

Lecture 3-1 Color Image Processing (chapter 6)

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Outline

➤ **Standard color spaces**

- RGB
- CMYK
- HSI
- Lab

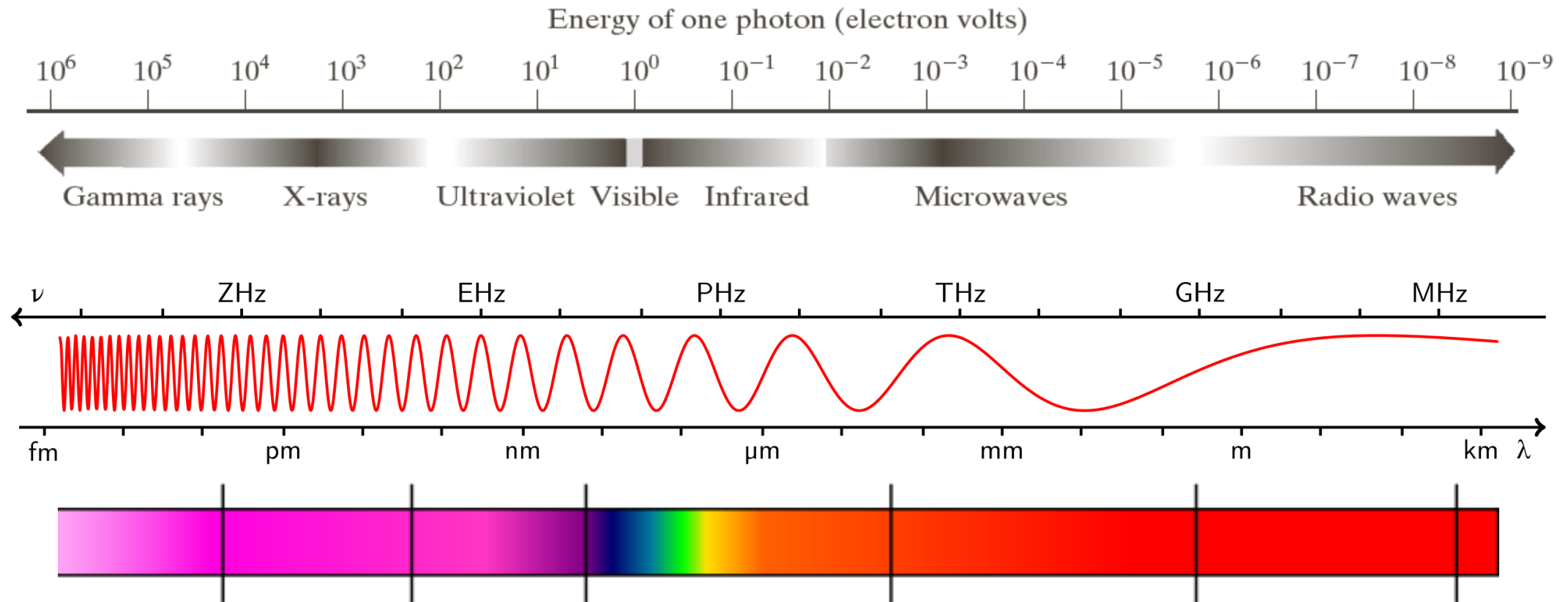
➤ **Transform between color spaces**

- RGB to gray scale
- RGB to
- HIS
- RGB to Lab

➤ **Color balance**



Electromagnetic spectrum

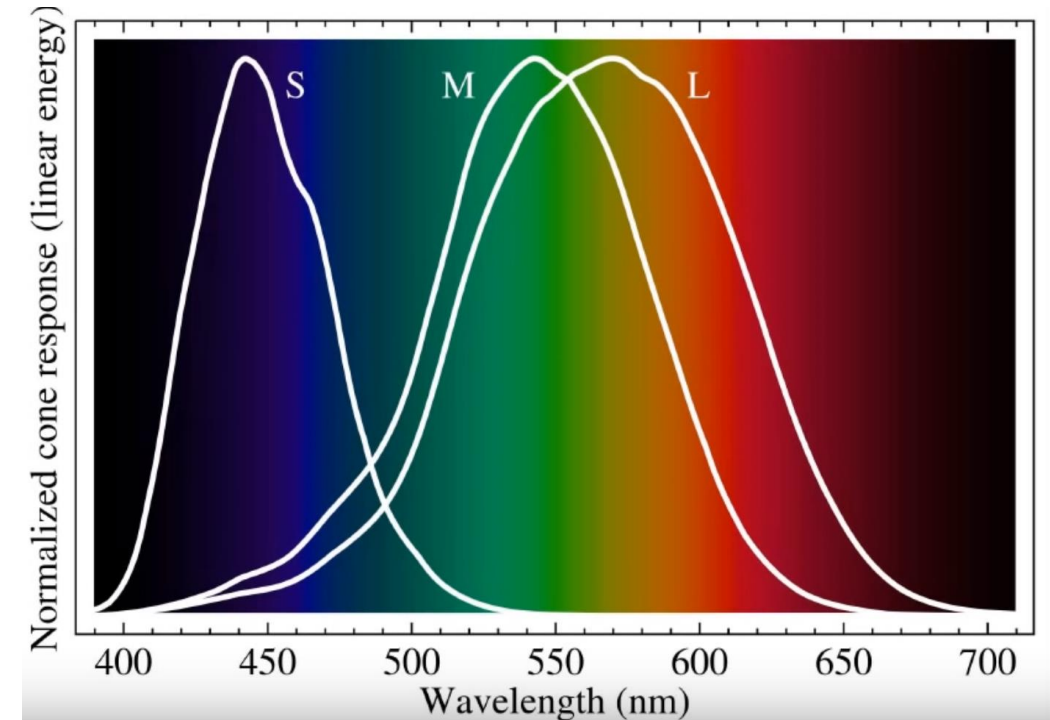


Dispersion of light



Human visual system color Space

- **The LMS color space:** Cones enable color perceptions;
- 3 Types of cones:
- **Long:** sensitive to “RED” (more yellow to blue) 65%
- **Middle :** sensitive to “GREEN” (more green to blue) 33%
- **Short :** sensitive to “BLUE” (more blue to purple) 2%
(But most sensitive)



