# Welcome to Deep Learning in Computer Vision 2021

We are extremely happy to see you!



# Before and after teaching:



If you feel ill, go home



Keep your distance to others, also during breaks



Disinfect table and chair



Respect the marking/do not move furniture



Do not share your equipment with others



If in doubt, please ask

## Outline

- Introduction to the course
- What is computer vision
- Deep learning
  - Neural Networks
  - Backpropagation
  - Loss functions

## Program for today

- 09.00-10.00 This lecture
- 10.00-12.00 Exercise
- 13.00-14.00 Lecture on convolutional neural networks
- 14.00-17.00 Exercise

#### Who are we?



Aasa Feragen
Professor at DTU Compute
Section for Visual Computing
<a href="mailto:afhar@dtu.dk">afhar@dtu.dk</a>



Morten Hannemose
Postdoc at DTU Compute
Section for Visual Computing
mohan@dtu.dk

## Teaching Assistants (TA)



**Kilian Maurus Zepf PhD student at DTU Compute** 



**Christian Keilstrup Ingwersen PhD student at DTU Compute** 



Frederik Warburg
PhD student at DTU Compute

#### General course structure

- 3 parts:
  - Image classification and detection
  - Image segmentation
  - 。 GANs
- Each part culminates in a group project, based on which you make a poster
- These posters will be presented (as a group) in the "poster session" part of the exam
- You will give each other peer feedback on the posters
  - The feedback is also part of the project
  - Experience is that you learn even more from the feedback that you give (and seeing other groups' projects) than the feedback that you get

## Project work

- You will be working in groups of 3 (in emergency cases 2).
  - Groups are mandatory (you cannot hand in individually)
  - Groups are a help both for helping each other learn, and for carrying out computations
- If you don't have a group, we will help you find one at the end of the lecture.
- The practical projects are the core of the course, which is designed for you to learn through the projects
- We expect you to at the end of the course understand the key components of the models you use and be able to explain those components at the exam

#### Curriculum

This is not a reading course :-) Your curriculum consists of:

- Lectures
- Exercises and projects, including handed out Jupyter notebooks and examples
- Papers referenced in these

#### Exam

The exam, taking place June 24, consists of 2 parts:

- A presentation (in groups) of one of the three projects, drawn at random
- A physical multiple choice exam (individual)

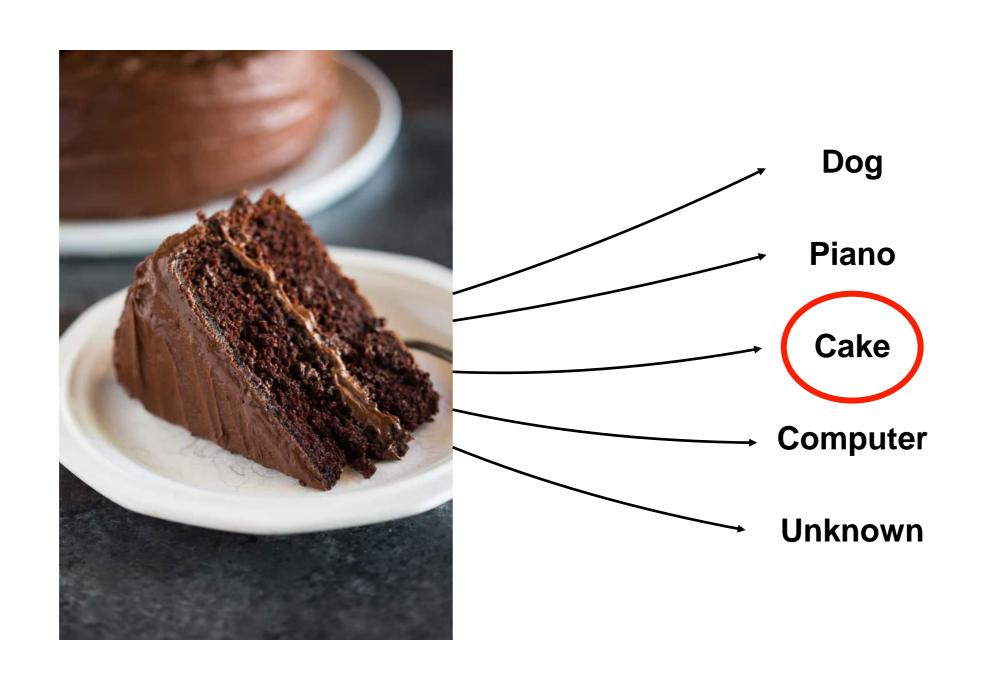
## Questions?

