# Case Study

Load in the important libraries.

```
library(here)
```

## here() starts at /Users/ianthomasdover/Reinsurance Case Study

```
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.4 v readr
                                 2.1.5
## v forcats 1.0.0 v stringr 1.5.1
## v ggplot2 3.5.1 v tibble 3.2.1
                   v tidyr
                                 1.3.1
## v lubridate 1.9.3
## v purrr
             1.0.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(dplyr)
library(tidyr)
library(ggplot2)
library(lubridate)
```

### Problem 1 – Data handling, analysis and plotting

The first problem of the case study builds on the data in the files  $p01-02\_portfolio.csv$  and  $p01-02\_rates.csv$ . One file contains membership information for a Group Life portfolio and one has information on the rates which should be charged.

```
# Load the CSV file
portfolio_data <- read_delim(
    "Case Study/data/p01-02_portfolio.csv",
    delim = ";",
    show_col_types = FALSE
)

# View the data
head(portfolio_data)</pre>
```

```
## # A tibble: 6 x 5
##
    SchemeName Date.of.Birth Gender DeathSI Industry
                        <chr> <chr>
##
             <chr>
               29.05.1949
                                             Government & Public Administration
## 1 Scheme2
                             F
                                     <NA>
## 2 Scheme2
               07.09.1950
                             F
                                     <NA>
                                             Government & Public Administration
## 3 Scheme2
             27.09.1956
                                   <NA>
                                             Government & Public Administration
                             F
## 4 Scheme2
             18.02.1942
                                             Government & Public Administration
                             F
                                     <NA>
## 5 Scheme2
                                             Government & Public Administration
               31.07.1951
                             F
                                     <NA>
## 6 Scheme2
               10.07.1960
                                     <NA>
                                             Government & Public Administration
# Load the CSV file
rates_data <- read_delim("Case Study/data/p01-02_rates.csv",</pre>
                         delim = ";",
                         show_col_types = FALSE)
# View the data
head(rates_data)
## # A tibble: 6 x 3
      Age Gender Rate
##
     <dbl> <chr> <dbl>
## 1
       18 M
                  0.32
## 2
       19 M
                  0.32
## 3
       20 M
                  0.32
## 4
       21 M
                  0.31
## 5
       22 M
                  0.31
## 6
       23 M
                  0.31
rates\_data
# Count occurrences of each combination of Gender and Age
duplicates <- rates_data %>%
 group_by(Gender, Age) %>%
  summarise(count = n()) %>%
filter(count > 1)
## 'summarise()' has grouped output by 'Gender'. You can override using the
## '.groups' argument.
# Check if any duplicates exist
if (nrow(duplicates) == 0) {
  message("Sanity Check Passed: 'Gender' and 'Age' form a unique key.")
} else {
  message("Sanity Check Failed: There are duplicate combinations of 'Gender' and 'Age'.")
  print(duplicates)
}
```

## Sanity Check Passed: 'Gender' and 'Age' form a unique key.

#### Question a.

Read the data from the two files into R's memory. The rates are applicable to each individual in the portfolio, depending on that individual's age and gender. Combine the two datasets into a single table by looking up the rate for each line of the portfolio.

```
# Step 1: Convert the Date.of.Birth column to Date format
# dmy is used for "day-month-year" format
portfolio data$Date.of.Birth <- dmy(portfolio data$Date.of.Birth)</pre>
# Step 2: Calculate the time difference in years
portfolio_data$age <- ceiling(interval(portfolio_data$Date.of.Birth, today()) / years(1))</pre>
# Step 3: View the updated data with age column
head(portfolio_data)
## # A tibble: 6 x 6
##
    SchemeName Date.of.Birth Gender DeathSI Industry
                                                                               age
                           <chr> <chr>
     <chr> <date>
                                             <chr>>
                                                                              <dbl>
## 1 Scheme2 1949-05-29
                             F
                                    <NA>
                                            Government & Public Administrat~
                                                                                76
## 2 Scheme2
              1950-09-07
                             F
                                    <NA>
                                            Government & Public Administrat~
                                                                                75
## 3 Scheme2
              1956-09-27
                            F
                                    <NA>
                                            Government & Public Administrat~
                                                                                68
## 4 Scheme2
                                                                                83
               1942-02-18
                                     <NA>
                                            Government & Public Administrat~
```

