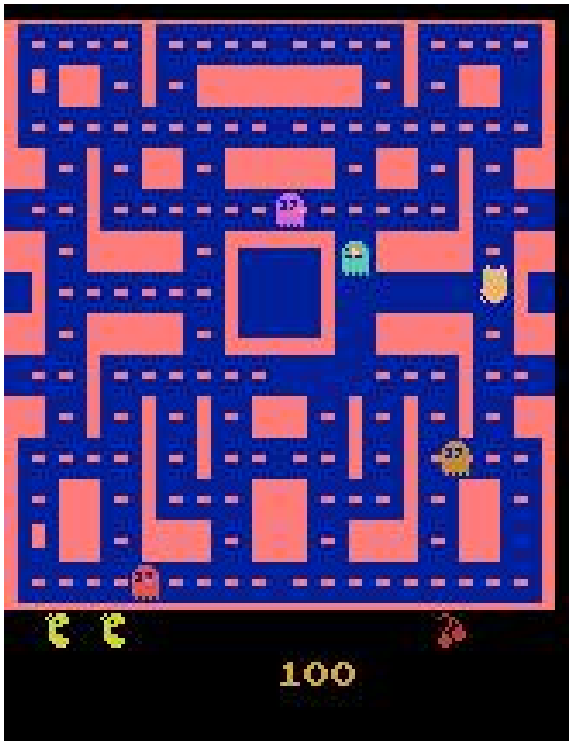
Yizhen Lao

Network as Generator



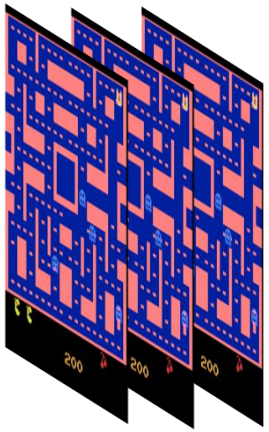
Source: https://github.com/dyelax/Adversarial_Video_Generation

Why distribution?



Real Video

Video Prediction



Previous frames

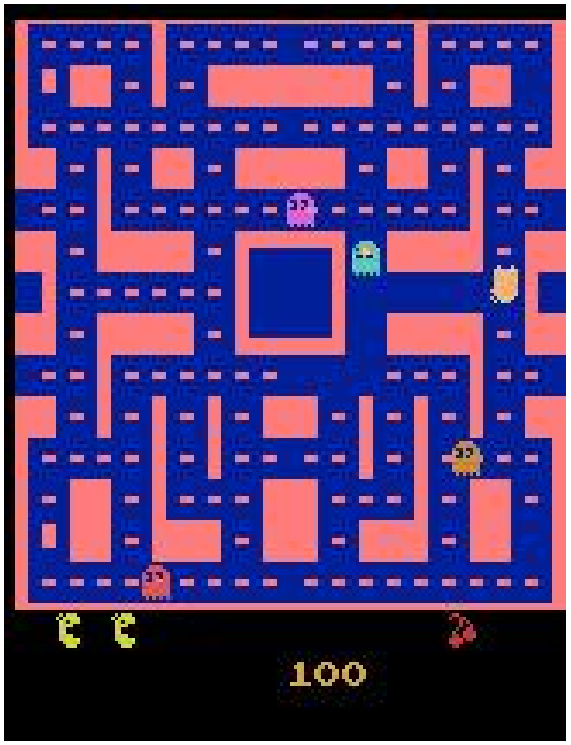
Network

y

next frame

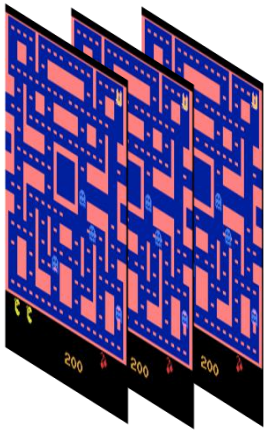
Source: https://github.com/dyelax/Adversarial_Video_Generation

Why distribution?



Prediction

Video Prediction

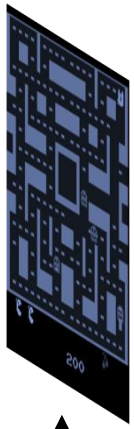


Previous frames

Network

y ???

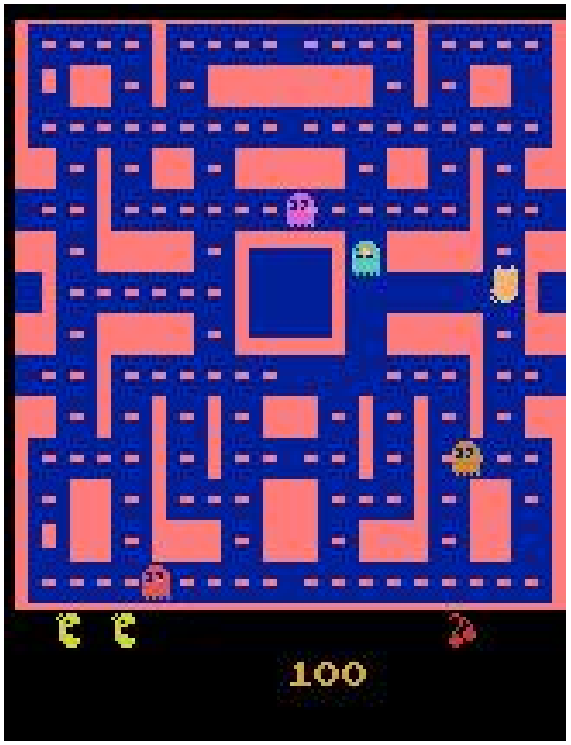
turn right



turn left

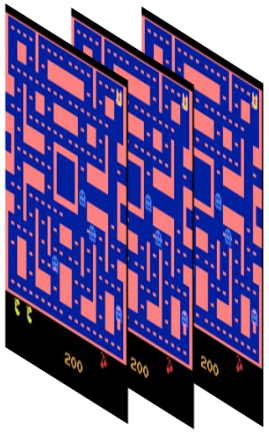
Source: https://github.com/dyelax/Adversarial_Video_Generation

Why distribution?



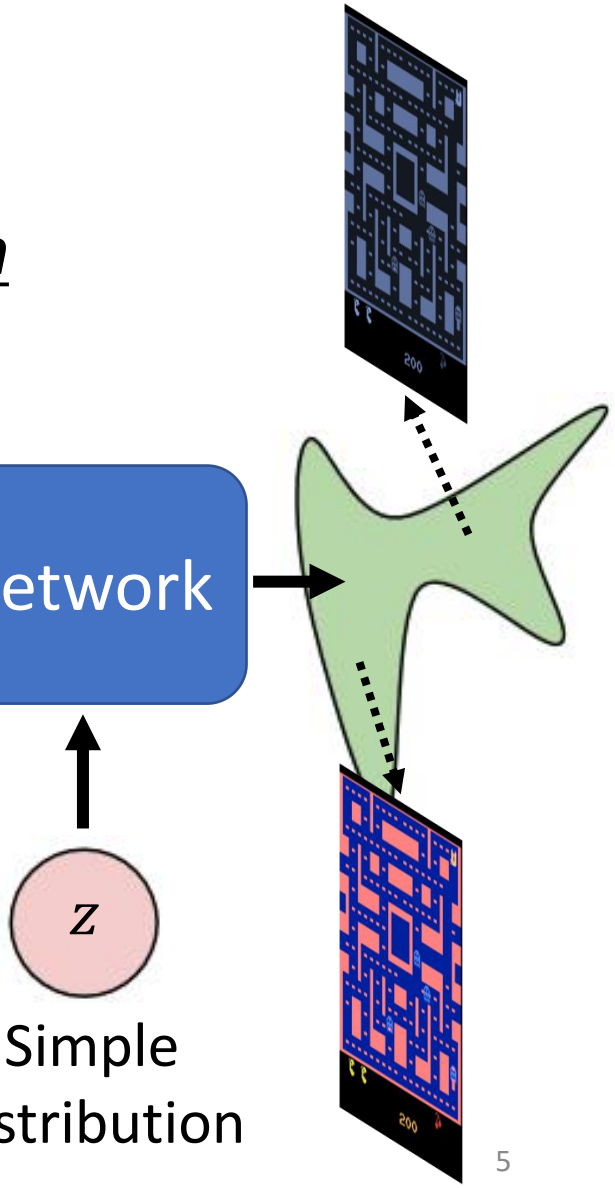
Prediction

Video Prediction



Previous frames

Network



z

Simple Distribution

Why distribution?

(The same input has different outputs.)

- Especially for the tasks needs "*creativity*"

Drawing

Character with red eyes → Network →


Chatbot

你知道辉夜是谁吗？ → Network →

她是秀知院学生会 ...

她开创了忍者时代 ...

GAN

GAN

- How to pronounce “GAN”?

Google 小姐

All Kinds of GAN …

https://github.com/hindupuravinash/the-gan-zoo

GAN

ACGAN

BGAN

CGAN

DCGAN

EBGAN

fGAN

GoGAN

⋮

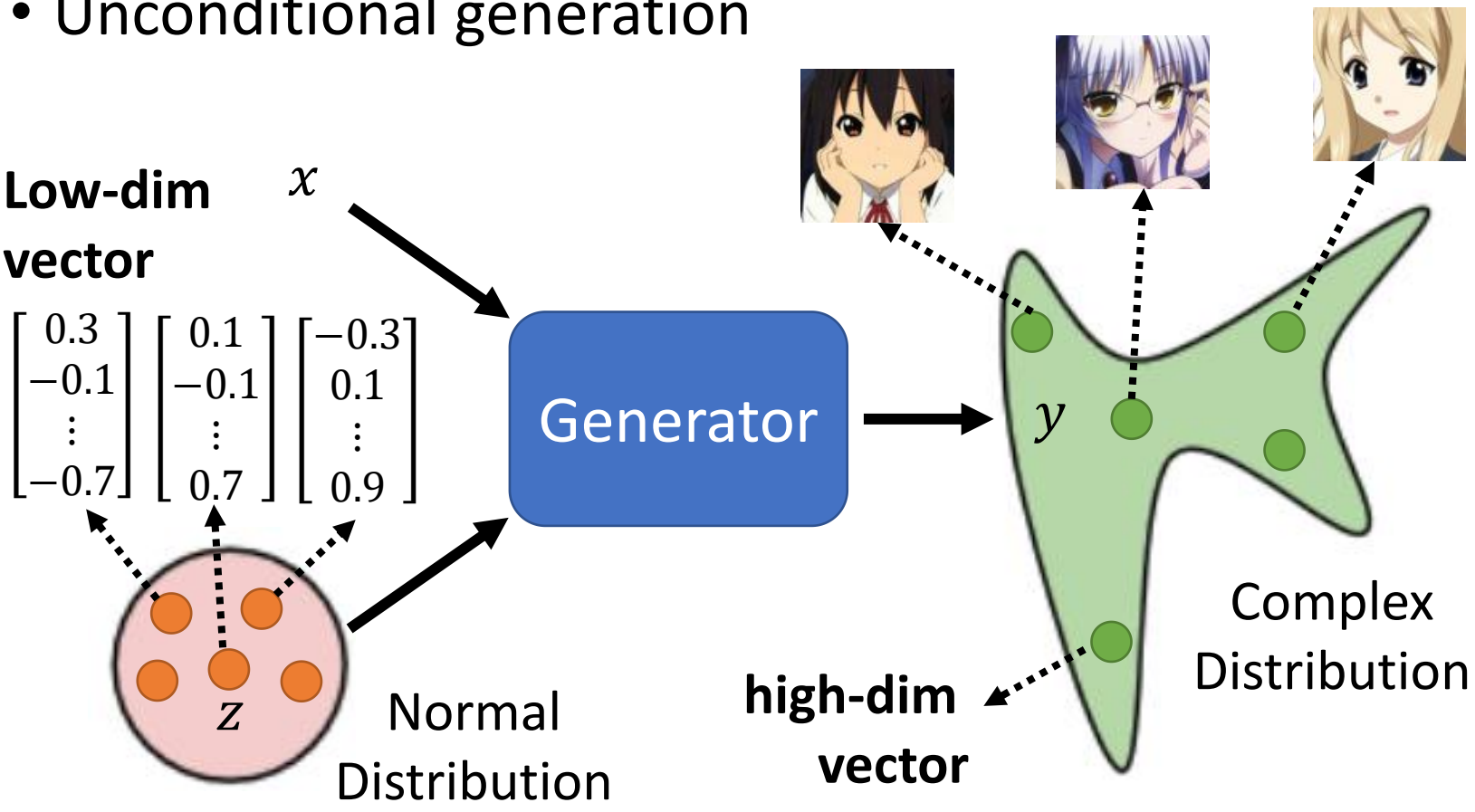
- SeUDA - Semantic-Aware Generative Adversarial Nets for Unsupervised Domain Adapt Segmentation
- SG-GAN - Semantic-aware Grad-GAN for Virtual-to-Real Urban Scene Adaption (githu
- SG-GAN - Sparsely Grouped Multi-task Generative Adversarial Networks for Facial Attr
- SGAN - Texture Synthesis with Spatial Generative Adversarial Networks
- SGAN - Stacked Generative Adversarial Networks (github)
- SGAN - Steganographic Generative Adversarial Networks
- SGAN - SGAN: An Alternative Training of Generative Adversarial Networks
- SGAN - CT Image Enhancement Using Stacked Generative Adversarial Networks and T Segmentation Improvement
- sGAN - Generative Adversarial Training for MRA Image Synthesis Using Multi-Contrast
- SiftingGAN - SiftingGAN: Generating and Sifting Labeled Samples to Improve the Rem Classification Baseline in vitro
- SiGAN - SiGAN: Siamese Generative Adversarial Network for Identity-Preserving Face H
- SimGAN - Learning from Simulated and Unsupervised Images through Adversarial Trai
- SisGAN - Semantic Image Synthesis via Adversarial Learning

Mihaela Rosca, Balaji Lakshminarayanan, David Warde-Farley, Shakir Mohamed, "Variational Approaches for Auto-Encoding Generative Adversarial Networks", arXiv, 2017

[2]We use the Greek α prefix for α-GAN, as AEGAN and most other Latin prefixes seem to have been taken https://deephunt.in/the-gan-zoo-79597dc8c347.

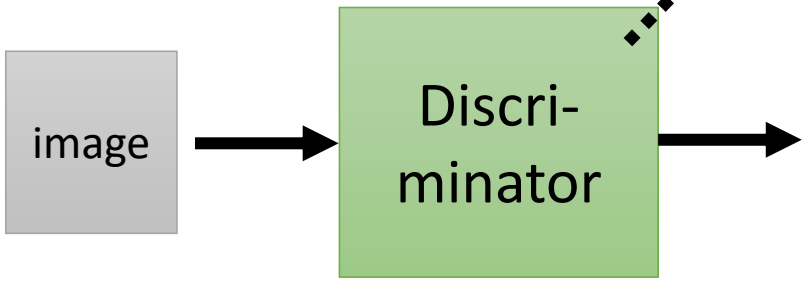
Anime Face Generation

- Unconditional generation



Discriminator

It is a neural network (that is, a function).



Scalar: Larger means real, smaller value fake.

Basic Idea of GAN

Brown

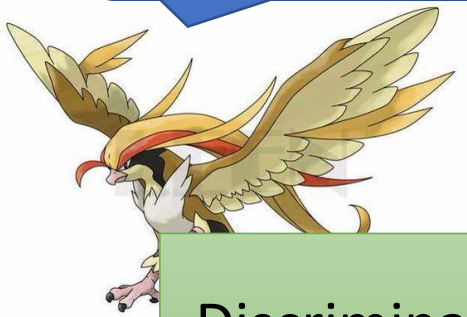
Generator

veins

Butterflies are not brown

Butterflies do not have veins

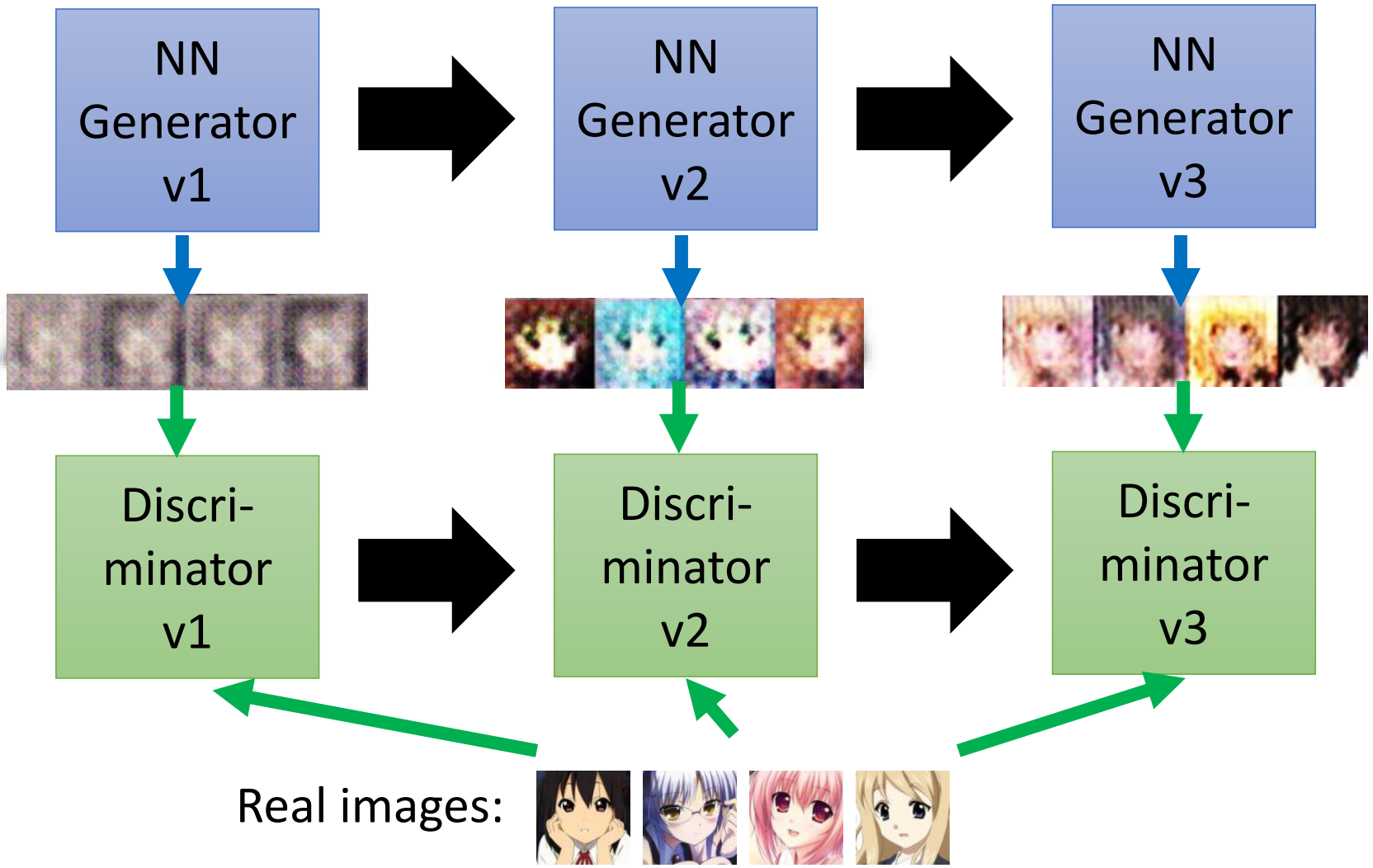
.....



Discriminator

Basic Idea of GAN

This is where the term "***adversarial***" comes from.



Basic Idea of GAN

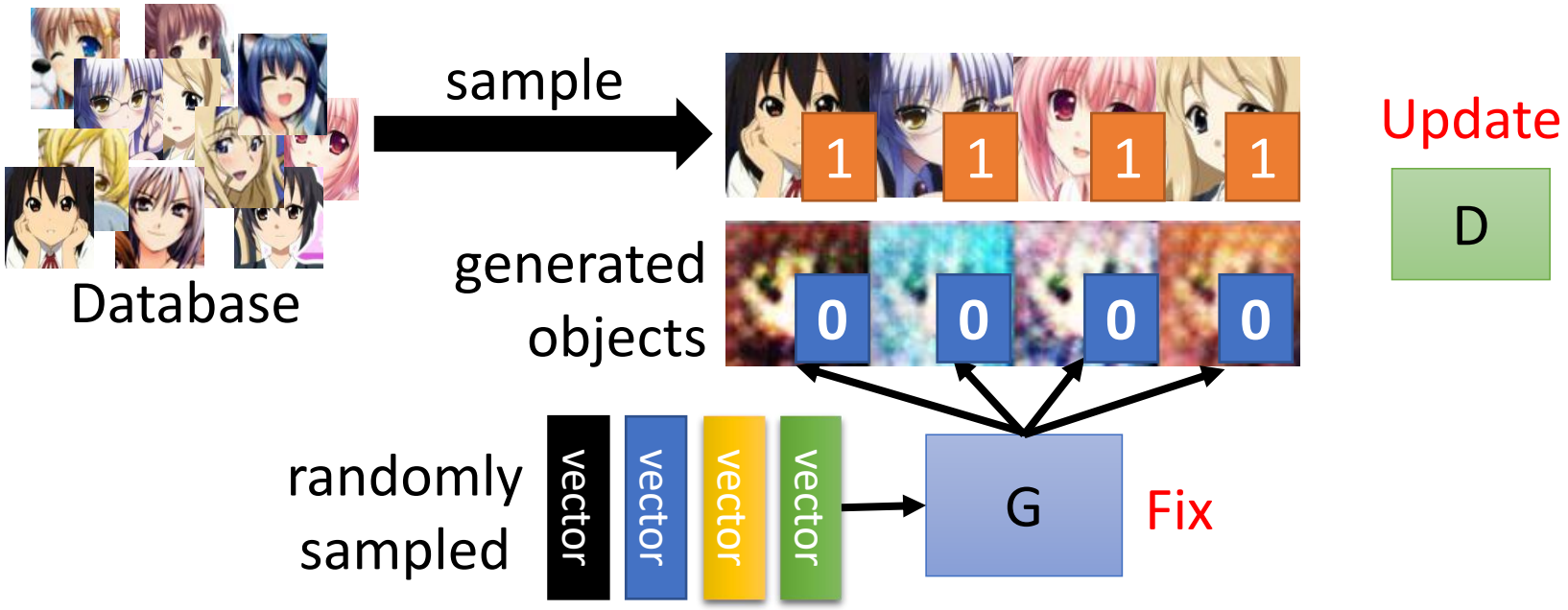
- 写作敌人，念作朋友

Algorithm

- Initialize generator and discriminator

- In each training iteration:

Step 1: Fix generator G, and update discriminator D



Discriminator learns to assign high scores to real objects and low scores to generated objects.

