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1 import numpy as np
2 import matplotlib.pyplot as plt
3 import networkx as nx
4 import pandas as pd
5 from tabulate import tabulate
6
7
8 plt.rcParams["figure.figsize"] = (11, 7)
9
10
11 def friedkin_johnsen(Lam, A, x0, k, node_of_intrst, t_step_propganda_mtrx,
12 plot_result = False) :
13     n = A.shape[0] # assuming everything is dimensioned right
14     I = np.eye(n)
15     xx = np.zeros((n,k))
16     xx[:,0] = x0
17     for i in range(1,k) :
18         xx[:,i] = Lam*A@xx[:,i-1] + (I-Lam)*x0
19         t_step_propganda_mtrx.append(xx[0:-2,i].sum())
20     if plot_result:
21         plt.plot(xx.T, label=["Fake Node", "Node 0", "Node 1", "Node 2", "Node 3",
22                               "Node 4", "Node 5", "Node 6", "Node 7", "Node 8",
23                               "Node 9"])
24         plt.legend(bbox_to_anchor=(0.1, 1.15), loc='upper left', borderaxespad=0,
25 ncol=6)
26         plt.title(f"{node_of_intrst} ---0.5---> 'FAKE' ")
27         plt.get_current_fig_manager().set_window_title(f"Results from Table 1.
28 {node_of_intrst}")
29         plt.show()
30
31     return xx, t_step_propganda_mtrx
32
33
34 def draw_from_matrix(A,draw_labels=False, drw_method='arc3, rad = 0.1') :
35     G = nx.from_numpy_matrix(np.matrix(A), create_using=nx.DiGraph)
36     layout = nx.spring_layout(G,seed=0)
37     nx.draw(G, layout, node_size=750, with_labels=True, font_weight='bold',
38 font_size=15, connectionstyle=f"{drw_method}")
39     if draw_labels :
40         labels = nx.get_edge_attributes(G, "weight")
41         nx.draw_networkx_edge_labels(G, pos=nx.circular_layout(),
42 edge_labels=labels, label_pos=.33);
43
44
45 def addNodeToNetwork(og_network, og_opinions):
46     new_network = []
47     # Add new col to end of each row
48     for row in range(len(og_network)):
49         new_col = og_network[row].copy()
50         new_col.append(0.0)
51         new_network.append(new_col)
52     new_row = [0.0 for col in range(len(new_network)+1)]
53     mod_new_network = new_network.append(new_row)
54     new_opinions = og_opinions.copy()
55     new_opinions.append(1.0)
56     new_network[-1][-1] = 1.0
57     return new_network, new_opinions
58
59
60 def addBadEdgeToNetwork(adjusted_network, node, bad_node):
61     for edge in range(len(adjusted_network[node])):

