High-Pass Filtered LIM $\times$ CMB Lensing $\langle I_\ell^{\mathsf{Hi}}(\chi; \Lambda)\kappa_{-\ell}\rangle'$