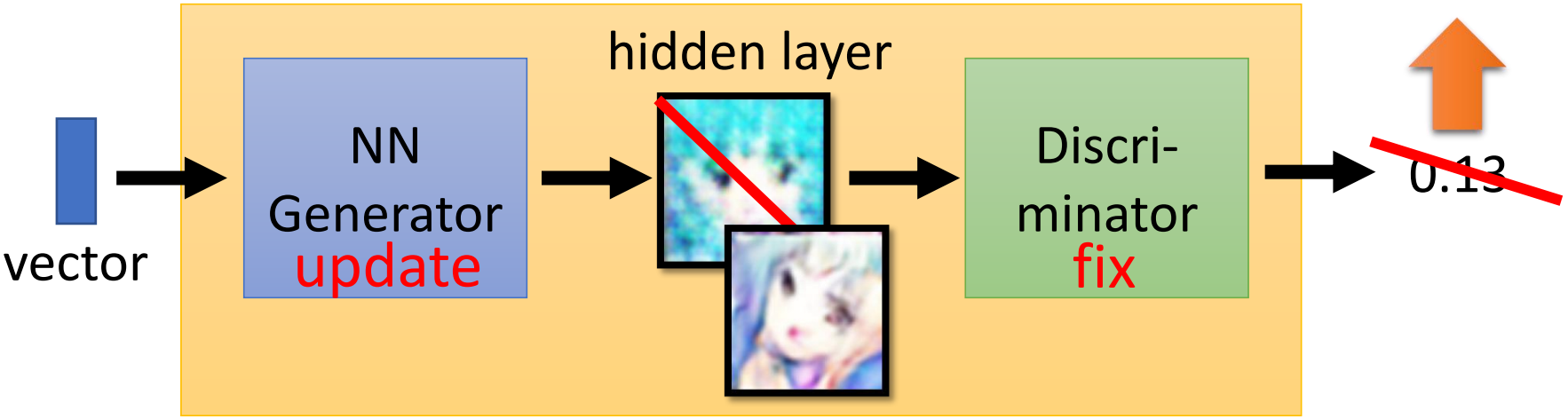
Algorithm

- Initialize generator and discriminator

- In each training iteration:

Step 2: Fix discriminator D, and update generator G

Generator learns to "fool" the discriminator

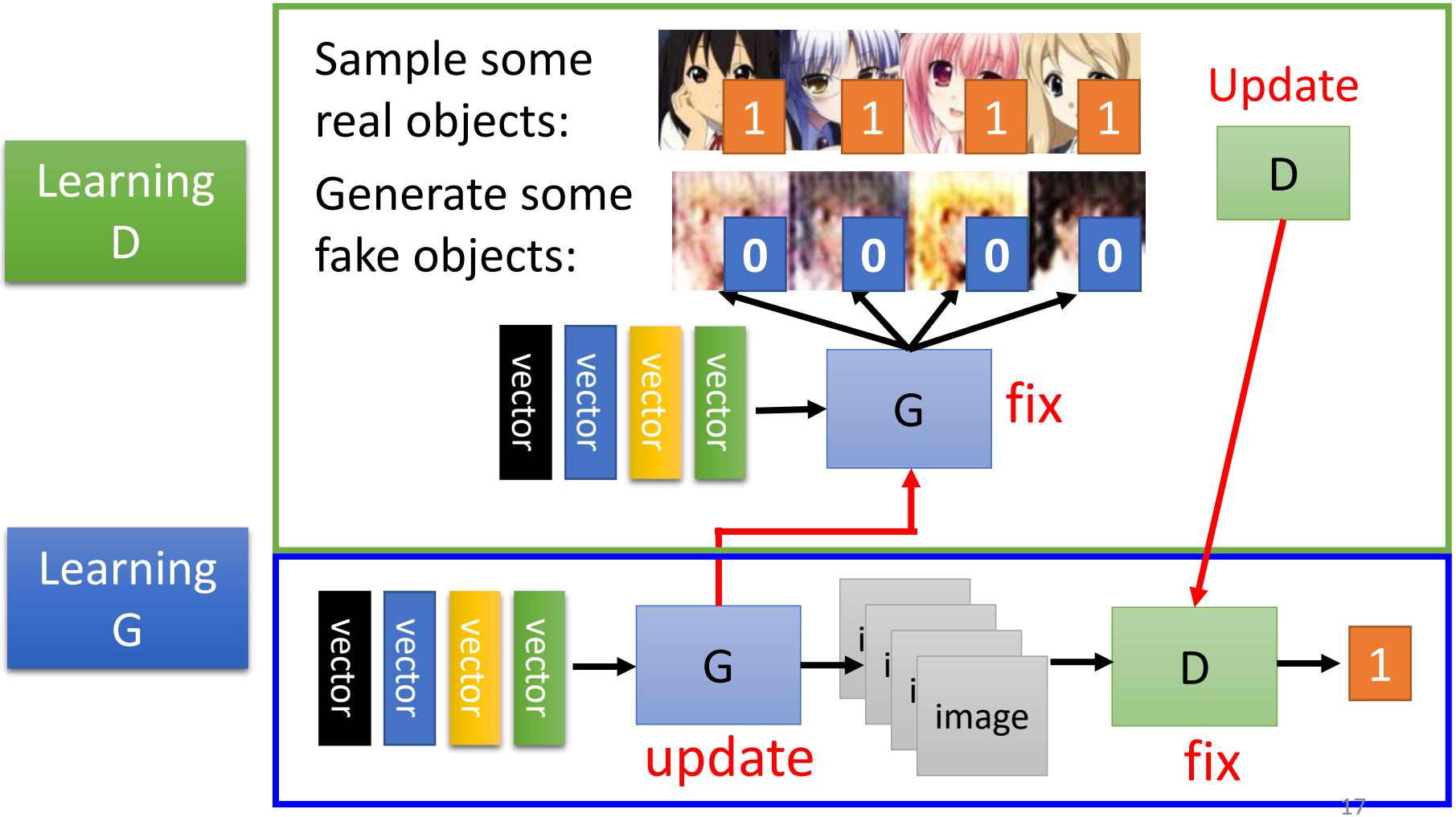


large network

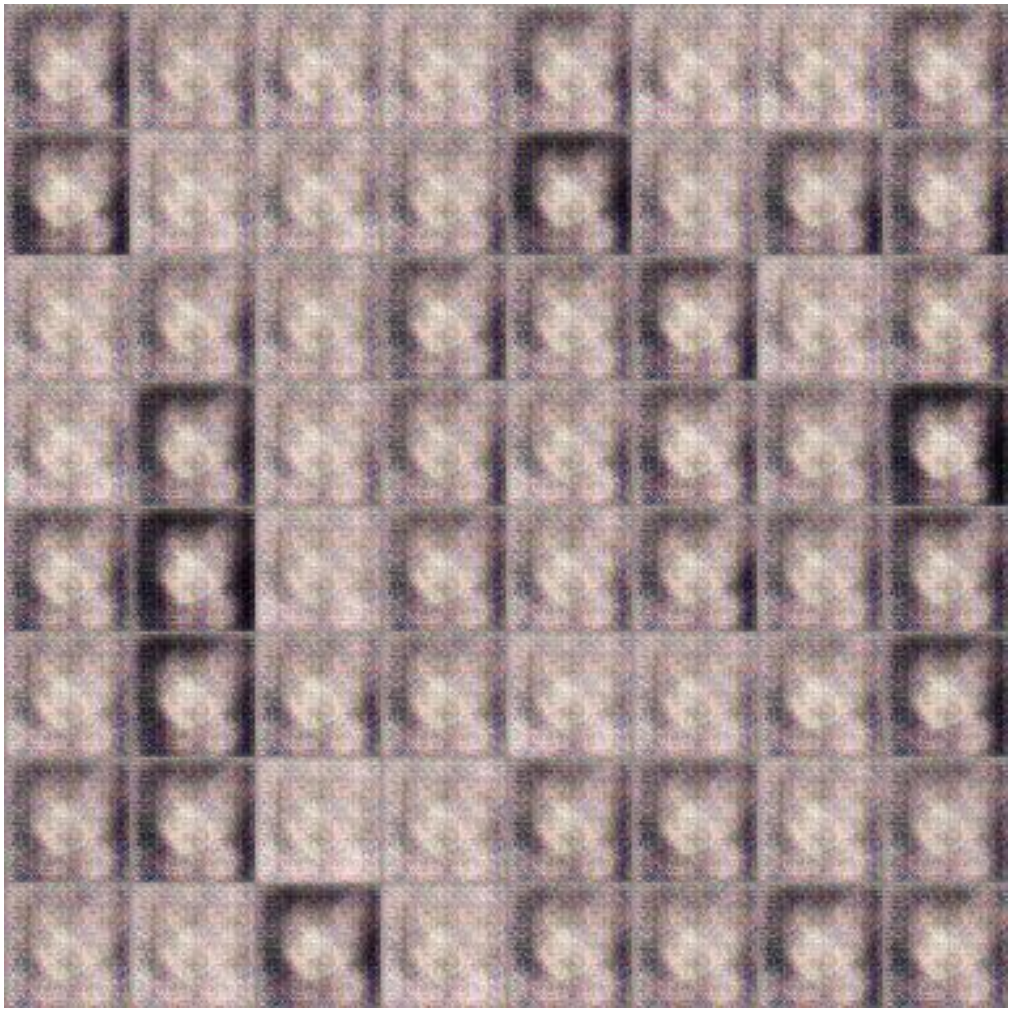
Algorithm

- Initialize generator and discriminator

- In each training iteration:



Anime Face Generation



100 updates

Source of training data: https://zhuanlan.zhihu.com/p/24767059

Anime Face Generation

1000 updates

Anime Face Generation

2000 updates

Anime Face Generation

5000 updates

Anime Face Generation

10,000 updates

Anime Face Generation

20,000 updates

Anime Face Generation

50,000 updates

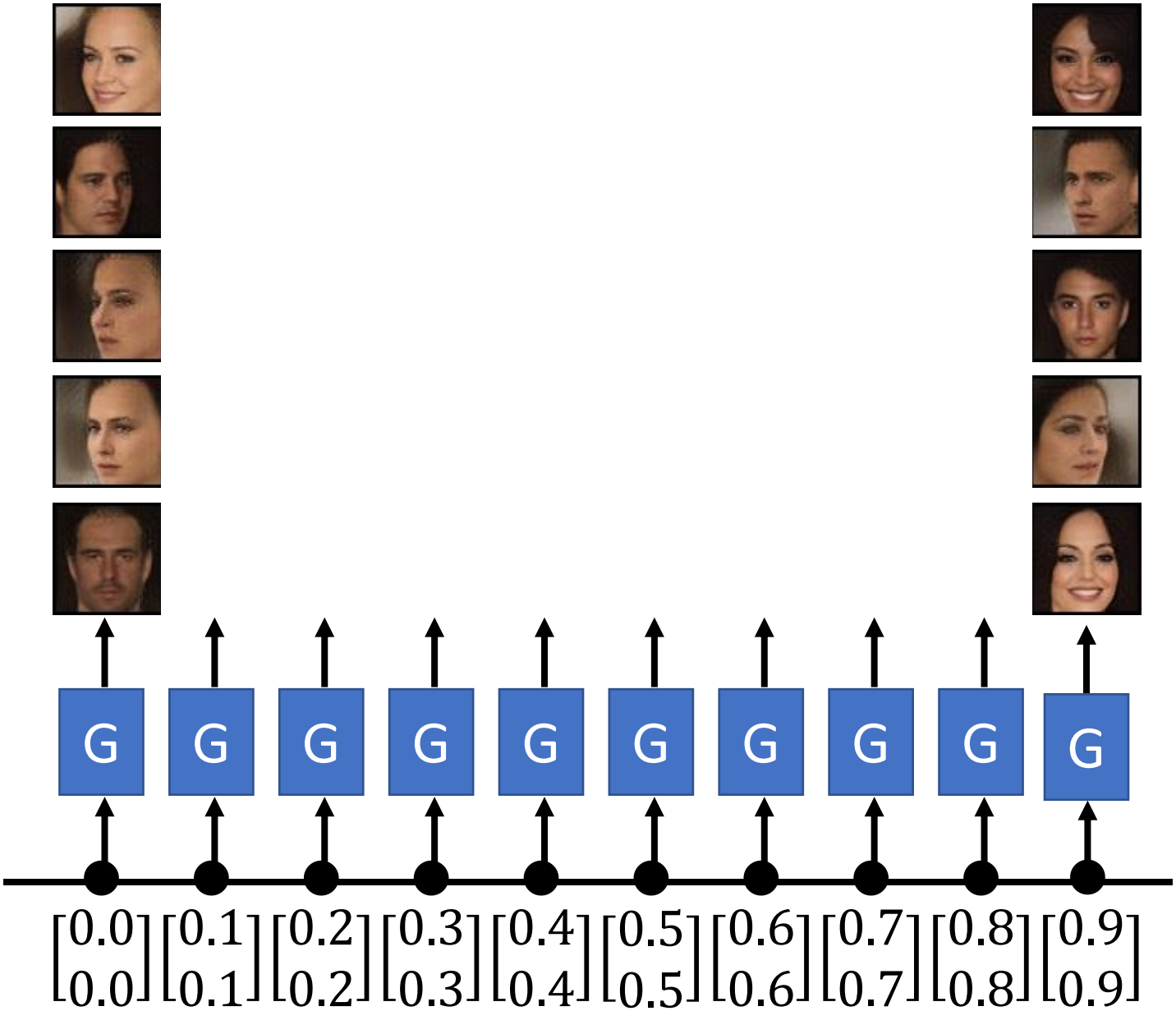
The faces generated by machine.

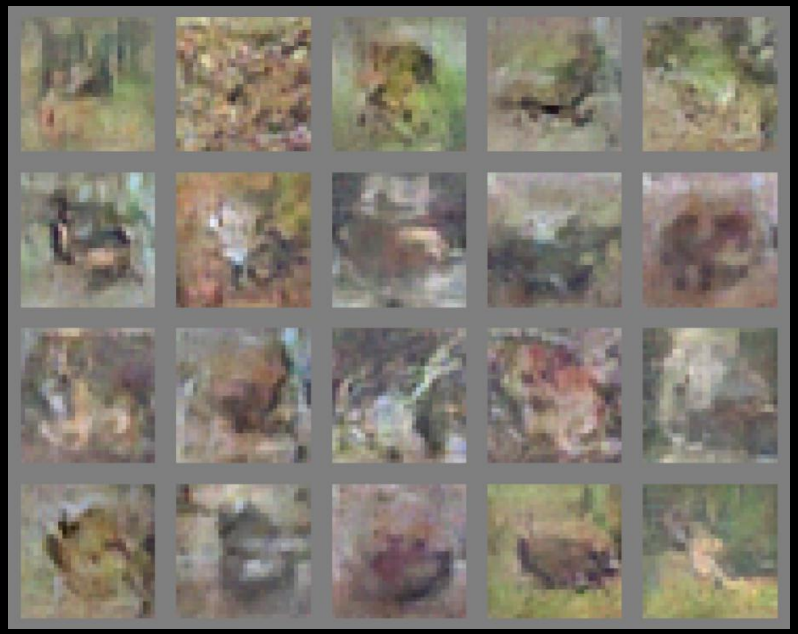
In 2019, with StyleGAN ……

Source of video:
https://www.gwern.net/Faces

Progressive GAN

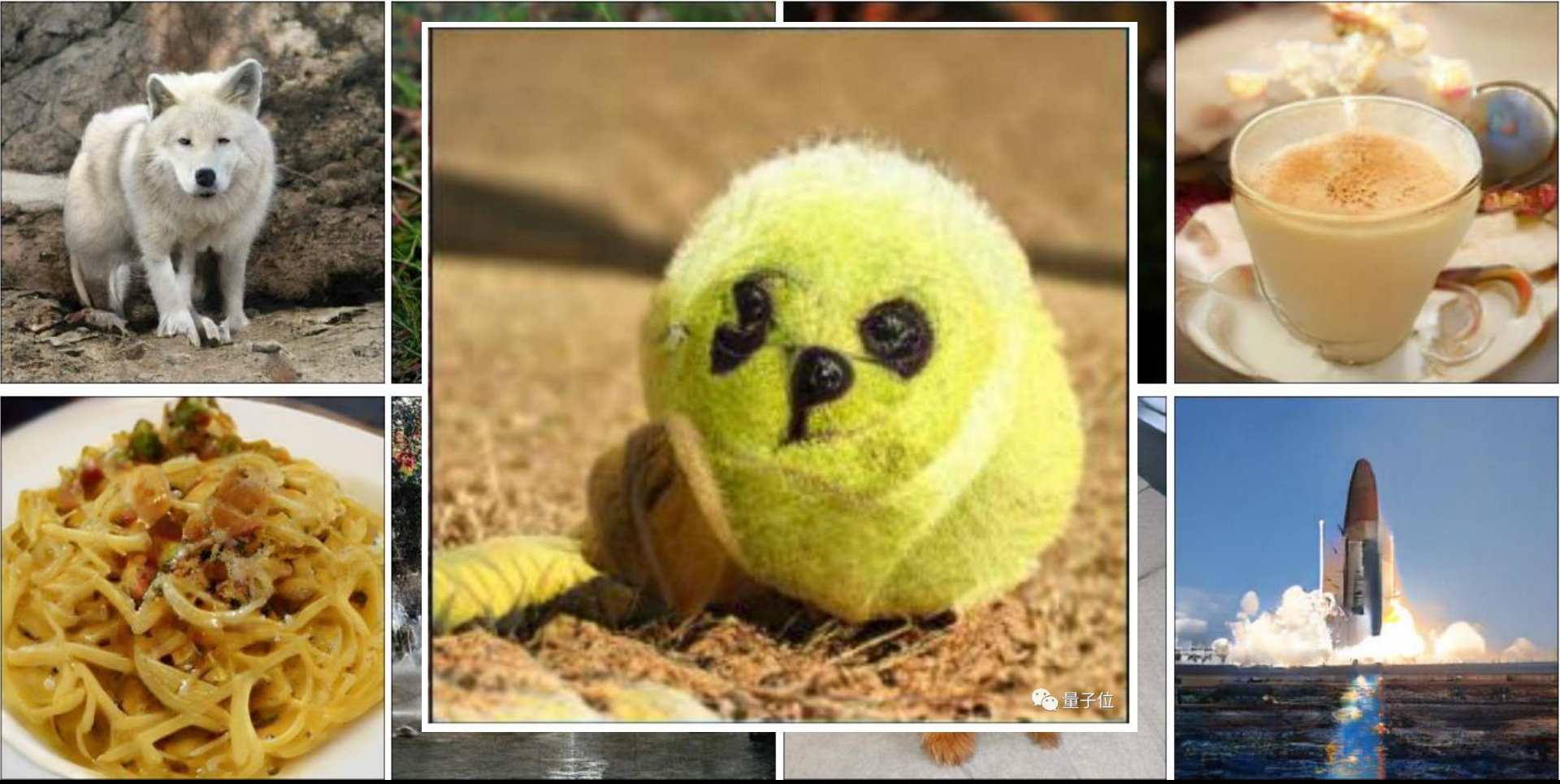
https://arxiv.org/abs/1710.10196


G G G G G G G G G G
[0.0 0.0] [0.1 0.1] [0.2 0.2] [0.3 0.3] [0.4 0.4] [0.5 0.5] [0.6 0.6] [0.7 0.7] [0.8 0.8] [0.9 0.9]



The first GAN

https://arxiv.org/abs/1406.2661 (Ian J. Goodfellow)



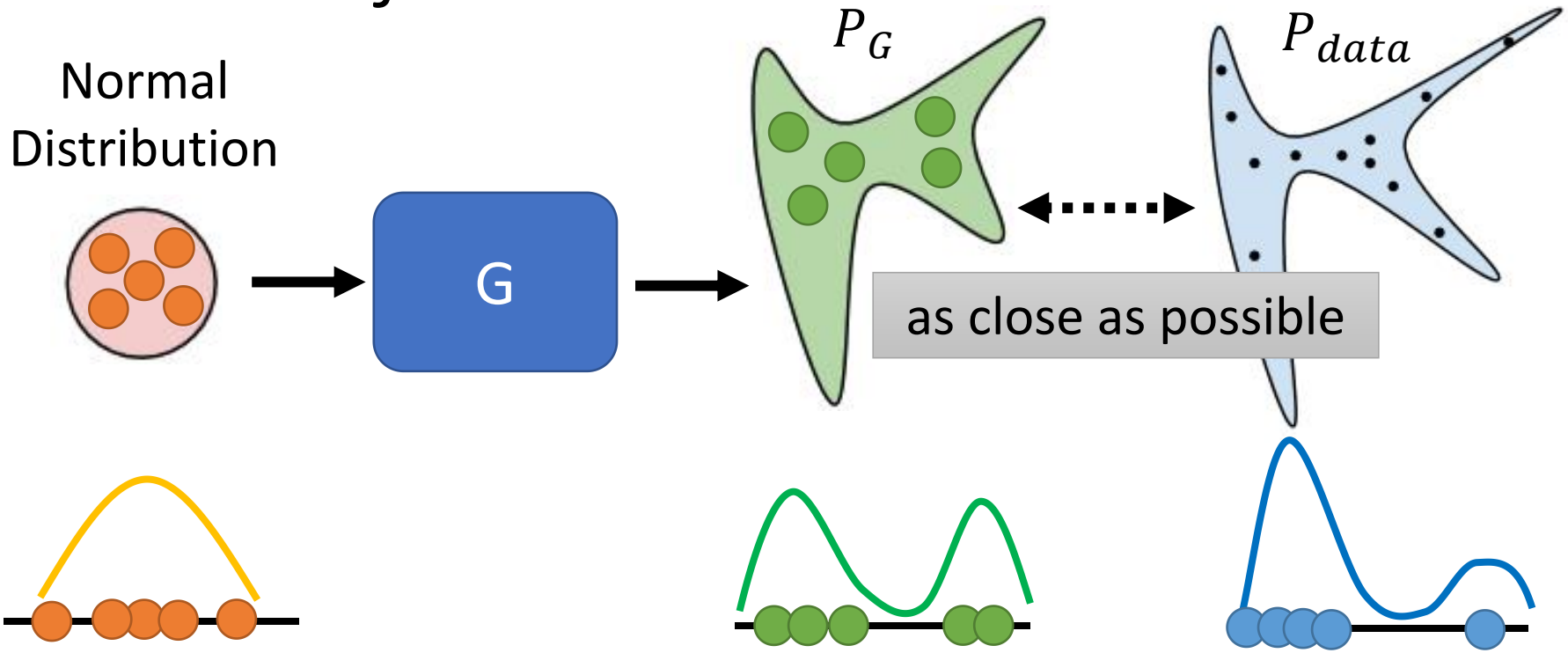
Today …… BigGAN

https://arxiv.org/abs/1809.11096

Theory behind GAN

c.f. $w^*, b^* = arg\min_{w,b} L$

Our Objective



$$G^* = arg\min_G \underline{Div(P_G, P_{data})}$$

Divergence between distributions P_G and P_{data}

How to compute the divergence?