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54         adjusted_network[node][edge] = adjusted_network[node][edge] * 0.5
55     adjusted_network[node][bad_node] = 0.5
56     return adjusted_network
57
58 def timestepsToPTable(t_step_matrix, p_t_stp_lst):
59     node_lst = [node for node in range(len(t_step_matrix))]
60     time_step_dict = {f"{node}" : [] for node in range(len(t_step_matrix))}
61
62     for t_stp in range(len(t_step_matrix[0])):
63         for node in range(len(t_step_matrix)):
64             time_step_dict.get(f"{node}").append(t_step_matrix[node][t_stp])
65
66     time_step_dict.update({"p(t)": p_t_stp_lst})
67
68     time_table = pd.DataFrame(time_step_dict, index=[f"t={t_stp}" for t_stp in
69 range(len(t_step_matrix[0]))])
70     tabHeaders = [f"node_{node}" for node in range(len(t_step_matrix))]
71     tabHeaders[-1] = f"node_fake"
72     tabHeaders.append("P(t)")
73
74     return tabulate(time_table, headers=tabHeaders, tablefmt="fancy_grid")
75
76 def networkPropagandaModel(og_network, og_opnions, num_iterations,
77 bad_node_neighbor, t_step_propganda_lst, draw_network=False, plot_result=False):
78     # Add node to network
79     mod_network, mod_opnions = addNodeToNetwork(og_network, og_opnions) # Adds
80 self-pointing edge to
81     # Multiplies the nodes row (it's edges) by 0.5 and add 0.5 edge from bad node
82     # to the one of the nodes of the original network.
83     prop_network = addBadEdgeToNetwork(mod_network, bad_node_neighbor,
84 len(mod_network)-1)
85
86     prop_lambda_diag_lst = np.diag(mod_opnions).tolist()
87     t_step_propganda_lst.append(sum(mod_opnions[0:-2]))
88     result , result_propganda_val =
89 friedkin_johnsen(np.array(prop_lambda_diag_lst), np.array(prop_network),
90 np.array(mod_opnions), num_iterations, bad_node_neighbor, t_step_propganda_lst,
91 plot_result)
92     return result, result_propganda_val
93
94 def plotProagandaValOverTime(p_of_t_matrix, node_of_intrest):
95     plt.plot(p_of_t_matrix.T, label=f"Propaganda-Value")
96     plt.legend(bbox_to_anchor=(0.1, 1.15), loc='upper left', borderaxespad=0,
97 ncol=6)
98     plt.title(f"Overall Propaganda Value when:\n{node_of_intrest} ---0.5--->
99 'FAKE' ")
100     plt.get_current_fig_manager().set_window_title(f"Overall Propaganda Value")
101     plt.show()
102
103 def plotAllProagandaValOverTime(all_prop_val):
104     plt.plot(all_prop_val.T, label=["Node 0", "Node 1", "Node 2", "Node 3", "Node
105 4",
106                                     "Node 5", "Node 6", "Node 7", "Node 8", "Node
107 9"])
108     plt.legend(bbox_to_anchor=(0.1, 1.15), loc='upper left', borderaxespad=0,
109 ncol=6)
110     plt.title(f"All possible 'FAKE' neighbor node")
111     plt.get_current_fig_manager().set_window_title(f"All possible 'FAKE' neighbor
112 node")
113     plt.show()

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101
102 proj_03_adj_ntwrk = [[0.0, 0.9, 0.0, 0.1, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0],
103                       [0.0, 0.0, 0.2, 0.1, 0.4, 0.3, 0.0, 0.0, 0.0, 0.0],
104                       [0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0],
105                       [0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0],
106                       [0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.9, 0.0, 0.1, 0.0],
107                       [0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0],
108                       [0.4, 0.0, 0.0, 0.2, 0.0, 0.0, 0.0, 0.4, 0.0, 0.0],
109                       [0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0, 0.0, 0.0, 0.0],
110                       [0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 1.0, 0.0, 0.0],
111                       [0.0, 0.0, 0.8, 0.0, 0.1, 0.0, 0.0, 0.0, 0.1, 0.0]]
112
113 node_opnins = [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95]
114
115 TRAINING_ITERATIONS = 10
116
117
118 p_t_steps=[]
119
120 overall_p_vals = []
121
122 # Iterate through each row of the matrix that represent each possible neighbor,
123 # that the bad node's one edge could be connected to.
124 for possible_neigh in range(len(proj_03_adj_ntwrk)):
125     print(f"Table 1.{possible_neigh}")
126     result, p_t_steps = networkPropagandaModel(proj_03_adj_ntwrk, node_opnins,
127     TRAINING_ITERATIONS, possible_neigh, p_t_steps, plot_result=True)
128     print("-----")
129     print(f" Node {possible_neigh} Directly influenced by 'fake node' test
130     results")
131     print("-----")
132     plotProagandaValOverTime(np.array(p_t_steps), possible_neigh)
133     temp_lst = p_t_steps.copy()
134     print(timestepsToPTable(result, temp_lst))
135     overall_p_vals.append(temp_lst)
136     p_t_steps.clear()
137     print("-----\n\n")
138
139 plotAllProagandaValOverTime(np.array(overall_p_vals))

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