<NA>

<NA>

Government & Public Administrat~

Government & Public Administrat~

74

65

#### Extrapolate Rates Data beyond 70 years

1951-07-31

1960-07-10

F

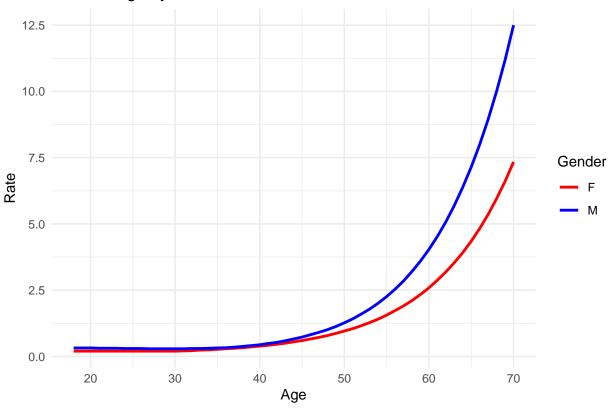
F

## 5 Scheme2

## 6 Scheme2

```
# Create the line plot with grouping by Gender
ggplot(rates_data, aes(
    x = Age,
    y = Rate,
    color = Gender,
    group = Gender
)) +
    geom_line(linewidth = 1) + # Use linewidth instead of size
    scale_color_manual(values = c("F" = "red", "M" = "blue")) + # Set colors for genders
    labs(title = "Rate vs Age by Gender", x = "Age", y = "Rate") +
    theme_minimal() # Use a clean theme for the plot
```

# Rate vs Age by Gender



## Fit an Exponential Model for Each Gender

## Number of iterations to convergence: 7
## Achieved convergence tolerance: 1.604e-06

```
# Fit an exponential model for each gender
exp_model_female <- nls(Rate ~ exp(a + b * Age), data = subset(rates_data, Gender == "F"), start = list
exp_model_male <- nls(Rate ~ exp(a + b * Age), data = subset(rates_data, Gender == "M"), start = list(a
# Summarize the models
summary(exp_model_female)
##
## Formula: Rate ~ exp(a + b * Age)
##
## Parameters:
##
      Estimate Std. Error t value Pr(>|t|)
## a -5.1051905 0.0584289 -87.37
                                    <2e-16 ***
## b 0.1012605 0.0008889 113.92
                                    <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 0.07425 on 51 degrees of freedom
```

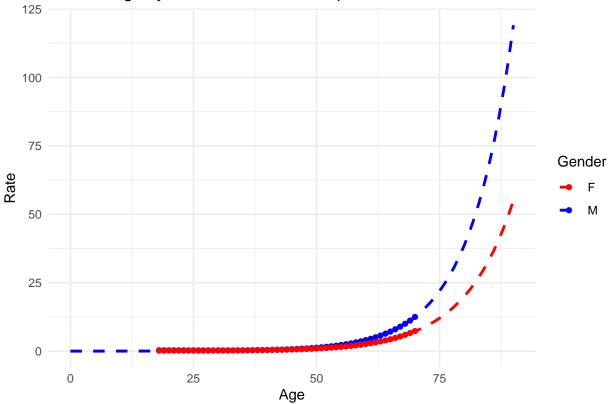
```
summary(exp_model_male)
```

```
##
## Formula: Rate ~ exp(a + b * Age)
##
## Parameters:
## Estimate Std. Error t value Pr(>|t|)
## a -5.35891    0.06689   -80.12   <2e-16 ***
## b    0.11266    0.00101    111.49    <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.1247 on 51 degrees of freedom
##
## Number of iterations to convergence: 6
## Achieved convergence tolerance: 4.649e-06</pre>
```

#### Plot the Data and the Fitted Exponential Curves

```
# Generate new data for ages 0 to 90 for both genders
new_data \leftarrow data.frame(Age = rep(0:90, 2), Gender = rep(c("F", "M"), each = 91))
# Predict rates for the new data using the fitted models
new_data$Rate_pred <- ifelse(</pre>
 new data$Gender == "F",
  predict(exp_model_female, newdata = subset(new_data, Gender == "F")),
  predict(exp_model_male, newdata = subset(new_data, Gender == "M"))
# Plot the original data along with the fitted exponential curves
ggplot() +
  geom_line(
    data = new_data,
    aes(x = Age, y = Rate_pred, color = Gender),
   linewidth = 1,
   linetype = "dashed"
  ) + # Fitted lines for each gender
  geom_point(data = rates_data, aes(x = Age, y = Rate, color = Gender)) + # Original data points
  scale_color_manual(values = c("F" = "red", "M" = "blue")) + # Set colors for genders
  labs(title = "Rate vs Age by Gender with Fitted Exponential Models", x = "Age", y = "Rate") +
  theme_minimal()
```