Sampling is good enough ……

$$G^* = arg\min_G Div(P_G, P_{data})$$

Although we do not know the distributions of P_G and P_{data}, we can sample from them.

Database

sample

Sampling from P_{data}

sample from normal

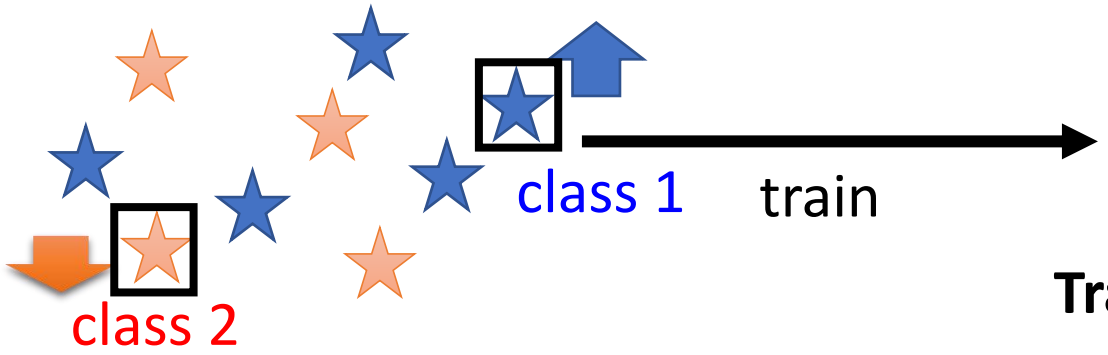
G

Sampling from P_G

https://arxiv.org/abs/1406.2661

Discriminator $G^* = arg\min_G Div(P_G, P_{data})$

★ : data sampled from P_{data} ★ : data sampled from P_G



Train a binary classifier

Training: $D^* = arg\max_D V(D, G)$

The value is related to JS divergence.

Objective Function for D

$$V(G, D) = E_{y \sim P_{data}}[logD(y)] + E_{y \sim P_G}[log(1 - D(y))]$$

$D^* = arg\max_D V(D, G)$

negative cross entropy

=

Training classifier:
minimize cross entropy

Discriminator

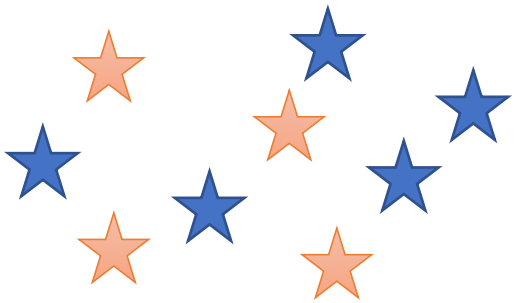
$$G^* = arg\min_G Div(P_G, P_{data})$$

: data sampled from P_{data}

: data sampled from P_G

Training:

$$D^* = arg\max_D V(D, G)$$



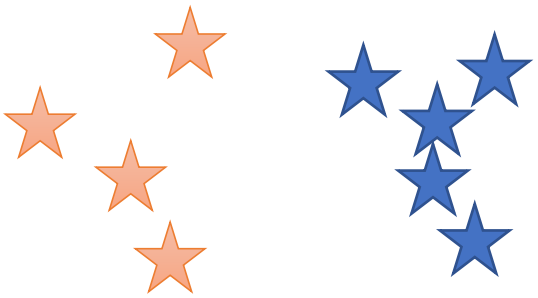
small divergence

train

Discriminator

hard to discriminate

Small $\max_D V(D, G)$



large divergence

train

Discriminator

easy to discriminate

$$G^* = arg\min_G L \max_D V(G,D)$$

$$D^* = arg\max_D V(D,G)$$

The maximum objective value is related to JS divergence.

- Initialize generator and discriminator
- In each training iteration:

  Step 1: Fix generator G, and update discriminator D

  Step 2: Fix discriminator D, and update generator G

Can we use other divergence?

Name	$D_f(P\|Q)$	Generator $f(u)$
Total variation	$\frac{1}{2}\int \lvert p(x)-q(x)\rvert \,\mathrm{d}x$	$\frac{1}{2}\lvert u-1\rvert$
Kullback-Leibler	$\int p(x)\log\frac{p(x)}{q(x)}\,\mathrm{d}x$	$u\log u$
Reverse Kullback-Leibler	$\int q(x)\log\frac{q(x)}{p(x)}\,\mathrm{d}x$	$-\log u$
Pearson χ^2	$\int \frac{(q(x)-p(x))^2}{p(x)}\,\mathrm{d}x$	$(u-1)^2$
Neyman χ^2	$\int \frac{(p(x)-q(x))^2}{q(x)}\,\mathrm{d}x$	$\frac{(1-u)^2}{u}$
Squared Hellinger	$\int \left(\sqrt{p(x)}-\sqrt{q(x)}\right)^2\,\mathrm{d}x$	$\left(\sqrt{u}-1\right)^2$
Jeffrey	$\int (p(x)-q(x))\log\left(\frac{p(x)}{q(x)}\right)\,\mathrm{d}x$	$(u-1)\log u$
Jensen-Shannon	$\frac{1}{2}\int p(x)\log\frac{2p(x)}{p(x)+q(x)}+q(x)\log\frac{2q(x)}{p(x)+q(x)}\,\mathrm{d}x$	$-(u+1)\log\frac{1+u}{2}+u\log u$
Jensen-Shannon-weighted	$\int p(x)\pi\log\frac{p(x)}{\pi p(x)+(1-\pi)q(x)}+(1-\pi)q(x)\log\frac{q(x)}{\pi p(x)+(1-\pi)q(x)}\,\mathrm{d}x$	$\pi u\log u-(1-\pi+\pi u)\log(1-\pi+\pi u)$
GAN	$\int p(x)\log\frac{2p(x)}{p(x)+q(x)}+q(x)\log\frac{2q(x)}{p(x)+q(x)}\,\mathrm{d}x-\log(4)$	$u\log u-(u+1)\log(u+1)$

Using the divergence you like ☺

https://arxiv.org/abs/1606.00709

Name	Conjugate $f^*(t)$
Total variation	t
Kullback-Leibler (KL)	$\exp(t-1)$
Reverse KL	$-1-\log(-t)$
Pearson χ^2	$\frac{1}{4}t^2+t$
Neyman χ^2	$2-2\sqrt{1-t}$
Squared Hellinger	$\frac{t}{1-t}$
Jeffrey	$W(e^{1-t})+\frac{1}{W(e^{1-t})}+t-2$
Jensen-Shannon	$-\log(2-\exp(t))$
Jensen-Shannon-weighted	$(1-\pi)\log\frac{1-\pi}{1-\pi e^{t/\pi}}$
GAN	$-\log(1-\exp(t))$

GAN is difficult to train ……

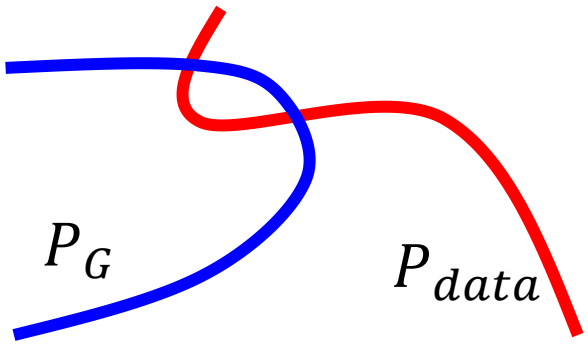
Tips for GAN

JS divergence is not suitable

- In most cases, P_G and P_{data} are not overlapped.
- 1. The nature of data

  Both P_{data} and P_G are low-dim manifold in high-dim space.

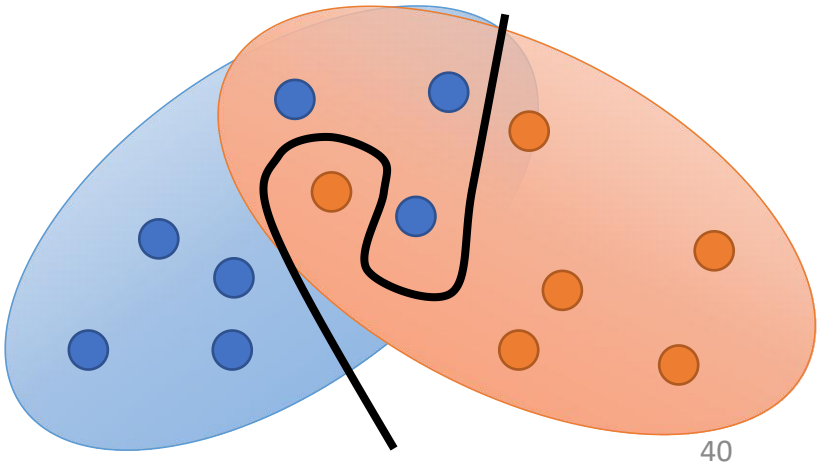
  The overlap can be ignored.



- 2. Sampling

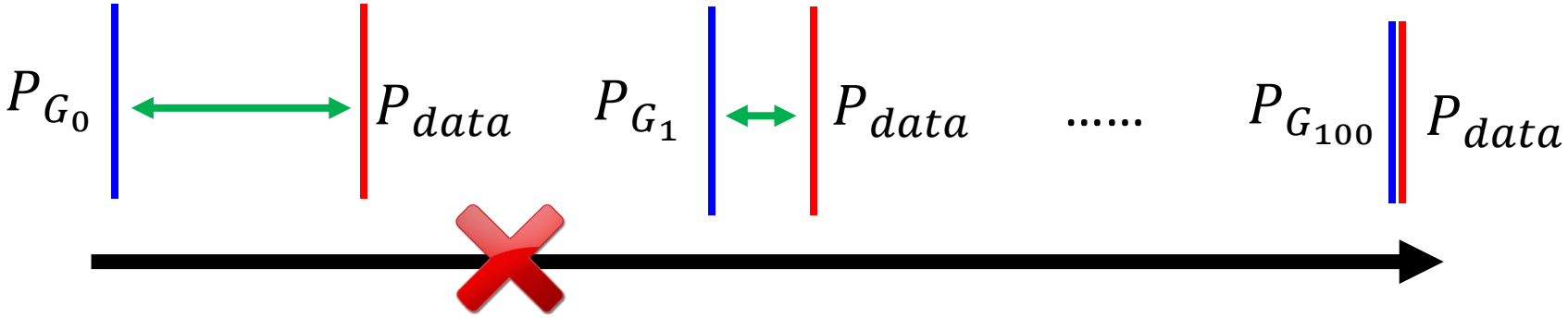
  Even though P_{data} and P_G have overlap.

  If you do not have enough sampling ……



What is the problem of JS divergence?

JS divergence is always log2 if two distributions do not overlap.

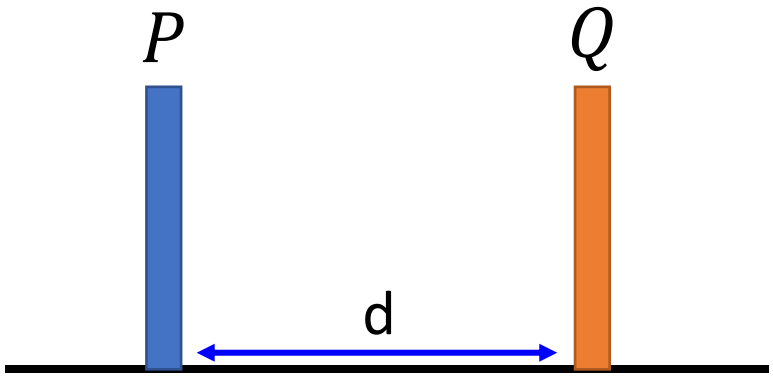


Intuition: If two distributions do not overlap, binary classifier achieves 100% accuracy.

The accuracy (or loss) means nothing during GAN training.

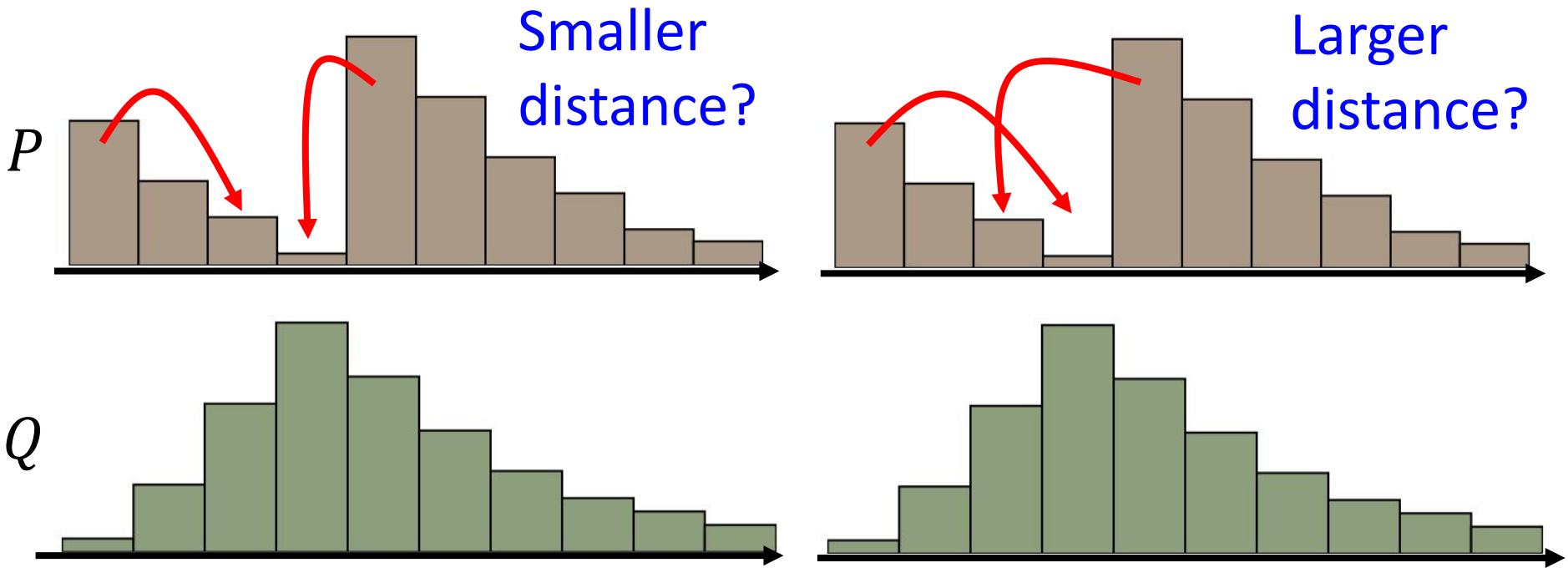
Wasserstein distance

- Considering one distribution P as a pile of earth, and another distribution Q as the target
- The average distance the earth mover has to move the earth.



$$W(P, Q) = d$$

Wasserstein distance

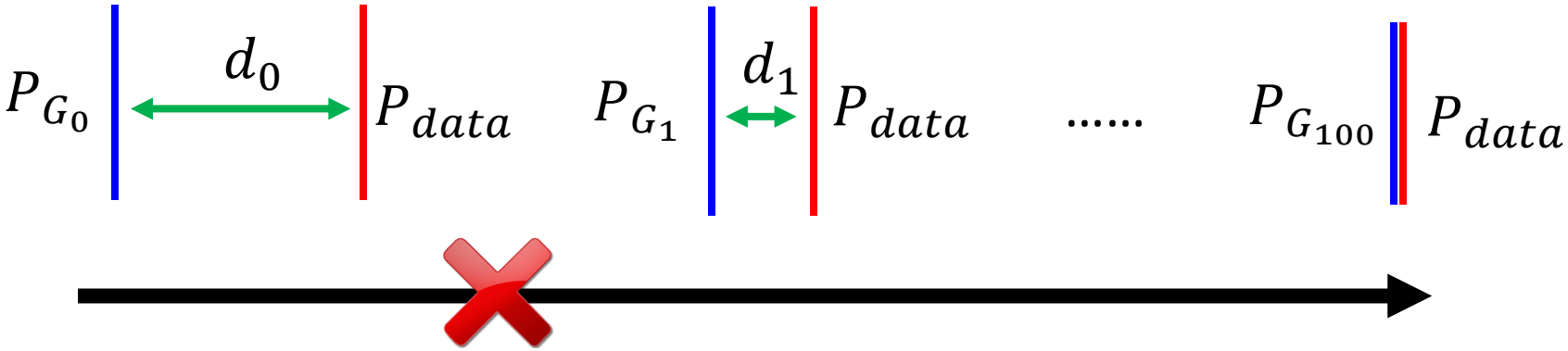


There are many possible “moving plans”.

Using the “moving plan” with the smallest average distance to define the Wasserstein distance.

Source of image: https://vincentherrmann.github.io/blog/wasserstein/

What is the problem of JS divergence?



$JS(P_{G_0}, P_{data}) = log2$

$JS(P_{G_1}, P_{data}) = log2$

..... $JS(P_{G_{100}}, P_{data}) = 0$

$W(P_{G_0}, P_{data}) = d_0$

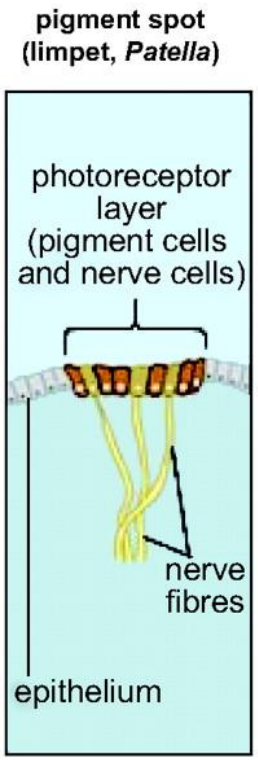
$W(P_{G_1}, P_{data}) = d_1$

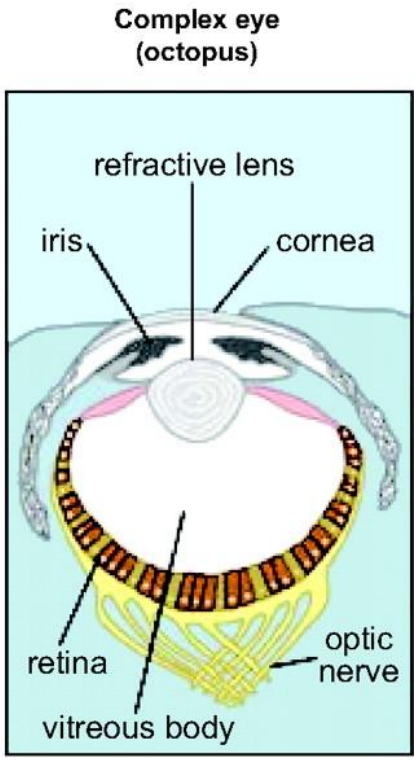
..... $W(P_{G_{100}}, P_{data}) = 0$

Better!

What is the problem of JS divergence?

P_{G_0} d_0 P_{data} P_{G_1} d_1 P_{data} ..... $P_{G_{100}}$ P_{data}





https://www.pnas.org/content/104/suppl_1/8567.figures-only

https://arxiv.org/abs/1701.07875

WGAN

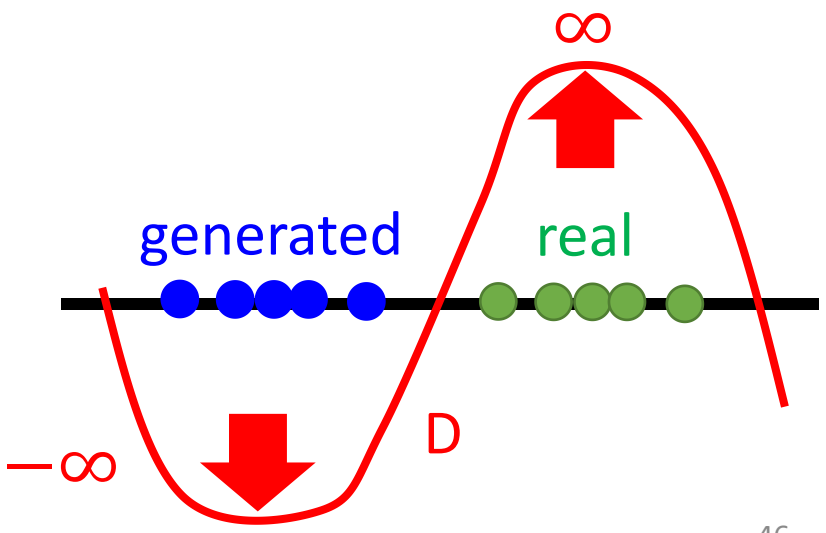
Evaluate Wasserstein distance between P_{data} and P_G

$$\max_{D \in 1-Lipschitz} \left\{ E_{y \sim P_{data}}[D(y)] - E_{y \sim P_G}[D(y)] \right\}$$

D has to be smooth enough. How to fulfill this constraint?

