

Lecture 6-2 Histogram 2 (chapter 3.6)

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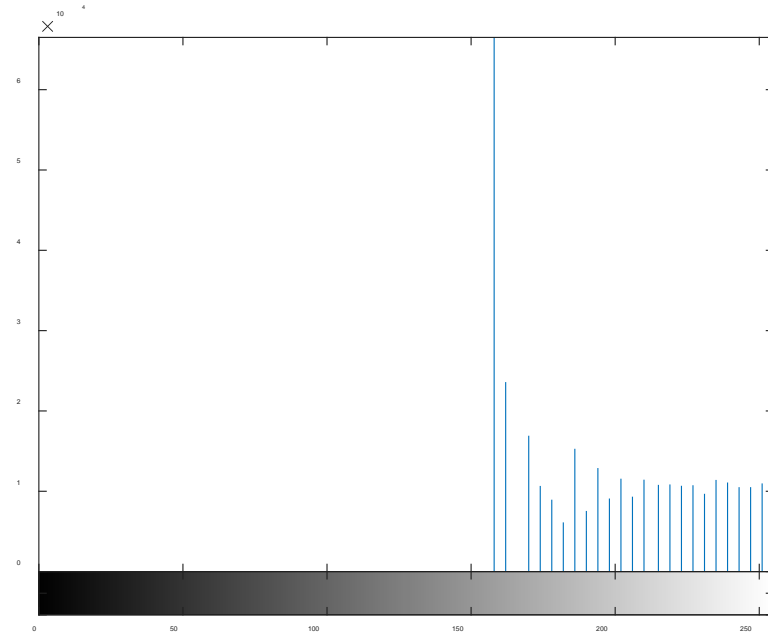
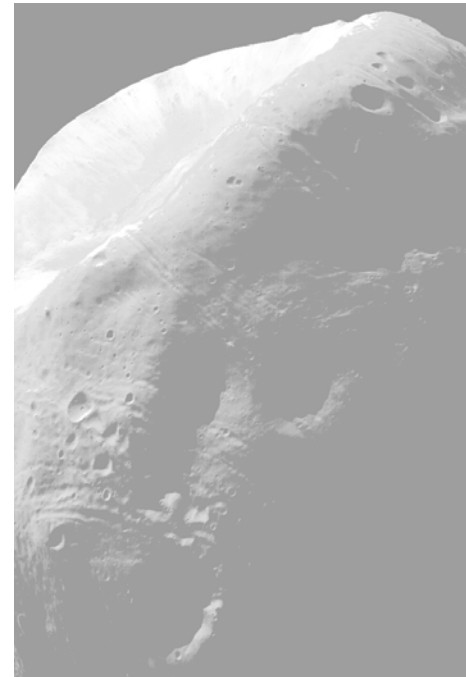
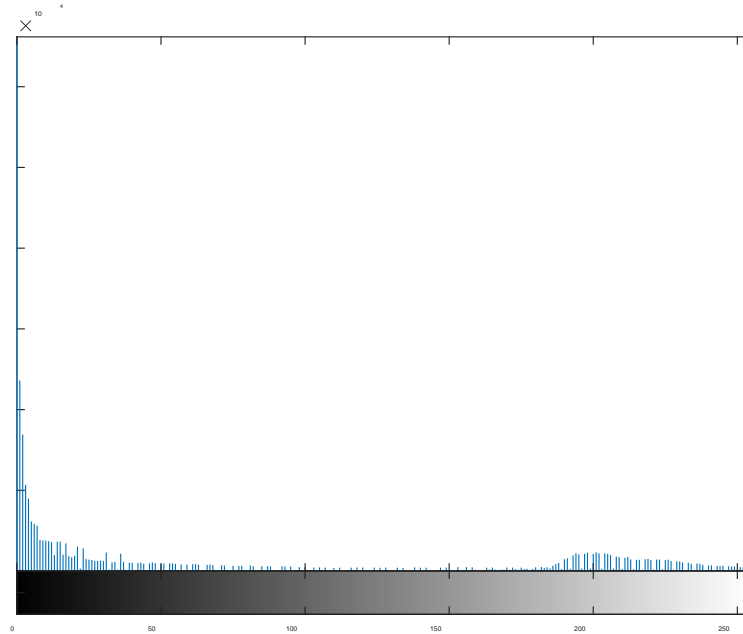
Outline