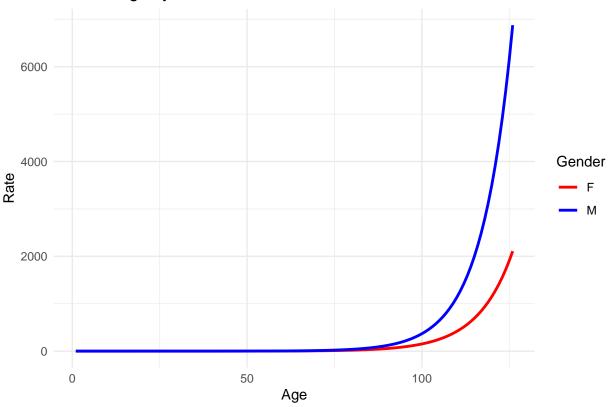


#### Add Extrapolated Values to Rates Data

```
# Get the unique values from the Gender column
unique_genders <- unique(rates_data$Gender)</pre>
# Print the unique values
unique_genders
## [1] "M" "F"
# Get the unique values from the Gender column
unique_genders <- unique(portfolio_data$Gender)</pre>
# Print the unique values
unique_genders
## [1] "F"
                 "M"
                          "Male"
                                   "Female"
# Convert "Male" to "M" and "Female" to "F" using ifelse
portfolio_data$Gender <- ifelse(</pre>
  portfolio_data$Gender == "Male",
  "M",
  ifelse(portfolio_data$Gender == "Female", "F", portfolio_data$Gender)
```

```
# Get the unique values from the Gender column
unique_genders <- unique(portfolio_data$Gender)</pre>
# Print the unique values
unique_genders
## [1] "F" "M"
# Step 1: Create a complete sequence of ages from 1 to 110 for both genders
complete_ages <- expand.grid(Age = 1:126, Gender = c("F", "M"))</pre>
# Step 2: Identify missing "Age" and "Gender" combinations in the existing data
# Perform an anti-join to find missing combinations (from dplyr)
missing_ages <- anti_join(complete_ages, rates_data, by = c("Age", "Gender"))
# Step 3: Predict the rates for the missing combinations using the fitted models
missing_ages$Rate <- ifelse(</pre>
 missing ages$Gender == "F",
  predict(exp_model_female, newdata = subset(missing_ages, Gender == "F")),
  predict(exp_model_male, newdata = subset(missing_ages, Gender == "M"))
# Step 4: Append the new data (with missing combinations filled) to the existing data
rates_data_extended <- rbind(rates_data, missing_ages)</pre>
# Create the line plot with grouping by Gender
ggplot(rates_data_extended,
       aes(
         x = Age
         y = Rate,
         color = Gender,
         group = Gender
       )) +
  geom_line(linewidth = 1) + # Use linewidth instead of size
  scale_color_manual(values = c("F" = "red", "M" = "blue")) + # Set colors for genders
  labs(title = "Rate vs Age by Gender", x = "Age", y = "Rate") +
  theme_minimal() # Use a clean theme for the plot
```





## Sanity Check Passed: The row count of combined\_data matches portfolio\_data.

```
# Get the unique values in the SchemeName column
unique_schemes <- unique(combined_data$SchemeName)
unique_schemes
```

```
## [1] "Scheme2" "Scheme1" "Scheme3" "Scheme5" "Scheme4"
```