# Deep Learning in Computer Vision

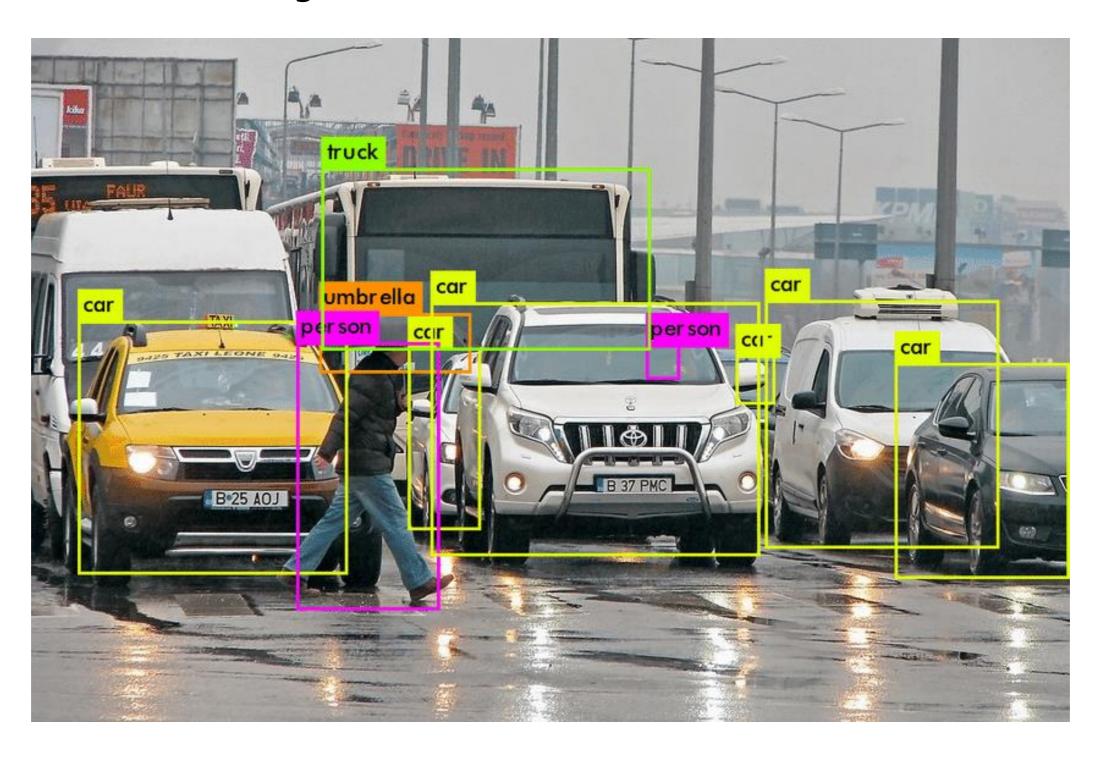
## What is Computer Vision

- The goal in computer vision is to extract useful information from images
- This includes, but is not limited to:
  - Reconstructing properties such as shape, illumination and color distributions
  - Detecting objects e.g. faces in images
  - Estimating motion in image sequences
  - Detecting and matching points of special interest between images e.g. for creating panorama images
  - •

# Image classification



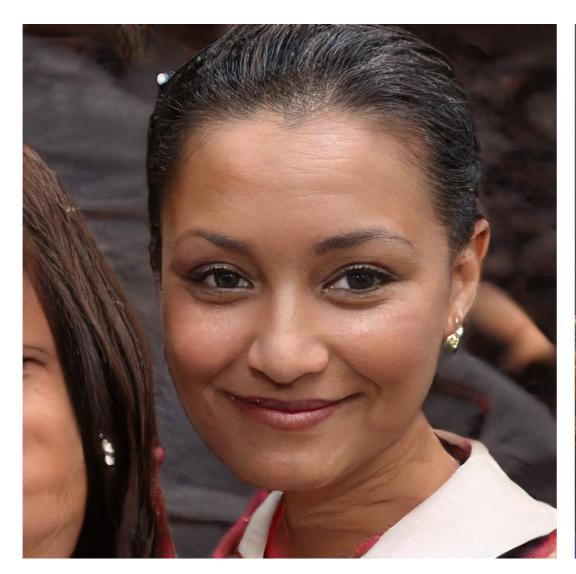
## Object Detection



## Segmentation



## Generative Models





# Deep Learning in Computer Vision

## Learning

- Supervised learning
  - Learn mapping from input to output given training examples with known output
- Unsupervised learning
  - Learn "something" about the distribution of input examples without having known output
- Reinforcement learning
  - Learn actions based on rewards