Primary colors

➤ **CIE RGB Standard** ([International Commission on Illumination](#))

- Blue = 435.8 nm [Commission International d'elairage](#)
- Green = 546.1 nm
- Red = 700 nm

➤ **The white light is** achieved with a mixture of RGB light with:

- 1.0000 : 4.5907 : 0.0601 of intensity (Luminous intensity) .

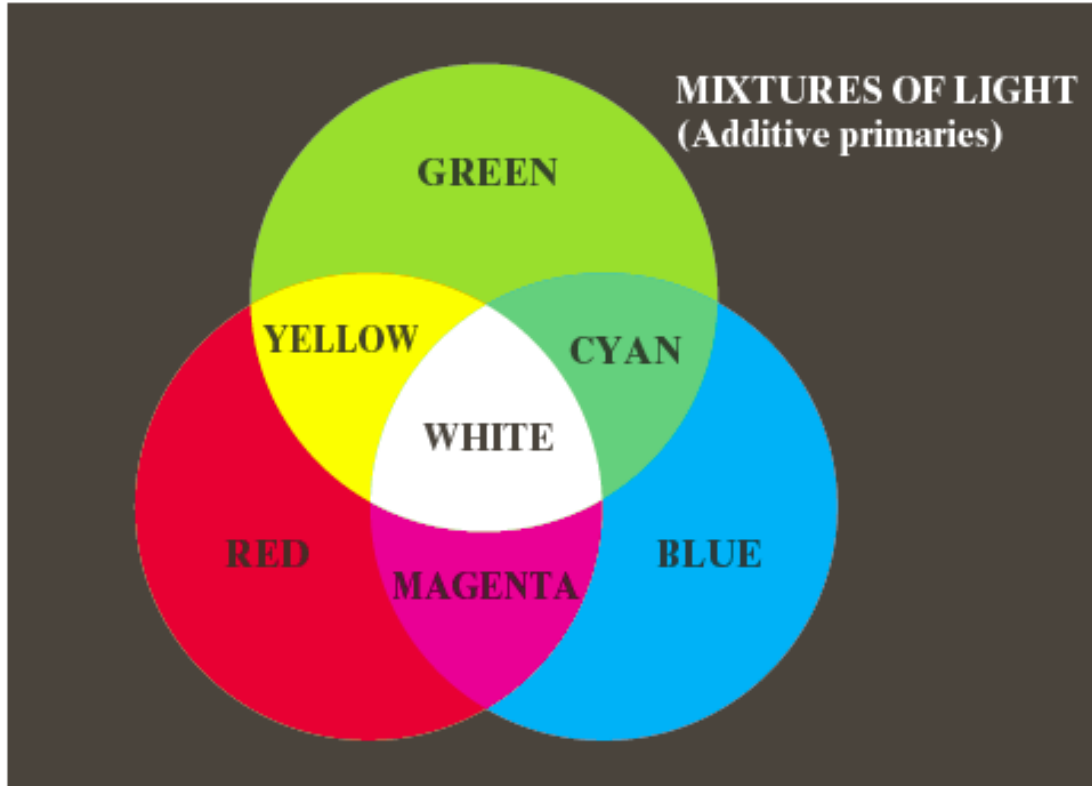
➤ **CMY and CMYK color**

- Cyan = White – Red
- Magenta = White – Green
- Yellow = White – Blue
- Black = White – Red - Green - Blue