#### Investigate missing matches

```
## [1] 0
```

#### Question b.

Group the Industry field into common-sense based groupings and determine the mean, standard deviation and quantiles of DeathSI for each of your industry groups.

```
industry_counts <- combined_data %>%
    count(Industry) %>%
    arrange(desc(n))

# View the result
print(industry_counts)
```

```
## # A tibble: 33 x 2
##
      Industry
                                              n
##
      <chr>>
                                          <int>
## 1 <NA>
                                         116769
## 2 Government & Public Administration 31304
## 3 Other
                                          14455
## 4 Sporting Club
                                           2243
## 5 Ex-Services Club
                                           1501
## 6 BSS-Business Services
                                           1228
## 7 MAN-Manufacturing
                                           1147
## 8 EDN-Education
                                           1004
## 9 COM-Communication Serv.
                                            878
## 10 FIN-Finance & Insurance
                                            851
## # i 23 more rows
```

```
"Australian Rules Football Club",
        "Leagues Club",
        "Associated with Club Industry"
      ) ~ "Clubs and Associations",
      Industry %in% c(
        "BSS-Business Services",
        "FIN-Finance & Insurance",
        "Professional Services",
        "LAW-Solicitors/Barrister",
        "ENG-Engineers",
        "MGE-Medical Services Gen"
      ) ~ "Professional and Business Services",
      Industry %in% c(
        "MAN-Manufacturing",
        "CON-Construction",
        "ELE-Electricians",
        "VEH-Vehicle Industry",
        "WEO-Wholesale Trades"
      ) ~ "Manufacturing, Construction, and Trades",
      Industry %in% c(
        "EDN-Education",
        "HEA-Health Industry",
        "MGE-Medical Services Gen"
      ) ~ "Education and Health",
      Industry %in% c(
        "RTL-Retail Trade",
        "ACR-Accom. Cafes & Rests",
        "F00-Food",
        "Hospitality"
      ) ~ "Retail, Hospitality, and Food",
      Industry %in% c("AGR-Farming/Agriculture", "EGW
-Electric/Gas/Water") ~ "Agriculture and Utilities",
Industry == "Other" ~ "Other",
TRUE ~ "Uncategorized" # Catch any uncategorized industries
   )
 )
# View the newly grouped data
print(combined_data)
## # A tibble: 177,922 x 8
##
     SchemeName Date.of.Birth Gender DeathSI Industry
                                                           age Rate Industry_Group
##
      <chr>
                <date>
                              <chr> <chr>
                                              <chr>
                                                         <dbl> <dbl> <chr>
                                                            76 13.3 Government an~
## 1 Scheme2
                              F
                                      <NA>
                 1949-05-29
                                              Governmen~
                              F
## 2 Scheme2
                1950-09-07
                                      <NA>
                                              Governmen~
                                                            75 12.1 Government an~
## 3 Scheme2
                              F
                                      <NA>
              1956-09-27
                                              Governmen~
                                                            68 5.96 Government an~
## 4 Scheme2
                1942-02-18
                              F
                                      <NA>
                                              Governmen~
                                                            83 27.1 Government an~
                              F
## 5 Scheme2
                 1951-07-31
                                      <NA>
                                              Governmen~
                                                            74 10.9 Government an~
## 6 Scheme2
                1960-07-10
                              F
                                      <NA>
                                                            65 4.35 Government an~
                                              Governmen~
                              F
## 7 Scheme2
                1954-12-24
                                      <NA>
                                              Governmen~
                                                            70 7.34 Government an~
                                                            83 27.1 Government an~
## 8 Scheme2
              1942-03-13
                              F
                                      <NA>
                                              Governmen~
## 9 Scheme2
                1958-02-28
                              F
                                      <NA>
                                              Governmen~
                                                            67 5.36 Government an~
```

```
## 10 Scheme2
                 1968-09-12
                                F
                                       <NA>
                                               Governmen~
                                                              57 1.91 Government an~
## # i 177,912 more rows
industry_counts <- combined_data %>%
  count(Industry_Group) %>%
  arrange(desc(n))
# View the result
print(industry_counts)
## # A tibble: 9 x 2
     Industry_Group
                                                   n
##
     <chr>>
                                               <int>
## 1 Uncategorized
                                              117899
## 2 Government and Public Services
                                               32805
## 3 Other
                                               14455
## 4 Clubs and Associations
                                                4944
## 5 Manufacturing, Construction, and Trades
                                                2529
## 6 Professional and Business Services
                                                2494
## 7 Education and Health
                                                1396
## 8 Retail, Hospitality, and Food
                                                1008
## 9 Agriculture and Utilities
                                                 392
  1. # Check the type of DeathSI
    typeof(combined_data$DeathSI)
    ## [1] "character"
    # Count the number of NA values in DeathSI when it was character type
    na_count <- sum(is.na(combined_data$DeathSI))</pre>
    na_count
    ## [1] 21531
     # Count the number of "NA" string values in DeathSI when it was character type
    na_string_count <- sum(combined_data$DeathSI == "NA", na.rm = TRUE)</pre>
    na_string_count
    ## [1] 0
     # Remove apostrophes and convert the DeathSI column from character to numeric
    combined_data$DeathSI <- as.numeric(gsub("'", "", combined_data$DeathSI))</pre>
     # Check the type of DeathSI
    typeof(combined_data$DeathSI)
    ## [1] "double"
```

```
# Count the number of NA values in DeathSI when it is the double type
na_count <- sum(is.na(combined_data$DeathSI))
na_count</pre>
```