Without the constraint, the training of D will not converge.

Keeping the D smooth forces D(y) become ∞ and $-\infty$



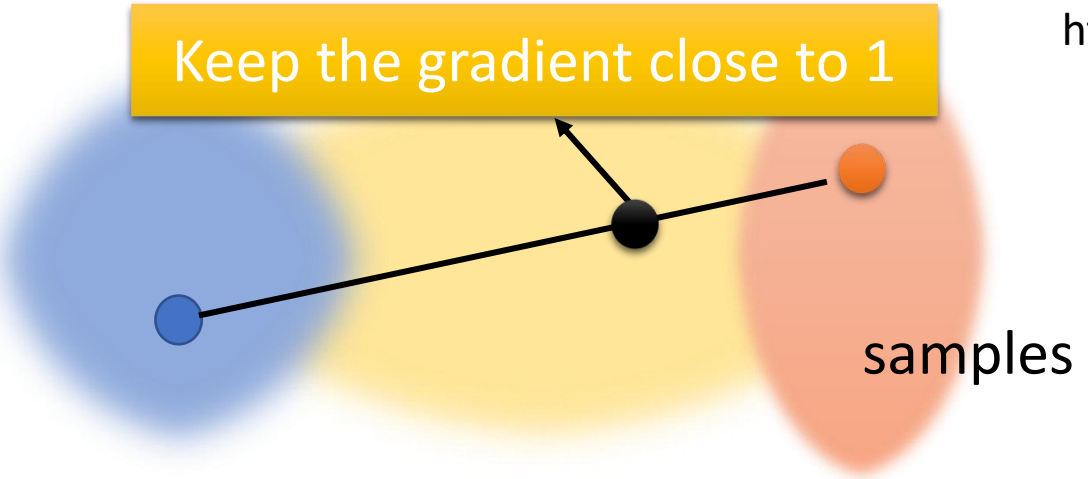
$$\max_{D \in 1-Lipschitz} \left\{ E_{y \sim P_{data}}[D(y)] - E_{y \sim P_G}[D(y)] \right\}$$

- Original WGAN → Weight

  Force the parameters w between c and -c

  After parameter update, if w > c, w = c; if w < -c, w = -c

- Improved WGAN → Gradient Penalty



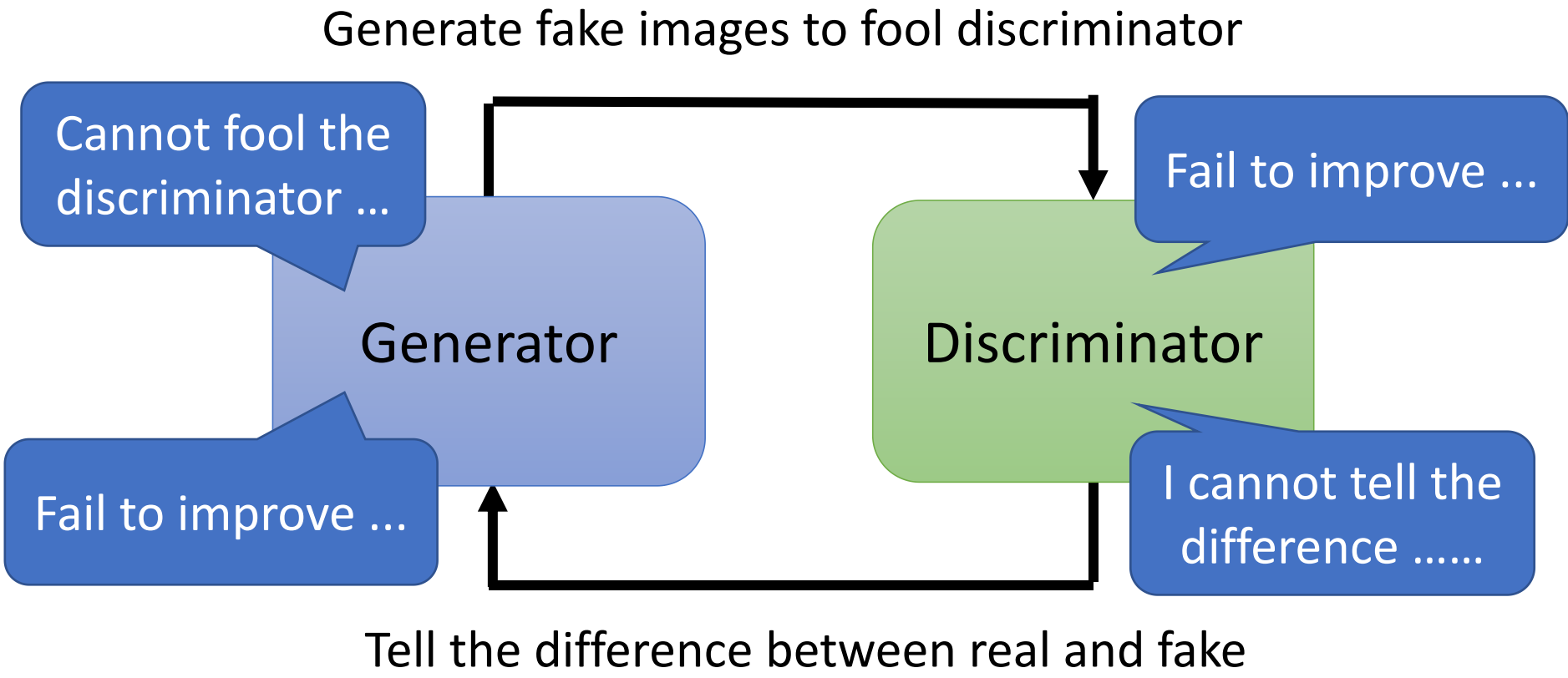
https://arxiv.org/abs/1704.00028

- Spectral Normalization → Keep gradient norm smaller than 1 everywhere

https://arxiv.org/abs/1802.05957

GAN is still challenging …

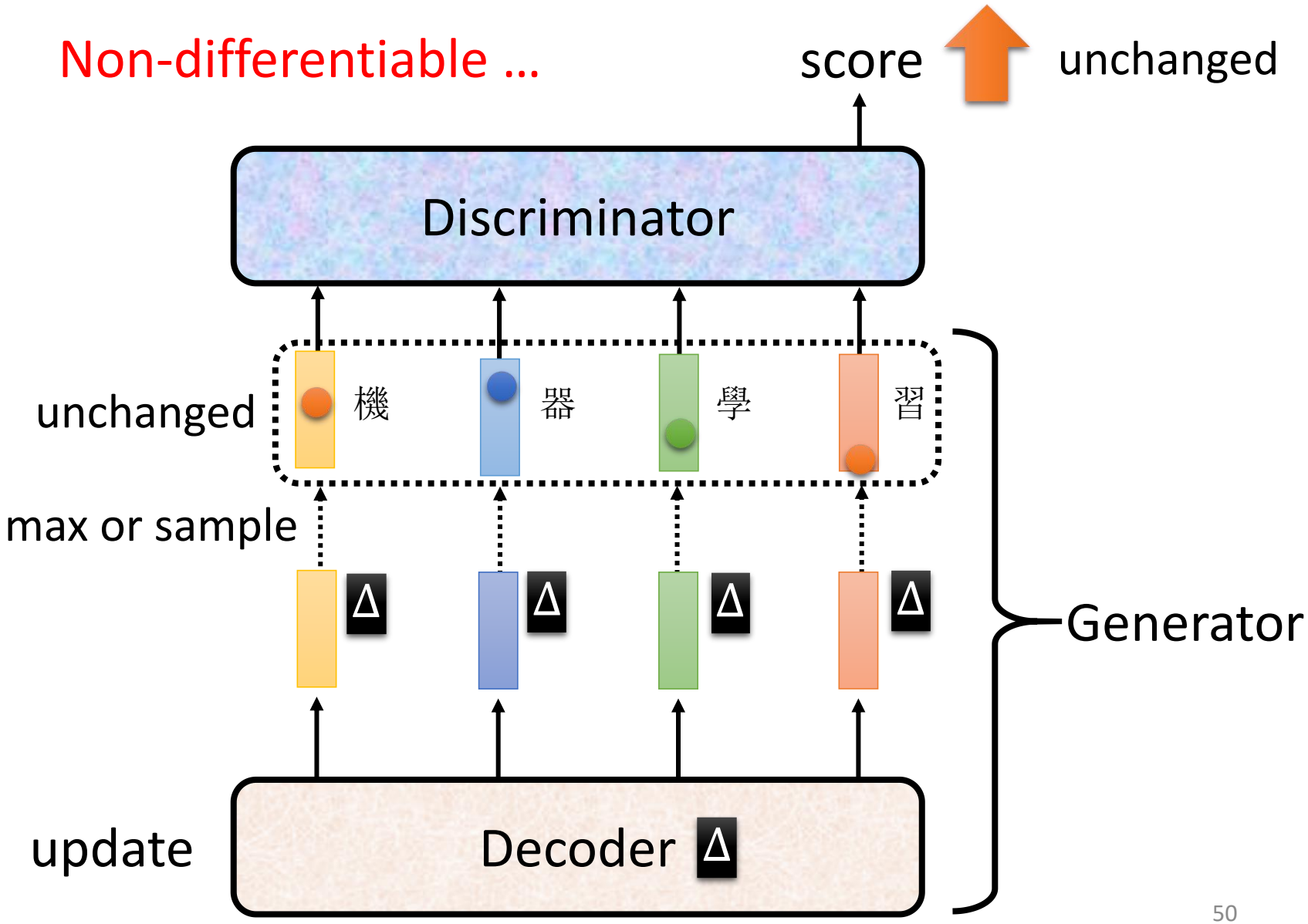
- Generator and Discriminator needs to match each other



More Tips

- Tips from Soumith
  - https://github.com/soumith/ganhacks
- Tips in DCGAN: Guideline for network architecture design for image generation
  - https://arxiv.org/abs/1511.06434
- Improved techniques for training GANs
  - https://arxiv.org/abs/1606.03498
- Tips from BigGAN
  - https://arxiv.org/abs/1809.11096

GAN for Sequence Generation

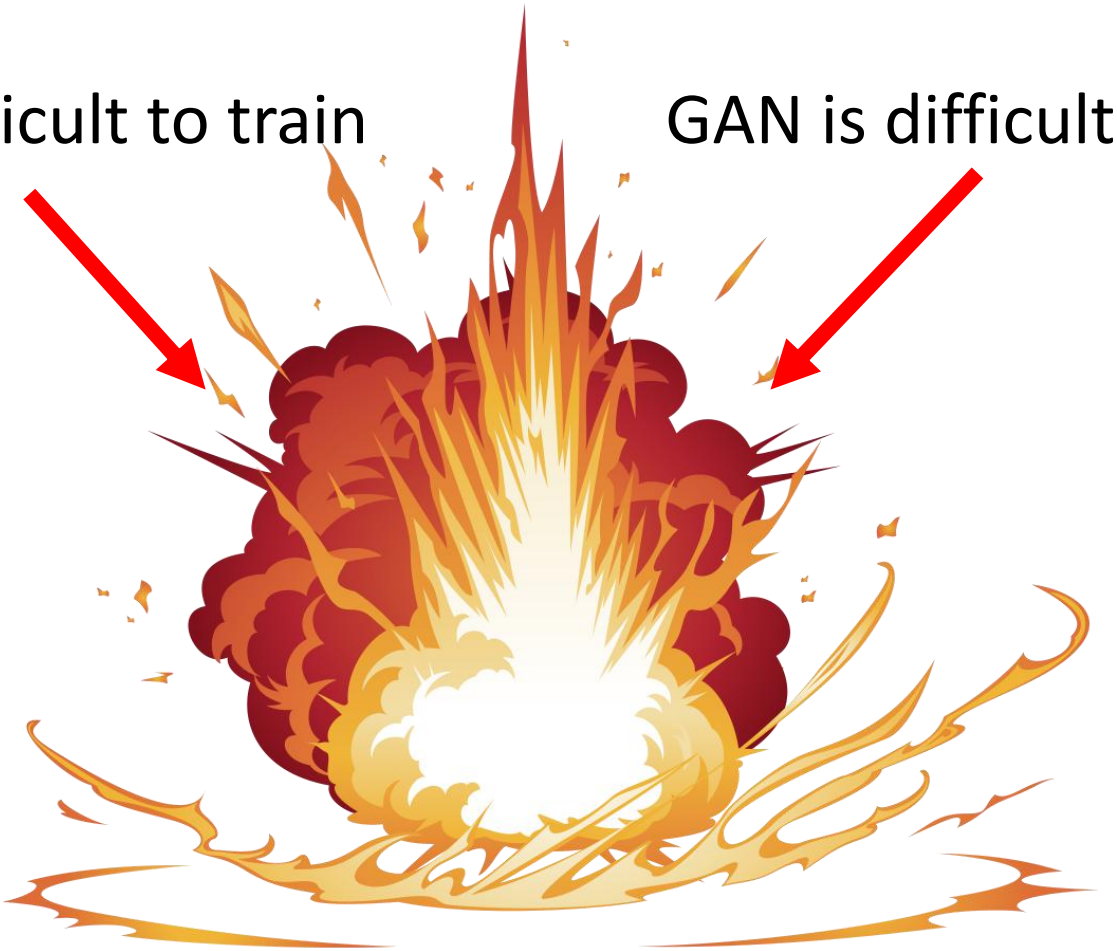


GAN for Sequence Generation

Reinforcement learning (RL) is involved ……

RL is difficult to train

GAN is difficult to train



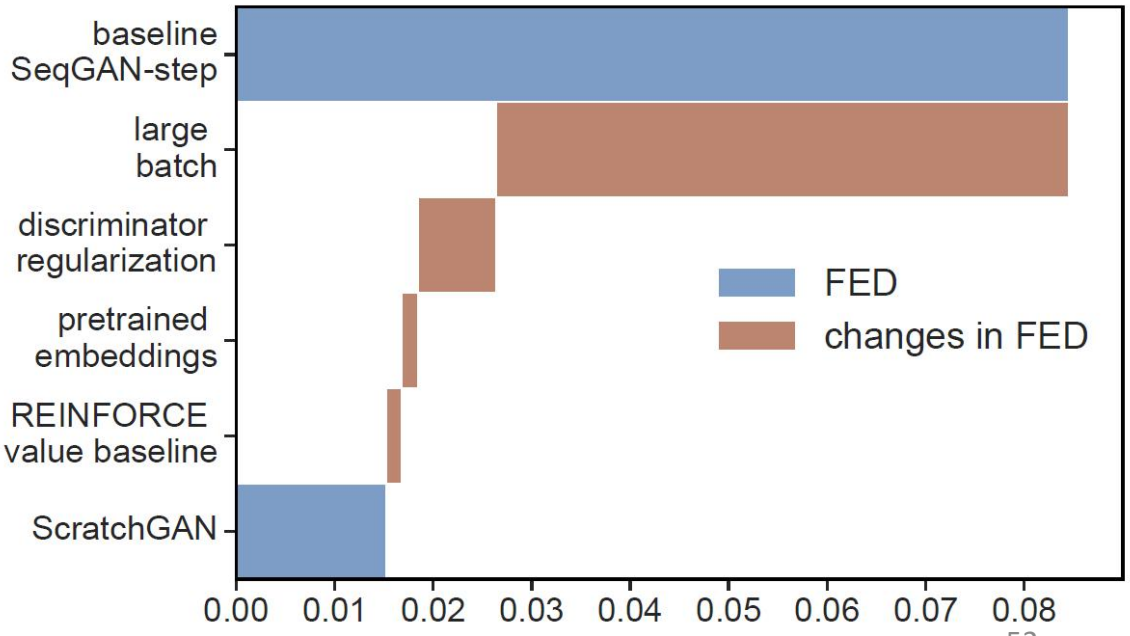
Sequence Generation GAN (RL+GAN)

GAN for Sequence Generation

- Usually, the generator are fine-tuned from a model learned by other approaches.
- However, with enough hyperparameter-tuning and tips, ScarchGAN can train from scratch.

Training language GANs from Scratch

https://arxiv.org/abs/1905.09922



Possible Solution?

$$\begin{bmatrix} 0.3 \\ -0.1 \\ \vdots \\ -0.7 \end{bmatrix}$$

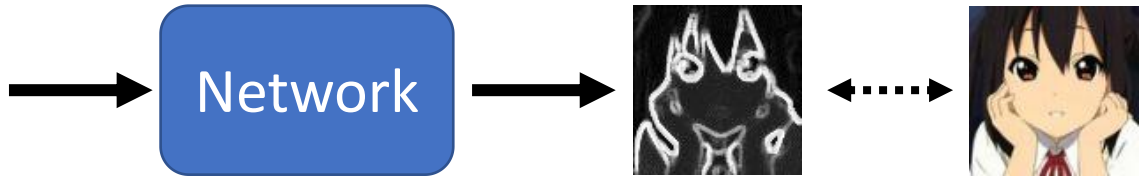
$$\begin{bmatrix} 0.1 \\ -0.1 \\ \vdots \\ 0.7 \end{bmatrix}$$

$$\begin{bmatrix} -0.3 \\ 0.1 \\ \vdots \\ 0.9 \end{bmatrix}$$

$$\begin{bmatrix} 0.7 \\ 0.1 \\ \vdots \\ -0.9 \end{bmatrix}$$

$$\begin{bmatrix} -0.1 \\ 0.8 \\ \vdots \\ 0.8 \end{bmatrix}$$

$$\begin{bmatrix} 0.3 \\ -0.1 \\ \vdots \\ -0.7 \end{bmatrix}$$



Using typical learning approaches?

