

Applied 354 Lecture Notes

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1 Notes: 02 Aug

Calculate Divergence Theorem Given the vector field, where $z = 0$: ¹

$$\underline{v} = 3y^2z\underline{i} + 2y^2\underline{j} + yz^2\underline{k} \quad (1)$$

$$\underline{v} = 2y^2\underline{j} \quad (2)$$

The divergence theorem is given by:

$$\iint_A \nabla \cdot \underline{v} dA = \oint \underline{n} \cdot \underline{v} dr \quad (3)$$

Calculating the inside of the LHS:

$$\nabla \cdot \underline{v} = \underline{j} \frac{\partial}{\partial y} \cdot 2y^2\underline{j} = 4y \quad (4)$$

Therefor calculating LHS:

$$\iint_A \nabla \cdot \underline{v} dA = \int_2^3 \int_2^4 4y \, dx dy \quad (5)$$

$$\iint_A \nabla \cdot \underline{v} dA = \left| 8 \frac{y^2}{2} \right|_2^3 = 20 \quad (6)$$

Calculating the RHS, using the graphic finding the normal vectors to each side. Only two terms are present as $\underline{i} \cdot \underline{j}$ will be zero, so the verticals are zero.

¹hello my name is periwinkle and im so cute and hungry

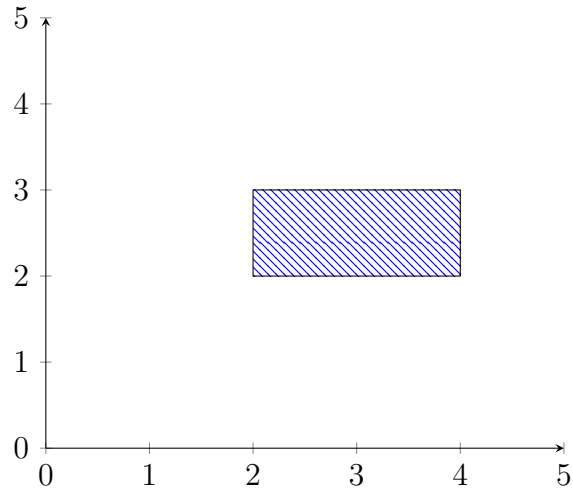
$$\oint \underline{n} \cdot \underline{v} dr = \int_2^4 -\underline{j} \cdot 2y^2 \underline{j} dx + \int_2^4 \underline{j} \cdot 2y^2 \underline{j} dx \quad (7)$$

Using Figure:1 replacing the y values from the graphic, 2 and 3 respectively

$$= \int_2^4 -8dx + \int_2^4 18dx = 20 \quad (8)$$

Therefor RHS = LHS

Figure 1: Vector Field Figure



Calculate Stokes Integral Theorem for the velocity field $v = x\underline{j}$