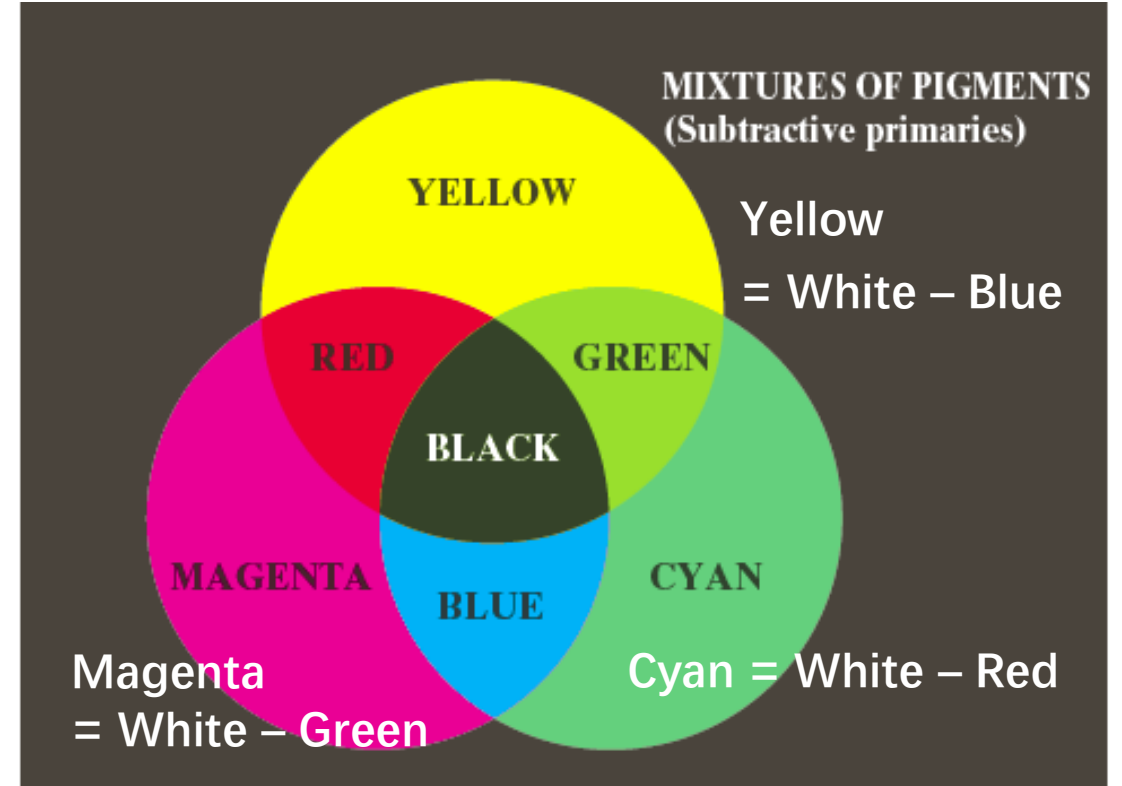


Secondary colors

RGB color



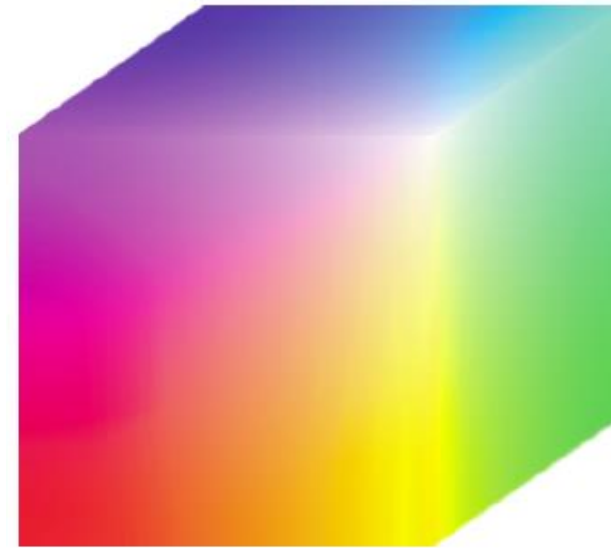
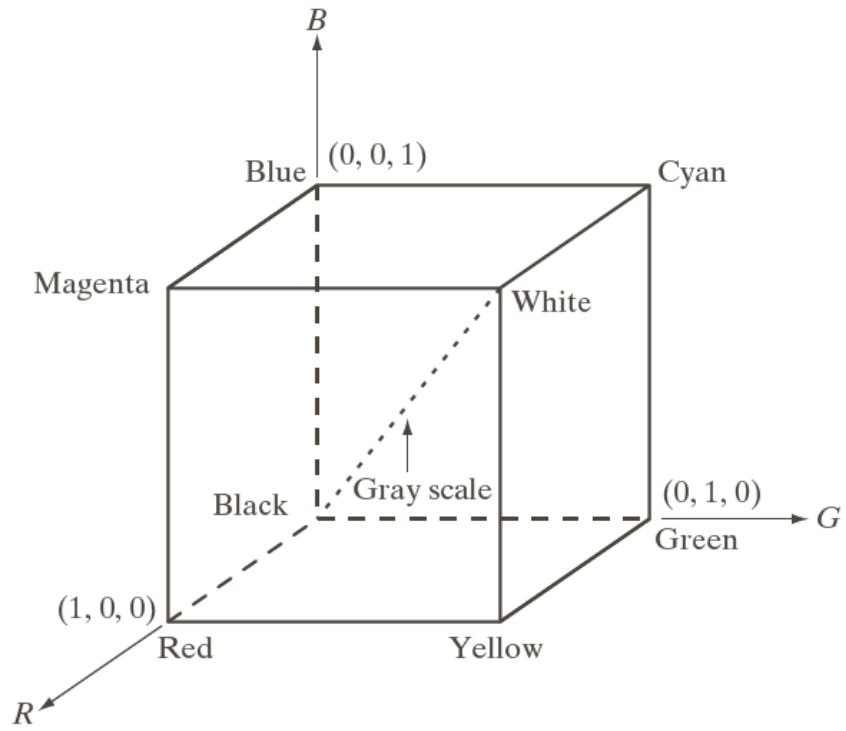
CMY and CMYK color



