Principal Component Analysis

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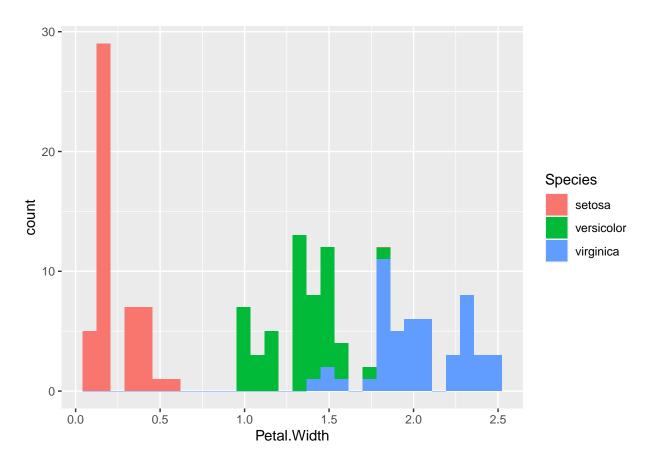
#EDA: Iris Dataset

```
summary(iris)
```

```
##
     Sepal.Length
                      Sepal.Width
                                      Petal.Length
                                                       Petal.Width
           :4.300
##
                            :2.000
                                             :1.000
    Min.
                    Min.
                                     Min.
                                                      Min.
                                                             :0.100
    1st Qu.:5.100
                    1st Qu.:2.800
                                     1st Qu.:1.600
                                                      1st Qu.:0.300
    Median :5.800
                    Median :3.000
                                     Median :4.350
##
                                                      Median :1.300
##
    Mean
           :5.843
                    Mean
                            :3.057
                                     Mean
                                             :3.758
                                                      Mean
                                                             :1.199
##
    3rd Qu.:6.400
                    3rd Qu.:3.300
                                     3rd Qu.:5.100
                                                      3rd Qu.:1.800
           :7.900
                            :4.400
##
    Max.
                    Max.
                                     Max.
                                             :6.900
                                                      Max.
                                                             :2.500
          Species
##
##
              :50
    setosa
##
    versicolor:50
##
    virginica:50
##
##
##
```

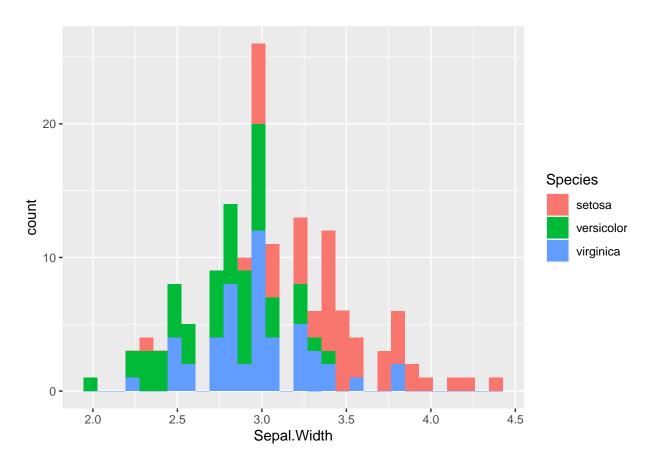
```
iris%>%
   ggplot(aes(x=Petal.Width, fill=Species))+
   geom_histogram()
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



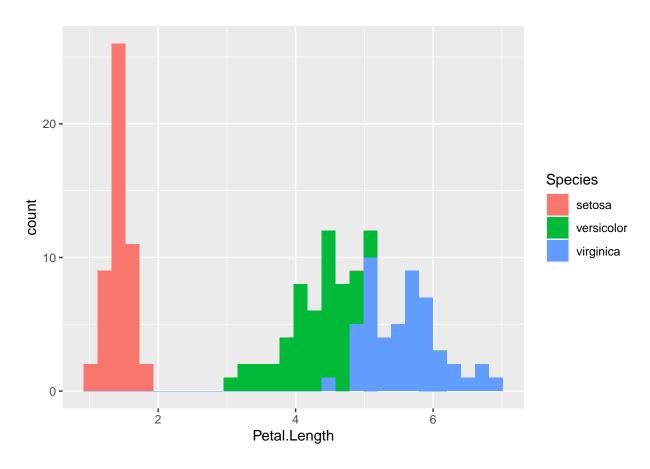
```
iris%>%
   ggplot(aes(x=Sepal.Width, fill=Species))+
   geom_histogram()
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



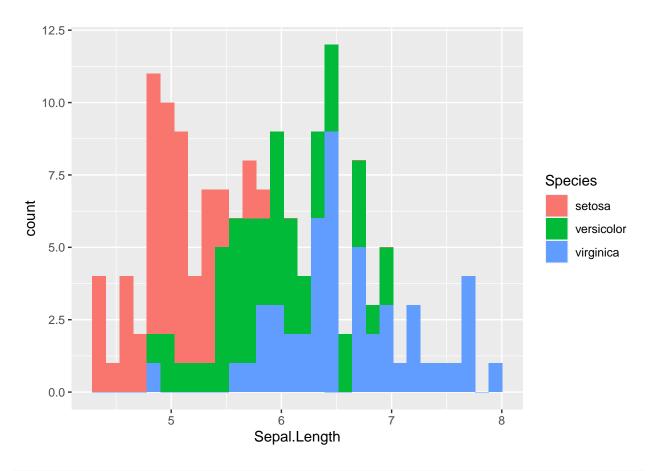
```
iris%>%
   ggplot(aes(x=Petal.Length, fill=Species))+
   geom_histogram()
```

