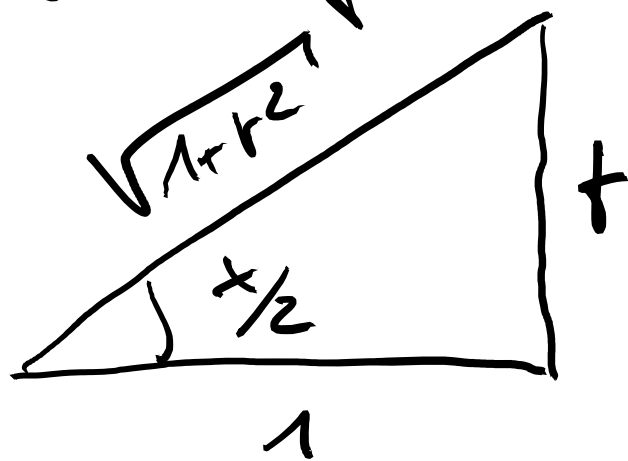


t. formules + sin en cos i. f. v. tg

subst: $\text{tg} \frac{x}{2} = t = \frac{t}{1}$



$$\sin\left(\frac{x}{2}\right) = \frac{t}{\sqrt{1+t^2}}$$

Stel $\frac{x}{2} = \alpha \Rightarrow$

$$\cos\left(\frac{x}{2}\right) = \frac{1}{\sqrt{1+t^2}}$$

$$\sin \alpha = \frac{\text{tg} \alpha}{\sqrt{1 + \text{tg}^2 \alpha}}$$

$$\cos \alpha = \frac{1}{\sqrt{1 + \text{tg}^2 \alpha}}$$

$\sin(2\theta) = 2 \sin(\theta) \cdot \cos(\theta)$

$$\sin(x) = 2 \cdot \frac{t}{\sqrt{1+t^2}} \cdot \frac{1}{\sqrt{1+t^2}} = \frac{2t}{1+t^2}$$

$\sin^2 x + \cos^2 x = 1 \Rightarrow \cos^2 x = 1 - \sin^2 x$

$$\cos^2(x) = 1 - \left(\frac{2t}{1+t^2}\right)^2 = \frac{1+t^4+2t^2-4t^2}{(1+t^2)^2} = \frac{1+t^4-2t^2}{(1+t^2)^2} = \frac{(1-t^2)^2}{(1+t^2)^2}$$

$$\Rightarrow \cos(x) = \frac{1-t^2}{1+t^2}$$

$$\text{tg}(x) = \frac{\sin x}{\cos x} = \frac{2t}{1+t^2} \cdot \frac{1+t^2}{1-t^2} = \frac{2t}{1-t^2}$$

$$\frac{dt}{dx} = \left(\text{tg}\left(\frac{x}{2}\right)\right)' = \frac{1}{2} \cdot \frac{1}{\cos^2\left(\frac{x}{2}\right)} \Rightarrow dx = 2 \cdot \cos^2\left(\frac{x}{2}\right) \cdot dt$$

$$dx = \frac{2}{1+t^2} dt$$