## [1] 21531

```
# Calculate mean, standard deviation, and quantiles for each industry group
summary_stats <- combined_data %>%
group_by(Industry_Group) %>%
summarize(
    mean_value = mean(DeathSI, na.rm = TRUE),
    sd_value = sd(DeathSI, na.rm = TRUE),
    q25 = quantile(DeathSI, 0.25, na.rm = TRUE),
    median_value = median(DeathSI, na.rm = TRUE),
    q75 = quantile(DeathSI, 0.75, na.rm = TRUE)
)

# View the result
print(summary_stats)
```

```
## # A tibble: 9 x 6
##
     Industry_Group
                                     mean_value sd_value
                                                            q25 median_value
     <chr>
                                          <dbl>
                                                   <dbl> <dbl>
                                                                       <dbl> <dbl>
                                                213974. 2.49e4
                                                                     106412. 1.79e5
## 1 Agriculture and Utilities
                                        153992.
## 2 Clubs and Associations
                                       275620.
                                                183697. 1.98e5
                                                                     219890. 2.96e5
## 3 Education and Health
                                       323269. 256159. 1.40e5
                                                                     279255 4.69e5
## 4 Government and Public Services
                                       215104. 104726. 1.5 e5
                                                                     220000
                                                                            3
                                                                                 e5
## 5 Manufacturing, Construction, a~
                                        289155.
                                                237042. 1.17e5
                                                                     250380
                                                                            3.96e5
## 6 Other
                                       259435. 115096. 2.05e5
                                                                     244264 2.85e5
## 7 Professional and Business Serv~
                                        438260. 332429. 2.40e5
                                                                     368416 5.44e5
## 8 Retail, Hospitality, and Food
                                        313829. 206804. 2.05e5
                                                                     245601 3.78e5
## 9 Uncategorized
                                        217656. 220107. 7.15e4
                                                                     162404 2.83e5
```

#### Question c.

The following code performs a Monte Carlo simulation on the data you have loaded and combined in Question a.:

```
set.seed(1234)
nsim <- 1000
res <- lapply(1:nsim, function(i,...) {
    x <- ifelse(
        runif(dim(combined_data)[1]) < combined_data$Rate / 1000,
        combined_data$DeathSI,
        0
     );
    list(cost = sum(x), count = length(x[x > 0]))
}
```

Apply this simulation to each scheme in the dataset you were provided, running 1000 simulations per scheme. Produce a plot of the simulated outcomes ("cost"). Your plot should show:

- a separate histogram per scheme;
- all 5 histograms below each other so that they can be easily compared;
- vertical lines in each graph indicating the median, mean and 99.5th percentile of each distribution.

Remove rows where DeathSI is NA for Monte Carlo simulation.

```
# Get the number of rows in the original dataset
original_row_count <- nrow(combined_data)</pre>
# Subset combined_data where DeathSI is not NA
combined_data_death_si_non_na <- subset(combined_data, !is.na(DeathSI))</pre>
# Get the number of rows in the filtered dataset
filtered_row_count <- nrow(combined_data_death_si_non_na)</pre>
# Print out the row counts to validate reduction
cat("Original row count:", original_row_count, "\n")
## Original row count: 177922
cat("Filtered row count (DeathSI not NA):", filtered_row_count, "\n")
## Filtered row count (DeathSI not NA): 156391
# Check if the row count was reduced
if (filtered_row_count < original_row_count) {</pre>
  cat("Row reduction validated: Rows were reduced after filtering.\n")
} else {
  cat("No row reduction: No NA values in DeathSI.\n")
## Row reduction validated: Rows were reduced after filtering.
monte_carlo_simulation <- function(data, nsim = 1000, seed = 1234) {
  # Set the seed for reproducibility
  set.seed(seed)
  # Perform the simulation
  res <- lapply(1:nsim, function(i, ...) {</pre>
    x <- ifelse(runif(dim(data)[1]) < data$Rate / 1000, data$DeathSI, 0)
    # Return the cost and count as a list
    list(cost = sum(x), count = length(x[x > 0]))
  })
  # Return the result of the simulation
  return(res)
# Get the unique values in the SchemeName column
```

```
unique_schemes <- unique(combined_data$SchemeName)</pre>
# Print the unique values
unique_schemes
## [1] "Scheme2" "Scheme1" "Scheme3" "Scheme5" "Scheme4"
# Filter rows where SchemeName is "Scheme_1", "Scheme_2", "Scheme_3", "Scheme_4", "Scheme_5"
combined_data_scheme_1 <- subset(combined_data_death_si_non_na, SchemeName == "Scheme1")
combined data scheme 2 <- subset(combined data death si non na, SchemeName == "Scheme2")
combined_data_scheme_3 <- subset(combined_data_death_si_non_na, SchemeName == "Scheme3")
combined_data_scheme_4 <- subset(combined_data_death_si_non_na, SchemeName == "Scheme4")
combined_data_scheme_5 <- subset(combined_data_death_si_non_na, SchemeName == "Scheme5")
# Sanity check that each subset has more than 0 rows
check_scheme_1 <- nrow(combined_data_scheme_1) > 0
check_scheme_2 <- nrow(combined_data_scheme_2) > 0
check_scheme_3 <- nrow(combined_data_scheme_3) > 0
check_scheme_4 <- nrow(combined_data_scheme_4) > 0
check_scheme_5 <- nrow(combined_data_scheme_5) > 0
# Print the results
cat("Scheme 1 has more than 0 rows:", check_scheme_1, "\n")
## Scheme 1 has more than 0 rows: TRUE
cat("Scheme 2 has more than 0 rows:", check_scheme_2, "\n")
## Scheme 2 has more than 0 rows: TRUE
cat("Scheme 3 has more than 0 rows:", check scheme 3, "\n")
## Scheme 3 has more than 0 rows: TRUE
cat("Scheme 4 has more than 0 rows:", check_scheme_4, "\n")
## Scheme 4 has more than 0 rows: TRUE
cat("Scheme 5 has more than 0 rows:", check_scheme_5, "\n")
## Scheme 5 has more than 0 rows: TRUE
# Perform a monte carlo simulation for each scheme
monte_carlo_scheme_1_result <- monte_carlo_simulation(combined_data_scheme_1)</pre>
monte_carlo_scheme_2_result <- monte_carlo_simulation(combined_data_scheme_2)</pre>
monte_carlo_scheme_3_result <- monte_carlo_simulation(combined_data_scheme_3)</pre>
monte_carlo_scheme_4_result <- monte_carlo_simulation(combined_data_scheme_4)</pre>
monte_carlo_scheme_5_result <- monte_carlo_simulation(combined_data_scheme_5)</pre>
```