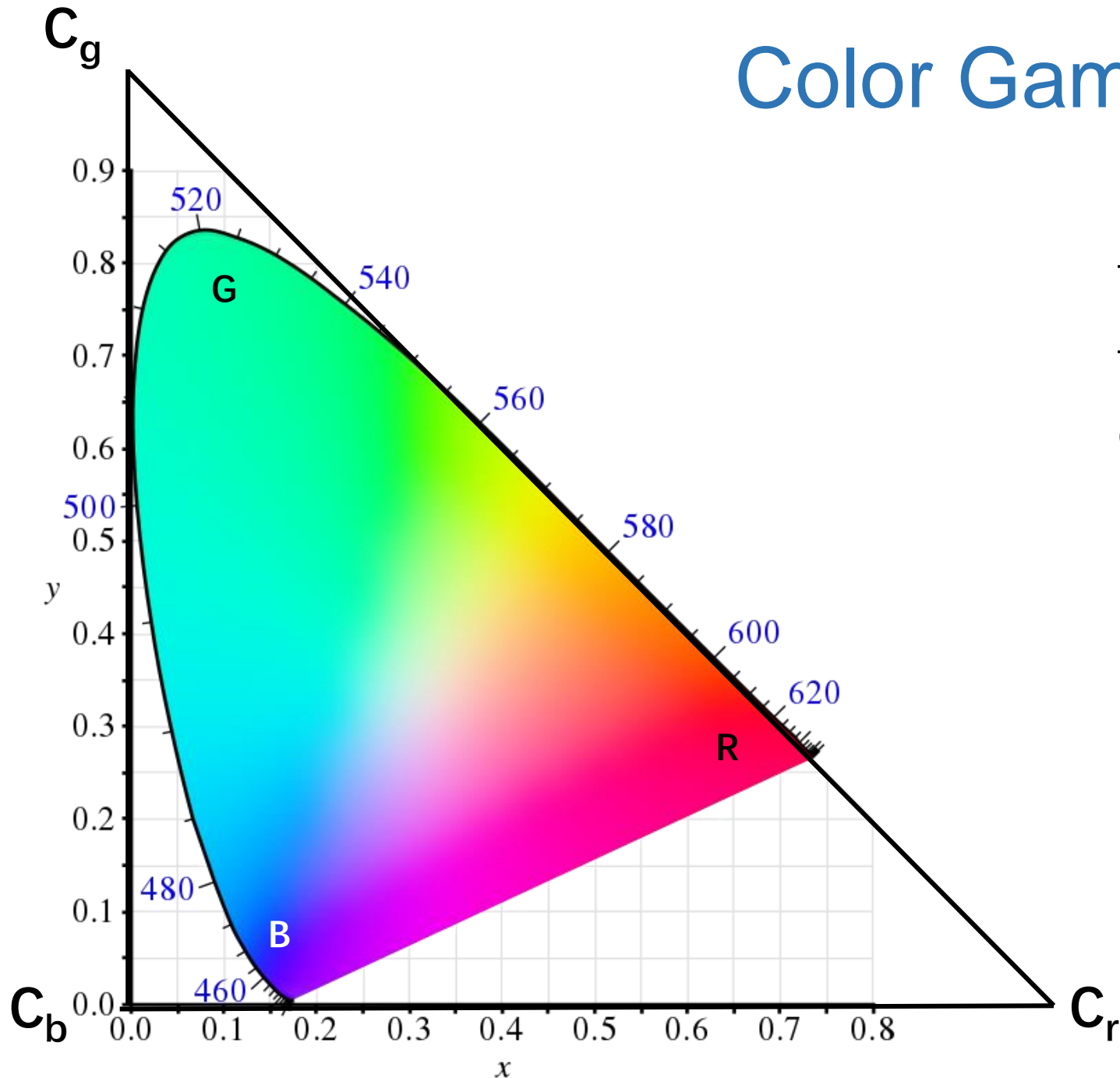
Black = White – Red – Green – Blue



RGB Color Model



Color Gamut



$$\text{➤ } x = \frac{R}{R+G+B}, y = \frac{G}{R+G+B}, z = \frac{B}{R+G+B}$$

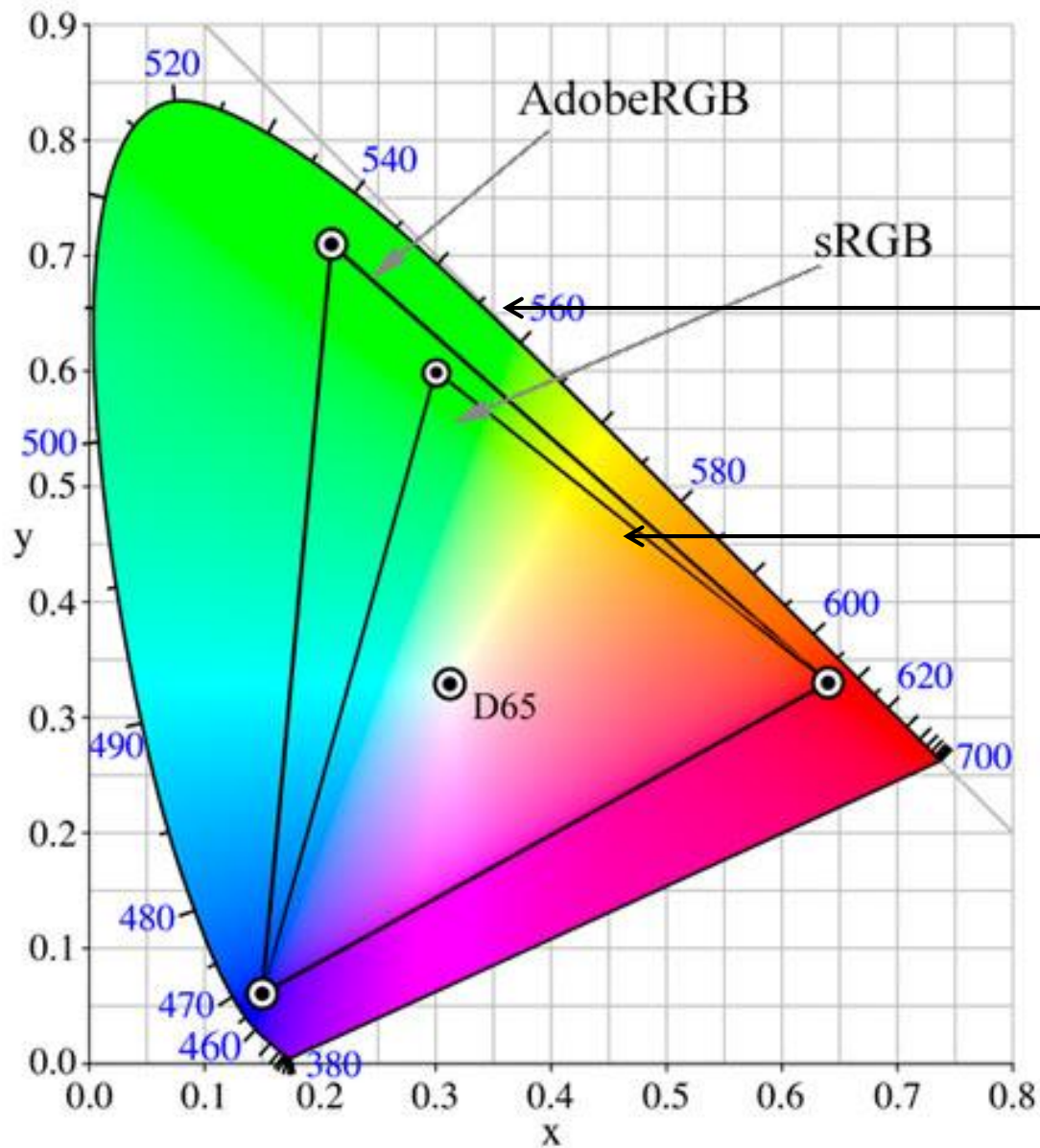
Then $z = 1 - x - y$.