'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



```
iris%>%
   ggplot(aes(x=Sepal.Length, fill=Species))+
   geom_histogram()
```

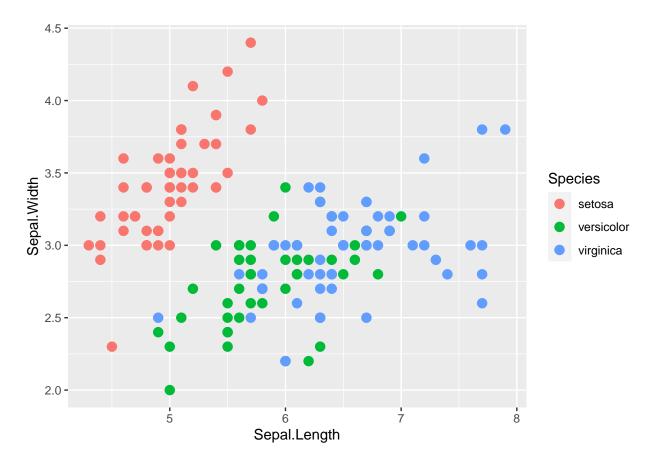
'stat_bin()' using 'bins = 30'. Pick better value with 'binwidth'.



```
iris%>%
   ggplot(aes(x = Petal.Length, y = Petal.Width, colour = Species))+
   geom_point(size = 3)
```



```
iris%>%
   ggplot(aes(x = Sepal.Length, y = Sepal.Width, colour = Species))+
   geom_point(size = 3)
```



#Splitting Data

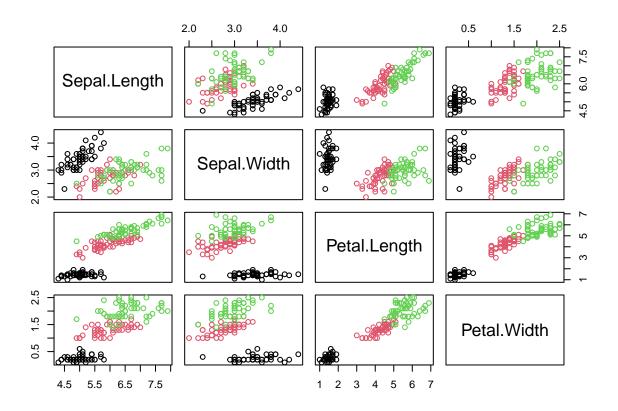
```
dt = sort(sample(nrow(iris), nrow(iris)*.7))
train<-iris[dt,]
test<-iris[-dt,]
summary(train)</pre>
```

```
##
     Sepal.Length
                      Sepal.Width
                                      Petal.Length
                                                       Petal.Width
##
    Min.
           :4.300
                    Min.
                            :2.000
                                     Min.
                                            :1.000
                                                      Min.
                                                             :0.100
    1st Qu.:5.200
                    1st Qu.:2.800
                                     1st Qu.:1.600
                                                      1st Qu.:0.300
    Median :5.800
                    Median :3.000
                                     Median :4.400
##
                                                      Median :1.400
    Mean
           :5.881
                    Mean
                           :3.053
                                     Mean
                                            :3.825
                                                             :1.223
##
                                                      Mean
##
    3rd Qu.:6.500
                    3rd Qu.:3.300
                                     3rd Qu.:5.100
                                                      3rd Qu.:1.800
                                             :6.700
##
    Max.
           :7.900
                    Max.
                            :4.400
                                     Max.
                                                      Max.
                                                             :2.500
##
          Species
##
    setosa
              :32
##
    versicolor:38
##
    virginica:35
##
##
##
```

summary(test)