Generative Latent Optimization (GLO), https://arxiv.org/abs/1707.05776

Gradient Origin Networks, https://arxiv.org/abs/2007.02798

Conditional Generation

Text-to-image

red eyes
black hair

yellow hair
dark circles

x

red eyes

Generator

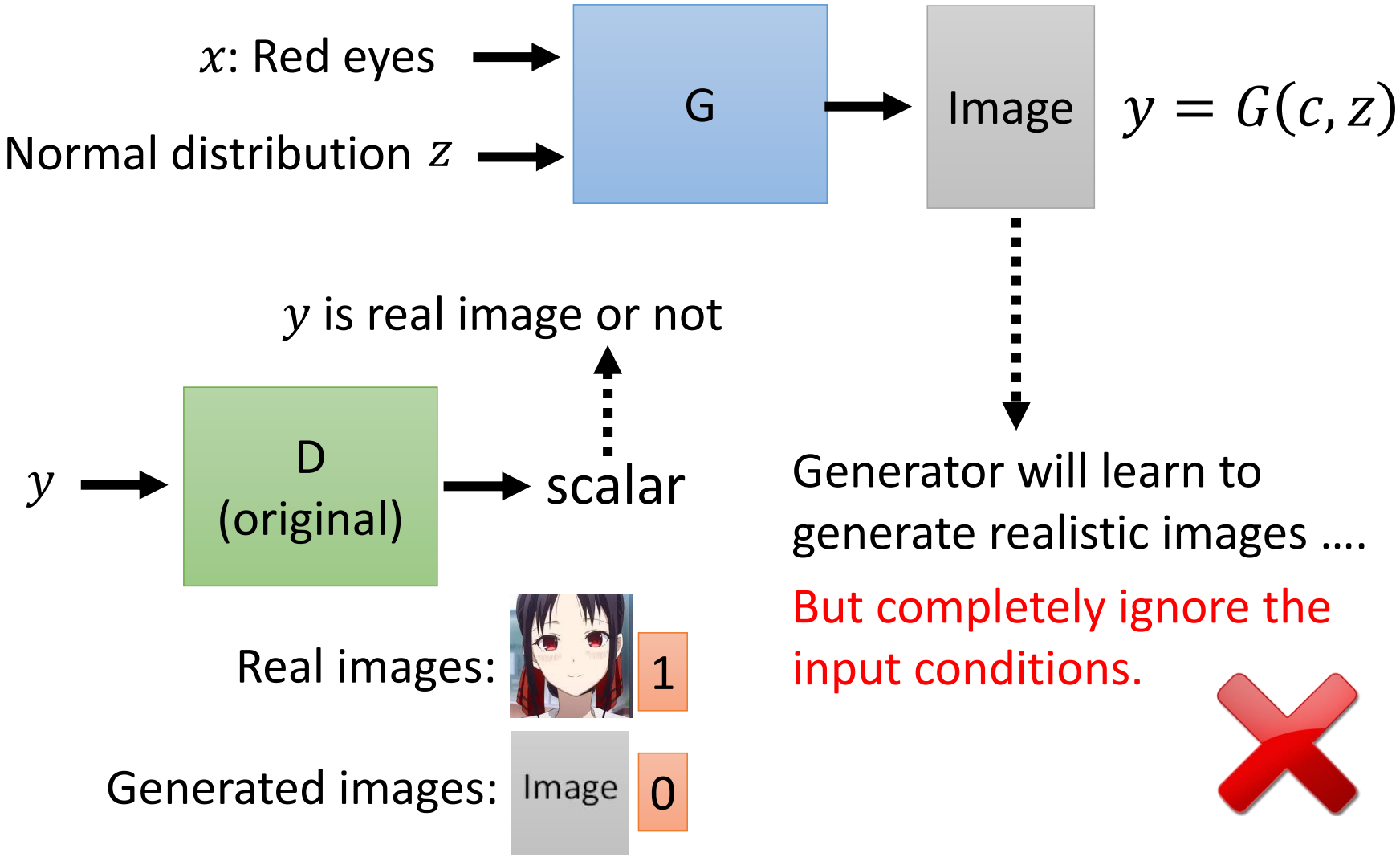
y

z

red hair,
green eyes

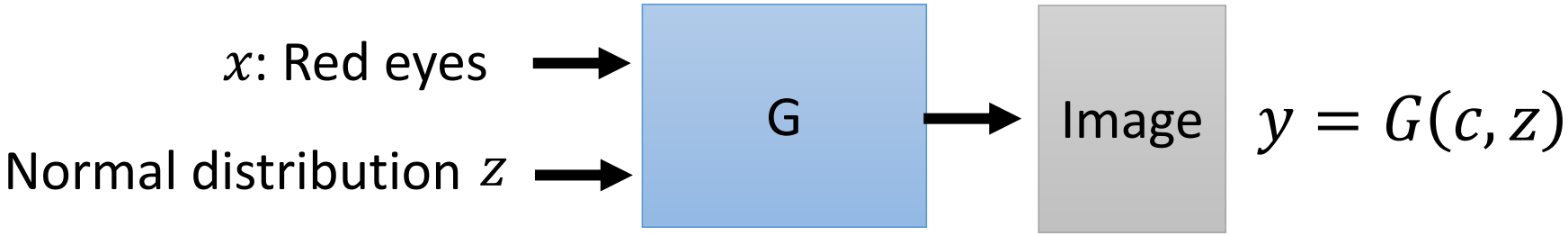
blue hair,
red eyes

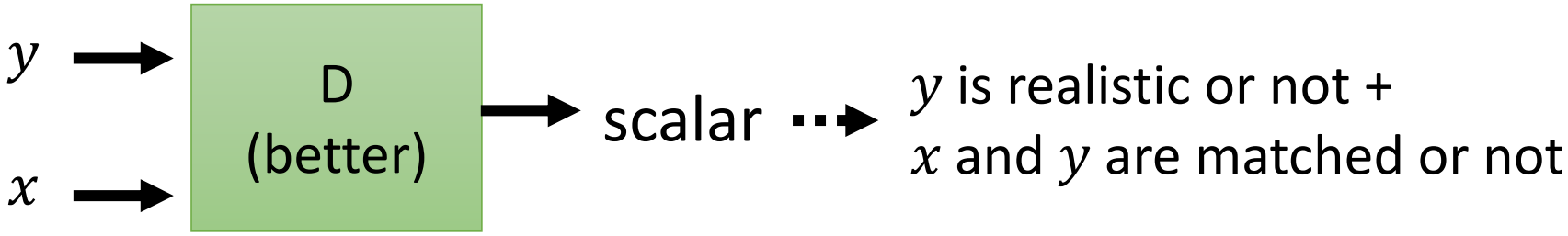
Conditional GAN



https://arxiv.org/abs/1605.05396

Conditional GAN





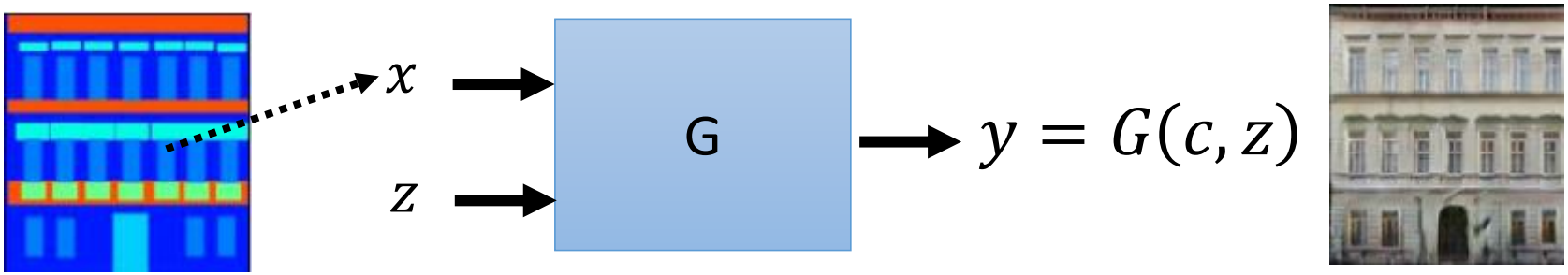
True text-image pairs: (red eyes, ) 1

(red eyes, ) 0

(red eyes, Image) 0

https://arxiv.org/abs/1611.07004

Conditional GAN



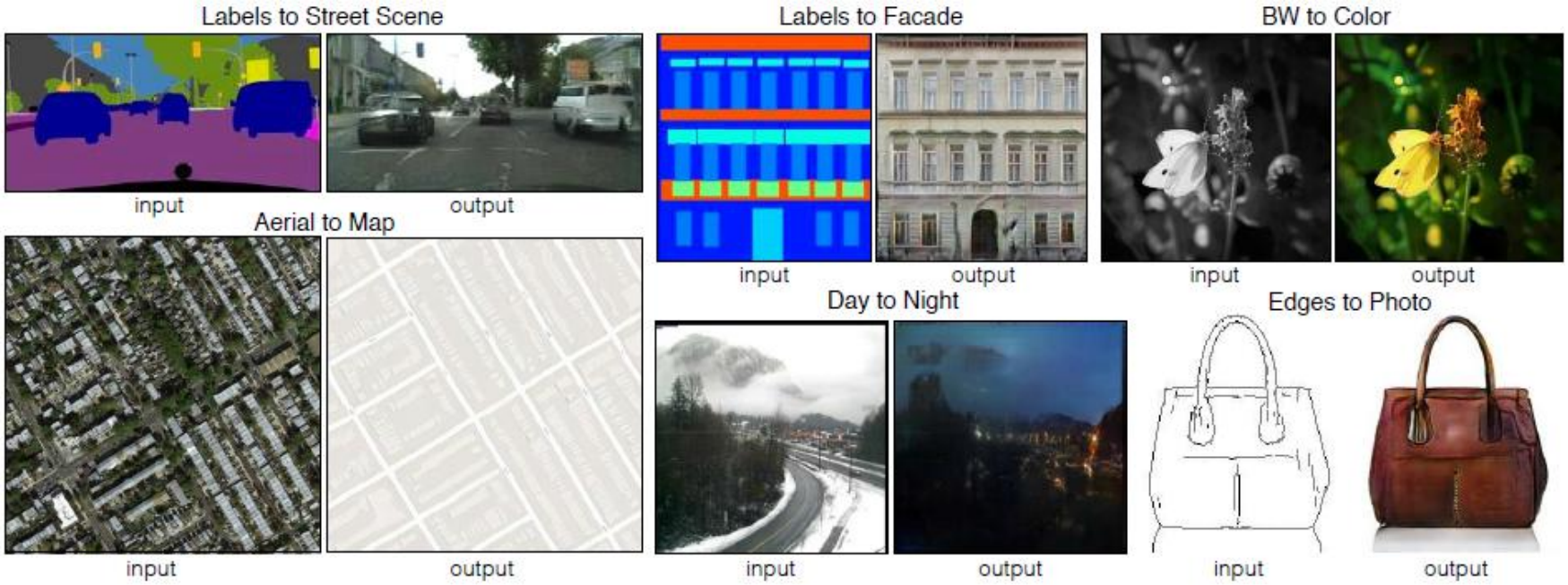
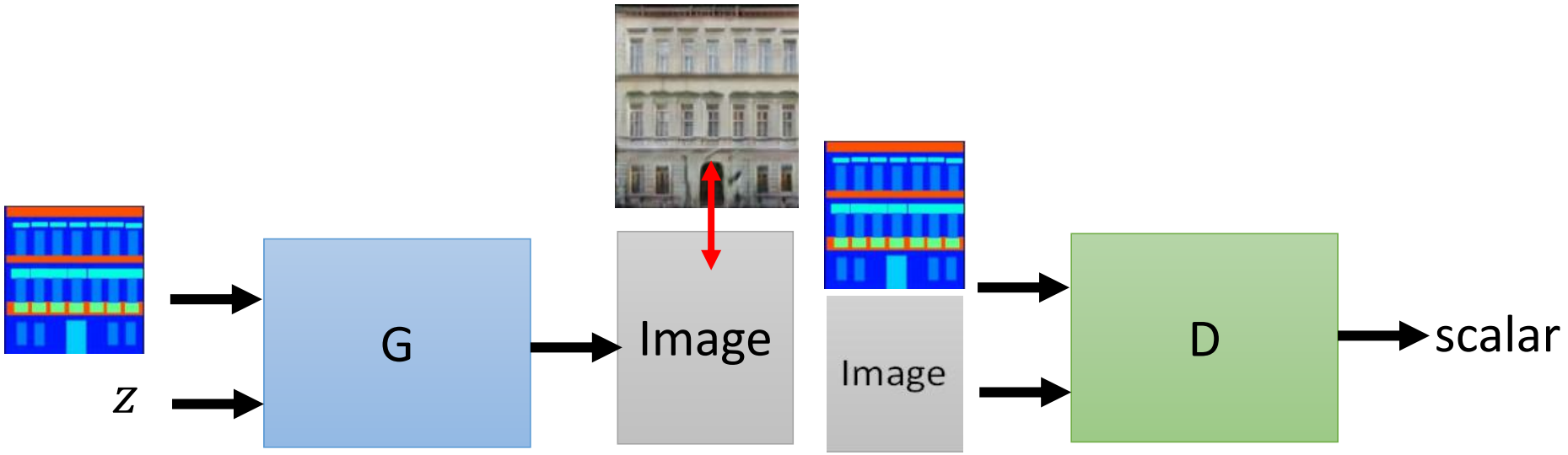


Image translation, or pix2pix

https://arxiv.org/abs/1611.07004

Conditional GAN

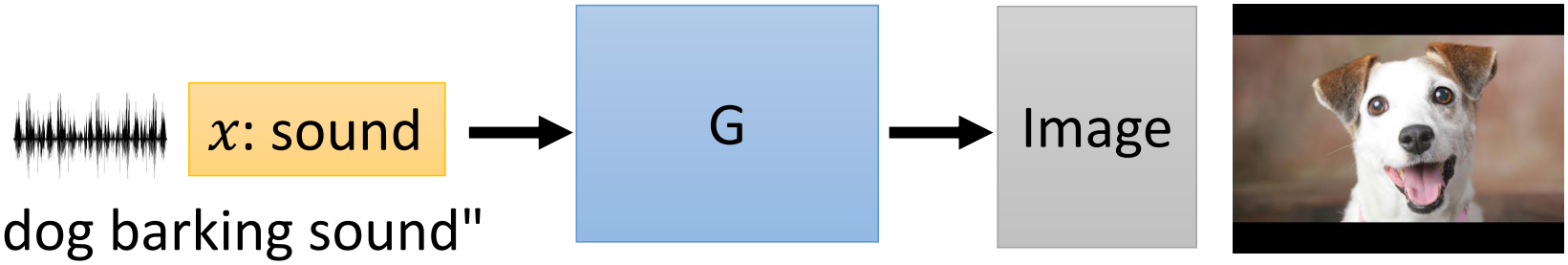


Testing:

input supervised GAN GAN + supervised

https://arxiv.org/abs/1808.04108

Conditional GAN



Training Data Collection

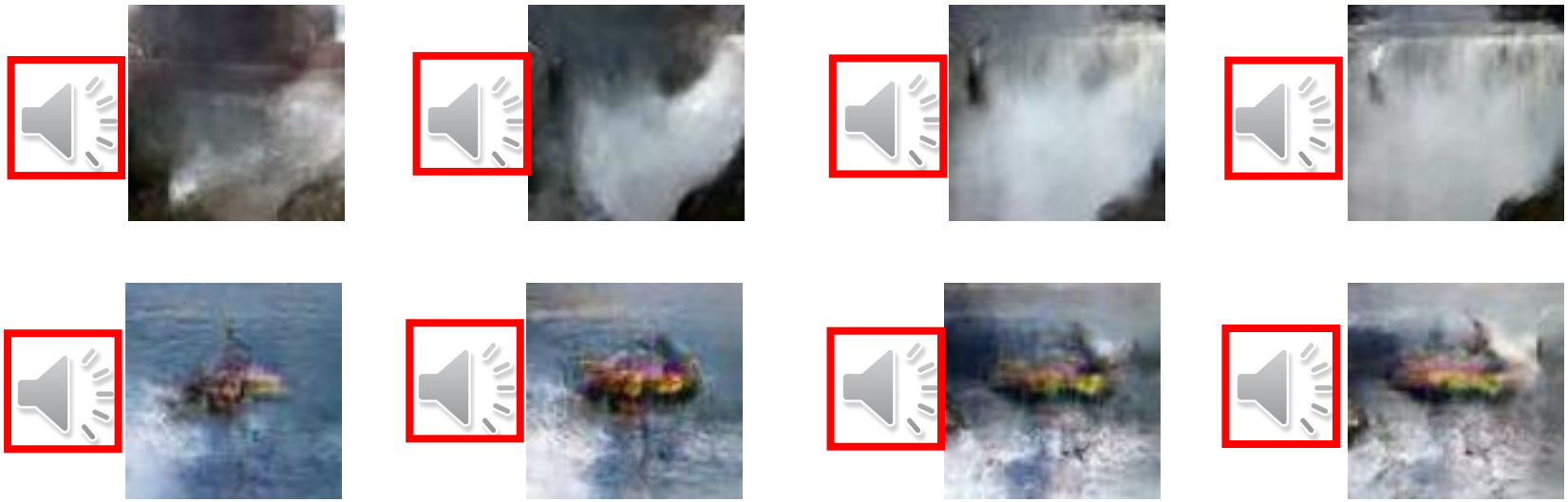
Conditional GAN

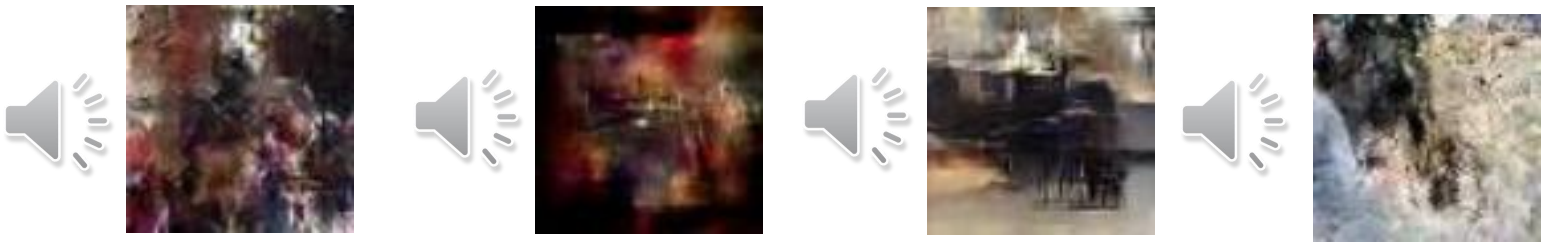
The images are generated by Chia-Hung Wan and Shun-Po Chuang

