## 1. Naive Definition of Probability.

Fix the 1st dice result, we know that for "21", it show be greater or equal to 3 (3+18=21); for "22", it show he greater or equal to 4 (4+18222).

Shen we tune "2" to "14", we can have more possibilities for the remaining three dices in "21" case.

(b) "=" (d)

Pr. that a random 2 lettersword is a palindrom (A):  $P(A) = \frac{1}{2b \times 1} \times 2b^2 = \frac{1}{2b}$ 

P(A) = 26 × 1)/ 20 - 26
Pr. - . . 3 letters - . . (B):

PCB) = (26+26×25×1)/263

= 1/26

2.
(a). Pr (+(u, b) = (4)(13)-1]

(\$\frac{1}{2}(\frac{4}{2})(\frac{4}{2})(\frac{4}{1})(\fra

By Taylor expansion on e at o,

Therefore, the Pr. is approximatly 1/e.

## I. Story Proofs

5. 
$$\sum_{k=0}^{n} {n \choose k} = 2^n$$
.  
I can't image a good story. However,

6. 
$$\frac{(2n)!}{2^n \cdot n!} = (2n-1)(2n-3) - \cdots + 1.$$
Let is a partnership story. Check the book.

7. 
$$\binom{n}{k} + \binom{n}{k-1} = \binom{n+1}{k}$$
,

for all positive integers n, k, with n > k.

$$= \frac{(n+1)!}{(k-1)!} + \frac{(k-1)!}{(k-1)!}$$

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To count of outcomes such that we select k people from these not people,

- Right side: Setraightforwardly.

- Left side: we divide it into 2 situations:

\*\*Done is any K are from a cottizens;

and plus the only choice of "president".