## Deep Learning

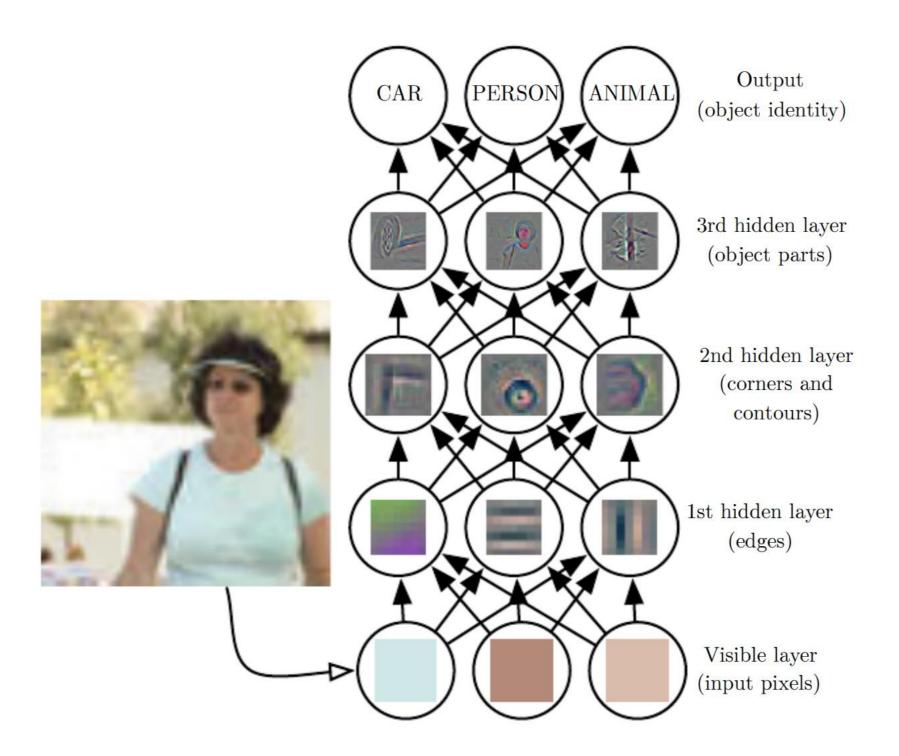
- Deep learning uses deep neural networks
  - Neural networks can approximate any function, if they have enough parameters

#### Neural Networks

- In deep learning we seek to map a set of input values to output values
- Going directly from input to output is in most cases not possible
- Instead, we learn representations of the inputs from which it is easier to predict the output
- In deep learning we learn increasingly complex representations/features that are expressed in terms of simpler representations/features

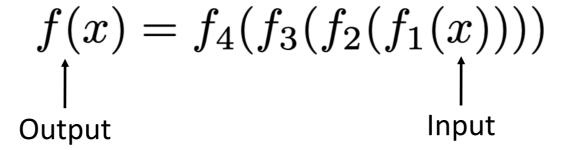


### Neural Networks



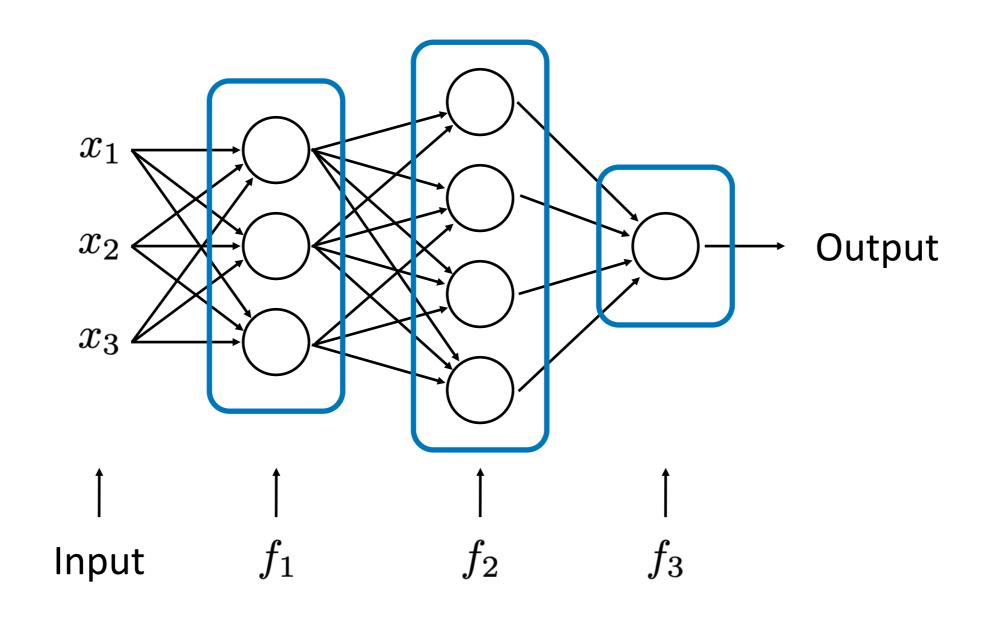
#### Neural networks

• The previous example can be written as:



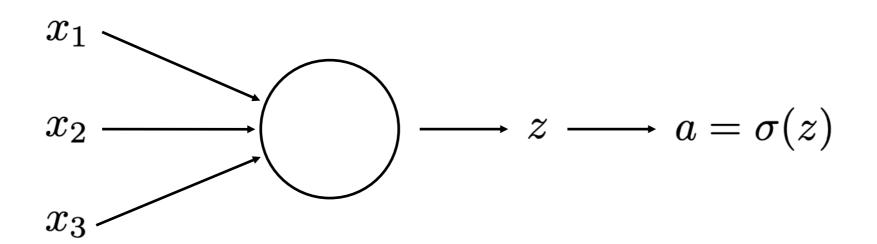
• How do we represent the functions  $f_1, f_2, f_3, f_4$ ?