https://wjohn1483.github.io/audio_to_scene/index.html

- Sound-to-image

Louder





Conditional GAN

Talking Head Generation

https://arxiv.org/abs/1905.08233

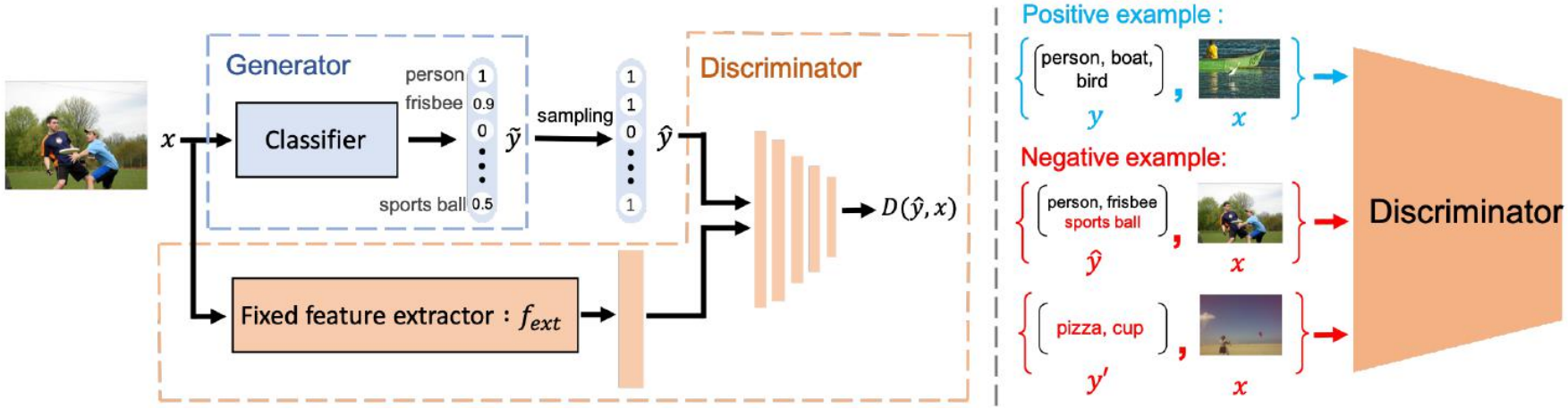
Conditional GAN

Multi-label Image Classifier = Conditional Generator

Input condition

person, sports ball,
baseball bat, baseball glove

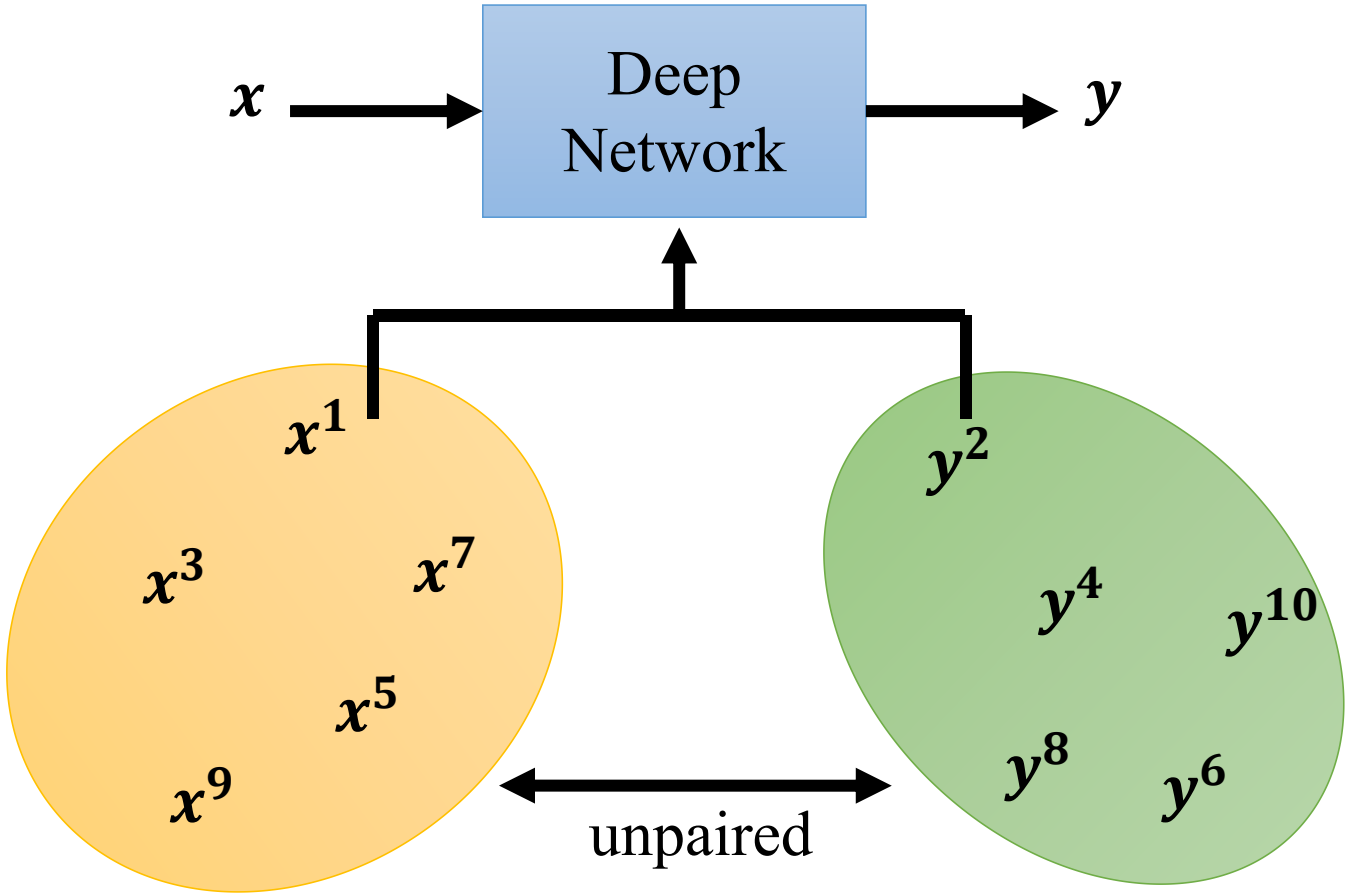
Generated output



https://arxiv.org/abs/1811.04689

Learning from Unpaired Data

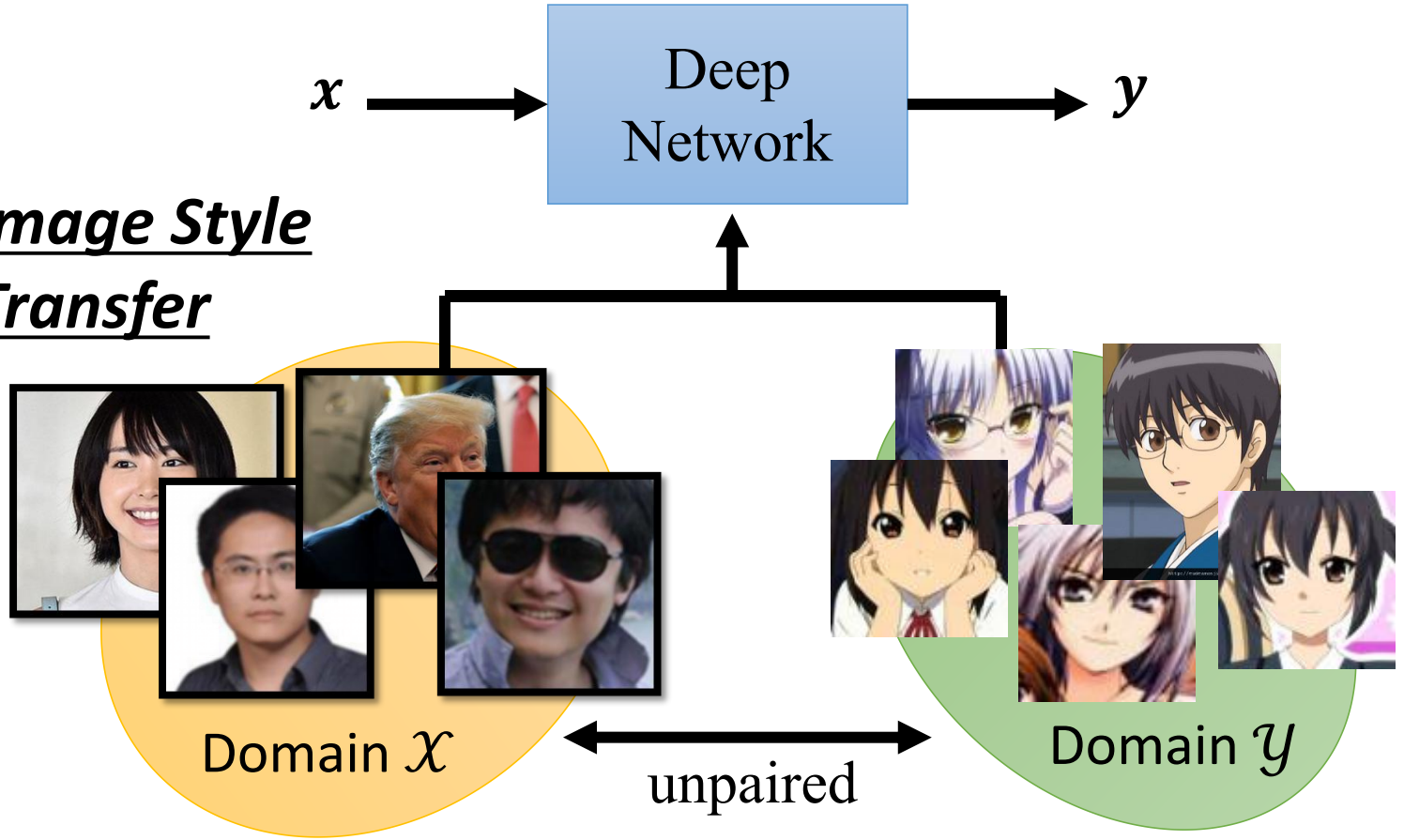
Learning from Unpaired Data



HW3: pseudo labeling
HW5: back translation

} Still need **some** paired data

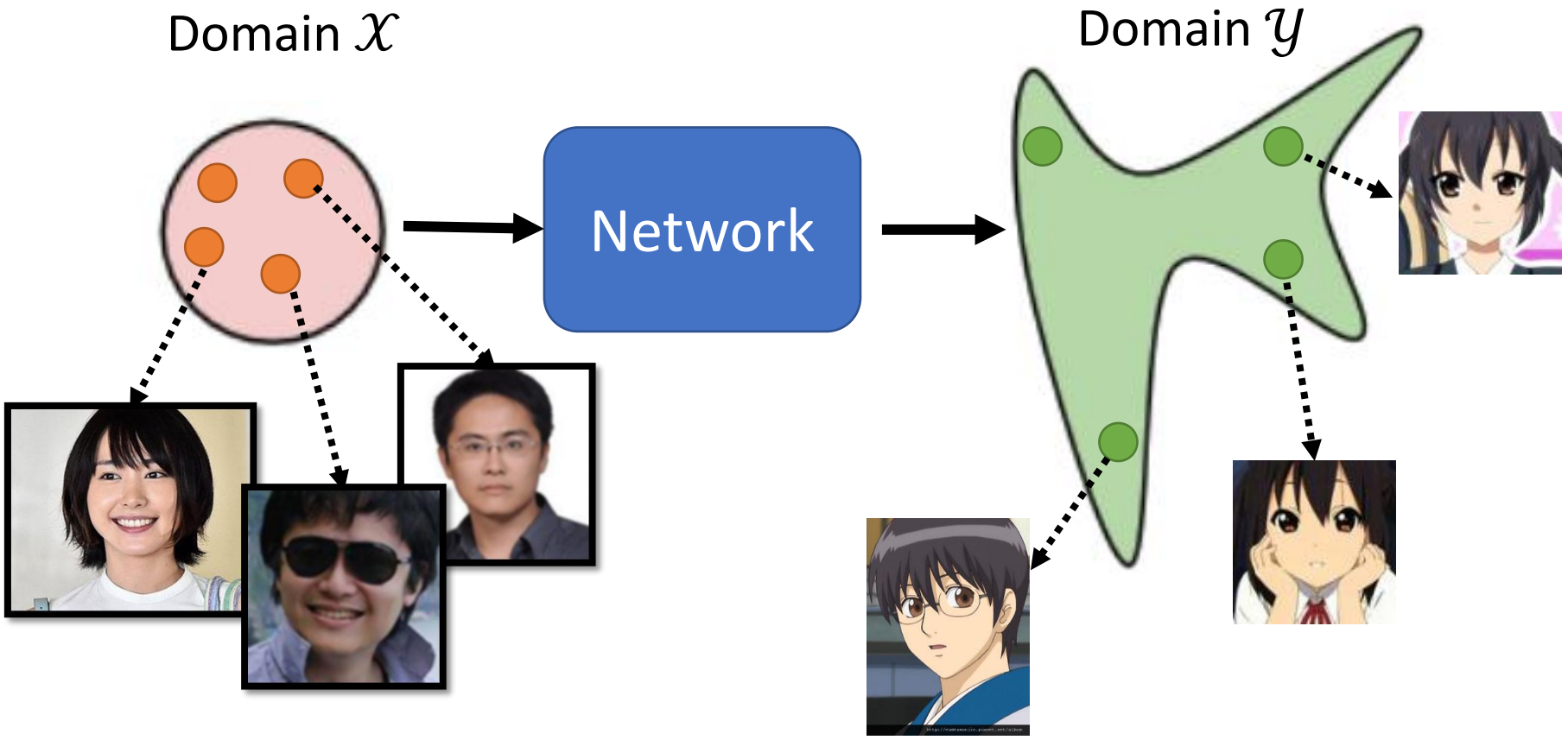
Learning from Unpaired Data



Can we learn the mapping without any paired data?

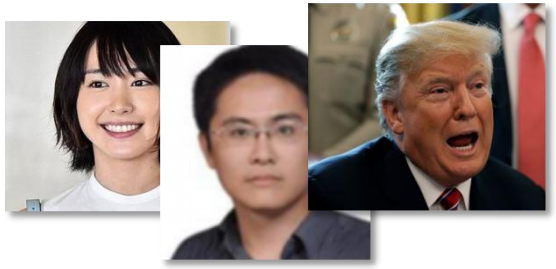
Unsupervised Conditional Generation

Learning from Unpaired Data



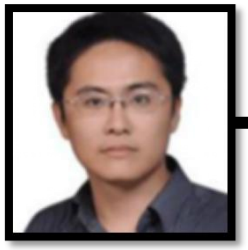
Cycle GAN

Domain X



Domain Y

Domain X



$G_{X \to Y}$

Become similar to domain Y

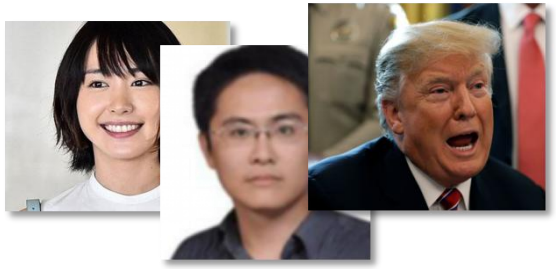
D_Y → scalar

Domain Y

Input image belongs to domain Y or not

Cycle GAN

Domain X



Domain Y

Domain X

$G_{X \to Y}$

Become similar to domain Y

ignore input

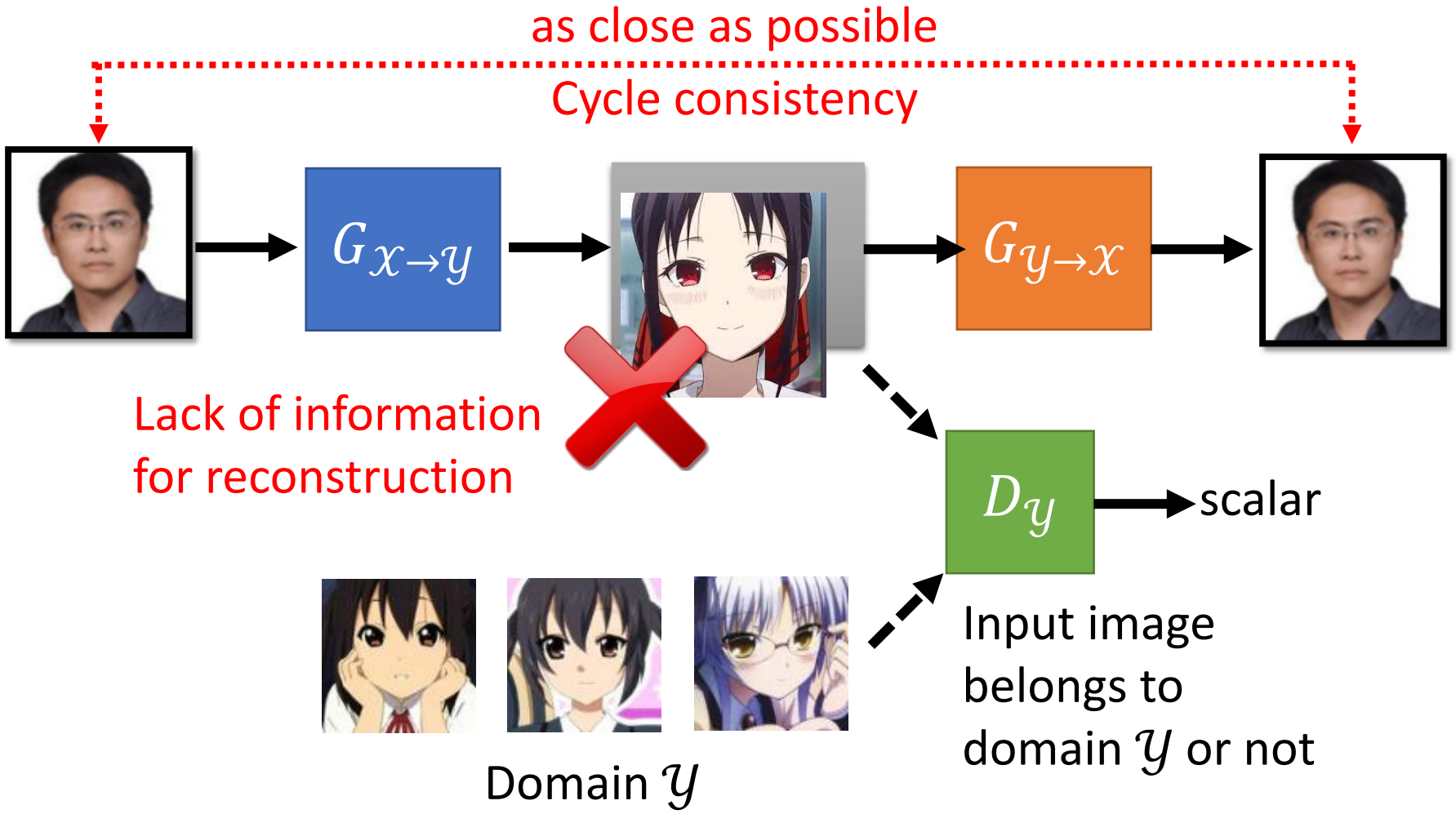
D_Y

scalar

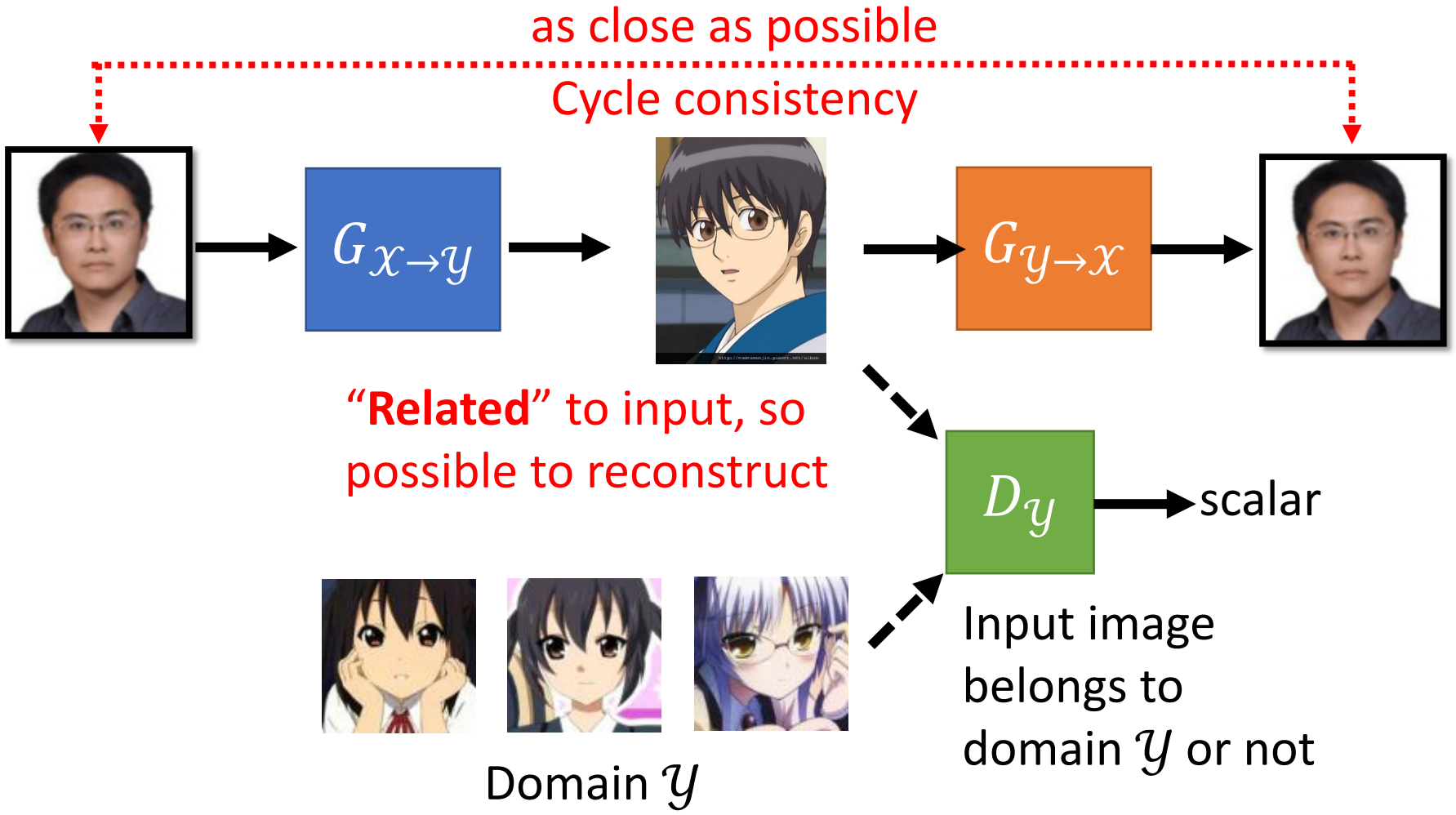
Input image belongs to domain Y or not

Domain Y

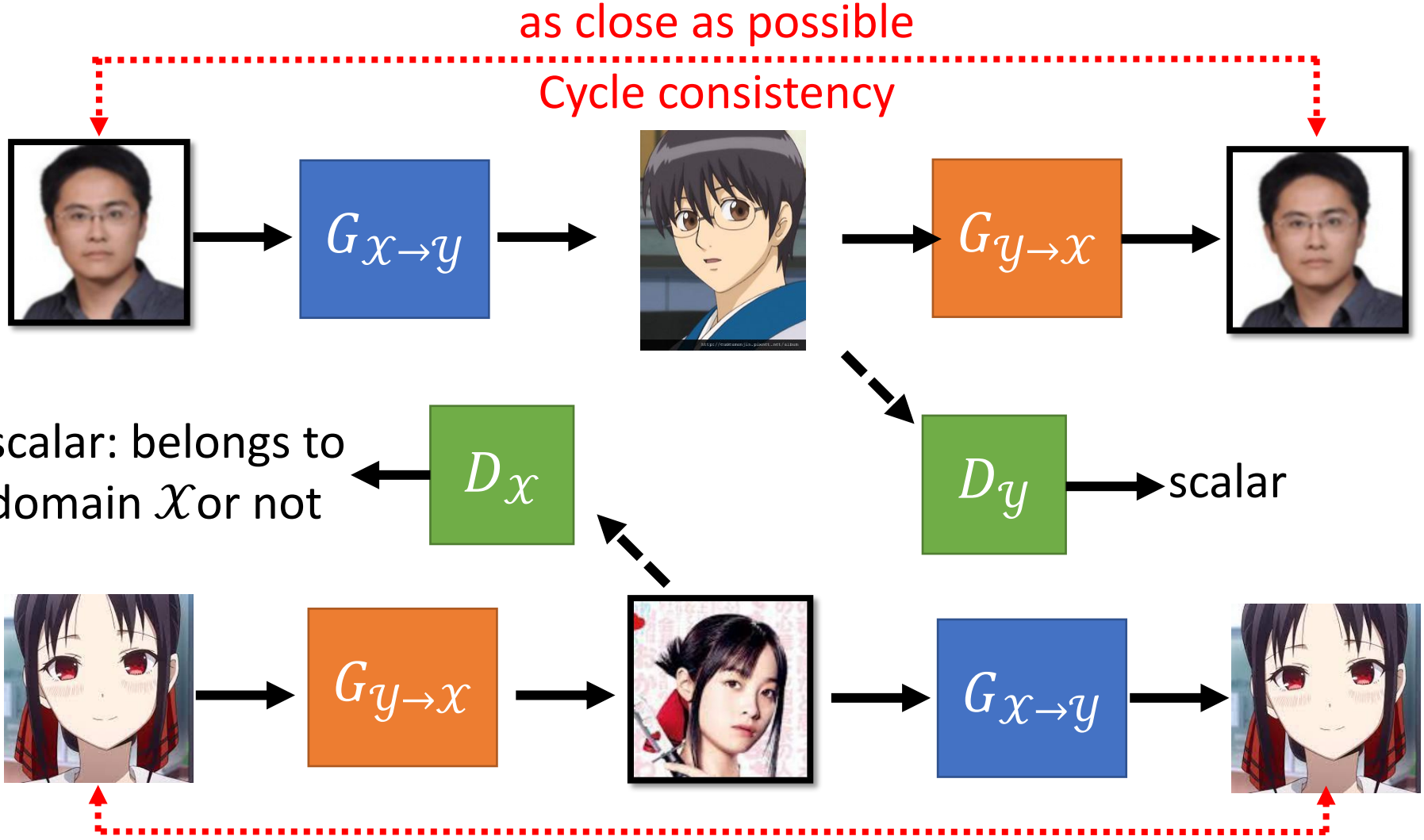
Cycle GAN


as close as possible
Cycle consistency
$G_{X\to Y}$
$G_{Y\to X}$
Lack of information
for reconstruction
D_Y
scalar
Input image
belongs to
domain Y or not
Domain Y

Cycle GAN

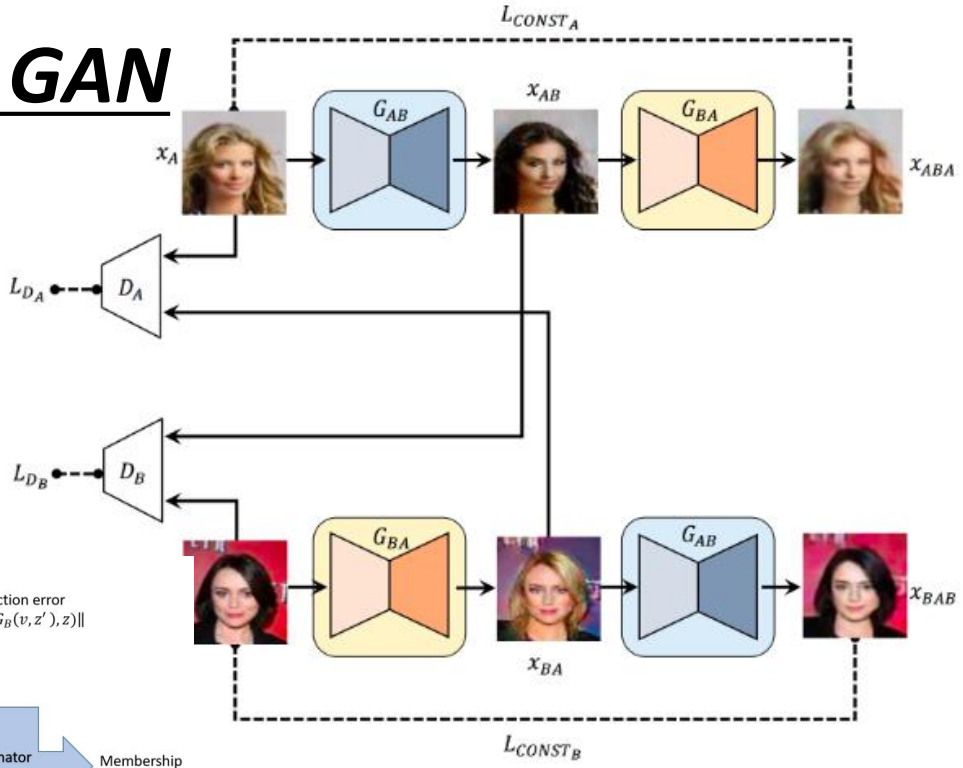

as close as possible
Cycle consistency
$G_{X\to Y}$
$G_{Y\to X}$
"**Related**" to input, so possible to reconstruct
D_Y
scalar
Input image belongs to domain Y or not
Domain Y