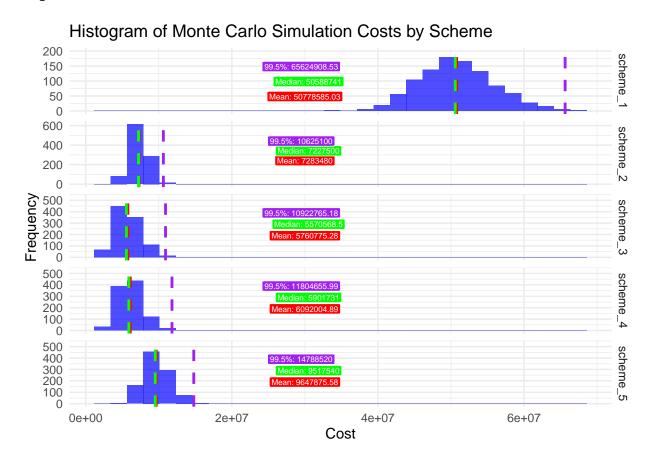
```
# Assuming you have 5 Monte Carlo simulation results, stored in a list
monte_carlo_results <- list(</pre>
  scheme 1 = monte carlo scheme 1 result,
  scheme_2 = monte_carlo_scheme_2_result,
 scheme 3 = monte carlo scheme 3 result,
 scheme_4 = monte_carlo_scheme_4_result,
 scheme_5 = monte_carlo_scheme_5_result
# Create an empty data frame to hold all the costs and corresponding scheme names
all_costs_data <- data.frame()</pre>
# Loop over each result and calculate costs, then combine into one data frame
for (scheme_name in names(monte_carlo_results)) {
  costs <- sapply(monte_carlo_results[[scheme_name]], function(x)</pre>
    x$cost)
 temp_data <- data.frame(Cost = costs, Scheme = scheme_name)</pre>
 all_costs_data <- rbind(all_costs_data, temp_data)</pre>
all_stats <- all_costs_data %>%
  group_by(Scheme) %>%
 summarise(
    mean_cost = mean(Cost),
    median_cost = median(Cost),
    percentile_99_5_cost = quantile(Cost, 0.995)
# Create different x and y positions for each label depending on the scheme
all_stats <- all_stats %>%
  mutate(
    # Dynamic x positions for each scheme
    x_position_mean = ifelse(
      Scheme == "scheme_1",
      3e+07,
      ifelse(
        Scheme == "scheme 2",
        3e+07,
        ifelse(
          Scheme == "scheme 3",
          3e+07,
          ifelse(Scheme == "scheme_4", 3e+07, 3e+07)
        )
      )
    ),
    x_position_median = x_position_mean + 0.5e+06,
    # Offset for median
    x_position_995 = x_position_mean - 0.5e+06,
    # Offset for 99.5th percentile
    # Dynamic y positions for each scheme
    y_position_mean = ifelse(
      Scheme == "scheme_1",
```

```
100,
      ifelse(
       Scheme == "scheme 2",
       400,
        ifelse(Scheme == "scheme_3", 325, ifelse(Scheme == "scheme_4", 325, 325))
      )
   ),
   y_position_median = ifelse(
     Scheme == "scheme 1",
      150,
      ifelse(
       Scheme == "scheme_2",
       500,
        ifelse(Scheme == "scheme_3", 425, ifelse(Scheme == "scheme_4", 425, 425))
      )
   ),
   y_position_995 = ifelse(
      Scheme == "scheme_1",
      200,
      ifelse(
       Scheme == "scheme_2",
       600,
       ifelse(Scheme == "scheme_3", 525, ifelse(Scheme == "scheme_4", 525, 525))
     )
   ),
  )
# Create the faceted plot with adjusted x and y positions for each level in the stack
ggplot(all_costs_data, aes(x = Cost)) +
  geom_histogram(bins = 30,
                 fill = "blue",
                 alpha = 0.7) + # Set the number of bins
  # Add vertical lines for mean, median, and 99.5th percentile
  geom_vline(
   data = all_stats,
   aes(xintercept = mean_cost),
   color = "red",
   linetype = "dashed",
   size = 1
  ) +
  geom_vline(
   data = all_stats,
   aes(xintercept = median_cost),
   color = "green",
   linetype = "dashed",
   size = 1
 ) +
  geom_vline(
   data = all_stats,
   aes(xintercept = percentile_99_5_cost),
   color = "purple",
   linetype = "dashed",
   size = 1
```

```
\# Add labels with dynamically adjusted x and y positions for each scheme
geom_label(
  data = all_stats,
  aes(
   x = x_position_mean,
   y = y_position_mean,
   label = paste("Mean:", round(mean_cost, 2))
  ),
  color = "white",
 fill = "red",
  size = 2,
 angle = 0,
 vjust = 2,
 hjust = 0.5
) +
geom_label(
  data = all_stats,
  aes(
   x = x_position_median,
   y = y_position_median,
   label = paste("Median:", round(median_cost, 2))
  ),
  color = "white",
 fill = "green",
 size = 2,
  angle = 0,
 vjust = 2,
 hjust = 0.5
) +
geom_label(
  data = all_stats,
  aes(
   x = x_position_995,
   y = y_position_995,
   label = paste("99.5%:", round(percentile_99_5_cost, 2))
  ),
  color = "white",
  fill = "purple",
  size = 2,
 angle = 0,
  vjust = 2,
 hjust = 0.5
) +
# Facet the plot vertically for each scheme
facet_grid(Scheme ~ ., scales = "free_y") +
labs(title = "Histogram of Monte Carlo Simulation Costs by Scheme", x = "Cost", y = "Frequency") +
theme_minimal()
```

