. (50 points) A real estate broker constructed a multiple linear regression model for house prices in his area using as explanatory variables size of a house, age of a house, lotsize and source of energy used to heat a house. He introduced the following variables:

- Price: sale price of a house (in $1000)
- Size: size of a house (in 100 sq ft)
- Age: age of a house (in years)
- Lotsize: size of a lot (in 1000 sq ft)

There are three sources of energy: electricity, heating oil and natural gas. He coded this information as follows

- Gas = 1 if a house is heated by natural gas and Gas = 0 if not
- Oil = 1 if a house is heated by heating oil and Oil = 0 if not

Answer the questions below based on the Minitab output on the next page (some numbers are concealed and denoted by ①,②,. . . ,etc).

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Regression Analysis: Price versus hsize, oil, gas, age, lotsize

Analysis of Variance

Source       DF        SS       MS  F-Value  P-Value
Regression   ①      ④     ⑥    ⑧    0.000
Error        9        ⑤     ⑦
Total        ③     6230.24

Model Summary

S    R-sq
4.71154     ⑨

Coefficients

Term        Coef  SE Coef  T-Value  P-Value
Constant    -5.5     13.7    -0.40    0.696
hsize      4.143    0.517     8.01    0.000
oil       -10.79     3.07    -3.52    0.007
gas         2.67     4.23     0.63    0.544
age        0.143    0.610     0.23    0.820
lotsize    3.137    0.944     3.32    0.009

Regression Equation
Price = -5.5 +4.143 hsize -10.79 oil +2.67 gas

+0.143 age +3.137 lotsize
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(a) What is the degree of freedom for sum of squares due to regression (SSR) in ① ?

(b) What is sum of squared errors SSE in ⑤ (round to the 2nd decimal place)?

(c) What is sum of squares due to regression (SSR) in ④ (round to the 2nd decimal place)?

(d) What is the F-value in ⑧ (round to the 2nd decimal place)?

(e) Calculate r^2 in ⑨ and interpret it.

(f) Is this **overall** multiple linear regression model **statistically significant** at $\alpha = 0.05$ (state the hypothesis, rejection rule and your conclusion)

(g) Identify and Interpret the estimated parameter of Gas and the estimated parameter of Oil.

(h) For houses of the same characteristics, which energy source gives, on average, the highest estimated sale price? Which gives the lowest price?

(i) Can you conclude at 1% level of significance that, all else equal, houses heated by oil sell for *less than* those heated by electricity (state hypothesis, rejection region and conclusion)?

(j) Construct a 95% confidence interval for the difference in average prices of the houses heated by gas and those heated by electricity holding all other predictors constant.

α	z_α
0.01	2.33
0.05	1.645
0.025	1.960
0.005	2.575

Table entry for p and C is the critical value t^* with probability p lying to its right and probability C lying between $-t^*$ and t^*.

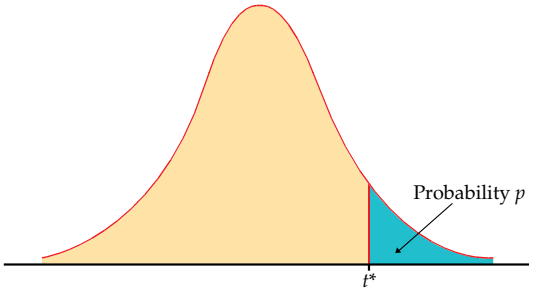

TABLE D

t distribution critical values

	Upper-tail probability p											
df	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	0.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	0.765	0.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92
4	0.741	0.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	0.727	0.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	0.718	0.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	0.711	0.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408
8	0.706	0.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5.041
9	0.703	0.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	0.700	0.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587
11	0.697	0.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437
12	0.695	0.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	0.694	0.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4.221
14	0.692	0.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	0.691	0.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	0.690	0.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015
17	0.689	0.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	0.688	0.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	0.688	0.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	0.687	0.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	0.686	0.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22	0.686	0.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
23	0.685	0.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	0.685	0.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
25	0.684	0.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725
26	0.684	0.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707
27	0.684	0.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	0.683	0.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	0.683	0.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
30	0.683	0.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.646
40	0.681	0.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	0.679	0.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
60	0.679	0.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460
80	0.678	0.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	0.677	0.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
1000	0.675	0.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
z^*	0.674	0.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%
	Confidence level C											