- Adaptive Histogram Equalization (AHE)
- Contrast Limited Adaptive Histogram Equalization (CLAHE)

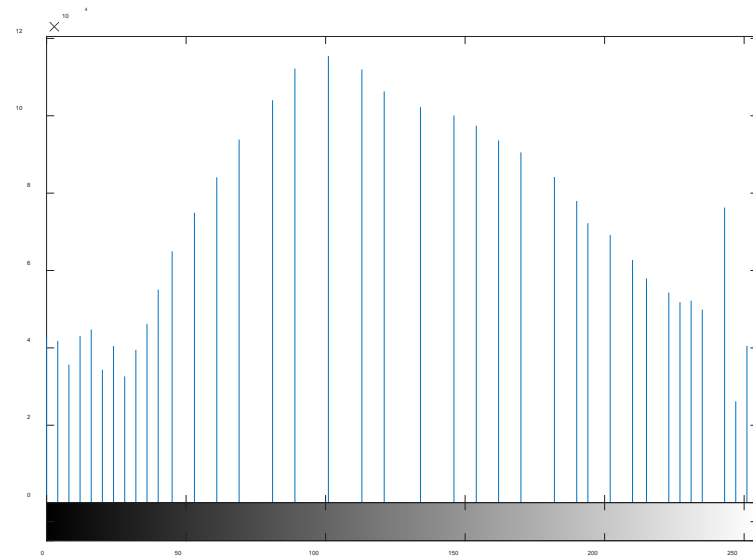
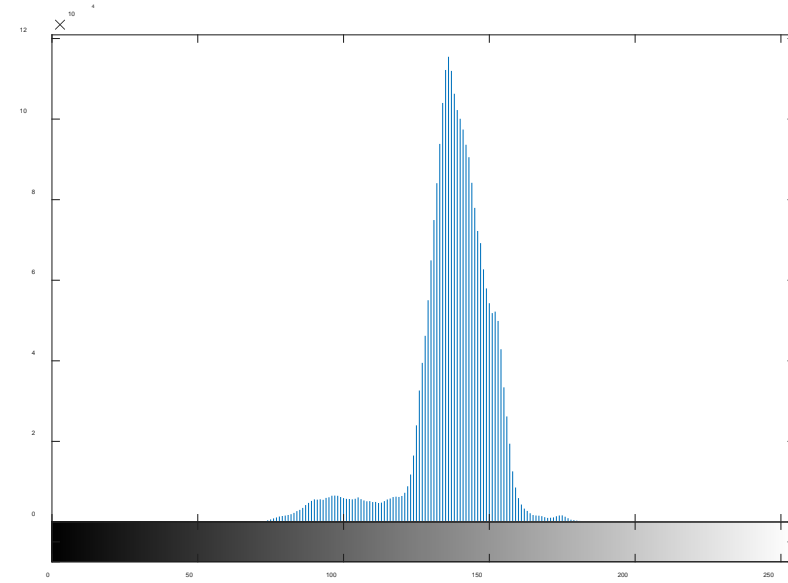


Key problem of HE

$$s = T(r) = (L - 1) \int_0^r p_r(w) dw = (L - 1) \sum_{j=0}^k p_r(r_j) = (L - 1) \sum_{j=0}^k \frac{n_j}{MN} = \frac{L - 1}{MN} \sum_{j=0}^k n_j$$



