

Lecture 22-2 Graph-cut Segmentation

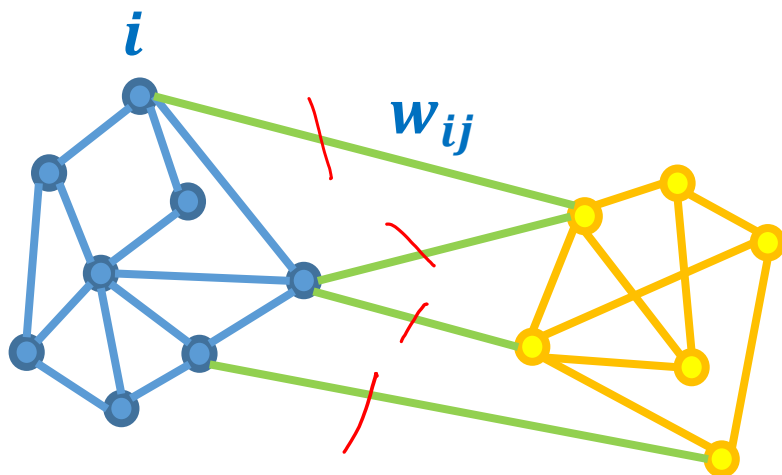
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SIST Building 2 302-F

min cut

Graph-cut segmentation



$$G = \{V, E\}$$

V : Graph nodes

Image = {pixels}

E : edges connection nodes

Pixel similarity



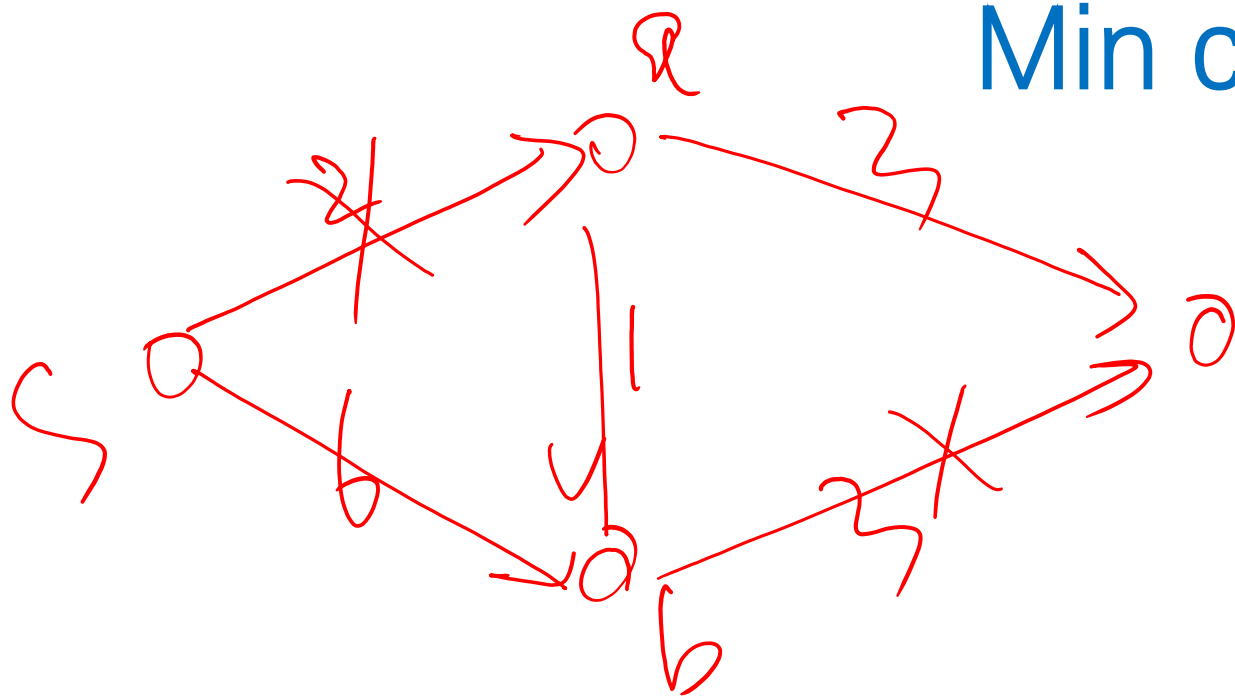
Segmentation = Graph partition



Right partition cost function?