#### Feed-Forward Neural networks



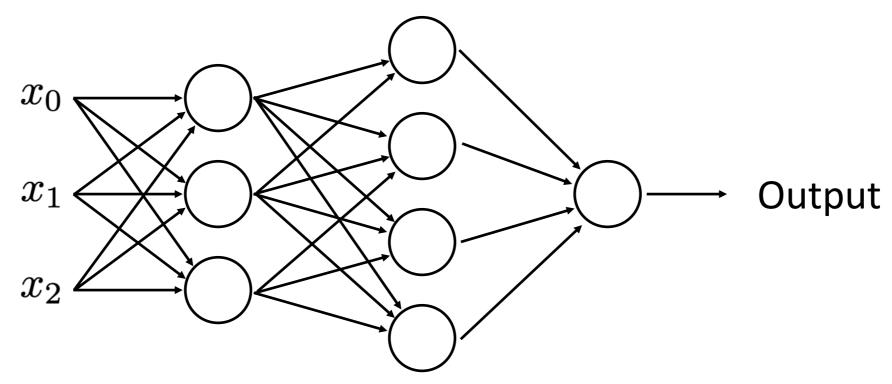
## Neurons - the building block

Originally inspired by neurons in the brain



$$z=w_1x_1+w_2x_2+w_3x_3+b=\mathbf{wx}+b$$
  $a=\sigma(z)$  is the output of the neuron  $\sigma(\cdot)$  is a non-linear activation function

## Feed-forward computation



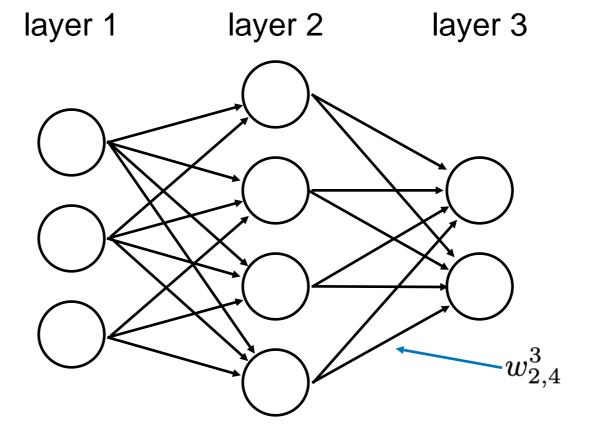
$$\mathbf{a}^{0} = \mathbf{x} = \begin{bmatrix} x_{0} \\ x_{1} \\ x_{2} \end{bmatrix} \qquad \mathbf{a}^{1} = \sigma(\mathbf{W}^{1}\mathbf{a}^{0} + \mathbf{b}^{1})$$

$$= \sigma \begin{pmatrix} \begin{bmatrix} w_{0,0}^{1} & w_{0,1}^{1} & w_{0,2}^{1} \\ w_{1,0}^{1} & w_{1,1}^{1} & w_{1,2}^{1} \\ w_{2,0}^{1} & w_{2,1}^{1} & w_{2,2}^{1} \end{bmatrix} \begin{bmatrix} a_{0}^{0} \\ a_{2}^{0} \\ a_{2}^{0} \end{bmatrix} + \begin{bmatrix} b_{0}^{1} \\ b_{1}^{1} \\ b_{2}^{1} \end{bmatrix} \right)$$

$$\mathbf{a}^{2} = \sigma(\mathbf{W}^{2}\mathbf{a}^{1} + \mathbf{b}^{2})$$

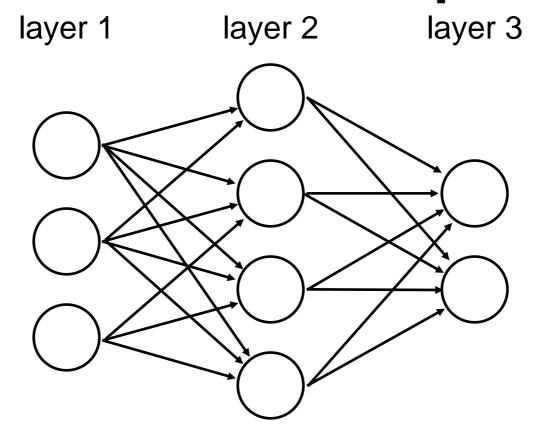
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## Feed-forward computation



$$\mathbf{a}^\ell = \sigma(\mathbf{W}^\ell \mathbf{a}^{\ell-1} + \mathbf{b}^\ell)$$
 is the weight from the  $k^{ ext{th}}$  neuron in the  $l^{ ext{th}}$  neuron in the  $l^{ ext{th}}$  layer  $\mathbf{a}^\ell = \sigma\left(\sum_k w_{j,k}^\ell a_k^{\ell-1} + b_j^\ell\right)$  is the bias of the  $l^{ ext{th}}$  neuron in the  $l^{ ext{th}}$  layer  $a_j^\ell$  is the activation of the  $l^{ ext{th}}$  neuron in the  $l^{ ext{th}}$  layer

## Feed-forward computation



- We need a non-linear activation function after each layer
  - Otherwise, the entire network is a linear model (i.e., only one layer)

## How do we obtain the parameters?

- Right now, the model is just a lot of math, but how do we choose the weights and biases in the model, so it works well on our data?
- We need a function (loss) that measures how well our network is doing for a given set of parameters W and b
- How can we use this to learn the parameters?