Key problem of HE



Naïve Adaptive Histogram Equalization

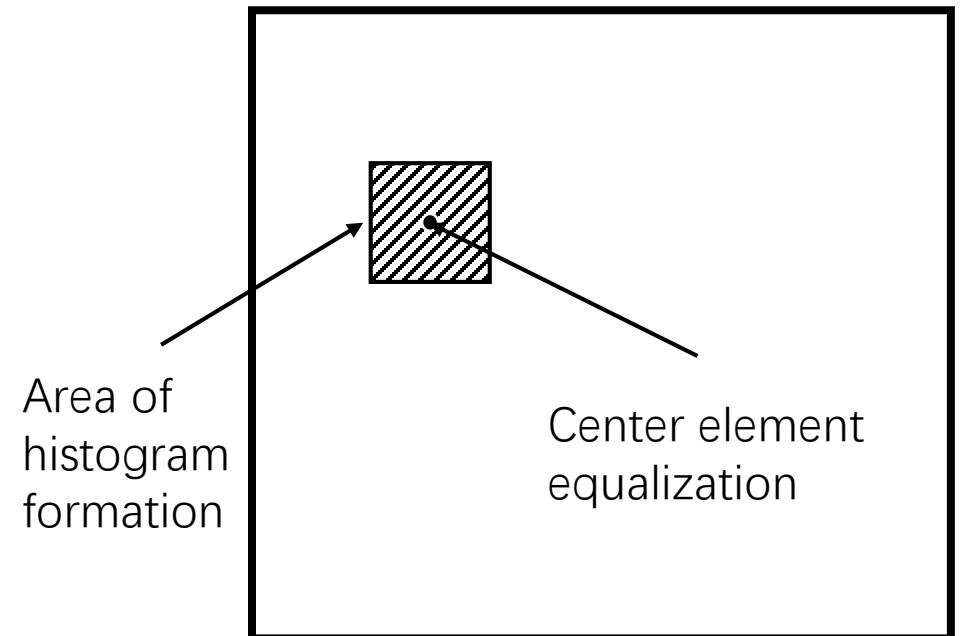
➤ Traverse every pixel with a $W * W$ patch, process histogram equalization within each patch and update the center pixel.

➤ Advantage: better uniform distributed histogram.

➤ Disadvantage: high complexity

$O(W * W + L)$ within each patch

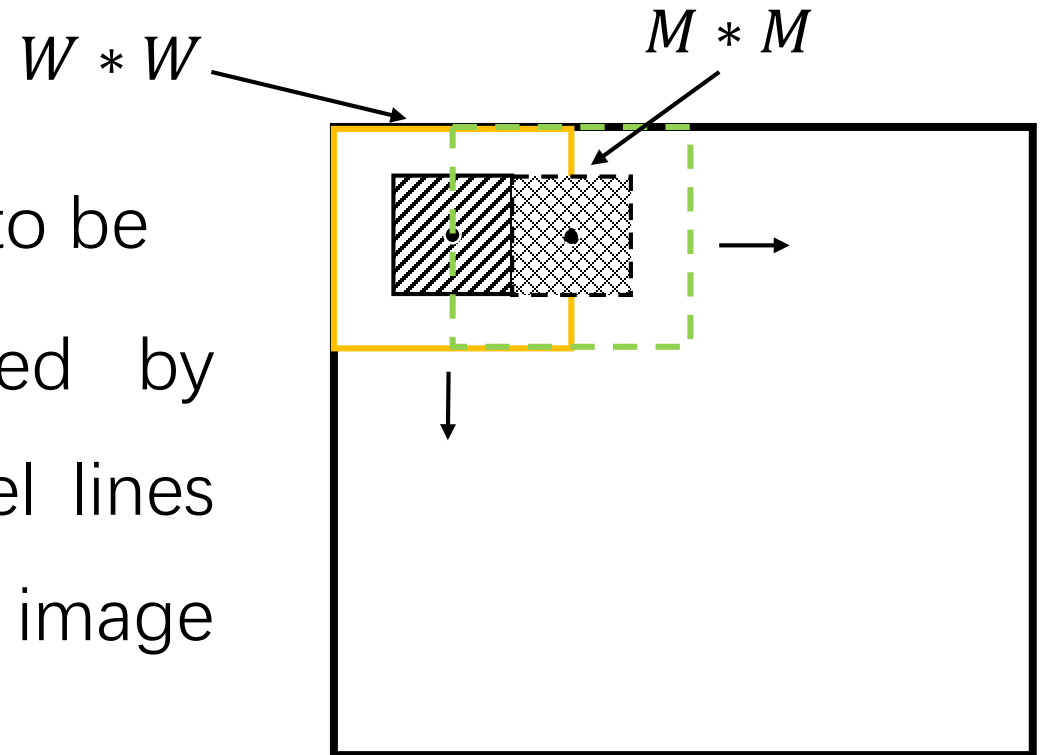
$O(M * N * (W * W + L))$ for whole image