The color cube is turns to a 2-D color gamut.

- It is seen that all visible chromaticities correspond to non-negative values of x , y , and z .
- An equal mixture of two equally bright colors will not generally lie on the midpoint of that line.



Color Gamut



White: D65 [0.3127,0.3290]

Red: [0.6400, 0.3300]

Green: [0.3000, 0.6000]

Blue: [0.1500, 0.0600]

CIE Chromaticity diagram

Color gamut for monitor

- **sRGB (standard Red Green Blue)** is an RGB color space and Microsoft created cooperatively in 1996 to use on monitors, printers, and the Internet.
- The **Adobe RGB (1998) color space** is an RGB color space developed by Adobe System, Inc. in 1998.



CMY Color Model

➤ RGB to CMY conversion

$$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

In order to produce true black in printing, a fourth color, black, is added into the CMYK color model



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➤ Transform between color spaces

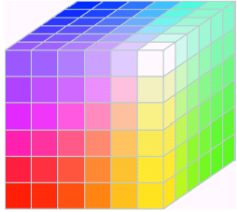
- RGB to gray scale
- RGB to
- HIS
- RGB to Lab

➤ Color balance

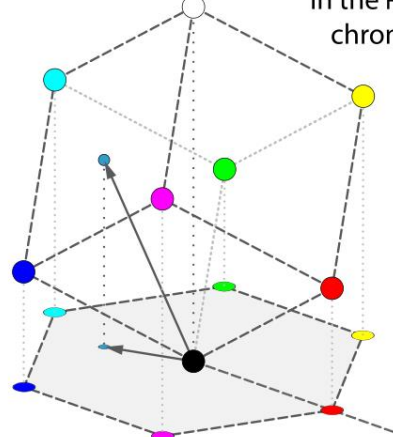


HSI/HSV Color Model

RGB color cube



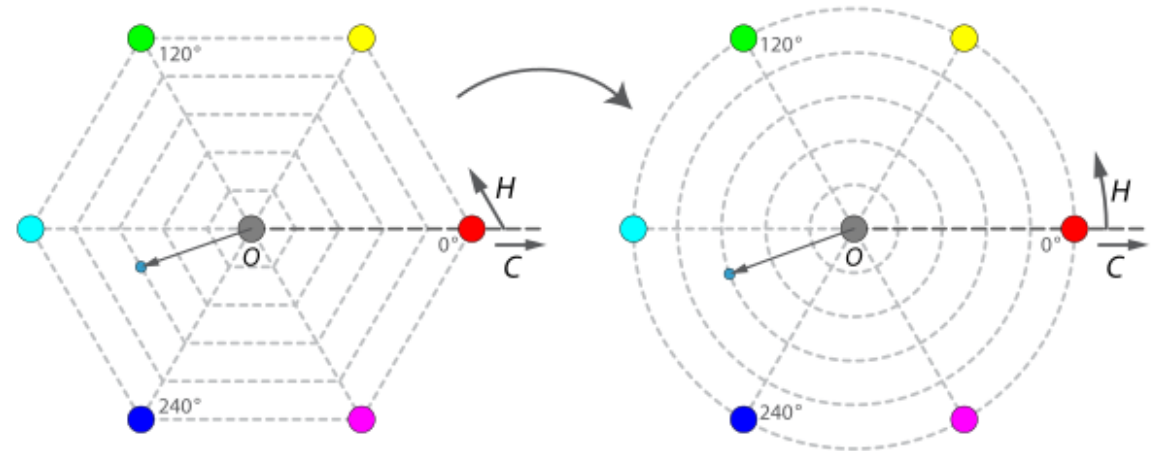
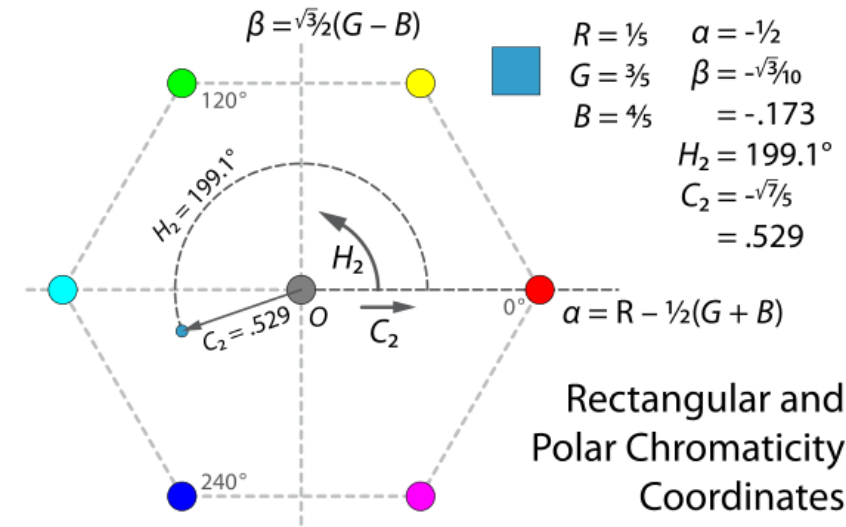
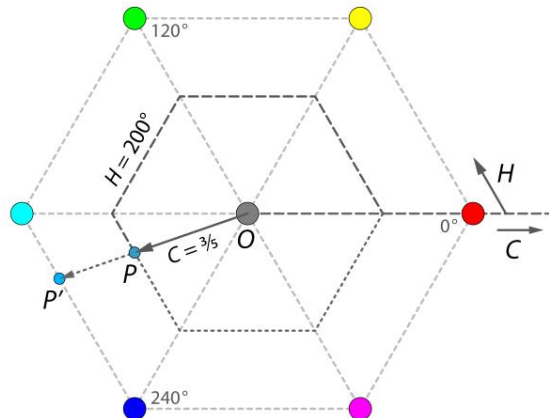
Hue and chroma
in the HSL/HSV
chromaticity
plane