Sepal.Length Sepal.Width Petal.Length Petal.Width

```
## Min. :4.500 Min. :2.200
                                  Min. :1.200
                                                 Min. :0.100
## 1st Qu.:5.000 1st Qu.:2.800 1st Qu.:1.500 1st Qu.:0.300
## Median: 5.600 Median: 3.100 Median: 4.000 Median: 1.300
## Mean :5.756 Mean :3.067
                                  Mean :3.602
                                                 Mean :1.144
##
   3rd Qu.:6.300
                 3rd Qu.:3.400
                                  3rd Qu.:5.100
                                                 3rd Qu.:1.800
## Max. :7.700
                 Max. :4.100 Max. :6.900
                                                 Max. :2.500
##
         Species
## setosa
             :18
## versicolor:12
## virginica:15
##
##
##
#PCA
pc <- prcomp(train[,-5],center = T,scale. = T)</pre>
## Standard deviations (1, .., p=4):
## [1] 1.7067707 0.9537263 0.3943775 0.1476700
##
## Rotation (n x k) = (4 \times 4):
                      PC1
                                 PC2
                                            PC3
                                                      PC4
## Sepal.Length 0.5112271 -0.41809359 0.7097605 -0.2451216
## Sepal.Width -0.2878382 -0.90574388 -0.2779918 0.1396343
## Petal.Length 0.5806955 -0.01493703 -0.1508142 0.7998904
## Petal.Width 0.5644366 -0.06784295 -0.6294566 -0.5297103
summary(pc)
## Importance of components:
                           PC1
                                  PC2
                                          PC3
                        1.7068 0.9537 0.39438 0.14767
## Standard deviation
## Proportion of Variance 0.7283 0.2274 0.03888 0.00545
## Cumulative Proportion 0.7283 0.9557 0.99455 1.00000
pairs(iris[,1:4],col=iris[,5])
```



```
pred <- predict(pc,train)</pre>
train_1 <- data.frame(pred,train[5])</pre>
pred1 <- predict(pc,test)</pre>
test_1 <- data.frame(pred1,test[5])</pre>
library(nnet)
set.seed(100)
mymodel <- multinom(Species~PC1 +PC2,data = train_1)</pre>
## # weights: 12 (6 variable)
## initial value 115.354290
## iter 10 value 21.028921
## iter 20 value 19.989171
## iter 30 value 19.899086
## final value 19.898081
## converged
summary(mymodel)
## Call:
## multinom(formula = Species ~ PC1 + PC2, data = train_1)
```

PC2

Coefficients:

(Intercept)

PC1

##

```
## versicolor
                 7.805943 10.04322 4.282975
## virginica
                 2.049043 15.37869 4.916588
##
## Std. Errors:
              (Intercept)
                                PC1
                                         PC2
                 62.23453 52.19538 77.39694
## versicolor
                 62.25177 52.21185 77.39917
## virginica
## Residual Deviance: 39.79616
## AIC: 51.79616
\# Confusion \ matrix
library(caret) #install caret package
## Warning: package 'caret' was built under R version 4.1.2
## Loading required package: lattice
prd <- predict(mymodel,train_1)</pre>
confusionMatrix(prd,train_1$Species)
## Confusion Matrix and Statistics
##
##
               Reference
## Prediction
                setosa versicolor virginica
##
                    32
                                           0
     setosa
                                0
##
     versicolor
                     0
                                32
                                           4
##
     virginica
                     0
                                 6
                                          31
##
## Overall Statistics
##
##
                  Accuracy : 0.9048
##
                    95% CI: (0.8318, 0.9534)
##
       No Information Rate: 0.3619
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.8569
##
##
  Mcnemar's Test P-Value : NA
##
## Statistics by Class:
##
##
                        Class: setosa Class: versicolor Class: virginica
## Sensitivity
                                1.0000
                                                  0.8421
                                                                    0.8857
                                1.0000
                                                  0.9403
                                                                    0.9143
## Specificity
## Pos Pred Value
                               1.0000
                                                  0.8889
                                                                    0.8378
## Neg Pred Value
                                                                    0.9412
                                1.0000
                                                  0.9130
## Prevalence
                                0.3048
                                                  0.3619
                                                                    0.3333
## Detection Rate
                                0.3048
                                                  0.3048
                                                                    0.2952
## Detection Prevalence
                                0.3048
                                                  0.3429
                                                                    0.3524
                                                                    0.9000
## Balanced Accuracy
                                1.0000
                                                  0.8912
```

```
prt <- predict(mymodel,test_1)
confusionMatrix(prt,test_1$Species)</pre>
```

```
## Confusion Matrix and Statistics
##
##
               Reference
## Prediction
                setosa versicolor virginica
##
     setosa
                    18
                                0
##
     versicolor
                     0
                               11
                                          1
                     0
                                         14
##
     virginica
                                1
##
## Overall Statistics
##
##
                  Accuracy : 0.9556
##
                    95% CI: (0.8485, 0.9946)
##
       No Information Rate: 0.4
       P-Value [Acc > NIR] : 2.842e-15
##
##
##
                     Kappa : 0.9324
##
##
   Mcnemar's Test P-Value : NA
## Statistics by Class:
##
##
                        Class: setosa Class: versicolor Class: virginica
## Sensitivity
                                  1.0
                                                  0.9167
                                                                   0.9333
## Specificity
                                                  0.9697
                                                                   0.9667
                                  1.0
## Pos Pred Value
                                  1.0
                                                  0.9167
                                                                   0.9333
## Neg Pred Value
                                  1.0
                                                  0.9697
                                                                   0.9667
## Prevalence
                                  0.4
                                                  0.2667
                                                                   0.3333
## Detection Rate
                                  0.4
                                                  0.2444
                                                                   0.3111
## Detection Prevalence
                                                                   0.3333
                                  0.4
                                                  0.2667
## Balanced Accuracy
                                  1.0
                                                  0.9432
                                                                   0.9500
```