Cycle GAN


as close as possible
Cycle consistency
$G_{X\to Y}$
$G_{Y\to X}$
D_X
D_Y
scalar: belongs to domain X or not
scalar
$G_{Y\to X}$
$G_{X\to Y}$

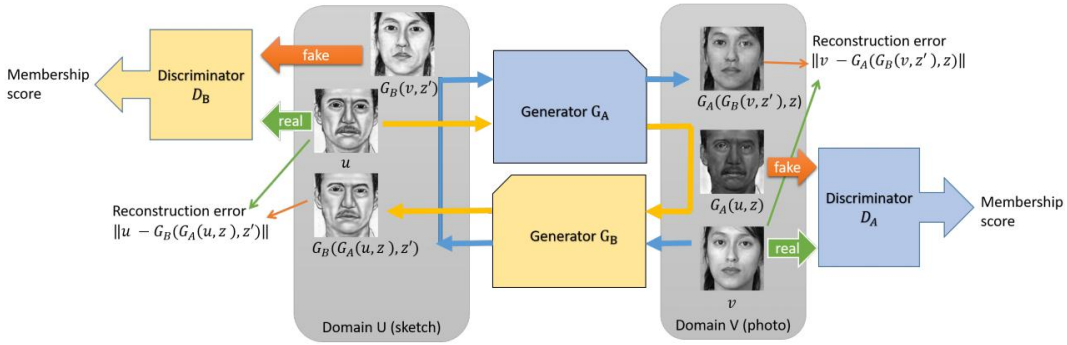
Disco GAN

https://arxiv.org/abs/1703.05192



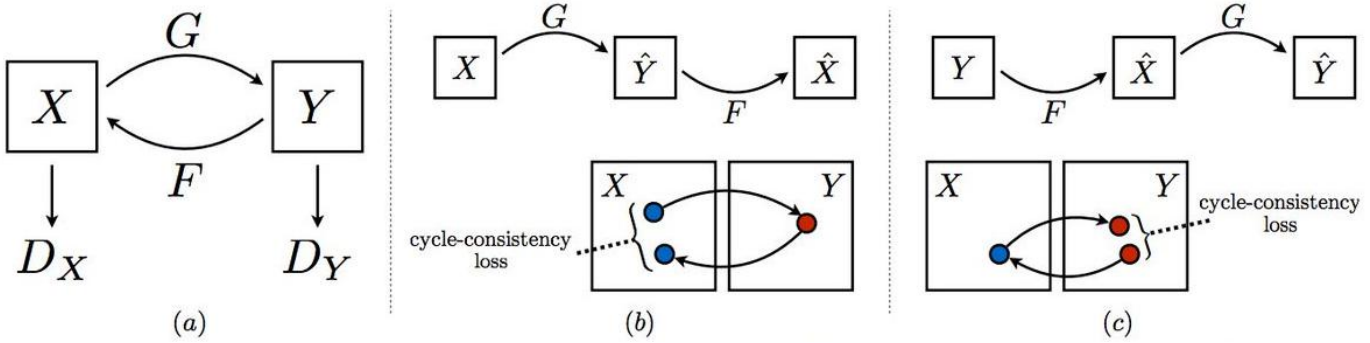
Dual GAN

https://arxiv.org/abs/1704.02510



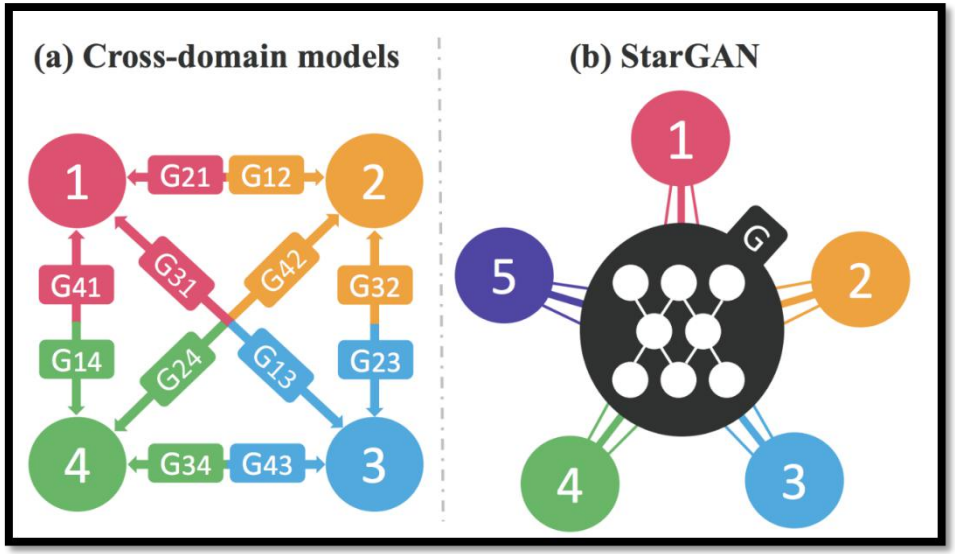
Cycle GAN

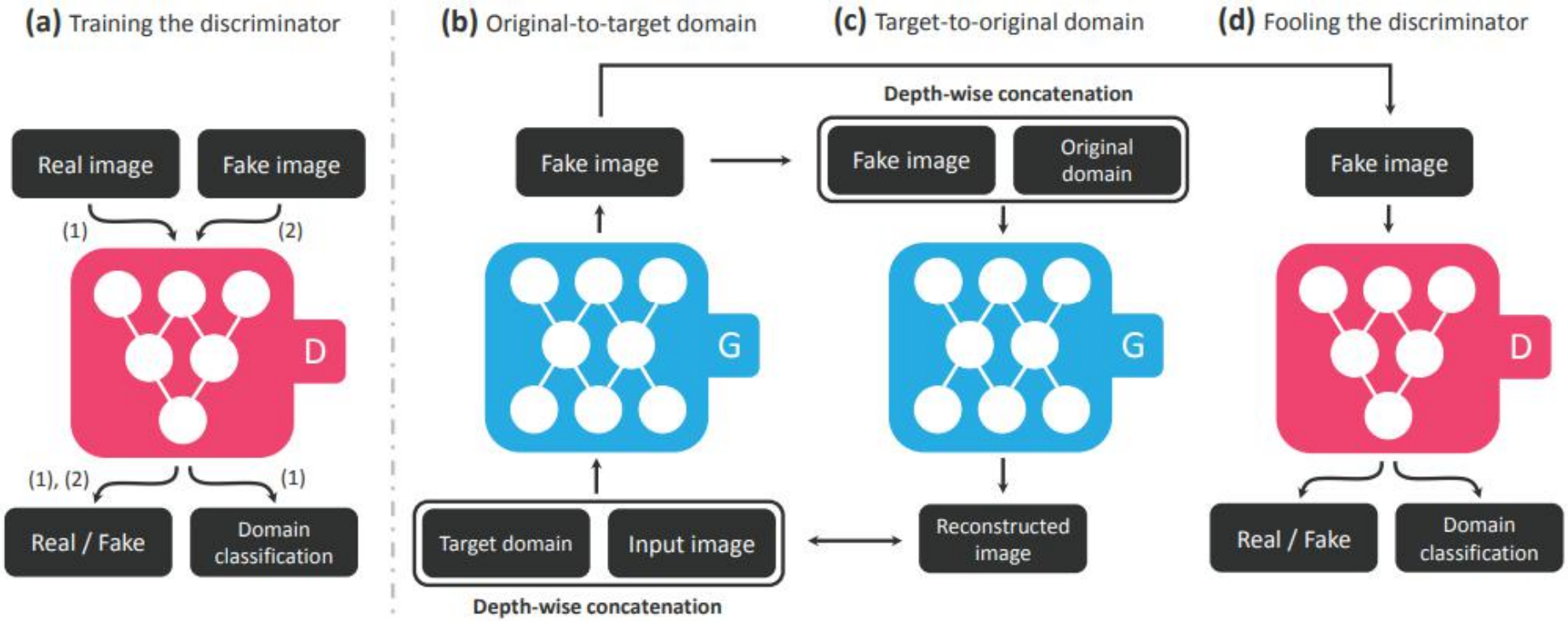
https://arxiv.org/abs/1703.10593



StarGAN

https://arxiv.org/abs/1711.09020



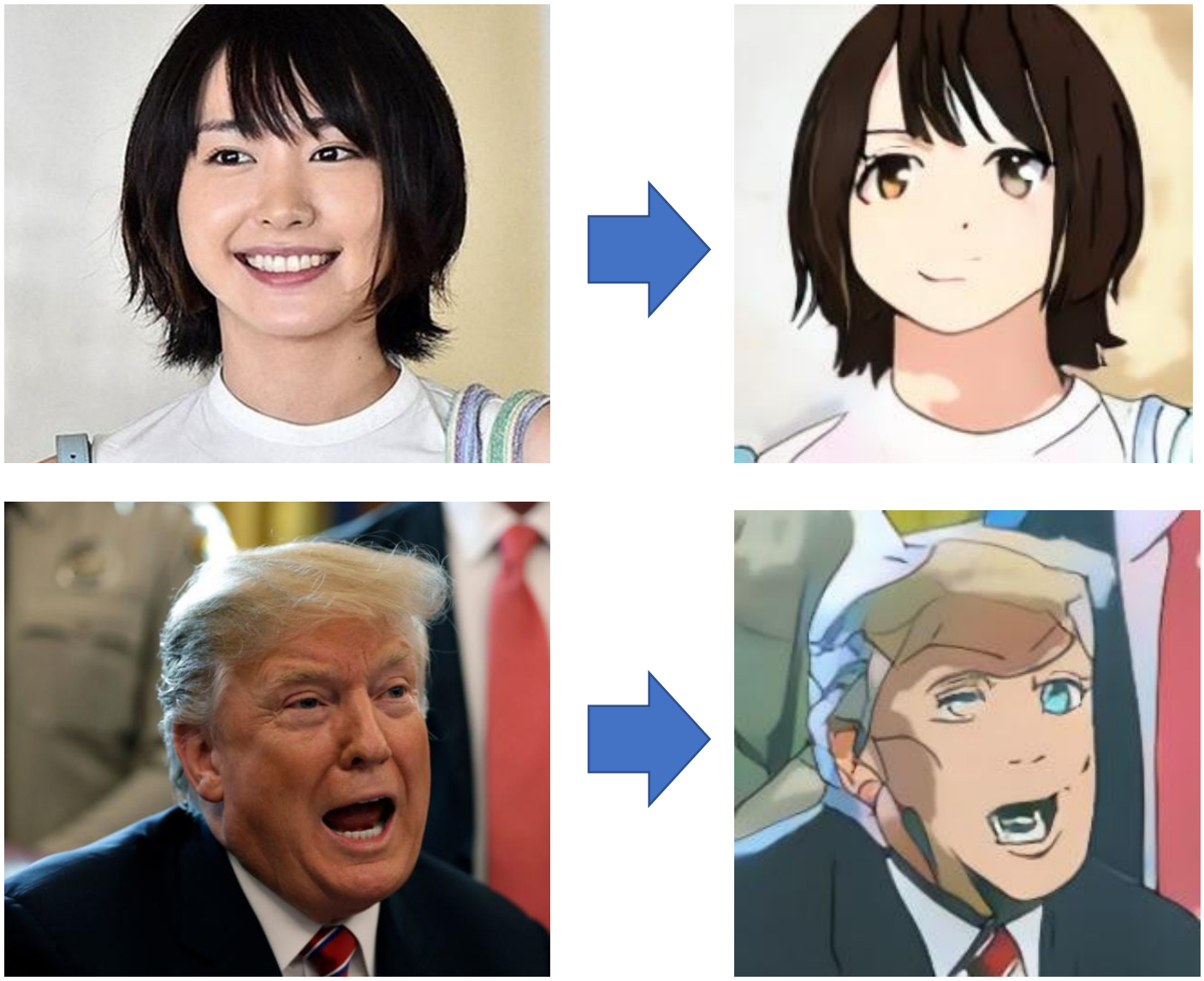



Q&A

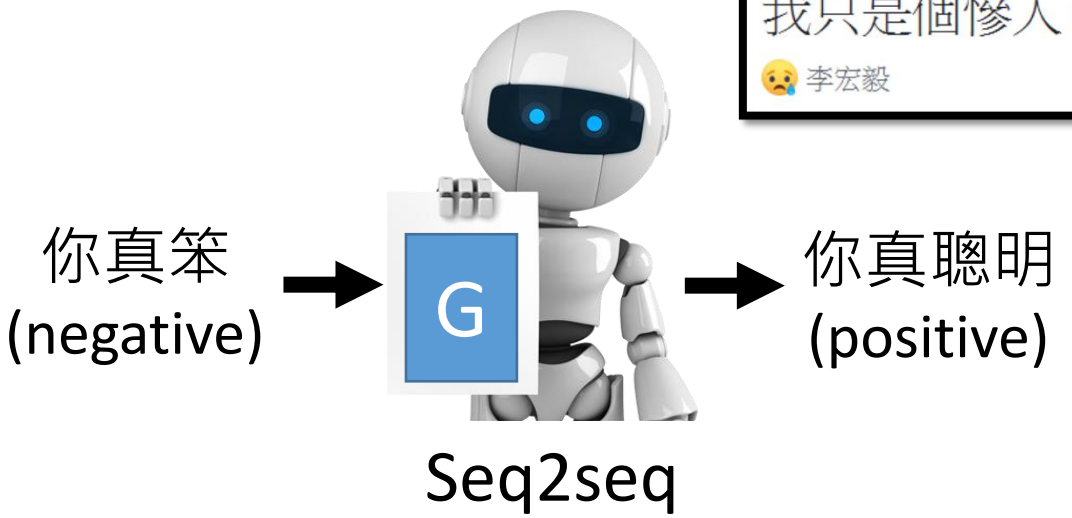
SELFIE2ANIME

https://selfie2anime.com/

https://arxiv.org/abs/1907.10830



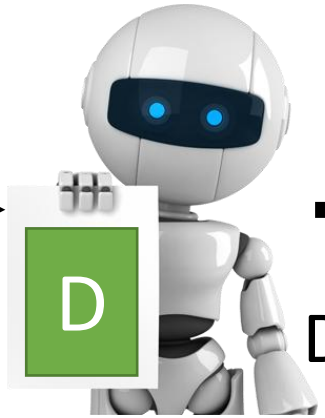
Text Style Transfer



Text Style Transfer

Cycle GAN

positive

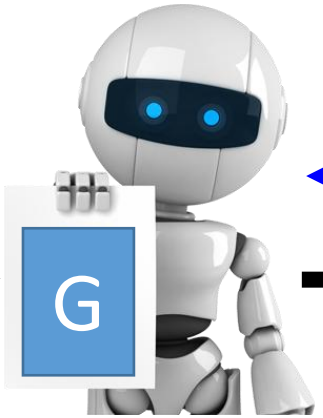


Positive or not?

Discriminator

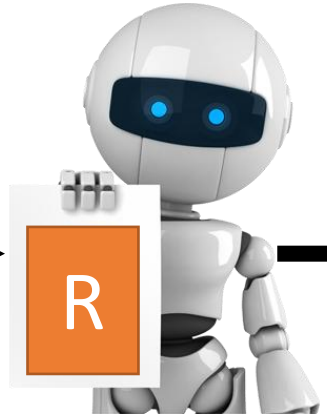
?

你真笨
(negative)



Seq2seq

你真聰明
??????
(positive)



Seq2seq

你真笨
(negative)

minimize the reconstruction error

感謝 張瓊之 同學提供實驗結果

Text Style Transfer

- From negative sentence to positive one

胃疼 , 沒睡醒 , 各種不舒服

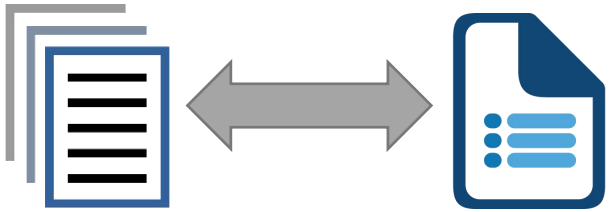
我都想去上班了, 真夠賤的!

暈死了, 吃燒烤、竟然遇到個變態狂

我肚子痛的厲害

Unsupervised Abstractive Summarization

https://arxiv.org/abs/1810.02851



document summary

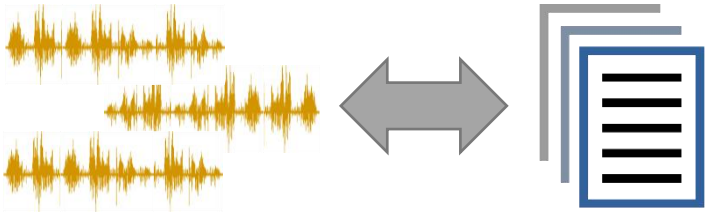
Unsupervised Translation

https://arxiv.org/abs/1710.04087
https://arxiv.org/abs/1710.11041

Language 1 Language 2

Unsupervised ASR

https://arxiv.org/abs/1804.00316
https://arxiv.org/abs/1812.09323
https://arxiv.org/abs/1904.04100

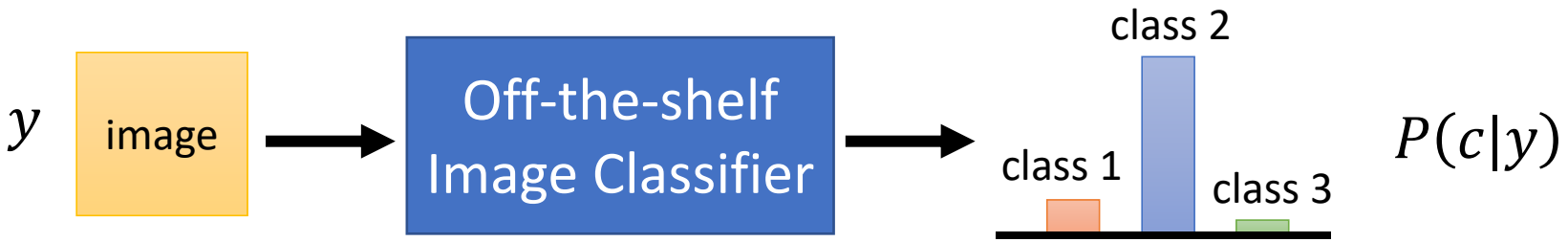


Audio Text

Evaluation of Generation

Quality of Image

- Human evaluation is expensive (and sometimes unfair/unstable).
- How to evaluate the quality of the generated images automatically?



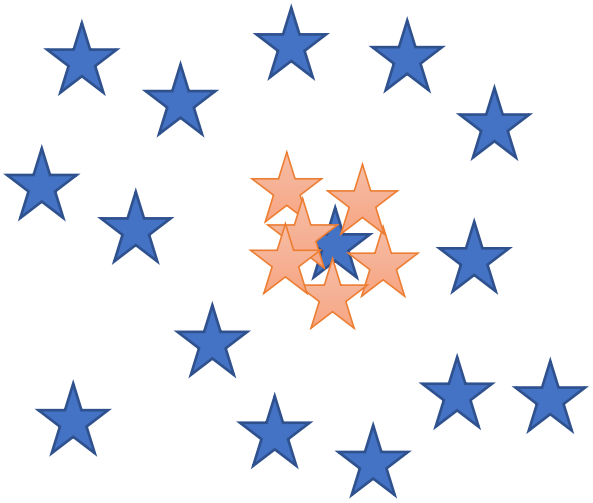
e.g., Inception net, VGG, etc.