$$\begin{aligned} R &= \frac{1}{5} \\ G &= \frac{3}{5} \\ B &= \frac{4}{5} \end{aligned}$$

$$C = \frac{OP}{OP'} = B - R = \frac{4}{5} - \frac{1}{5} = \frac{3}{5} = .6$$

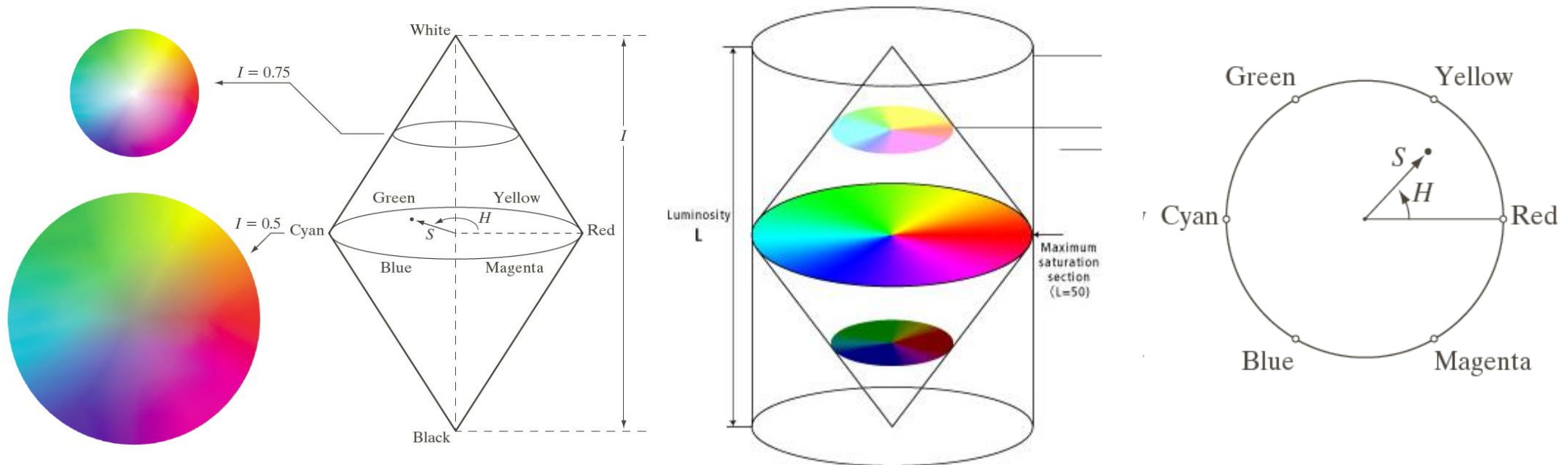
$$H = 60^\circ \times \left(4 + \frac{R-G}{C} \right) = 60^\circ \times \left(4 - \frac{2}{3} \right) = 200^\circ$$