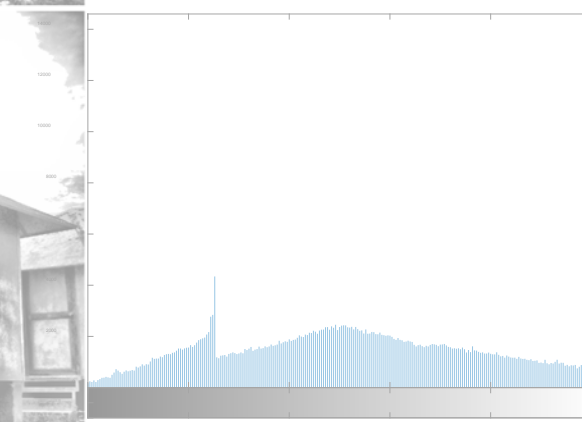
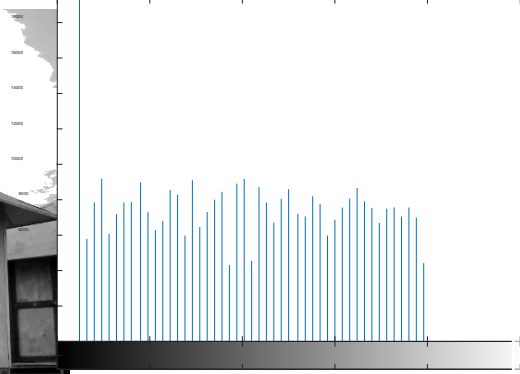
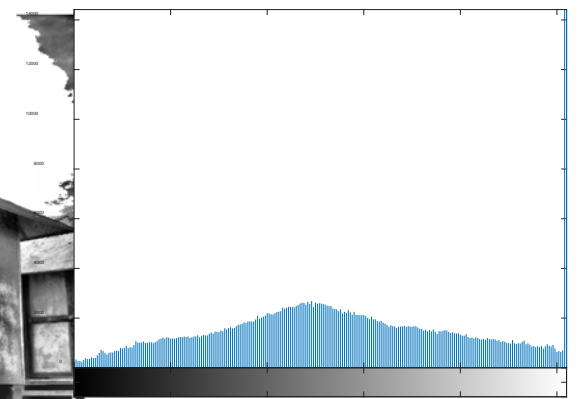
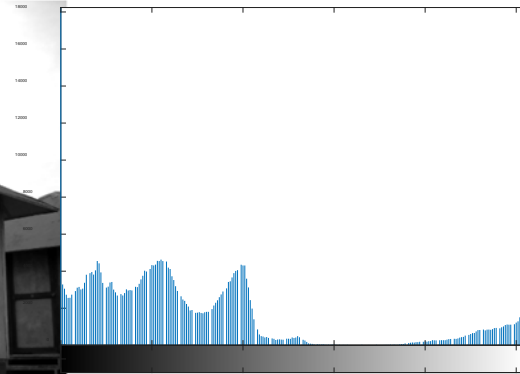
Naïve Adaptive Histogram Equalization

➤ For faster processing AHE, it is proposed to update a center patch of size $M * M$ instead of just the center pixel in each HE in each within the $W * W$ patch HE.

➤ Pixels near the image boundary have to be treated specially, This can be solved by extending the image by mirroring pixel lines and columns with respect to the image boundary.



Effect of AHE



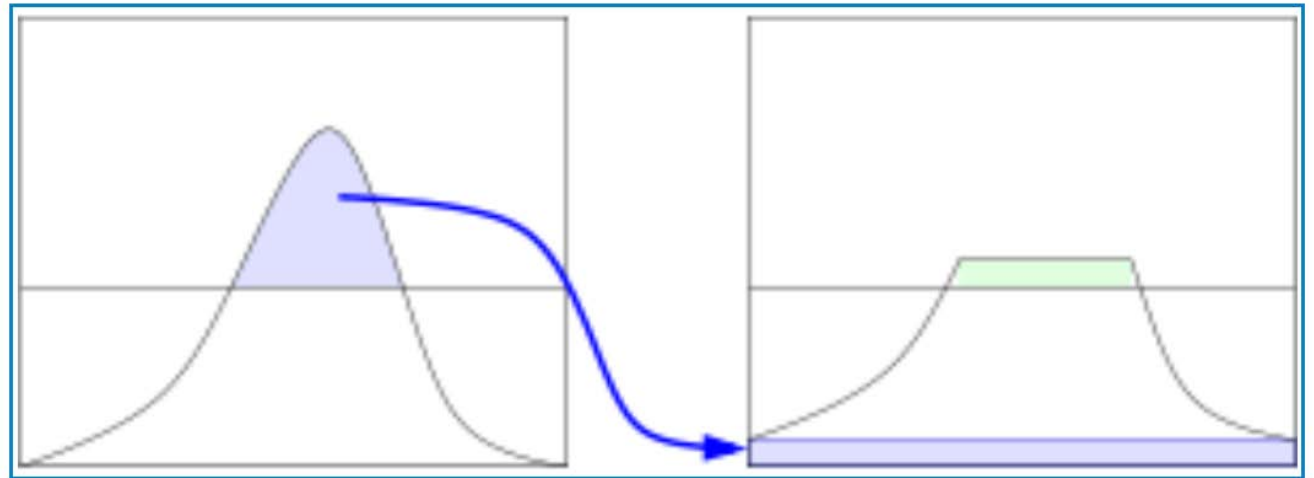
Contrast Limited Adaptive Histogram Equalization (CLAHE)