Concentrated distribution means higher visual quality

Diversity - Mode Collapse

: real data

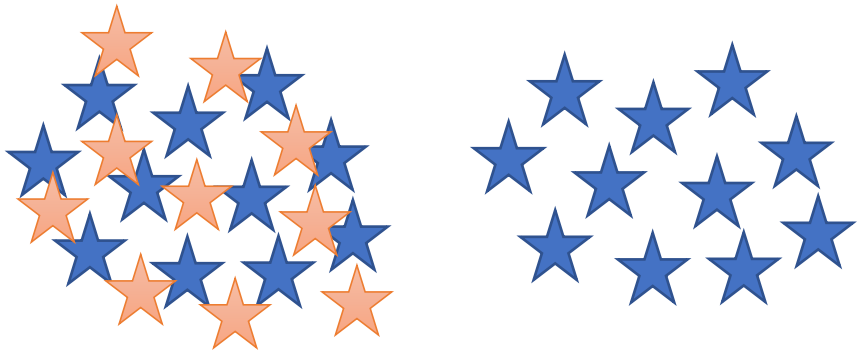
: generated data



Diversity - Mode Dropping

: real data

: generated data

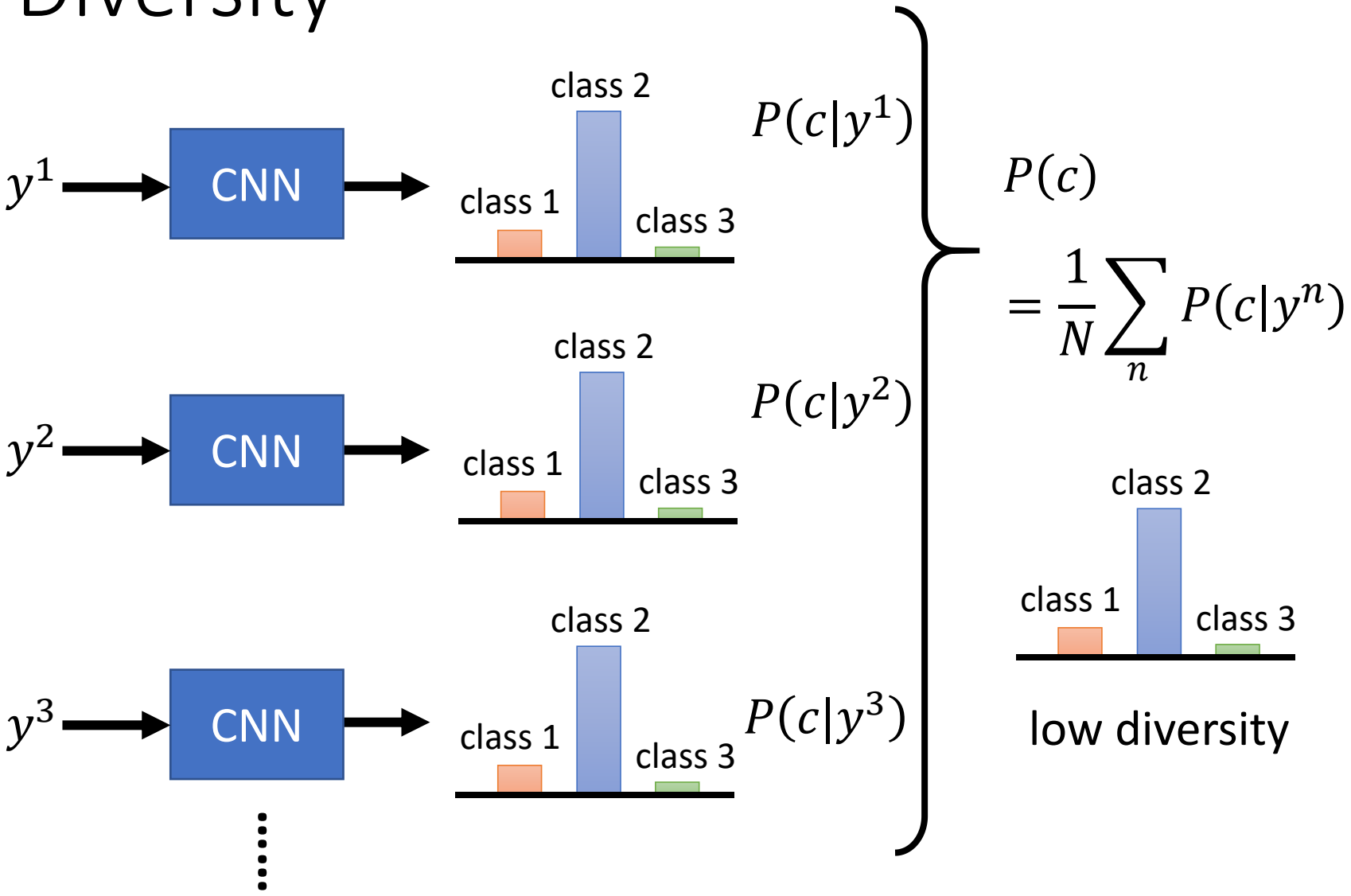


Generator
at iteration t

Generator
at iteration t+1

(BEGAN on CelebA)

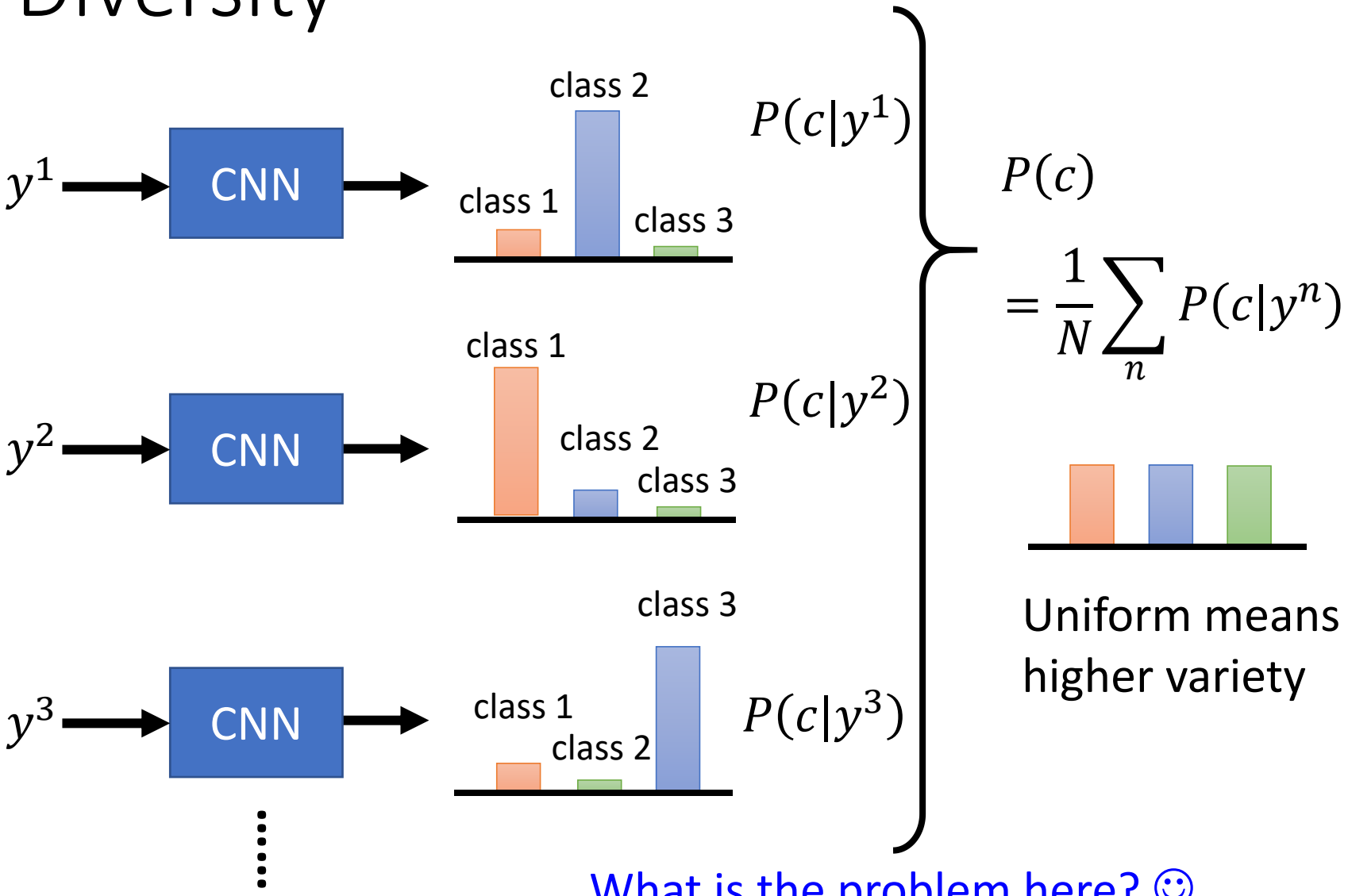
Diversity


y^1
CNN
class 2
class 1
class 3
$P(c|y^1)$
y^2
CNN
class 2
class 1
class 3
$P(c|y^2)$
y^3
CNN
class 2
class 1
class 3
$P(c|y^3)$
$P(c)$
$= \frac{1}{N}\sum_n P(c|y^n)$
class 2
class 1
class 3
low diversity

Diversity

Inception Score (IS):

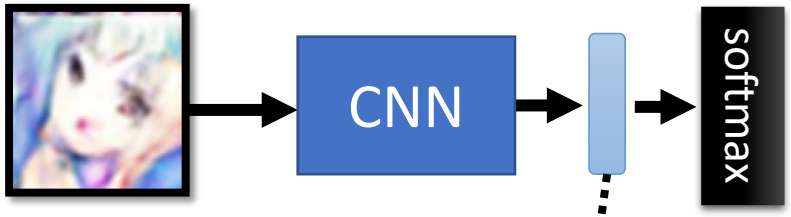
Good quality, large diversity → Large **IS**



What is the problem here? ☺

https://arxiv.org/pdf/1706.08500.pdf

Fréchet Inception Distance (FID)

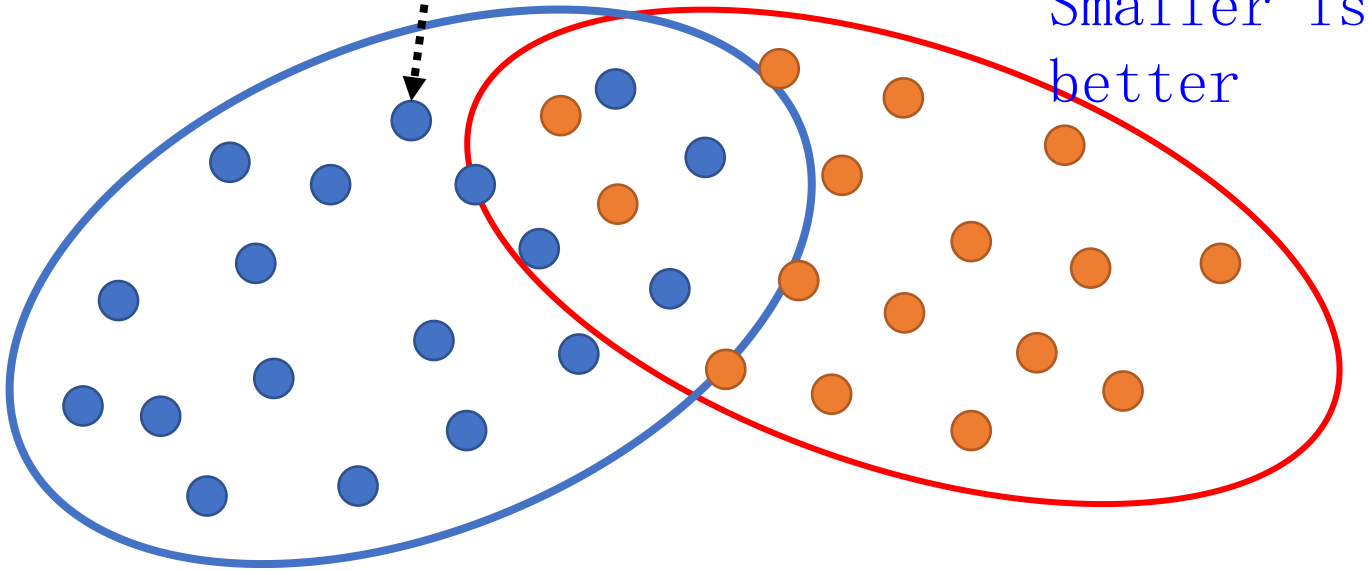


red points: real images

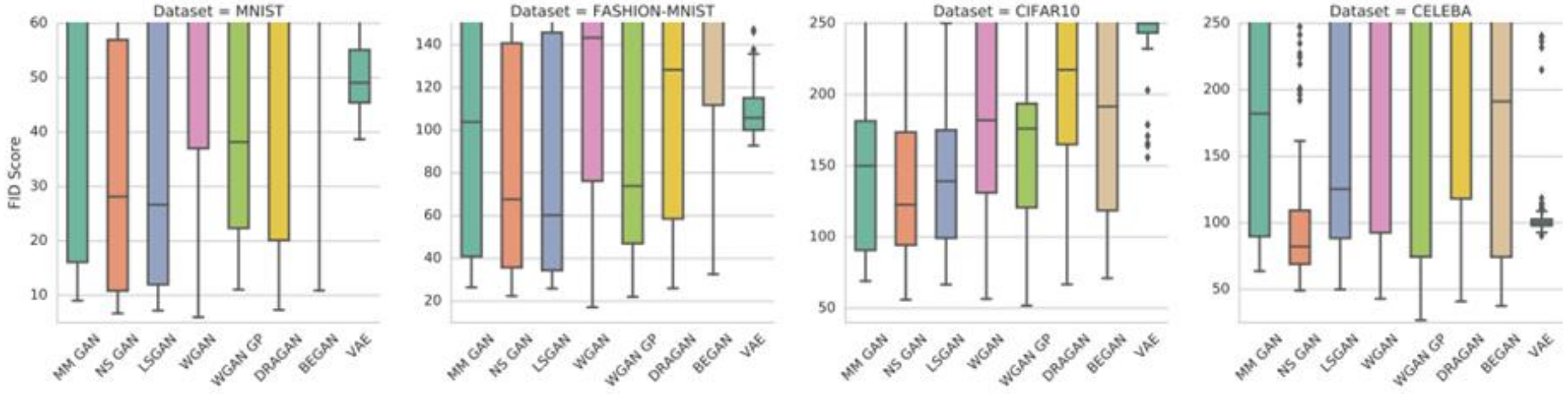
blue points: generated images

FID = Fréchet distance between the two **Gaussians** ???

Smaller is better



GAN	Discriminator Loss	Generator Loss
MM GAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{GAN}} = -\mathbb{E}_{x\sim p_d}[\log(D(x))] + \mathbb{E}_{\hat{x}\sim p_g}[\log(1-D(\hat{x}))]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{GAN}} = -\mathcal{L}_{\mathrm{D}}^{\mathrm{GAN}}$
NS GAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{NSGAN}} = \mathcal{L}_{\mathrm{D}}^{\mathrm{GAN}}$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{NSGAN}} = \mathbb{E}_{\hat{x}\sim p_g}[\log(D(\hat{x}))]$
WGAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{WGAN}} = -\mathbb{E}_{x\sim p_d}[D(x)] + \mathbb{E}_{\hat{x}\sim p_g}[D(\hat{x})]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{WGAN}} - = \mathcal{L}_{\mathrm{D}}^{\mathrm{WGAN}}$
WGAN GP	$\mathcal{L}_{\mathrm{D}}^{\mathrm{WGAN}} = \mathcal{L}_{\mathrm{D}}^{\mathrm{WGAN}} + \lambda\mathbb{E}_{\hat{x}\sim p_g}[(\|\nabla D(\alpha x + (1-\alpha\hat{x})\|_2 - 1)^2]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{WGAN}} = -\mathbb{E}_{\hat{x}\sim p_g}[D(\hat{x})]$
LS GAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{LSGAN}} = -\mathbb{E}_{x\sim p_d}[(D(x)-1)^2] + \mathbb{E}_{\hat{x}\sim p_g}[D(\hat{x})^2]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{LSGAN}} = -\mathbb{E}_{\hat{x}\sim p_g}[(D(\hat{x}-1)^2]$
DRAGAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{DRAGAN}} = \mathcal{L}_{\mathrm{D}}^{\mathrm{GAN}} + \lambda\mathbb{E}_{\hat{x}\sim p_d+\mathcal{N}(0,c)}[(\|\nabla D(\hat{x})\|_2 - 1)^2]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{DRAGAN}} = -\mathcal{L}_{\mathrm{D}}^{\mathrm{NS\ GAN}}$
BEGAN	$\mathcal{L}_{\mathrm{D}}^{\mathrm{BEGAN}} = \mathbb{E}_{x\sim p_d}[\|\|x - \mathrm{AE}(x)\|\|_1] - k_t\mathbb{E}_{\hat{x}\sim p_g}[\|\|\hat{x} - \mathrm{AE}(\hat{x})\|\|_1]$	$\mathcal{L}_{\mathrm{G}}^{\mathrm{BEGAN}} = \mathbb{E}_{\hat{x}\sim p_g}[\|\|\hat{x} - \mathrm{AE}(\hat{x})\|\|_1]$



FIT: Smaller is better

Are GANs Created Equal? A Large-Scale Study

https://arxiv.org/abs/1711.10337

https://arxiv.org/pdf/1511.01844.pdf

We don't want memory GAN.

Real Data

Generated Data

Same as real data …

Generated Data

Simply flip real data …

To learn more about evaluation …

	Measure	Description
Quantitative	1. Average Log-likelihood [18, 22]	• Log likelihood of explaining realworld held out/test data using a density estimated from the generated data (*e.g.* using KDE or Parzen window estimation). $L = \frac{1}{N}\sum_i \log P_{model}(\mathbf{x}_i)$
	2. Coverage Metric [33]	• The probability mass of the true data "covered" by the model distribution $C := P_{data}(dP_{model} > t)$ with t such that $P_{model}(dP_{model} > t) = 0.95$
	3. Inception Score (IS) [3]	• KLD between conditional and marginal label distributions over generated data. $\exp\left(\mathbb{E}_{\mathbf{x}}\left[\mathrm{KL}\left(p(y \mid \mathbf{x}) \parallel p(y)\right)\right]\right)$
	4. Modified Inception Score (m-IS) [34]	• Encourages diversity within images sampled from a particular category. $\exp(\mathbb{E}_{\mathbf{x}_i}[\mathbb{E}_{\mathbf{x}_j}[(\mathbb{KL}(P(y\|\mathbf{x}_i)\|P(y\|\mathbf{x}_j))]])$
	5. Mode Score (MS) [35]	• Similar to IS but also takes into account the prior distribution of the labels over real data. $\exp\left(\mathbb{E}_{\mathbf{x}}\left[\mathrm{KL}\left(p(y \mid \mathbf{x}) \parallel p\left(y^{\text{train}}\right)\right)\right] - \mathrm{KL}\left(p(y) \parallel p\left(y^{\text{train}}\right)\right)\right)$
	6. AM Score [36]	• Takes into account the KLD between distributions of training labels vs. predicted labels, as well as the entropy of predictions. $\mathrm{KL}(p(y^{\text{train}}) \parallel p(y)) + \mathbb{E}_{\mathbf{x}}\left[H(y\|\mathbf{x})\right]$
	7. Fréchet Inception Distance (FID) [37]	• Wasserstein-2 distance between multi-variate Gaussians fitted to data embedded into a feature space $FID(r, g) = \|\mu_r - \mu_g\|_2^2 + Tr(\Sigma_r + \Sigma_g - 2(\Sigma_r\Sigma_g)^{\frac{1}{2}})$
	8. Maximum Mean Discrepancy (MMD) [38]	• Measures the dissimilarity between two probability distributions P_r and P_g using samples drawn independently from each distribution. $M_k(P_r, P_g) = \mathbb{E}_{\mathbf{x},\mathbf{x}'\sim P_r}[k(\mathbf{x},\mathbf{x}')] - 2\mathbb{E}_{\mathbf{x}\sim P_r,\mathbf{y}\sim P_g}[k(\mathbf{x},\mathbf{y})] + \mathbb{E}_{\mathbf{y},\mathbf{y}'\sim P_g}[k(\mathbf{y},\mathbf{y}')]$
	9. The Wasserstein Critic [39]	• The critic (*e.g.* an NN) is trained to produce high values at real samples and low values at generated samples $\hat{W}(\mathbf{x}_{test}, \mathbf{x}_g) = \frac{1}{N}\sum_{i=1}^{N} \hat{f}(\mathbf{x}_{test}[i]) - \frac{1}{N}\sum_{i=1}^{N} \hat{f}(\mathbf{x}_g[i])$
	10. Birthday Paradox Test [27]	• Measures the support size of a discrete (continuous) distribution by counting the duplicates (near duplicates)
	11. Classifier Two Sample Test (C2ST) [40]	• Answers whether two samples are drawn from the same distribution (*e.g.* by training a binary classifier)
	12. Classification Performance [1, 15]	• An indirect technique for evaluating the quality of unsupervised representations (*e.g.* feature extraction; FCN score). See also the GAN Quality Index (GQI) [41].
	13. Boundary Distortion [42]	• Measures diversity of generated samples and covariate shift using classification methods.
	14. Number of Statistically-Different Bins (NDB) [43]	• Given two sets of samples from the same distribution, the number of samples that fall into a given bin should be the same up to sampling noise
	15. Image Retrieval Performance [44]	• Measures the distributions of distances to the nearest neighbors of some query images (*i.e.* diversity)
	16. Generative Adversarial Metric (GAM) [31]	• Compares two GANs by having them engaged in a battle against each other by swapping discriminators or generators. $p(\mathbf{x}\|y=1; M_1^{'})/p(\mathbf{x}\|y=1; M_2^{'}) = \left(p(y=1\|\mathbf{x}; D_1)p(\mathbf{x}; G_2)\right)/\left(p(y=1\|\mathbf{x}; D_2)p(\mathbf{x}; G_1)\right)$
	17. Tournament Win Rate and Skill Rating [45]	• Implements a tournament in which a player is either a discriminator that attempts to distinguish between real and fake data or a generator that attempts to fool the discriminators into accepting fake data as real.
	18. Normalized Relative Discriminative Score (NRDS) [32]	• Compares n GANs based on the idea that if the generated samples are closer to real ones, more epochs would be needed to distinguish them from real samples.
	19. Adversarial Accuracy and Divergence [46]	• Adversarial Accuracy. Computes the classification accuracies achieved by the two classifiers, one trained on real data and another on generated data, on a labeled validation set to approximate $P_g(y\|\mathbf{x})$ and $P_r(y\|\mathbf{x})$. Adversarial Divergence: Computes $\mathrm{KL}(P_g(y\|\mathbf{x}), P_r(y\|\mathbf{x}))$
	20. Geometry Score [47]	• Compares geometrical properties of the underlying data manifold between real and generated data.
	21. Reconstruction Error [48]	• Measures the reconstruction error (*e.g.* L_2 norm) between a test image and its closest generated image by optimizing for z (*i.e.* $min_{\mathbf{z}}\|\|G(\mathbf{z}) - \mathbf{x}^{(test)}\|\|^2$)
	22. Image Quality Measures [49, 50, 51]	• Evaluates the quality of generated images using measures such as SSIM, PSNR, and sharpness difference
	23. Low-level Image Statistics [52, 53]	• Evaluates how similar low-level statistics of generated images are to those of natural scenes in terms of mean power spectrum, distribution of random filter responses, contrast distribution, etc.
	24. Precision, Recall and F_1 score [23]	• These measures are used to quantify the degree of overfitting in GANs, often over toy datasets.
Qualitative	1. Nearest Neighbors	• To detect overfitting, generated samples are shown next to their nearest neighbors in the training set
	2. Rapid Scene Categorization [18]	• In these experiments, participants are asked to distinguish generated samples from real images in a short presentation time (*e.g.* 100 ms); *i.e.* real v.s fake
	3. Preference Judgment [54, 55, 56, 57]	• Participants are asked to rank models in terms of the fidelity of their generated images (*e.g.* pairs, triples)
	4. Mode Drop and Collapse [58, 59]	• Over datasets with known modes (*e.g.* a GMM or a labeled dataset), modes are computed as by measuring the distances of generated data to mode centers
	5. Network Internals [1, 60, 61, 62, 63, 64]	• Regards exploring and illustrating the internal representation and dynamics of models (*e.g.* space continuity) as well as visualizing learned features

Pros and cons of GAN evaluation measures

https://arxiv.org/abs/1802.03446

Concluding Remarks

- Introduction of Generative Models
- Generative Adversarial Network (GAN)
- Theory behind GAN
- Tips for GAN
- Conditional Generation
- Learning from unpaired data
- Evaluation of Generative Models


Q&A