### How do we obtain the parameters?

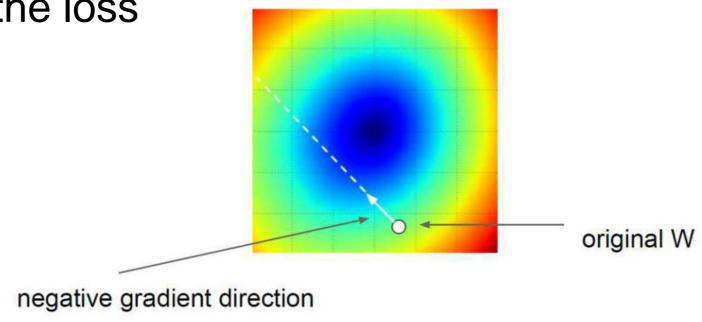
- Random search?
  - Try many different random weights and biases and choose the best one
- Random local search?
  - Generate random weights and biases close to our current and choose the best one
- Gradient Descent
  - Use the gradient of our loss function, which gives the direction of maximum descent at any point x

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#### Gradient descent

- Gradient descent
  - The gradient of a parameter, describes how the loss will change if we change this parameter
- Gradient descent
  - We change the value of the parameter slightly in the direction that should decrease the loss



#### Gradient descent

- If  $\mathcal{L}$  is the loss function, we wish to minimize with respect to parameters p
  - The gradient  $\nabla_p \mathcal{L}$  gives us the direction of maximum ascent of the loss function
  - $-\nabla_p \mathcal{L}$  is the direction of maximum descent
- Gradient descent algorithm:
  - Compute the gradient
  - Take a step in the negative gradient direction

$$p \to p' = p - \alpha \nabla_p \mathcal{L}$$

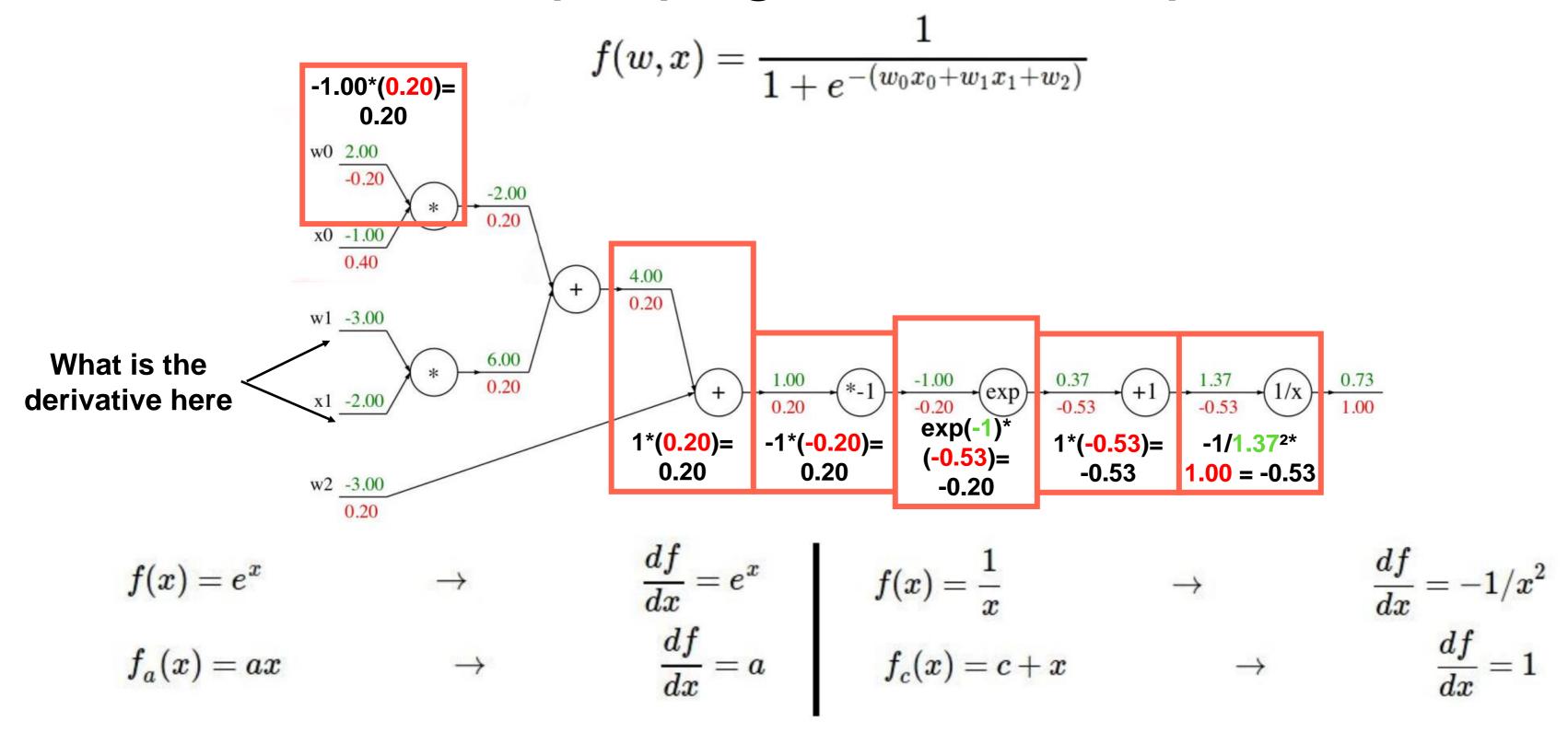
- Here  $\alpha$  is called the learning rate and determines the step size
- Repeat until convergence