HSI/HSL Color Model

➤ HSI Color Model

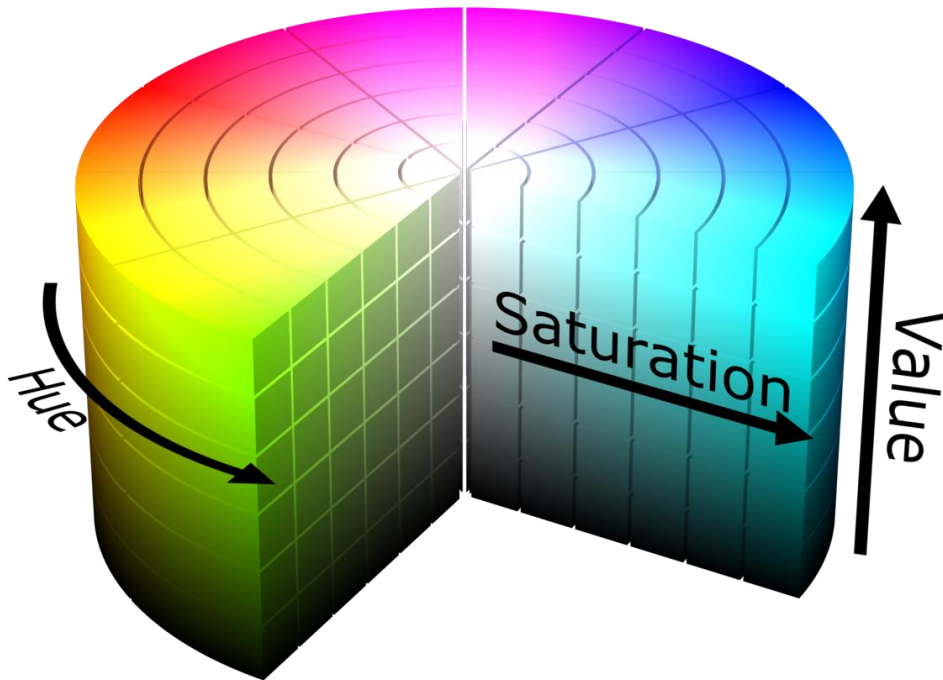
- **Hue:** Dominant color associated with wavelength.
- **Saturation:** relative purity, the amount of white light mixed with a hue
- **Intensity/Lightness.** $I = (r + g + b) / 3$



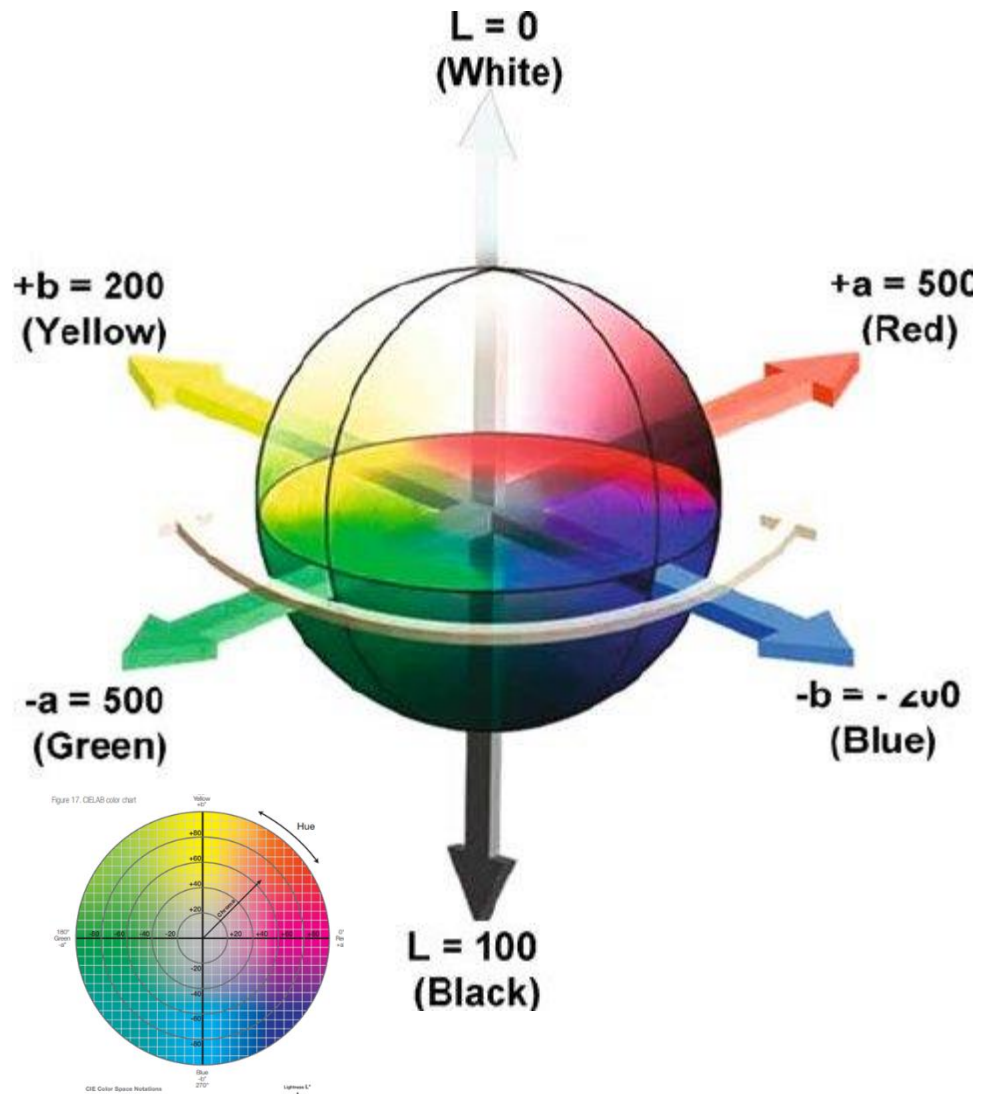
HSV Color Model

➤ HSI Color Model

- **Hue:** Dominant color associated with wavelength.
- **Saturation:** relative purity, the amount of white light mixed with a hue
- **Value.** $v = \max(r, g, b);$



Lab Color Model



- **L*:** Lightness
- **a*:** Red/Green Value
- **b*:** Blue/Yellow Value
- The a* axis runs from left to right. A color measurement movement in the +a direction depicts a shift toward red.
- Along the b* axis, +b movement represents a shift toward yellow.
- The center L* axis shows L = 0 (black or total absorption) at the bottom.
- At the center of this plane is neutral or gray.