Efficient optimization algorithm?

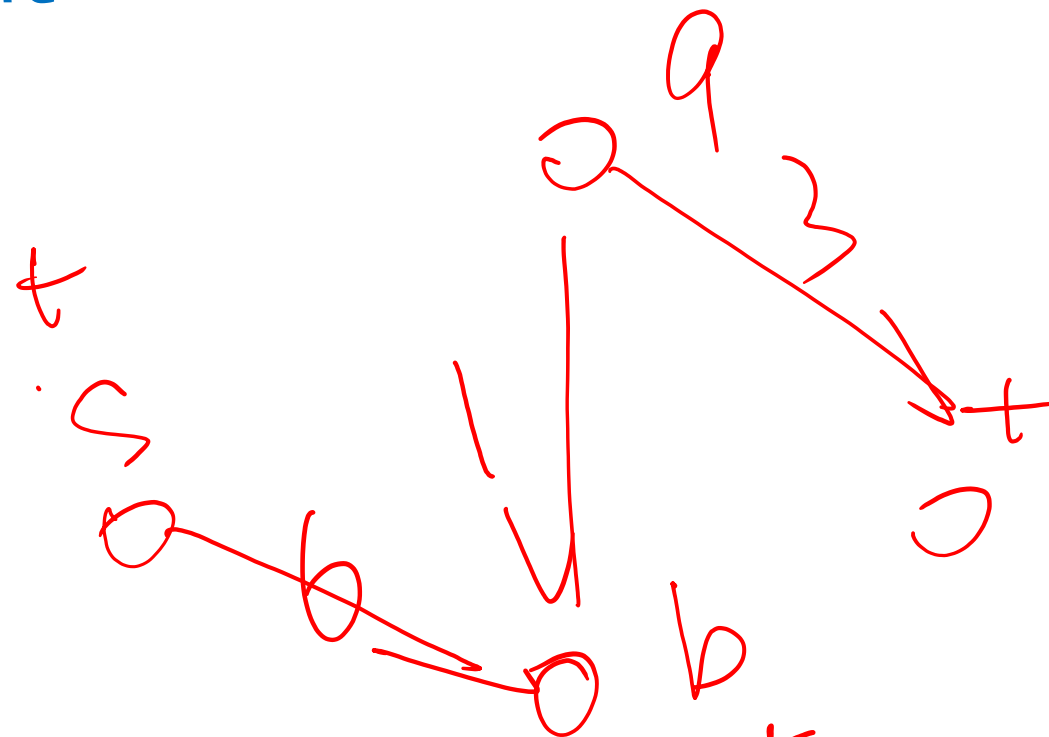
Min cut



$s \rightarrow a \rightarrow t$

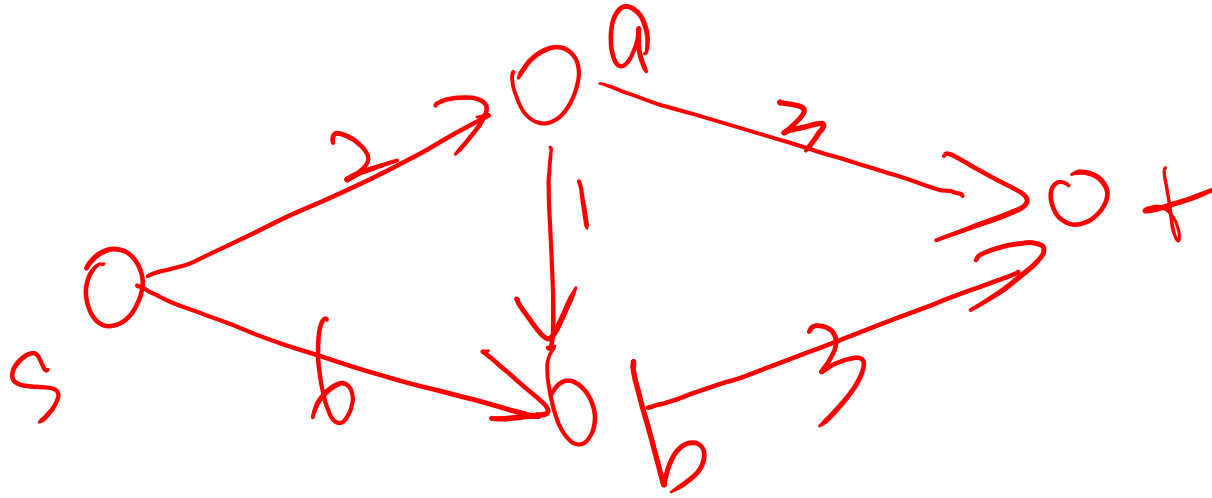
$a \rightarrow b \rightarrow t$

$a \rightarrow a \rightarrow b \rightarrow t$



min Out
 $2+3=5$

Max flow



$s \rightarrow t$
max flow

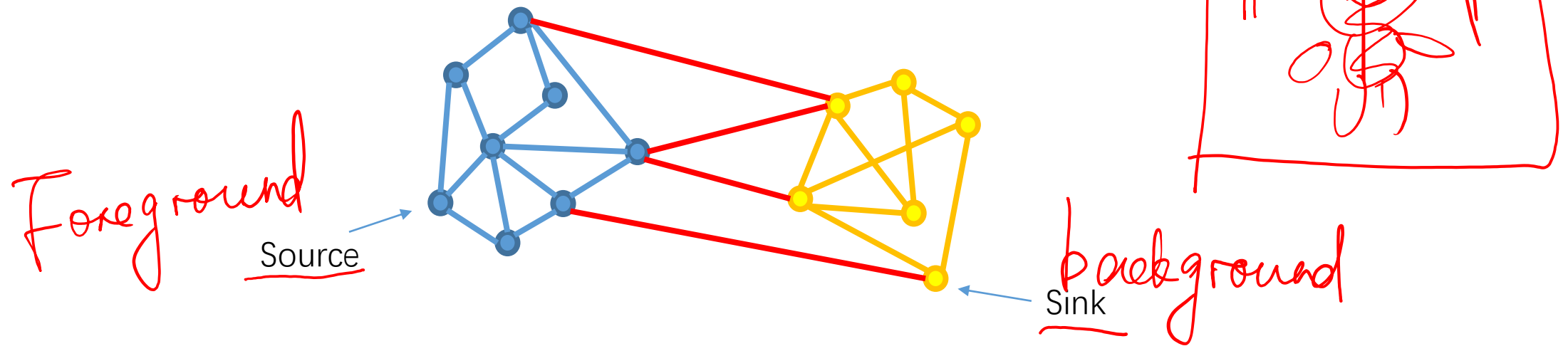
① $s \rightarrow a \rightarrow t : 2$

② $s \rightarrow b \rightarrow t : 3$

$s \rightarrow a \rightarrow b \rightarrow t : 0$

① + ② = 5

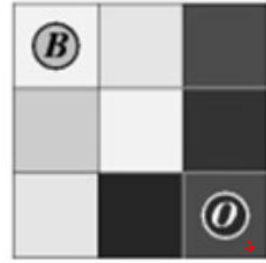
Graph Cut and Flow



- 1) Given a source (s) and a sink node (t)
- 2) Define Capacity on each edge, $C_{ij} = W_{ij}$
- 3) Find the maximum flow from $s \rightarrow t$, satisfying the capacity constraints:

