

Programming (G54PRG)

4th exercise

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This exercise is about object oriented programming in Python. Your task is to use objects to implement a representation of Boolean expressions which can be printed and evaluated. On top of this, you should implement a method to produce truth tables and a tautology checker which determines whether the expression is *true* for every assignment of truth values.

1. In particular you are supposed to implement the following classes:

Expr superclass for all boolean expressions,

Not represents logical negation,

And represents logical and,

Or represents logical or,

Eq represents logical equivalence,

Var represents logical variables

with constructors, so that, we can define the following expression trees:

```
e1 = Or(Var("x"),Not(Var("x")))
e2 = Eq(Var("x"),Not(Not(Var("x"))))
e3 = Eq(Not(And(Var("x"),Var("y"))),Or(Not(Var("x")),Not(Var("y"))))
e4 = Eq(Not(And(Var("x"),Var("y"))),And(Not(Var("x")),Not(Var("y"))))
```

2. Each class should implement an `__str__` method, so that, the above expressions print as follows:

```
x|!x
x==!!x
!(x&y)==!x|!y
!(x&y)==!x&!y
```

It is ok but not perfect if you implement a version that prints too many brackets (that is better than printing not enough).

To minimise the number of brackets you should take into account that:

(a) Not (!) binds stronger than And (&), e.g.

```
>>> print(And(Not(Var("p")),Var("q")))
!p&q
>>> print(Not(And(Var("p"),Var("q"))))
!(p&q)
```

(b) And (&) binds stronger than Or (|),e.g.

```
>>> print(Or(And(Var("p"),Var("q")),Var("r")))
p&q|r
>>> print(And(Var("p"),Or(Var("q"),Var("r"))))
p&(q|r)
```

(c) Or (|) binds stronger than Eq (==),e.g.

```
>>> print(Eq(Or(Var("p"),Var("q")),Var("r")))
p|q==r
>>> print(Or(Var("p"),Eq(Var("q"),Var("r"))))
p|(q==r)
```

This order is transitive, e.g. ! binds stronger than | and ==, and so on.

All binary operations (including ==) are associative, hence there is no need to use brackets when only one kind of operation is used. E.g.

```
>>> print (And(Var("x"),And(Var("y"),Var("z"))))
x&y&z
>>> print (And(And(Var("x"),Var("y")),Var("z")))
x&y&z
```

3. Implement a method `make_tt` which returns the truthtable as a string. That is for example `print(e4.make_tt())` should produce the following output:

y	x	!(x&y)==!x&!y
True	True	True
False	True	False
True	False	False
False	False	True

The order in which you produce the lines doesn't matter.

The method should work for any collections of variables, not just for two called `x` and `y`.

4. A proposition is called a tautology if it is always *true*. That is, the truthtable contains only `True` in the last column. Implement a method `isTauto` which determines whether the proposition is a tautology. E.g.

```
>>> e1.isTauto()
True
>>> e4.isTauto()
False
```

As above, this method should work correctly for propositions with any collection of variables.

Test your code with the test in `test04.py` which can be downloaded from Moodle. However, it should also work for other examples.

To get full marks your program should work, be well documented, not be unnecessarily complicated and you should use inheritance to avoid code duplication.

Important notes:

- Use only the operations that have been introduced in the lectures.
- Make sure you note down the name of the demonstrator.
- We will not give you the marks immediately.
- **Submission deadline: 29th of November.**
- **Demo deadline: 6th of December.**