## Warning: Using 'size' aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use 'linewidth' instead.

## This warning is displayed once every 8 hours.
## Call 'lifecycle::last\_lifecycle\_warnings()' to see where this warning was
## generated.



## Problem 2 – Statistical learning

The following code loads the data used in Problem 2. The data is stored in two .csv files containing a data set and a scoring set, respectively. These data are NOT related to Problem 1.

The goal of this problem is to predict the value of the variable outcome in the dataset defined above. The measure of goodness of fit is the area under the receiver operating characteristic curve (AUC) and will be measured on the scoring set.

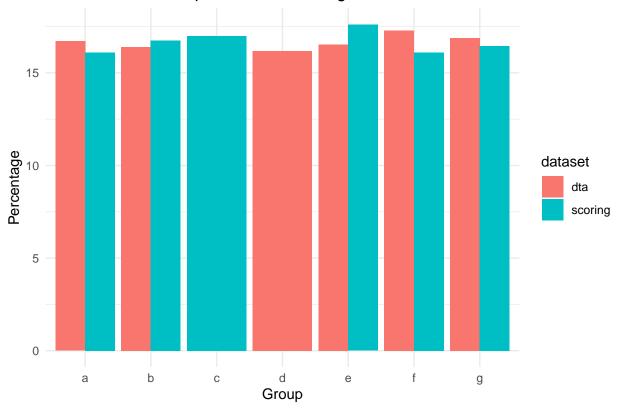
```
dta <- read_csv(</pre>
 here("Case Study/data/p02re_data.csv"),
 col_types = cols()
)
scoring <- read_csv(</pre>
 here("Case Study/data/p02re_scoring.csv"),
 col_types = cols()
)
head(dta)
## # A tibble: 6 x 11
   outcome group q r
                                     t
                              s
                                             u
                                                   V
                            <dbl> <dbl> <dbl> <dbl> <
##
      <dbl> <chr> <dbl> <dbl> <dbl>
                                                       <dbl>
                                                                <dbl>
## 1
         0 b
                2.70
                        NA 1.69 -0.0179 1.09
                                                 0.938 0.296
                                                               0.620
## 2
                         NA -0.951 -0.223 -0.384 0.328 0.160 -0.307
         1 b
                 0.647
         0 d
## 3
                1.60
                         NA -0.219 0.480 -0.630 -0.242 -0.435 -0.0416
                         NA 0.224 0.0942 -0.163 0.975 0.826
## 4
         0 a
                 2.90
## 5
         0 f
                 0.572
                         NA 0.0153 -1.23 0.322 -0.668 -0.0807 -0.367
## 6
         0 g
                 0.860
                         NA -0.916 -1.05 1.60 0.144 -0.933 -0.461
## # i 1 more variable: z <dbl>
head(scoring)
## # A tibble: 6 x 10
                           s t
    group
                                         u
                                               V
                                                               x
           q
                 r
    <chr> <dbl> <dbl>
                        <dbl> <dbl> <dbl>
                                             <dbl>
                                                    <dbl>
                                                           <dbl>
                                                                   <dbl>
## 1 f
         0.602 NA
                     0.242 -0.414 0.736 0.466
                                                   0.826
                                                          0.764
                                                                 0.720
                     -0.00545 1.25 -0.768
                                            0.0911 -0.0695 0.979 -0.857
## 2 g
         1.83 NA
## 3 c
         0.171
## 4 a
         2.31 NA
                     -0.214 0.231 0.143 -0.123
                                                   0.163 -0.0892 0.745
         0.957 0.199 0.755
## 5 e
                              2.02 -0.0480 -0.550
                                                   0.177
                                                          0.640
                                                                 0.0659