## Backpropagation

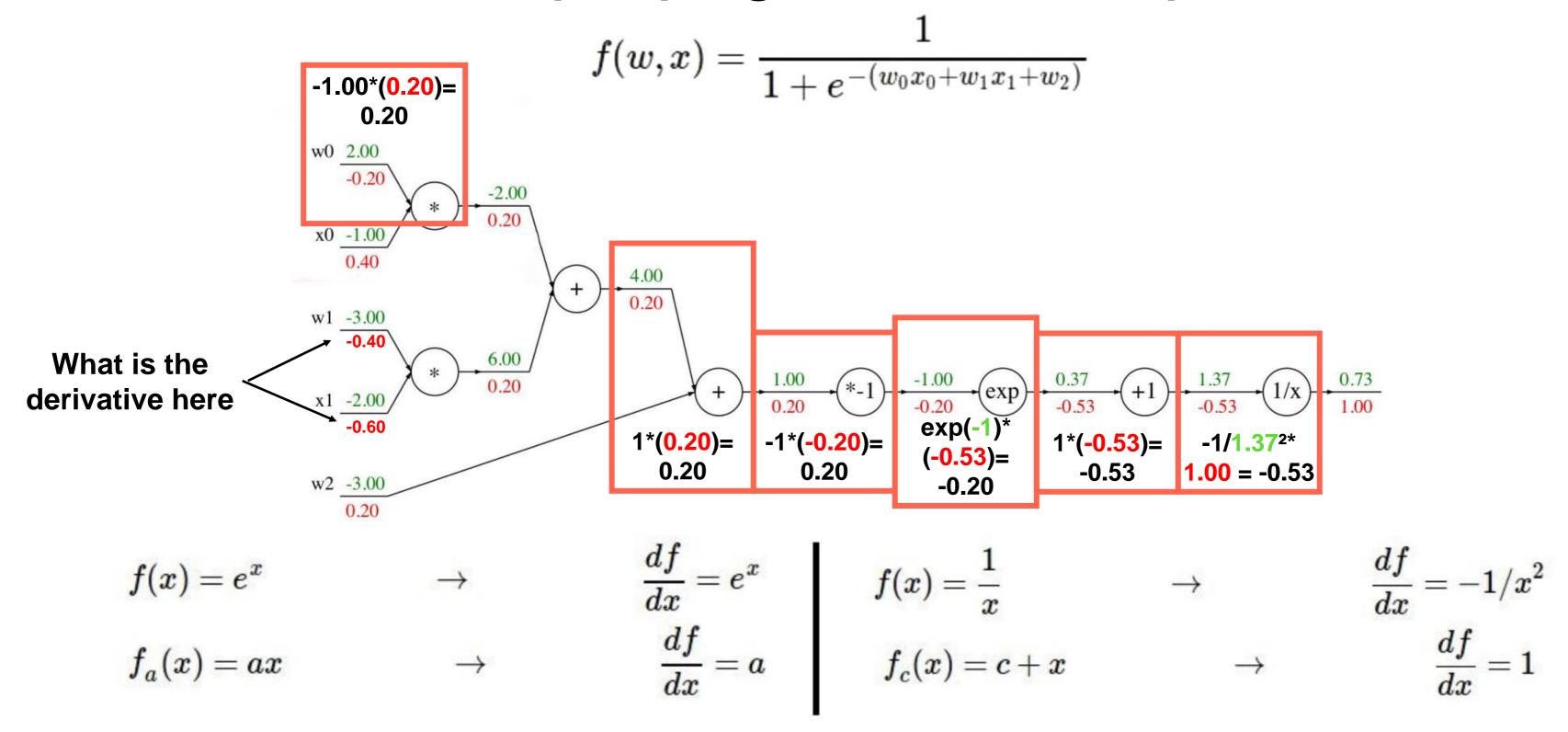
- Which parameters do we want to find the partial derivates of \( \mathcal{L} \) with respect to?
  - The weights **W** and biases **b**
- How?
  - We propagate the error back through the network

## Short break

#### Backpropagration example



### Backpropagration example



# The equations of backpropagation

- Our goal is to find the partial derivatives of the loss function  $\mathcal{L}$  with respect to any weight  $w_{j,k}^{\ell}$  or bias  $b_j^{\ell}$
- The forward pass is defined by  $z_k^{\ell+1} = \sum_j w_{k,j}^{\ell+1} \sigma(z_j^\ell) + b_k^{\ell+1}$
- By the chain rule we have that

$$\begin{split} \frac{\partial \mathcal{L}}{\partial w_{j,k}^{\ell}} &= \frac{\partial \mathcal{L}}{\partial z_{j}^{\ell}} \frac{\partial z_{j}^{\ell}}{\partial w_{j,k}^{\ell}} = a_{k}^{l-1} \frac{\partial \mathcal{L}}{\partial z_{j}^{\ell}} \\ \frac{\partial \mathcal{L}}{\partial b_{j}^{\ell}} &= \frac{\partial \mathcal{L}}{\partial z_{j}^{\ell}} \frac{\partial z_{j}^{\ell}}{\partial b_{j}^{\ell}} = \frac{\partial \mathcal{L}}{\partial z_{j}^{\ell}} \\ \end{split}$$