Min. Cut = Max. Flow

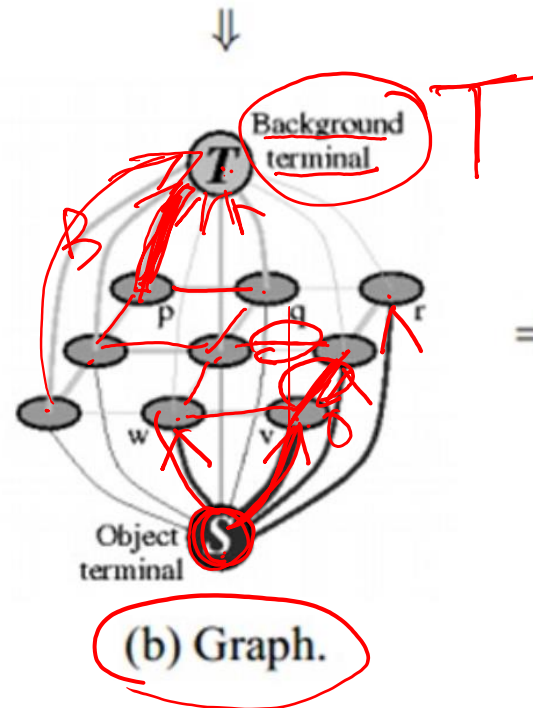
Min Cut



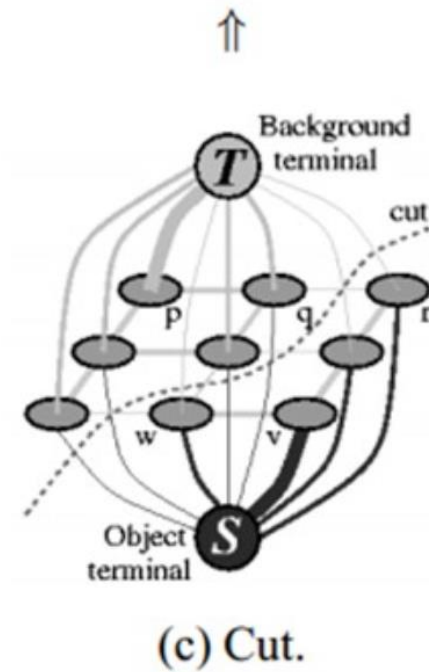
(a) Image with seeds.



(d) Segmentation results.



⇒



Min Cut

- The minimum cut: i.e. C that minimizes

$$\arg \min C = \sum_{(i,j) \in C} w_{ij}$$

min cut \rightarrow max flow



- N-links: between adjacent pixels, we could use

if $I_i \approx I_j \Rightarrow w_{ij} \rightarrow 1$

if I_i far from $I_j \Rightarrow w_{ij} \rightarrow 0$

$$w_{ij} = e^{-\frac{\|I_i - I_j\|^2}{2\delta^2}}$$

G \rightarrow E

- T-links: let user "scribble" on image to denote some initial foreground and background pixels, which forms probability distributions F_B, F_F .

$I_i \in \text{foreground} \Rightarrow w_{iF} \rightarrow 1$

$$w_{iF} = F_F(I_i); w_{iB} = F_B(I_i)$$

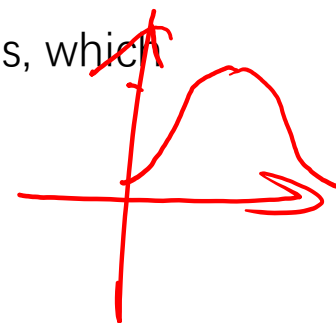
$w_{iB} \rightarrow 0$

$$\arg \min aR(L) + E(L)$$

if $I_i \in BG$

$w_{iF} \rightarrow 0$

$w_{iB} \rightarrow 1$



Resource

- <https://vision.cs.uwaterloo.ca/code/>
- <http://www.cs.cornell.edu/~rdz/graphcuts.html>
- <http://pub.ist.ac.at/~vnk/software.html>