## 6 b
         1.76 NA
                    -0.132 -0.617 -0.454 0.818
                                                   0.579 -1.28
                                                                 0.284
unique_values <- sort(unique(dta$group))</pre>
print(unique_values)
## [1] "a" "b" "d" "e" "f" "g"
unique_values <- sort(unique(scoring$group))</pre>
print(unique_values)
## [1] "a" "b" "c" "e" "f" "g"
# For the first dataset (dta)
dta_percent <- dta %>%
 group_by(group) %>%
 summarise(count = n()) %>%
 mutate(percentage = count / sum(count) * 100, dataset = "dta")
```

```
# For the second dataset (scoring)
scoring_percent <- scoring %>%
  group_by(group) %>%
  summarise(count = n()) %>%
  mutate(percentage = count / sum(count) * 100, dataset = "scoring")

# Combine both datasets
combined_data <- bind_rows(dta_percent, scoring_percent)

ggplot(combined_data, aes(x = group, y = percentage, fill = dataset)) +
  geom_bar(stat = "identity", position = "dodge") + # side-by-side bars
  labs(title = "Distribution of Group in dta and scoring datasets", x = "Group", y = "Percentage") +
  theme_minimal()</pre>
```

# Distribution of Group in dta and scoring datasets



#### Question a.

Describe the statistical learning problem. Explain the difficulties in training a model with the above dataset.

This learning problem falls under **semi-supervised learning**, which combines labeled data (10,000 rows with targets from the "data" set) with a smaller amount of unlabeled data (2,000 rows without targets from the "scoring" set). The goal is to leverage both to improve the model's performance, typically by learning the structure of the data from the unlabeled dataset and refining predictions on the labeled dataset.

#### **Key Challenges:**

- 1. Handling Missing Values (NaNs in "R"): Missing data in the independent variable "R" will make it harder to apply some models directly. Techniques like imputation (e.g., mean, median, or model-based imputation) or excluding rows with missing values might be necessary. However, these methods can introduce bias or lead to information loss.
- 2. Bias Between Datasets: The distribution of the features in your labeled and unlabeled datasets might differ. If the 2,000 rows (without a target) are from a different distribution than the 10,000 rows (with targets), the model may struggle to generalize well.
- 3. Model Complexity: Semi-supervised models often require complex techniques such as self-training, co-training, or graph-based methods to use the unlabeled data efficiently. These techniques can be computationally expensive and tricky to fine-tune.
- 4. Feature Engineering for Unlabeled Data: Without a target in the 2,000-row dataset, extracting meaningful patterns is challenging. You may need to create features based on clustering, dimensionality reduction (e.g., PCA), or distance-based approaches to make the most of the unlabeled data.
- 5. Class Imbalance: If there's an imbalance in the target variable in your labeled dataset, the model might overfit to the more common class, especially with so much unlabeled data that has no class information to aid the minority class.
- 6. Semi-supervised Algorithms: The choice of a semi-supervised algorithm, such as Label Propagation, Self-learning, or Generative Models, impacts how well you can use both datasets. Many conventional algorithms like decision trees or linear models won't naturally extend to semi-supervised scenarios.

Each of these issues will need specific strategies for data preparation, model selection, and evaluation to get robust results.