We thus need a way to calculate

$$rac{\partial \mathcal{L}}{\partial z_j^\ell}$$

## The equations of back propagation

• For the last layer in our network this is easily done (*L* is the last layer)

$$\frac{\partial \mathcal{L}}{\partial z_{j}^{L}} = \frac{\partial \mathcal{L}}{\partial a_{j}^{L}} \frac{\partial a_{j}^{L}}{\partial z_{j}^{L}} = \frac{\partial \mathcal{L}}{\partial a_{j}^{L}} \sigma'(z_{j}^{L})$$

 The first term after the last equals sign depends on both the choice of loss function and choice of activation function

# The equations of back propagation

$$ullet$$
 Recall:  $z_k^{\ell+1} = \sum_j w_{k,j}^{\ell+1} \sigma(z_j^\ell) + b_k^{\ell+1}$ 

 For the rest of the layers in the network we have (⊙ is elementwise product)

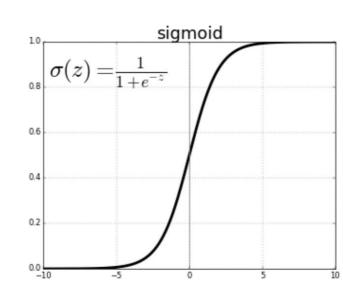
$$\begin{split} \frac{\partial \mathcal{L}}{\partial z_{j}^{\ell}} &= \sum_{k} \frac{\partial \mathcal{L}}{\partial z_{k}^{\ell+1}} \frac{\partial z_{k}^{\ell+1}}{\partial z_{j}^{\ell}} \\ &= \sum_{k} w_{k,j}^{\ell+1} \sigma'(z_{j}^{\ell}) \frac{\partial \mathcal{L}}{\partial z_{k}^{\ell+1}} \\ \frac{\partial \mathcal{L}}{\partial z^{\ell}} &= ((\mathbf{W}^{\ell+1})^{T} \frac{\partial \mathcal{L}}{\partial z^{\ell+1}}) \odot \sigma'(z^{\ell}) \end{split}$$

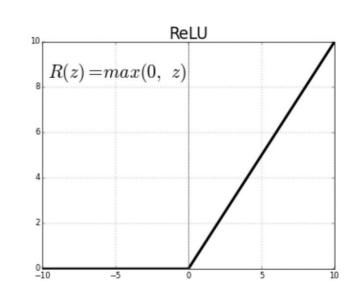
### Activation functions

- The two most commonly used activation functions are:
- Sigmoid  $\sigma(x) = \frac{1}{1 + e^{-x}}$  Closer to how the brain works Vanishing gradient problem
- Rectified Linear Unit:  $\sigma(x) = \operatorname{ReLU}(x) = \max(0, x)$ Works well in most cases

  Not differentiable at zero

  Not a problem in practice





#### Derivatives of activation functions

Sigmoid

$$\sigma(x) = \frac{1}{1 + e^{-x}} \qquad \sigma'(x) = \sigma(x)(1 - \sigma(x))$$

Rectified Linear Unit:

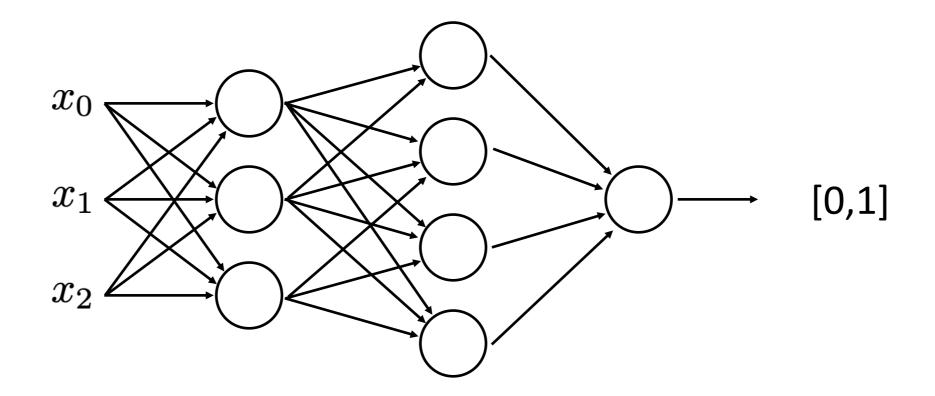
$$\sigma(x) = \text{ReLU}(x) = \max(0, x) \qquad \sigma'(x) = \begin{cases} 1 & x > 0 \\ 0 & x \le 0 \end{cases}$$