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➤ Transform between color spaces

- RGB to gray scale
- RGB to CMY
- RGB to HSI/HSV

➤ Color balance



RGB to Gray scale

- Maximum value:

$$g_R(x, y) = g_G(x, y) = g_B(x, y) = \max[f_R(x, y), f_G(x, y), f_B(x, y)]$$

- Average value

$$g_R(x, y) = g_G(x, y) = g_B(x, y) = [f_R(x, y) + f_G(x, y) + f_B(x, y)]/3$$

- Weighted value

$$g_R(x, y) = g_G(x, y) = g_B(x, y) = 0.299f_R(x, y) + 0.587f_G(x, y) + 0.114f_B(x, y)$$



Transform to CMY Color Space

- $$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$



- $$\begin{bmatrix} g_R(x, y) \\ g_G(x, y) \\ g_B(x, y) \end{bmatrix} = \begin{bmatrix} 255 - f_R(x, y) \\ 255 - f_G(x, y) \\ 255 - f_B(x, y) \end{bmatrix}$$



Transform from RGB to HSI

$$\theta = \arccos \left\{ \frac{\frac{1}{2}[(R - G) + (R - B)]}{[(R - G)^2 + (R - G)(G - B)]^{\frac{1}{2}}} \right\}$$

$$H = \begin{cases} \theta, & G \geq B \\ 360 - \theta, & G < B \end{cases}$$

$$S = 1 - \frac{3}{R + G + B} [\min(R, G, B)]$$

$$I = \frac{R + G + B}{3} \quad V = \max(R, G, B);$$

$$S = 0 \rightarrow H = 0, \quad I = 0 \rightarrow S = 0, \quad H = 0$$



Transform from HSI to RGB

➤ $0^\circ \leq H < 120^\circ$

$$B = I(1 - S), \quad R = I \left[1 + \frac{S \cos(H)}{\cos(60^\circ - H)} \right], \quad G = 3I - (R + B)$$

➤ $120^\circ \leq H < 240^\circ$

$$R = I(1 - S), \quad G = I \left[1 + \frac{S \cos(H - 120^\circ)}{\cos(180^\circ - H)} \right], \quad B = 3I - (R + G)$$

➤ $240^\circ \leq H < 360^\circ$

$$G = I(1 - S), \quad B = I \left[1 + \frac{S \cos(H - 240^\circ)}{\cos(300^\circ - H)} \right], \quad R = 3I - (G + B)$$



Color Balance

➤ White balance:

$$I(x, y) = 0.299f_R(x, y) + 0.587f_G(x, y) + 0.114f_B(x, y)$$

$$k_R = \frac{\bar{I}}{\bar{f}_R} \quad k_G = \frac{\bar{I}}{\bar{f}_G} \quad k_B = \frac{\bar{I}}{\bar{f}_B}$$

$$\begin{bmatrix} g_R(x, y) \\ g_G(x, y) \\ g_B(x, y) \end{bmatrix} = \begin{bmatrix} k_R & & \\ & k_G & \\ & & k_B \end{bmatrix} \begin{bmatrix} f_R(x, y) \\ f_G(x, y) \\ f_B(x, y) \end{bmatrix}$$

➤ Maximum value balance

$$S_{RGB} = \min[R_{max}, G_{max}, B_{max}]$$

$$k_R = \frac{S_{RGB}}{T_R} \quad k_G = \frac{S_{RGB}}{T_G} \quad k_B = \frac{S_{RGB}}{T_B}$$

$$\begin{bmatrix} g_R(x, y) \\ g_G(x, y) \\ g_B(x, y) \end{bmatrix} = \begin{bmatrix} k_R & & \\ & k_G & \\ & & k_B \end{bmatrix} \begin{bmatrix} f_R(x, y) \\ f_G(x, y) \\ f_B(x, y) \end{bmatrix}$$

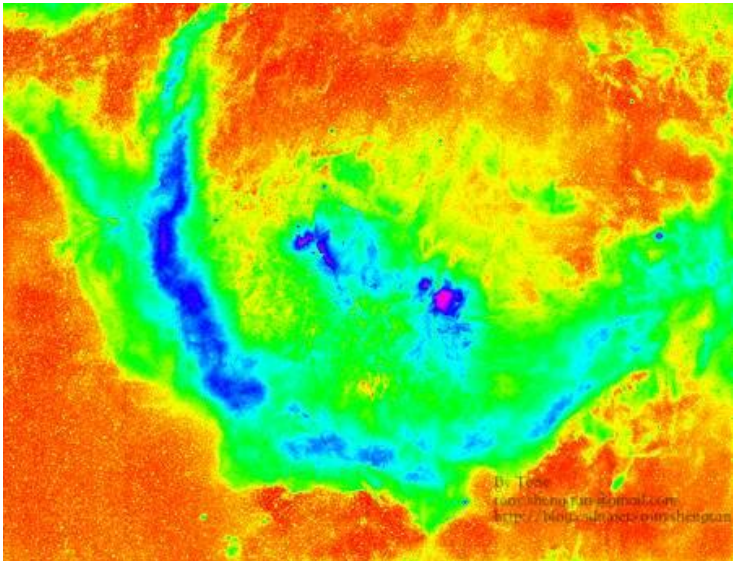
1. Find the smallest max value S_{RGB} in each color channel.

2. Calculate the number of intensities N_r, N_g, N_b that larger than S_{RGB} in each color channel. Then find the largest number $N_{max} = \max[N_r, N_g, N_b]$.

3. Sort the intensities in each channel and find the the $N_{max_{th}}$ intensity value $[T_r, T_g, T_b]$ in each color channel.



Pseudo color enhancement



Take home message

- 1. The color that you perceived depends on the cone cells in your eye.
- 2. There are variety of different color space defined by CIE. Each color space has its unique advantage.
- 3. When the intensity in each color channel is unbalance, the color looks weird. Try to practice color space transform by implementing a color balance correction method.