- CLAHE differs from naïve AHE in its contrast limiting.
- CLAHE was developed to prevent the over amplification of noise that AHE can give rise to.
- This feature can also be applied to global histogram equalization, giving rise to contrast limited histogram equalization.

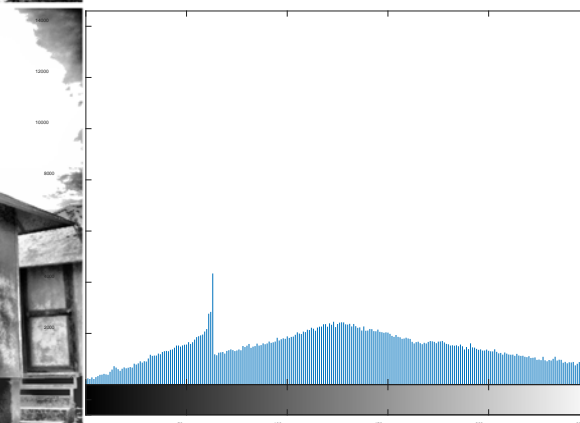
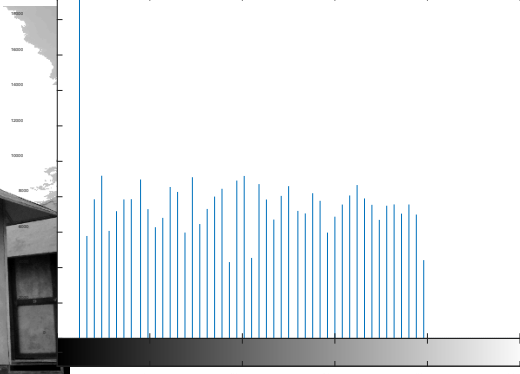
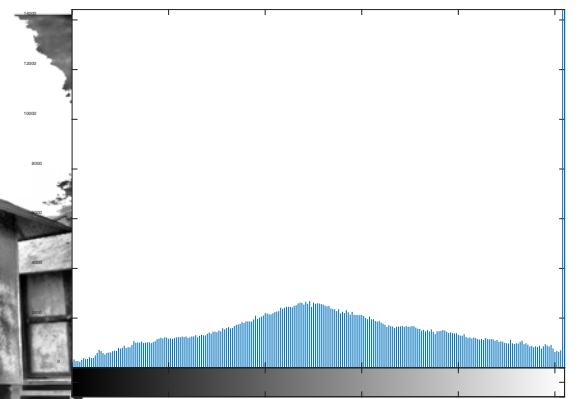
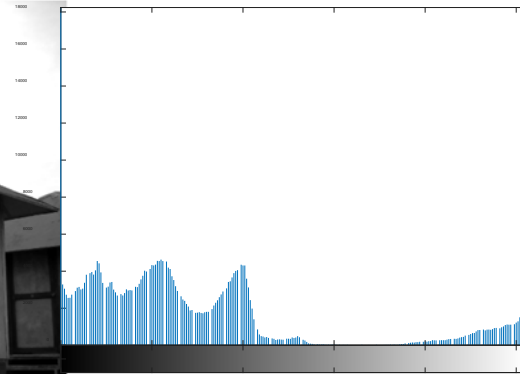


CLAHE

- CLAHE limits the amplification by clipping the histogram at a predefined value before computing the CDF.
- This limits the slope of the CDF and therefore of the transformation function.
- The so-called clip limit depends on the normalization of the histogram and thereby on the size of the neighbourhood region.



Effect of CAHE



Take home message

- Key idea: AHE&CLAHE was developed to prevent the over amplification of noise.