### Loss functions

- The choice of loss functions depends on the task
  - For regression: L2 (squared) or L1 (absolute)
  - For two-class classification: Binary cross-entropy
  - For multi-class classification: Cross-entropy

•

### Two-class classification



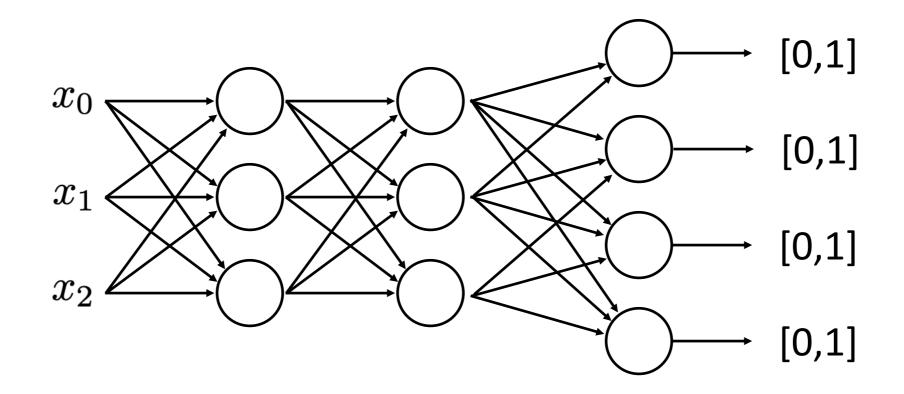
• The output from the neuron in the last layer is mapped to the range [0,1] by using a sigmoid activation function on last neuron

# Binary cross-entropy

• If  $\hat{y} \in [0,1]$  is the output from a neural network and  $y \in \{0,1\}$  is the true value for an input x the binary crossentropy is given by

$$\mathcal{L}(\hat{y}, y) = -y \log \hat{y} - (1 - y) \log(1 - \hat{y})$$
$$\frac{\partial \mathcal{L}}{\partial a^{L}} = \frac{\partial \mathcal{L}}{\partial \hat{y}} = -\frac{y}{\hat{y}} + \frac{1 - y}{1 - \hat{y}}$$

#### Multi-class classification



• The output from the neurons in the last layer is mapped to the range [0,1] such that they sum to 1 by using a softmax activation function in the last layer

#### Softmax activation function

• The softmax activation function maps the outputs from all neurons in layer to the range [0,1] such that they sum to 1

$$\operatorname{softmax}(x_i) = \frac{e^{x_i}}{\sum_{j} e^{x_j}}$$

$$\sum_{i} x_i = 1$$

 Softmax is shift invariant (if you add a constant to all x, the probabilites are the same)

# Cross-entropy

The cross-entropy is given by

$$\mathcal{L}(\hat{y}, y) = -\sum_{i} y_i \log \hat{y}_i = -\log \hat{y}_I, \quad I = \arg_i(y_i = 1)$$

- i.e., the negative log likelihood
- Remember that to start the backpropagation we need to compute

$$\frac{\partial \mathcal{L}}{\partial z_j^L} = \frac{\partial \mathcal{L}}{\partial a_j^L} \frac{\partial a_j^L}{\partial z_j^L} = \frac{\partial \mathcal{L}}{\partial a_j^L} \sigma'(z_j^L)$$

 For softmax+cross-entropy we can calculate this term directly instead of computing the two terms after the last equal sign

# Updating the parameters

 The parameters can now be updated by taking a small step in the negative gradient direction

$$w_{j,k}^{\ell} \to w_{j,k}^{\overline{\ell}} = w_{j,k}^{\ell} - \alpha \frac{\partial L}{\partial w_{j,k}^{\ell}}$$

$$b_j^{\ell} \to \bar{b_j^{\ell}} = b_j^{\ell} - \alpha \frac{\partial L}{\partial b_j^{\ell}}$$

## Stochastic gradient descent

- So far, we only discussed how to train a network based on a single example
  - This is called *stochastic gradient descent*
- We can train over multiple training examples by simply averaging the loss and gradients over the examples
- If we use all our training examples, we call it batch gradient descent
- If we use random subsets of our examples, it is called mini-batch gradient descent
  - Note: this is often called stochastic gradient descent (which is wrong, but widespread)
- In practice we always use mini-batch gradient descent
  - The size of the minibatches is a hyperparameter
  - Typically chosen as large as RAM allows

#### You have learned

- What neural networks are
- How to find the parameters for a neural network from data
  - Loss functions
  - Backpropagation

## Now it's time for your exercise

- The exercise is in an iPython notebook
- We suggest that you use Google Colab to do the exercises and projects
  - You can run into usage limitations, but with three members in each group, it should be fine
  - If you decide to use your own hardware, please ask the TAs if they think it's fast enough
    - The first project is not very compute-intensive
- https://colab.research.google.com/drive/1Xq9UGwhxa4cgNOo\_\_loN8SQwmiM222M4

# Forming groups

If you do not have a group of 3 students, please go to the designated area and try to find one. Please try to align:

- Your level of ambition
- Your expected work hours

It is fine if you have different background/expertise. This can even be an advantage!